

Commands

21 September 2021 11:23 AM

```
from functools import cmp_to_key
.sort( key = cmp_to_key(compare_function) )
```

2. Building a cache

```
def memo(f):
    cache = {}
    @wraps(f)
    def wrap(*args):
        if args not in cache:
            cache[args] = f(*args)
        return cache[args]
    return wrap
```

Use with @memo

Basic Printer

16 September 2021 9:17 PM

$$N + N-1 + N-2 + \dots + 1 = N*(N+1) / 2 = O(N^2)$$

From <<https://www.interviewbit.com/problems/nestedcml2/>>

What does it mean when we say that an algorithm X is asymptotically more efficient than Y?
X will always be a better choice for large inputs

From <<https://www.interviewbit.com/problems/choose4/>>

Maths

16 September 2021 9:23 PM

```
int a = 0, i = N;
while (i > 0)
{
    a += i;
    i /= 2;
}
 $O(\log N)$ 
```

From <<https://www.interviewbit.com/problems/whilecml/>>

```
int count = 0;
for (int i = N; i > 0; i /= 2) {
    for (int j = 0; j < i; j++) {
        count += 1;
    }
}
 $O(N)$ 
```

```
int i, j, k = 0;
for (i = n/2; i <= n; i++) {
    for (j = 2; j <= n; j = j * 2) {
        k = k + n/2;
    }
}
 $\theta(N \log N)$ 
```

```
int gcd(int n, int m) {
    if (n%m == 0) return m;
    if (n < m) swap(n, m);
    while (m > 0) {
        n = n%m;
        swap(n, m);
    }
    return n;
}
 $\theta(\log N)$ 
```

Array Maths

16 September 2021 9:31 PM

1. Pick from both sides:

Pick B elements from some combination of left and right side of the array.

Solution - Make prefix and suffix array. Compute max sum possible. $O(N)$

2. Min Step in Infinite Grid

Cost to move from point (x, y) to (x1, y1) when 8 movements are possible.

Cost = $\max(\text{abs}(x1-x), \text{abs}(y1-y))$

3. Minimum Lights to activate

Start with spot=0,

Find rightmost light j which is less than B distance from 0. [spot-B, spot+B-1].

Update the spot = j+B. As the found light j can cover next B areas.

Update the counter for each found spot. And fail if even single case fails.

4. Max Sum Triplet

$\max(A_i + A_j + A_k)$ such that $0 \leq i < j < k < \text{len}(A)$ and $A_i < A_j < A_k$

Solution:

- Prepare a prefix matrix. Prefix[j] will have maximum number from (0, i-1) but smaller than A[i]. Use bisect.insort_left
- Prepare a suffix array. Suffix[i] will contain the maximum element from (i+1, len(A))
- Compute $\max(A[i] + \text{prefix}[i] + \text{suffix}[i])$

5. Max Sum Contiguous Array

Contiguous subarray of any length with maximum sum.

Solution:

- Use variable max_so_far and max_end_here.
- From i = 0 to len(A)-1
 - Add A[i] to max_end_here
 - If max_end_here is less than max_so_far:
 - A[i] is part of contiguous array, update max_so_far to contain A[i]
 - If max_end_here become negative i.e. Adding A[i] makes the solution infeasible:
 - Reset index to start again from i. And max_end_here = 0

6. Add one to number

String of number, add 1. Solution: Add 1, store carry, use in next iteration.

7. Max Absolute Difference

$$\max(f(i, j)) = \max(|A_i - A_j| + |i - j|)$$

$$|A_i - A_j| + |i - j| = \begin{cases} (A_i + i) - (A_j + j) & A_i > A_j \text{ and } i > j \\ -(A_i + i) + (A_j + j) & A_i < A_j \text{ and } i < j \\ (A_i - i) - (A_j - j) & A_i > A_j \text{ and } i < j \\ -(A_i - i) + (A_j - j) & A_i < A_j \text{ and } i > j \end{cases}$$

Case 1 and 2 are same, Case 3 and 4 are same.

Max1 = $A_i + 1$

Min1 = $A_i + 1$

Max2 = $A_i - 1$

Min2 = $A_i - 1$

Ans = $\max(\max1 - \min1, \max2 - \min2)$

8. Partitions:

No of ways to split arrays into 3 parts such that sum of all partitions are same.

Solution:

- Splitsum = $\text{sum}(A) // 3$
- Prepare a suffix array such that suffix[i] contains number of indexes where sum == splitsum
- Do a forward pass adding elements, if sum == splitsum : add suffix[i] to total.

9. Maximum Area of Triangle

Maximum area of triangle parallel to y axis with different vertices.

Solution:

For each column, find the leftmost and rightmost index of 'r' and 'g' and 'b' nodes.

And the most topmost different colour than colour of each node (i, j)

For each column:

For each pair of colours in ('r', 'g', 'b'):

$\text{Max}(0.5 * \text{maxdiff}(c1, c2) * \max(\text{left}[c3], \text{right}[c3]))$

10. Flip

Choose two indices l, r to flip array to maximize the numbers of 1's.

Solution:

Find index l, r such that $\max(\text{count}(0) - \text{count}(1))$

Update the array to make '0' -> 1 and '1' -> -1

Apply "Max Sum Contiguous Array".

Range with max sum means $\max(\text{number of '0' - number of '1'})$

Value Ranges

16 September 2021 11:48 PM

1. Min Max

```
Max, min = A[0], A[1]
For x in A:
    If x > max: max = x
    Elif x < min: min = x
```

2. Merge Intervals

Insert and merge the intervals

- a. Insert new interval
- b. Sort based on start value
- c. Out = [i[0]]
- d. For x in i[1:]:
 - i. If x.start < out[-1].end:
 - 1) Out[-1].end = max(out[-1].end, x.end)
 - ii. Else:
 - 1) Out.append(x)

Simulation Array

17 September 2021 12:05 AM

1. Perfect Peak of an Array

Find A_i such that it is greater than all element on left and smaller than all element on right.

Solution:

Build Prefix and Suffix to store maxtill and mintill i.

Iterate and find which $prefix_i < A_i < suffix_i$

2. Kth row of a pascal triangle

Start with [1]

Build newA = A[i-1] + A[i] for i in [1, len(A)]

3. Spiral Order Matrix

startRow, endRow, startCol, endCol = 0, A, 0, A

Out = 0[A][A]

While sr < er and sc < ec:

For j in range(sc, ec):

Out[sr][j] = counter++

Sr += 1

For i in range(sr, er):

Out[i][ec-1] = counter++

Ec -= 1

If sc < ec:

For j in range(ec-1, sc, -1):

Out[er-1][j] = counter++

Er -= 1

If sr < er:

For i in range(er-1, sr, -1):

Out[i][sc] = counter++

Sc += 1

4. Anti Diagonals

Iterate $0 \leq i < 2*size - 1$

And for each i $\begin{cases} 0 \leq j \leq i & \text{for } i < size \\ size - 1 \leq j < i - size & \text{for } i \geq size \end{cases}$

Bucketing

17 September 2021 12:29 AM

1. Triplets with sum in a range(A, B)

- a. Filter out the element greater than B.
- b. Sort the array.
- c. Index, l, r = 0, 1, len(arr)-1
- d. While l < r:
 - i. Tsum = A_l + A_l + A_r
 - ii. If tsum in range: return 1
 - iii. If tsum less than A: increase index, l
 - iv. If tsum is more than B: decrease r

2. Balance Array

Count ways to remove A_i to make array balanced.

Make suffix array. Add even element, subtract odd element.

Make forward pass, check if presum == suffix[i+1].

Then add even element to presum, subtract odd element to presum

3. Duplicate in Array

Sum(A) - (Sum of first N Natural Numbers)

4. Maximum Consecutive Gap

- a. Find max and min of Array
- b. Initialise the buckets of max and min elements.
- c. Make a delta = max - min // (len(A)
- d. Store the values as per the bucket
- e. Iterate the buckets in order and find max_gap.

Arrangement

17 September 2021 1:49 AM

1. Sort Array with squares.

Notice the sorted given array. Find $O(N)$ solution

2. Largest Number

Arrange positive number to form largest number.

Solution:

- a. Sort the numbers using custom comparator.

Cmpfn(a, b):

$L, r = \text{str}(a) + \text{str}(b), \text{str}(b) + \text{str}(a)$

If $\text{int}(L) < \text{int}(r)$: return 1

Return -1

- b. Join numbers and return

3. Rotate Matrix

Swap(A_{ij}, A_{ji}) for all $0 \leq i < R$ and $i \leq j < C$.

Swap(A_{ij}, A_{ik}) for all $0 \leq i < C$ and (j=0, k=C-1 ; j < k; j++, k--)

4. Next Permutation

Solution:

- a. Find a index from right where $A_i \geq A_{i+1}$
- b. If all element are descending : return sorted(A)
- c. Find cindex where strictly greater than A[index] on right
- d. Swap A[index], A[cindex]
- E. Sort the right side (Already reverse sorted)

5. Find Permutation

Given string of I and D and len(numbers). Find perm such that I and D are satisfied.

Min, max = 1, B

N times: add minv for I and maxv for D.

Sorting

17 September 2021 2:24 AM

1. Noble Integers

Find p in array A such that $\text{num}(A_i > p) == p$

Traverse in sorted order, store the number of elements greater than $A[i]$

2. Wave Array

Sort into wave like array

- a. Sort into ascending
- b. Switch two elements at a time.

3. Hotel Bookings Possible

Sort datelists

For each element in datelists:

If start_time is greater than time t : Remove top element. Add to booklist

Elseif start_time is less than time t : if empty slot available push it.

4. Max Distance

Find $\max(j - i)$ with $A_j \geq A_i$.

Make leftMin prefix and rightMax suffix array.

Traverse and keep updating $(j-i)$

5. Maximum Unsorted Subarray

Minimum subarray to sort to make whole array sorted

Assume that A_l, \dots, A_r is the minimum-unsorted-subarray which is to be sorted.

then $\min(A_l, \dots, A_r) \geq \max(A_0, \dots, A_{l-1})$

and $\max(A_l, \dots, A_r) \leq \min(A_{r+1}, \dots, A_{N-1})$

- a. Compute MAX prefix and MIN suffix
- b. For i in $\text{range}(0, \text{len}(\text{prefix}))$
 - i. If $\text{prefix}[i] \neq \text{suffix}[i]$:
 - 1) If $\text{flag} == 0$: $\text{start}, \text{flag} = i, 1$
 - 2) Else: $\text{end} = i$
- c. Return $[\text{start}, \text{end}]$

Space Recycle

17 September 2021 2:50 AM

1. Set Matrix Zero

Set entire row and column 0 if there exist a 0.
Store row and col info. Update matrix

2. First Missing Integer

Find first missing positive integers from unsorted array in range(1, N)

Solution:

- a. Move all negative element before j and positive number after j. Make negative numbers positive.
- b. For each abs(element) after j. If in range. Make the element negative.
- c. Find first positive element . Return index.

3. Maximum Sum Square Submatrix

Matrix with maximum sum
Compress Column sum.
Then perform rowsum.

Missing/ Repeated Number

17 September 2021 3:03 AM

1. Repeat and Missing NumberArray

Make all element negative if found. If already negative, this is a repeat number.
Check which element is not negative, that element is missing number.

2. N/3 Repeat Number

Find two most occurring element. The count their frequency and find N/3 repeat number.

```
for(int i=0;i<n;i++)
{
    if(first == A[i])        count1++;
    else if(second == A[i])  count2++;
    else if(count1 == 0)     { count1++;  first = A[i];  }
    else if(count2 == 0)     { count2++;  second = A[i]; }
    else                     { count1--;  count2--;    }
}
```

ADHOC

17 September 2021 3:08 AM

1. Total Moves for Bishop

Diagonal distance between (x, y) and (x1, y1) = $\min(\text{abs}(x-x1), \text{abs}(y-y1))$
Ans = $\min(8-A, 8-B) + \min(8-A, B-1) + \min(A-1, 8-B) + \min(A-1, B-1)$

2. Prime Sum

Brute Force check prime

3. Sum of Pairwise Hamming Distance

Work with respect to the 32 bits. Find count of 1 and 0 in each row.
Sum = $\text{count0} * \text{count1} * 2$ for each bit .
AND with 2^i or $1 < i$ to get ith bit

4. Step by Step

Given a number N find out how many steps required to reach n. At ith step take i steps forward or backward.

Solution:

- Find n such that $n^2 + n - 2 * A \geq 0$ Take ceil for all values.
- Calculate sum till n terms. Return n if sum is equal to target
- If diff is odd. Increase n by 1 , add n to sum.
- Check again if diff is odd, increase n by 1. Return n

5. Power of Two Integers

Check if n can be expressed as A^P .

Solution:

```
for p in range(2,33):
    if round( A ** (1/p) ) ** p == A:
        return 1
return 0
```

Digit Op

17 September 2021 1:00 PM

1. Palindrome Integer

$A == A[::-1]$

2. Reverse Integer

Reverse the number. If the number is greater than $2^{31} - 1$
Return 0 else the reverse numbers

3. Next Smallest Palindrome

- a. Make String Mutable
- b. Find size, mid.
- c. Traverse from mid to size :
 - i. If equal continue,
 - ii. If left side is less than right side then incr is necessary.
 - iii. If right side is less than than left side then incr is not necessary
- d. Take left half of the array.
- e. If incr is true:
 - i. Carry =1
 - ii. Traverse from i = mid-1, 0:
 - 1) If carry is 0: break
 - 2) If $A[i] == 9$: set 0
 - 3) Else: $A[i], \text{carry} = A[i] + \text{carry}, \text{carry} - 1$
 - iii. If carry: return '1' + n-1 '0's + '1'
- f. If $\text{size} \% 2 == 0$: $A = A + A'$
- g. Else: $A = A + A[::-1][::-1]$
- h. Return buidstring(A)

Number Theory

17 September 2021 6:00 PM

1. GCD

$\text{Gcd}(A, B) = A$ if $B == 0$
 $\text{Gcd}(B, A \% B)$ else

2. Nth Fibonacci

$M = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$
 $F = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$
Do matrix multiplication N times
 F^N = then $F[0][0]$ is Nth fibonacci number.

3. Trailing zeros in Factorial

Count = 0
While $A \geq 5$:
 $A = A // 5$
 Count += A

4. Sorted Permutation Rank

For each character C at index i,
Rank += (Count of characters less than C) * (N-1!)

5. Largest Coprime Divisor(A, B)

X divides A and X and B are coprime

Repeat:
- Set a, b = A, B
- While $B \neq 0$:
 Set a, b = b, a % b
- If a = 1: return A
- $A = A // a$

6. Sorted Permutation Rank with repeats

No of permutation with char C as first character:
 $(N-1)! // p_1! * p_2! * p_3! \dots$
Use inverse modulus division.

Rank(A):
- Rank = 1
- For each character in A:
 Count elements less than A
 Count of repetition of elements after c
 Calculate $(\text{minCount} * \text{Fact}(\text{total} - i - 1)) // \text{repeat facts}$

Number Encoding

19 September 2021 12:12 PM

1. Next Similar Number

- Travel from right to left and find i where $C_i < C_{i+1}$.
- Find smallest greater element than above element i .
- Swap above digits.
- Sort all digits after i .

2. Rearrange Array

- $A[i] = A[i] + (A[A[i]] \% n) * n$
- $A[i] = A[i] // n$

3. Number of length N and value less than K

Set A, How many number of len B are possible with value less than C

Case1 : If $B > \text{len}(C)$: $d = 0$

Case2: If $B < \text{len}(C)$: if 0 in A: d^B else $(d-1) * d^{(B-1)}$

Case3: If $B == \text{len}(C)$:

Digit[]

First(i) = numbers formed by first i digits

Lower(i) = number of elements in A less than i . Similar to prefixSum

Dp[i] =

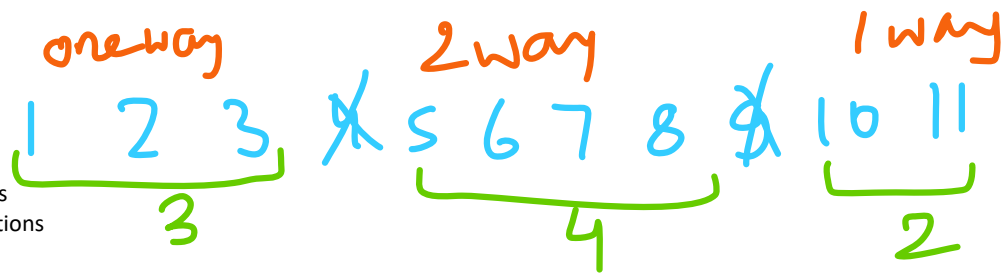
- For all numbers $F(i-1)$ is less than $F(i-1)$ of C, $\text{dp}[i] += \text{dp}[i-1] * d$
- For all number $F(i-1) == F(i-1)$ of C, $\text{dp}[i] += \text{lower}[\text{digit}[i]]$

Combinatorics

19 September 2021 3:01 PM

1. City Tour

- Calculate total together elements
- Totalperm * twoways // reductions



$$\frac{n!}{n_1! n_2! \dots n_k!} \times (2^{n_1-1} \cdot 2^{n_2-1} \dots)$$

$$= \frac{9!}{3! 4! 2!} \times 2^{4-1}$$

2. Grid Unique Paths

Top row and left col = 1

Else: $M[i][j] = M[i-1][j] + M[i][j-1]$

Simple Binary Search

19 September 2021 5:03 PM

Binary Search

```
def b_search(self, A):
    l, r = 0, len(A)-1
    while(l <= r):
        mid = (l+r)//2
        if( A[mid] > A[mid-1] ):
            l = mid + 1
        elif ( A[mid] < A[mid-1] ):
            r = mid - 1
        else:
            return mid
    return -1
```

1. Bitonic Array

First Increasing then decreasing sequence.

- a. Use binary search to find point of switch. Apply bsearch in increasing and inverse binary search in decreasing part

To find point, go to mid point: if mid element is less than mid-1, set index=mid shift left r else shift right l.

2. Smaller or equal elements

Find the point where $A[i] \leq B$

```
def greater_search( A, ele ):
    l, r, index = 0, r, len(A)
    while(l <= r):
        mid = (l+r)//2
        if( A[mid] <= ele ):
            l = mid + 1
        else:
            index, r = mid, mid - 1
    return index

def smaller_search( A, ele ):
    l, r, index = 0, r, -1
    while(l <= r):
        mid = (l+r)//2
        if( A[mid] < ele ):
            l, index = mid, mid + 1
        else:
            r = mid - 1
    return index
```

3. Woodcutting made easy

Binary Search : At mid point, find the amount of wood generated. Else repeat binary search process.

4. Matrix Search

Search for proper row, then search for proper column

5. Search for range

Apply greater search and smaller search to get immediate larger and smaller element.

6. Sorted Insert Position

Apply greater binary search with equality to index side.

Search Answer

19 September 2021 7:42 PM

1. Matrix Median

Find the max and min element by comparing the max and min of each row.

The median is $R * C + 1 // 2$

Apply binary search.

For each mid, calculate the number of element less than mid. Use binary search method.

2. Square Root of Integer.

Sqrt(A):

a. Lo, hi, root = 0, A, -1

b. While lo <= hi:

i. Mid, sq = (lo + hi)//2, mid*mid

ii.	If sq > A:	Hi = mid-1
	Else	Root, lo = mid, mid + 1

c. Return root

3. Allocate Books

Allocate books to B students so that pages are minimized.

a. Lo, hi, root = max(A), sum(A), -1

b. While lo <= hi:

i. Mid = (lo + hi)//2

ii. Sq = Check(A, B, mid)

iii.	If sq > A:	Hi = mid-1
	Else	Root, lo = mid, mid + 1

c. Return root

The check function will compute how many students will get books if mid pages are atleast allotted to each student.

4. Painter Partition Problem

Same as above, just the valid function will receive mid which will denote how much time one painter can spend.

Keep assigning board to painters till timetaken < mid.

Search Step Simulation

19 September 2021 8:03 PM

1. Power Function

$$x^n \% d$$

```
def pow(self, x, n, d):  
    res = 1 % d # Cover case d == 1  
    while n > 0:  
        if n & 1: # Odd?  
            res = (res * x) % d  
            x = x**2 % d  
            n >>= 1  
    return res
```

2. Simple Queries

a. Sieve of Eratosthenes

Product of all divisor of i.

```
p = [1] * (max(A) + 1)  
for i in range(1, len(p)):  
    for j in range(i, len(p), i):  
        p[j] = (p[j] * i) % 1000000007
```

- a. For each element , find how many subarray has x as max.
Find no of smaller element in left and number of smaller element in right
- b. Store prod of divisor with their frequency. Sort the values.
- c. Store cummulative sum of frequency. Apply binary search for each query.

3.

Sort Modification

19 September 2021 8:35 PM

1. Median Of Array

Switch Arrays if $\text{len}(A) > \text{len}(B)$

$\text{lo}, \text{hi}, \text{combined} = 0, m, m+n$

```
while lo <= hi:
    partX = (lo + hi) / 2
    partY = ((combined + 1) / 2) - partX
    LeftX, rightX = self.get_max(A, partX), self.get_min(A, partX)
    LeftY, rightY = self.get_max(B, partY), self.get_min(B, partY)
    if LeftX <= rightY and LeftY <= rightX:
        if combined % 2 == 0:
            return (max(LeftX, LeftY) + min(rightX, rightY)) / 2.0
        else:
            return max(LeftX, LeftY)
    if LeftX > rightY:
        hi = partX - 1
    else:
        lo = partX + 1
return -1
```

2. Rotated Sorted Array Search

```
def search(self, A, B):
    l, r = 0, len(A) - 1
    while( l <= r):
        mid = (l+r)//2
        if(A[mid] == B):
            return mid
        if( A[mid] <= A[r] ):
            if( B > A[mid] and B <= A[r] ):
                l = mid + 1
            else:
                r = mid - 1
        else:
            if( A[l] <= B and B < A[mid] ):
                l = mid + 1
            else:
                r = mid - 1
    return -1
```

Search

19 September 2021 8:51 PM

KMP StrStr()

```
def create_lps(pat):
    lps = [0] * len(pat)
    i = 1
    j = 0
    while(i < len(pat)):
        if pat[i] == pat[j]:
            j += 1
            lps[i] = j
            i += 1
        else:
            if j == 0:
                lps[i] = 0
                i += 1
            else:
                j = lps[j-1]
    return lps
class Solution:
    def strStr(self, A, B):
        lps = create_lps(B)
        i = 0
        j = 0
        while( i < len(A) ):
            if A[i] == B[j]:
                i += 1
                j += 1
            if j == len(B):
                return i - j
            elif i < len(A) and A[i] != B[j]:
                if j != 0 :
                    j = lps[j-1]
                else:
                    i += 1
        return -1
```

2. Stringholics

Minimum time after rotated produce same string

Compute LPS of repeat array

```
def computeLPSArray(self, pat):
    i=(pat+pat).find(pat,1,-1)
    return len(pat) if i == -1 else i
def solve(self, A):
    ans = 1
    for s in A:
        res = self.computeLPSArray(s)
        for i in range(1, 2*res+1):
            t = ( i * (i+1) // 2 ) % res
            if t == 0:
                ans = ( ans * i )// gcd(ans, i)
                break
    return ans % 1000000007
```

Tricks

19 September 2021 9:15 PM

1. Min characters to add to make palindromic

Lps of str + '*' + str
Return len(str) - lps[-1]

2. Convert to Palindrome

Remove one character to make the string palindromme
Traverse l, r
If $A_l \neq A_r$: Check Palindrome without l or r element. If exist return 1 else 0
Else: l++, r--

3. Minimum Appends for Palindrome

Minimum insert at end to make it palindrome
Lps = createlps(A.reverse() + '*' + A)
Return len(A) - lps[-1]

4. Minimum Parenthese

Minimum parenthesis to add to make it valid.
Push '(', Pop '(' for ')'.
If '(' does not exist for ')' Increase counter by 1
Return counter + len(stack)

5. Longest Palindromic Substring

For each i, scan toward left and right till matching sequence exist. Update the max values if necessary

String Maths

20 September 2021 7:23 AM

1. Roman To Int

Add value of symbol:

If prev value is less than current value. Decrease twice the value

2. Binary Addition

Half adder	Full Adder
Sum = a ^ b	Sum = a ^ b ^ c
Carry = a and b	Carry = (a and b) or (b and c) or (a and c)

Keep adding s1 and s2 untill one of them is empty

Empty the remaining strng

Add the carry

3. Power of 2

If A and (A-1) is zero : return 1

4. Multiply Strings

```
def multiply(self, A, B):
    result = [0] * (len(A) + len(B))
    i_n1, i_n2 = 0, 0
    for i in range(len(A) - 1, -1, -1):
        carry, n1, i_n2 = 0, ord(A[i]) - 48, 0
        for j in range(len(B) - 1, -1, -1):
            n2 = ord(B[j]) - 48
            sumv = n1 * n2 + result[i_n1 + i_n2] + carry
            carry = sumv // 10
            result[i_n1 + i_n2] = sumv % 10
            i_n2 += 1
        if(carry > 0):
            result[i_n1 + i_n2] += carry
            i_n1 += 1

    i = len(result) - 1
    while( i >= 0 and result[i] == 0): # Ignore leading zeros
        i -= 1

    if( i == -1 ): # Check if result does not exist
        return "0"

    s = "" # Build the string
    while( i >= 0):
        s += chr(result[i] + 48)
        i -= 1
    return s
```


Bit Play

20 September 2021 7:55 AM

1. Number of 1 bits, Trailing Zeros

$A \& 1$ and $A \gg 1$

2. Reverse Integers

```
int x = 0, t;
for(int i = 0; i < 32; i++)
{
    t = A&1;
    A = A >> 1;
    x = (x << 1) | t;
}
return x;
```

3. Divide integers using bit operation

```
q, t = 0, 0
for i in range(31, -1, -1):
    if( t + ( B << i ) <= A ):
        t += B << i
        q |= 1 << i
```

4. Different Bits Sum Pairwise = Max hamming distance

For each bit $sum += count0 * count1 * 2$

Bit Tricks

20 September 2021 8:08 AM

1. Min XOR values

Minimum xor value is between consecutive values. Sort and find out.

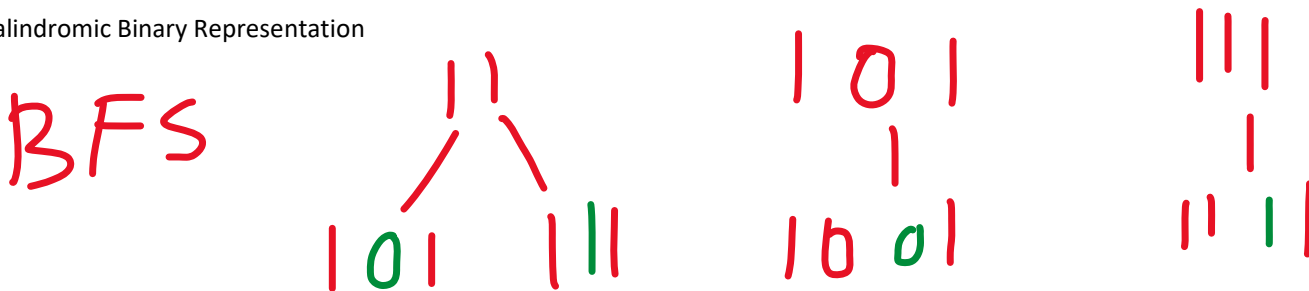
2. Count total set bits

Total set bits for perfect power of 2's = $(x * 2^{x-1}) + (N - 2^x + 1)$

Where N is the number and x is the power with $2^x \leq N$

```
def solve(self, A):  
    if( A <= 1 ):  
        return A  
    x = findmaxpow(A)  
    cnt1 = x * 2**(x-1) # Count of set bits before power of 2  
    cnt2 = A - 2**x + 1 # Count of set bits after power of 2  
    prevcnt = self.solve( A - 2**x ) # Count of set bits after power of 2 subsearch  
    return ( cnt1 + cnt2 + prevcnt ) % 1000000007
```

3. Palindromic Binary Representation



Run n times, with start element as '11'. Keep pop queue n times and return the number.

4. Xoring subarrays

Elements occurring only odd number of times will count in final result.

Value at ith index will occur $(i+1) * (N-i)$ times.

If N is even : Answer is zero.

Else : Answer is xor of even indexed elements.

```
def solve(self, A):  
    ans, n = 0, len(A)  
    for i in range(n):  
        # count the number of subarrays containing A[i]  
        # there are i+1 choices for starting index and  
        # n-i choices for ending index  
        num = (i + 1) * (n - i)  
  
        # if a number occurs in an even number of subarrays,  
        # it will be XORed an even number of times and  
        # hence will not be reflected into the final answer  
        # else it will be reflected just once.  
        if num & 1: ans ^= A[i]
```

```
return ans
```

5. Single Number with other having 3 occurrence

```
def singleNumber(self, A):  
    res = 0  
    for i in range(31, -1, -1):  
        count = 0  
        for x in A:  
            count += (x >> i) & 1  
        if( count % 3 == 1 ): res = (res << 1) + 1  
        else: res = (res << 1) + 0  
    return res
```

Sorting

20 September 2021 9:45 AM

1. Pair with given difference

Make a set. Check if $B+x$ or $x-B$ exist in set.

2. 3 Sum

For each element, apply two pointer.

Two pointer, take left index and right index. Keep shifting index as per requirement

3. Counting Triangles

Sort(A)

For each edge, apply two pointer.

$$A_i < A_j < A_k$$

Then check only for $A_i + A_j > A_k$.

If possible, then A_j and all values from i to $j-1$ will form a triangle.

Add $j-i$ to count.

4. DiffK

Same as 1st question

Tricks

20 September 2021 10:06 AM

1 . Max Ones after Modification

Two pointer, left and right. Move right by one if zero count \leq B.
Move left by one if zero count $>$ B.
Update bestl, bestl

2. Counting SubArrays

Same as above. Move right by one if sum + A[ir] $<$ B. Update count = ir - il as all subarrays with ir and rest of previous element have sum less than B
Move left by one if sum + A[il] \geq B

3. Subarray with distinct Integers

Count of atmost B values :

```
il, ir = 0, 0
count = 0
while ir < len(A):
    Add A[ir] into the data
    while len(freq) > B :
        Remove A[il] from data
        il += 1
    count += ir - il + 1
    ir += 1
return count
```

Count of exactly B values:

countAtmost(A, B) - countAtmost(A, B-1)

4. Max continuous series of 1s

Same as 1

5. Array 3 Pointers

Find i, j, k such that

$\max(|A_i - B_j|, |B_j - C_k|, |C_k - A_i|)$ is minimized.

```
def minimize(self, A, B, C):
    i, j, k = 0, 0, 0
    store_max = sys.maxsize
    while( i < len(A) and j < len(B) and k < len(C) ):
        minv = min(A[i], B[j], C[k])
        maxv = max(A[i], B[j], C[k])
        store_max = min( maxv - minv, store_max )
        if store_max == 0: break
        if A[i] == minv: i += 1
        elif B[j] == minv: j += 1
        else: k += 1
    return store_max
```

Keep changing the minimum value to next index.

6. Container with most water

$(i, A[i])$ denotes a coordinate. Find max water holding capacity by a container with x axis and two wall.

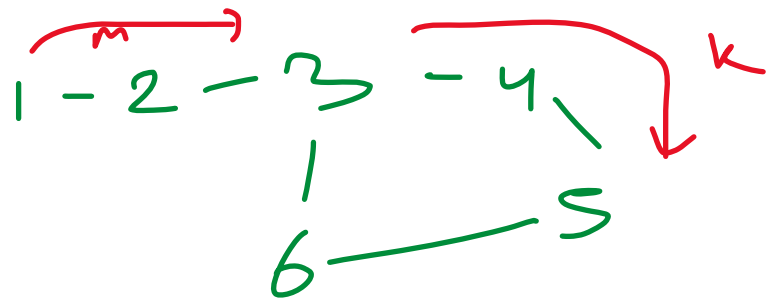
Keep inward moving pointers. $L = 0, R = \text{MAX}$

Shift lower bar inward. $\text{Area} = R - L * \min(A[L], A[R])$

Cycle List Detection

20 September 2021 11:56 AM

```
ListNode *slow = A, *fast = A;
slow = slow->next;
fast = fast->next->next;
while( fast && fast->next )
{
    if ( slow == fast )
        break;
    slow = slow->next;
    fast = fast->next->next;
}
if( slow != fast )
    return NULL;
slow = A;
while( slow != fast )
{
    slow = slow->next;
    fast = fast->next;
}
return slow;
```



$$m + k = C(1) - 2(1)$$

Simple Problems

20 September 2021 1:43 PM

1. Balanced Paranthesi

Add '(' to stack
Pop '(' for ')'

2. Simple Directory Path

Do nothing for '.'
Pop one for '..'
Push everything else

3. Redundant Braces

When ')' is found.
Set flag = 1, pop element till '(' is found and set flag = 0 if any operation is found.
If flag is 0, braces are redundant.

4. Min Stack

Easy Solution

Push	Add x to stack. Add x to minstack if x is less than or equal to top of minstack
Pop	Return last element of stack, If last element is same as top of minstack, then remove top of minstack also
getMin	Last element of Minstack

Complex Solution:

Push	If x is less than minele: Add $2x - minele$ to stack and make x the new minele. If x is greater or equal: Simply add x to stack
Pop	If top element is less than minele : $minele = 2 * minele - top$
Top	If top element is less than minele: return minele Else: return top element

If lower element arises, add $2*x$ to minele and update minele
Therefore if current element in stack is greater than minele, then the current element is not the minele
If current element become less than minele, the current element is the minele. Removing it will require
To update minele to previous minele.

CleverStack

20 September 2021 2:13 PM

```
specials = []
stack = []
for i in range(len(A)):
    while len(stack) and stack[-1] >= A[i] :
        stack.pop()
    if len(stack):
        specials.append(stack[-1])
    else:
        specials.append(-1)
    stack.append( A[i] )
```

Cleverstack is way to find the strictly greater or lower element in left or right of it.

For a minimum cleverstack in left.

Traverse from $i = 0$ --- $> \text{len}(A)$:

While $A[i] \leq \text{top}$: keep removing the top

For ith element, minimum element on the left is the top of stack if it exists.

After that, add $A[i]$ to stack.

1. MAXPROD

Max of (leftSpecialValue * RightSpecialValue)

leftSpecialValue(i) is rightmost j in the left with greater element

rightSpecialValue is leftmost j in the right with greater element.

Run cleverstack twice, store leftspecialvalue for each index, then calculate rightspecialvalue. Return max

2. Nearest Smaller Element

Simple cleverstack problem with popping of larger and equal elements.

3. Largest Rectangle in histogram

For each bar i.

If stack is empty or $A[i] > \text{stack_top_value}$:

Add index i to stack

Else:

Top = s.pop()

If element in stack:

// Area is height of top(popped element) * (difference between current and previous minimum)

Area = $A[\text{top}] * (i - s[-1] - 1)$

Else:

// If top is the minumum of all, area = top * (current element - 0)

Area = $A[\text{top}] * i$

// Clear the stack

While stack:

Area = top * (i - s[-1] - 1) or top * i

Keep updating max area.

--- Simple Solution :

Use simple cleverstack. Keep removing the smaller valued element from stack.

At every point in time, cleverstack contains the index for which height is minimum in the left.

```
height.append(0)
stack = [-1]
ans = 0
for i in range(len(height)):
    // While curr height is smaller than previous minumums, pop the
    // indeex. Calculate the area. Finally add current height
    while height[i] < height[stack[-1]]:
        h = height[stack.pop()]
        w = i - stack[-1] - 1
        ans = max(ans, h*w)
    stack.append(i)
height.pop()
return ans
```

Queue

20 September 2021 4:15 PM

1. First non repeating in steam of characters.

Use ordered map or map + queue

2. Sliding Window Maximum

CleverQueue.

Remove from queue back untill a higher value exist. Then append value. Operate with indexes
For each index i, remove all indexes $\leq i-B$. Add top of queue.

3. Evaluate Expresion

Push to stack, numbers, pop last 2 and operate

4. Rain Water Trapped

Easy Solution :

Keep a left max and right max.

At each step, either shift left or right whichever is less.

Update leftMax and rightmax

Add water += leftMax - A[l] or rightMax - A[r]

Maths

20 September 2021 5:30 PM

1. Maximal String

If $A_i < A_j$:
Swap them, recurse with one less swap

2. Kth permutation sequence

At every point we have to find $k/(n-1)!$
 $K = k \% (n-1)!$
 $N = n - 1$

3. Gray code:

Return [$i \wedge (i // 2)$ for i in range($2^{**}A$)]

Or
Start = [0, 1]
Add 0 to add values , then add 1 to all values
Join above two sets

Subsets

20 September 2021 5:46 PM

1. Subsets

Add A_i to subset, Recurse with it. Remove the element

2. Combination Sum

Add the element , increase sum. Recurse with it.

Remove the element, decrease sum

3. Combination sum.

While recursing increase index by 1 to avoid repeated use of same element.

4. Subsets 2 (Contains duplicates)

Same as 1

Brute Force Builder

20 September 2021 5:53 PM

1. Letter phone

Build dictionary . Recurse normally

2. Palindrome Partitoning

If palindrome, recurse with right values.

3. Generate all parenthesis 2.

If left is less than N : Try to append (. Recurse
If right is less than N: Try to append) . Recurse

4. Permutations

For each i in (l, r):
 Swap A_l, A_r
 Permute with l+1
 Swap again l,r

5. Nqueens

Use rowmask, leftdmask, rightdmask
Recurse for each column starting with 0:
 For i in range(columns):
 Set row, ld, rd masks
 Recurse to next row
 Reset masks
Return true or false as required.

6. Sudoku

Row, Column, Block Mask
Preporcess masks
Recurse in row order format:
 For i in range(i, row,col):
 Add i to row, col and mask it
 If possible(i, row, col):
 Recurse with next empty box

 Reset i to row, col and unmask it

Search

20 September 2021 6:07 PM

1. Largest Continuous Sequence zero sum

Calculate prefix sum

For each element i :

Keep adding $\text{prefix}[i]$

Update if $\text{prefix}[i]$ is zero or negative of sum exist.

2. Longest Subarray length

Largest range with 1 more 1 than 0

Change 0 to -1

Apply above method with target sum as 1

3. 4 SUM

Use two loops and one two pointer

4. DiffK

Easy add $B + A_i$ and $A[i] - B$

Keys and Maths

20 September 2021 6:19 PM

1. Linked List Copy

Create nodes and add these nodes to map
Retravel nodes and add links wherever necessary

2. Rearrange to form palindrome

Only one character can exist as 1 others should be even

3. Points on Straight Line

Add slope and intercept m, c to map

Incremental Hash

20 September 2021 6:36 PM

1. Two out of Three

Set 1 for elements in A
Or with 2 for element in B
Or with 4 for elements in C

If key is 1, 2 or 4 : Single Occurrence.
Else : more than 2 value exist

2. Subarray with B odd numbers

Create prefix sum with odd counts. Use to hash

3. Window String

Prepare target hash, source hash.
Keep adding element till counter == m
Then keep increasing l till counter < m

Update max length windows size

Map

20 September 2021 7:09 PM

1. Distinct Numbers in A windows

Add an element, Fill lenght, Remove left elemnt

2. LRU Cache

INIT	Lru Array Map Dictionary Capacity
GET	If key does not exist : return -1 Update lru, return value
SET	Add value and update lru. If size > capacity : remove least used element

Heaps

20 September 2021

8:07 PM

1. Ways to form max heap

$$F(n) = N - 1 - C_l \times F(l) \times F(r)$$

For i in range 2, A+1:

Calculate number of left keys

Apply F(i)

To calculate no of elements in left

Getleft(N):

Left = N // 2

Right = N - 1 - left

While (left + 1) & left != 0 and right + 1 & right != 0

Left, Right = +1, -1

Atleast one of the sides should have power of 2 elements.

2. N Pair Max Combinations

Sort A, B

Push A[-1] + B[-1] with key as (N-1, N-1)

At every iteration, pop an element and push to out.

For popped element i, j. Push i-1, j and i, j-1 in heap if does not exist.

3. Profit Maximization

Add all element to heap.

Pop element with highest cost, add to cost. Push again with 1 less cost.

4. Merge K sorted Arrays

Push first element of each row. Pop minimum along with row and col info. Add popped value to out, and next value to heap.

5. Magicians and Chocolates

Heapify with max cost. Pop maximum and push back value // 2

6.

Easy

20 September 2021 8:32 PM

1. Highest Product of 3 values

Find 3 maximum and 2 minimum values

Return $\max(\max1 * \max2 * \max3, \max1 * \min1 * \min2)$

2. Bulbs

Minimum switch flips to turn on all bulbs

Traverse from left to right

If count % 2 == 1: count += (A[i] == 1)

If count % 2 == 0: count += (A[i] == 0)

If count is even:

If current bulb state is 0 : mean bulb will be actually off

Else: bulb was on

If count is odd:

If current bulb state is 1: bulb will be actually off

Else: bulb will be on

3. Disjoint Intervals

Sort the intervals by last value.

Start with first value.

Keep moving forward. If start is more than prev end, update end and count

4. Largest Permutation

Make atmost B swaps to make the array largest.

Algorithm:

a. Make a map with index of all elements

b. Run B times:

i. Find i where $\text{Max} - i \neq A[i]$

ii. Find the position of $(\text{Max} - i)$

iii. Swap the elements and update the hashmap

Medium

20 September 2021 8:47 PM

1. Meeting Rooms

Assign Meeting Room as per schedule
Sort by start time
Create a min heap to store end time.

Traverse through all meetings:

If meeting start time is more than end time of active meeting.
Remove active meeting
Add the current meeting to active meeting.

Active meeting always contains parallel ongoing meetings

2. Distribute Candy

Give each child more candies than their neighbor if their rating is higher
Create a prefix and suffix array.

```
def candy(self, A):
    left, right = [1] * len(A), [1] * len(A)
    for i in range(1, len(A)):
        inv = len(A) - i - 1
        if A[i] > A[i-1]: left[i] = left[i-1] + 1
        if A[inv] > A[inv + 1]: right[inv] = right[inv+1] + 1
    candies = []
    for i in range(len(A)): candies.append( max(left[i], right[i]) )
    return sum(candies)
```

3. Seats

Create the seats array.
Find the median.

For each element in seats position array:

Start = Seats[i]
End = PositionInOriginalArray - MedianIndex + i
Seats += end - start

```
def seats(self, A):
    seats = [i for i in range(len(A)) if A[i] == 'x']
    med = len(seats) // 2
    moves = 0
    for i in range(len(seats)):
        start, end = seats[i], seats[med] - med + i
        moves += abs( end - start )
    return moves % 10000003
```

4. Assign Mice to Holes

Heapify A and B

While A is not empty:

$X = \max(X, \text{abs}(\text{heapop}(A) - \text{heappop}(B)))$

5. Majority Element

Apply similar to N/3 Repeat Numbers.

Cancel out occurrences of elements.

```
ele, count = A[0], 1
for x in A[1:]:
    if x != ele:        count -= 1
    else:               count += 1
    if count == 0:      ele, count = x, 1
return ele
```

6. Gas Stations

```
def canCompleteCircuit(self, gas, cost):
    if sum(gas) - sum(cost) < 0: return -1
    tank = 0          # gas available in car till now
    start = 0         # Consider first gas station as starting point
    for i in range(len(gas)):
        tank += gas[i] - cost[i]
        if tank < 0:   # the car has deficit of petrol
            start = i+1 # change the starting point
            tank = 0    # make the current gas to 0,
            #
            # as we will be starting again from next station
    return start
```

BST Traversal

20 September 2021 9:30 PM

1. Valid BST from Preorder

Idea : Use stack to always store the larger elements.

Algorithm:

For each x in A:

Check if x is less than root. If yes return 0

Remove smaller element from stack and make it root.

Add current element to x

```
def solve(self, A):
    stack, root = [], -sys.maxsize
    for x in A:
        if x < root:
            return 0
        while stack and x > stack[-1]:
            root = stack.pop()
        stack.append(x)
    return 1
```

Root always contains the value left maximum. Use stack to track the root.

While traversing, the mid node will be in stack, while travelling left root value will be the unchanged. Only when travelling right, root will be updated to contain the popped element.

2. Kth smallest element in Tree

In order traversal, update a counter instead of print statement

3. 2 Sum Binary Tree

PreOrder Traversal, Add Sum - root.val to set instead of print

4. BST Iterator

Init	Stack = [] Apply Fill_Left() to root
hasNext	Check if elements exist in stack
Next	Pop the top element from stack Apply Fill_Left() to top.right Return top.value
Fill_Left	While root: Add root to stack Root = root.left

5. Recover Binary Search Tree

Do an inorder traversal

Keep check of prev, first, last

Instead of print, Check if current val is less than previous value. If yes, it means a smaller element is after larger element.
Therefore add the prev index to first and current place to last. Also, last can be later element, so last should be updated to next nodes also.

Inorder	<pre>traverse(A.left) if prev and A.val < prev: if not first: first = prev last = A.val prev = A.val traverse(A.right)</pre>
---------	--

Trie

21 September 2021 11:21 AM

```
class TrieNode:
    def __init__(self):
        self.child = [None] * 26
        self.end = False

class Trie:
    def __init__(self):
        self.root = TrieNode()
    def insert(self, key):
        temp = self.root
        for x in key:
            if temp.child[ ord(x) - 97 ] == None:
                temp.child[ ord(x) - 97 ] = TrieNode()
            temp = temp.child[ ord(x) - 97 ]
        temp.end = True
    def find(self, key):
        temp = self.root
        for x in key:
            if temp.child[ ord(x) - 97 ] == None:
                return 0
            temp = temp.child[ ord(x) - 97 ]
        return int(temp.end)
```

1. Hotel Reviews

Sort with respect to good words
Make trie of good words
Sort with respect to count in trie

2. Shortest Unique Prefix

Easy, make a dictionary, store the prefix count + 1 for each word found.
Run again if count is 1, prefix is that substring for that word

Same for trie. Build the trie. Add additional information about child count for each child.

Whenever visiting the child, update its count by 1 in insert function.

3. Xor between two arrays

To find element with maximum xor, given binary string.
For each element, search the element in trie after that,
Insert the inverse of the element in the trie.

```
def insert(self, key):
    temp = self.root
    for i in range(31, -1, -1):
        bit = (key >> i) & 1
        if temp.child[bit] == None:
            temp.child[bit] = TrieNode()
```

```
temp = temp.child[bit]
```

```
def find_max(self, key):  
    temp, res = self.root, 0  
    for i in range(31, -1, -1):  
        index = int((key >> i) & 1 == 0)  
        res = res * 2  
        if temp.child[index]:  
            res += 1  
            temp = temp.child[index]  
        else:  
            temp = temp.child[ 1 ^ index ]  
    return res
```

Simple Tree Operations

21 September 2021 11:50 AM

1. Path to given node.

Traverse and return path recursively

2. Remove half nodes

Remove nodes with single child.

Pass the information upward. Let the node be as it is if leftvalue and rightvalue == 1

```
def check(self, A):
    if A == None:
        return None
    A.left = self.check(A.left)
    A.right = self.check(A.right)
    if A.left == None and A.right != None:
        return A.right
    if A.right == None and A.left != None:
        return A.left
    return A
```

3. Balanced Binary Tree

Return max of left and right tree height. If at any node, left height and right height diff is more than 1,

Return False

4. Maximum Edge Removal

Function depth return removal_count and total nodes.

For each edge in node x:

 Add node counter and remove counter to total

 If nodes in that edge are in even number:

 Increase remove_counter

Return total_remove_counter and total_nodes + 1 (for current node)

If no edge exist: remove 0, 1

5.

2 Trees

21 September 2021 12:11 PM

1. Merge Two Binary Tree

Travel the nodes together. Add the values of both the values

Cases:

If both left are None : Travel a.left, b.left

If a.left = None : Make a.left = b.left

Same for right side

2. Symmetric Binary Tree

Travel in opposite direction.

If both are none return 1, if one is none return 0.

If either values are unequal or left or right return 0 return 0 else 1

3. Identical Binary tree

Travel in same direction.

```
def equal(self, A, B):  
    if A == None and B == None:          return 1  
    if A == None or B == None:           return 0  
    return int (  
        A.val == B.val  
        and self.equal(A.left, B.left)  
        and self.equal(A.right, B.right) )
```

Traversal

21 September 2021 12:19 PM

1. Vertical Order Traversal

Keep a map with level value.

Queue = [(start, 0)]

Apply level order traversal,

Explore nodes,

Add node, level-1 for left node

Add node, level+1 for right node

Store the map in sorted order.

2. Diagonal Order Traversal

Keep a map with level value.

Queue = [(start, 0)]

Apply level order traversal,

Explore nodes,

Add node, level+1 for left node

Add node, level for right node

Preorder traversal with adding into map with key as slope the value

Level Order Traversal

21 September 2021 12:30 PM

1. Right View of Binary Tree

Level Order Traversal, add last value in each queue in the answer.

2. Cousins In Binary Tree

Level Order Traversal,

If B in left or right:

Break

Explore all other nodes in that level.

If flag becomes one, the nodes in the queue are siblings.

3. Reverse Level Order

Easy as Level Order Traversal

4. Zig Zag Traversal

Easy as level order Traversal

5. Populate Next Right Pointers Tree

Easy as level order Traversal

Root To Leaf

21 September 2021 12:49 PM

1. Burn A Tree

Function Run(Takes A Tree, Node B) : Return f (State to check if B is found) and d cost

```
def run(self, A, B):
    if A == None: return False, 0
    if A.val == B: return True, 0
    f1, d1 = self.run( A.left, B )
    f2, d2 = self.run( A.right, B )
    if f1 == False and f2 == False: return False, max(d1, d2) + 1
    self.out = max( self.out, d2 + d1 + 1 )
    return True, f1*d1 + f2*d2 + 1
```

2. Sum Root To leaf

Recursively pass numbers till now. At leaf add the number

3. Path Sum

Same as 2

4. Min Depth of Binary Tree

Return 1 if both left and right are None

Check for left path and right path. Return minimum

5. Roots to leaf paths with sum

Same as 2 track path.

Tree Construction

21 September 2021 1:27 PM

1. Inorder Traversal of Cartesian Tree

At each iteration.

Make root with max in Array

Make left subtree with left values

Make right subtree with right value

```
def buildTree(self, A):  
    if not A: return None  
    i = A.index(max(A))  
    root = TreeNode(A[i])  
    root.left = self.buildTree(A[:i])  
    root.right = self.buildTree(A[i+1:])  
    return root
```

2. Sorted Array to Balanced BST

Same as above. Make mid as root node to generate balanced bst.

3. Construct Binary tree from inorder and preorder.

Set preIndex = 0

Shift index everytime you make a node.

Root index i = inorder.index(preOrder[preIndex])

Make root with index i

```
def builder(self, inorder):  
    if not inorder:  
        return None  
    i = inorder.index( self.preorder[self.preindex] )  
    self.preindex += 1  
    root = TreeNode(inorder[i])  
    root.left = self.builder(inorder[:i])  
    root.right = self.builder(inorder[i+1:])  
    return root
```

4. Binary Tree From Inorder an PostOrder

Same as above, travel backwards

postIndex = len(A) - 1

Root index i = inorder.index(postOrder[postIndex])

Decrease preIndex

Inplace Change

21 September 2021 1:35 PM

1. Invert The Binary Tree

Easy, Travel , swap left and right move left and right

2. Lowest Common Ancestor

Easy: Get Path for A and B. Find lowest common.

Complex:

```
def findLCA(root, n1, n2):
    if root is None:
        return [0, 0], None
    lcheck, lnode = findLCA(root.left, n1, n2)
    rcheck, rnode = findLCA(root.right, n1, n2)
    comb = [lcheck[0] or rcheck[0], lcheck[1] or rcheck[1]]
    if lcheck == [1, 1]: # If both present in left subtree
        return [1, 1], lnode
    if rcheck == [1, 1]: # If both present in right subtree
        return [1, 1], rnode
    if comb == [1, 1]: # If each present in each subtree, current root is answer
        return [1, 1], root

    if n1 == n2 and root.val == n1: # If n1 = n2 == current root
        return [1, 1], root
    if root.val == n1: # If root is n1 , search n2 in subtrees
        if lcheck[1] == 1 or rcheck[1] == 1:
            return [1, 1], root
        return [1, 0], None

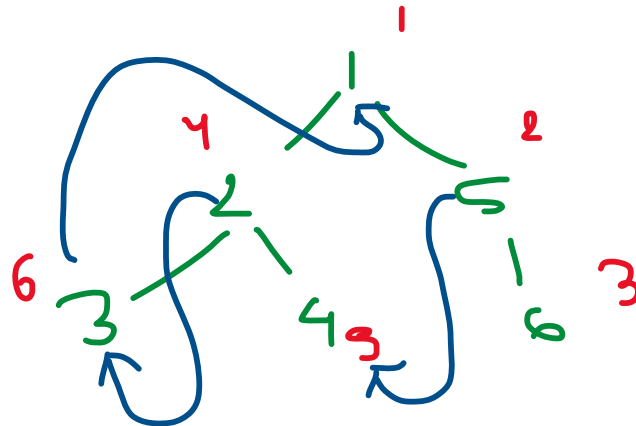
    if root.val == n2: # If root is n2, search n1 in subtrees
        if lcheck[0] == 1 or rcheck[0] == 1:
            return [1, 1], root
        return [0, 1], None

    return comb, None # return found elements.
```

3. Linked List Tree

Keep moving right, while returning return current node as prev.
This prev can be used to set as next node for rightest node in the left.

```
def flatten(A, prev=None):
    if not A: return prev
    prev = flatten(A.right, prev)
    prev = flatten(A.left, prev)
    A.right, A.left, prev = prev, None, A
    return prev
```



4. Order of People Heights

Easy Solution:

Take (height, index) as tuple into a list. Reverse Sort with respect to heights.

Traverse the list, add the heights to their respective index.

In the sorted list, all larger elements are already filled, so index will tell the current position to insert.

```
def order(self, A, B):
    l, out = [(A[i], B[i]) for i in range(len(A))], []
    l = sorted(l, reverse=True)
    for val, inf in l:
        out.insert(inf, val)
    return out
```

Segment Tree : Can be used to store sum or max

Initiation : For n nodes, we require n array of size $2*n - 1$

The left child = $2*p$

The right child = $2*p + 1$

Build Tree :

Add all element from nth position to right

For i in range(N):	Tree[n+i] = A[i]
For i in range(N-1, -1, -1):	Tree[i] = Tree[2*i] + Tree[2*i + 1]

Update Tree :

Set tree[n+ index] = value

Set i = index + n

While i > 1:

Tree[i//2] = Tree[i] + Tree[i+1]

Update i = i // 2

Query Tree:

Sum = 0

L, R = L + N, R + N

While L < R:

If L & 1:	Sum += Tree[L] L += 1
If R & 1:	R -= 1 Sum += Tree[R]

L, R = L//2, R//2

Return sum

Segment Tree Solution :

s

2D Strings DP

21 September 2021 3:49 PM

1. Longest Common Subsequence

if $A_i == B_j$: $dp_{i,j} = dp_{i-1,j-1} + 1$
else: $dp_{i,j} = \max(dp_{i-1,j}, dp_{i,j-1})$

2. Longest Palindromic Subsequence

Longest Common Subsequence with A, A.reverse()

3. Edit Distance

Minimum move to Make string A equal to B.

In the main case: if character at i and j index match , try with next item

If they do not match, try removing character (left) , try adding character (up), try update(leftup)

if i and $j == 0$: $dp_{i,j} = 0$
else if $i == 0$: $dp_{i,j} = dp_{i,j-1} + 1$
else if $j == 0$: $dp_{i,j} = dp_{i-1,j} + 1$
Else
 If $A_i == B_j$: $dp_{i,j} = dp_{i-1,j-1}$
 Else: $dp_{i,j} = 1 + \min(\text{left}, \text{up}, \text{leftup})$

4. Repeating Sub Sequence

Longest common subsequence on one diagonal matrix (upper diagonal matrix for $i < j$)

The $dp[R-1][C]$ will contain the value.

5. Distinct Subsequences

Idea:

First Column = 0 : As empty string cant have any subsequence

First Row = 1 : As empty string is subsequence at all points.

If A_i matches B_j : Count without A_i $dp[i-1][j]$ + Count without A_i and B_j $dp[i-1][j-1]$

Else : Count without A_i $dp[i-1][j]$

6. Scramble String

isScramble(A, B)

 If $A == B$: return 1

 If $\text{len}(A) \neq \text{len}(B)$: return 0

 For i in range($\text{len}(A) - 1$):

 If $\text{leftElement}(A, i) == \text{leftElement}(B, i)$:

 Check isScramble($A[i+1:]$, $B[i+1:]$) and isScramble($A[:i+1]$, $B[:i+1]$)

 If $\text{leftElement}(A, i) == \text{rightElement}(B, \text{len}(B) - i)$

 Check isScramble($A[i+1:]$, $B[\text{len}(B) - i:]$) and isScramble($A[:i+1]$, $B[:\text{len}(B) - i]$)

7. Regular Expression Match

For '*' in pattern: Check all possible combination with and without taking the next elements

For equal character or '?' in pattern: Check with next string and pattern

If `pattern.len - count(*) > string.len`: Then there exist extra elements in pattern so false

`Dp = [1] * [0] * len(string)`

For c in pattern:

 If `c == '*'`:

`Dp[i+1] = dp[i+1] or dp[i]` for i in `[0, len(string)]`

 Else:

`Dp[i+1] = dp[i]` and (`c == string[i]` or `c == '?'`) for i in `[len(string)-1 0]`

`Dp[0] = dp[0]` and `c == '*'`

Return 1 if `dp[-1]` else 0

Keep single array of size `len(string) + 1`.

For every char in pattern:

 Update the whole array.

 If `c == '*'`: make all value next to it true

 Else: Make all values which matches `pattern[0]` true whose previous value was true

8. Regular Expression 2

Easier, Apply recursive implementation

9. Interleaving Strings

```
def rec(self, A, B, C):
    a, b, c = len(A), len(B), len(C)
    if a == 0 and b == 0 and c == 0:    return 1
    if a + b != c: return 0
    flag = 0
    if a > 0 and A[0] == C[0]:    flag = flag or self.rec(A[1:], B, C[1:])
    if b > 0 and B[0] == C[0]:    flag = flag or self.rec(A, B[1:], C[1:])
    return flag
```

Simple Array DP

21 September 2021 7:15 PM

1. Length of Longest Subsequence

Longest subsequence first increasing then decreasing

```
def longestSubsequenceLength(self, A):
    inc, dec = [1] * len(A), [1] * len(A)
    for i in range(1, len(A)):
        for j in range(i):
            if( A[i] > A[j] and inc[i] < inc[j] + 1 ):
                inc[i] = inc[j] + 1

        rev_i = len(A) - i - 1
        for j in range(len(A)-1, rev_i, -1):
            if( A[rev_i] > A[j] and dec[rev_i] < dec[j] + 1 ):
                dec[rev_i] = dec[j] + 1

    maxi = 0
    for i in range(len(A)):
        maxi = max( maxi, (inc[i] + dec[i]
- 1))
    return maxi
```

2. Smallest Subsequence with given primes

Return array of size D denoting first D integers having A, B, C or combination of these as their prime factors.

Out = [1]

Ai, Bi, Ci = 0, 0, 0

While len(out) <= D:

Minele = min(out[ai] * A, out[bi] * B, out[ci] * C)

Out.append(minele)

If out[ai] * A == minele: ai += 1

If out[bi] * B == minele: bi += 1

If out[ci] * C == minele: ci += 1

Return out

3. Largest Area of Rectangle with Permutations

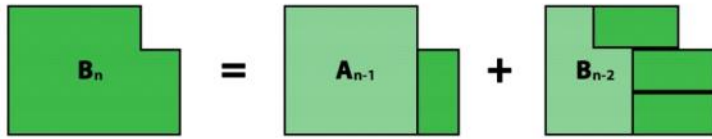
- Calculate consecutive 1's in every column
- Reverse sort each row. (Reverse Sorting will make every value in reverse order).
Left of each value will always be greater
- Traverse each row and check for max area. Area = Column Number * Histogram[i][j]
At each point column number and consecutive number of 1's in that point is the area.
Since the row is reverse sorted, previous row must have equal or higher number of 1's in the left

4. Tiling with Dominoes

3xN board with 2x1 dominoes.



$$A_n = A_{n-2} + 2 B_{n-1} \text{ and } A_0 = 1, A_1 = 0$$



$$B_n = A_{n-1} + B_{n-2} \text{ and } B_0 = 0, B_1 = 1$$

5. Paint Houses

$$Dp[i][j] = \min(dp[i-1][a] + A[i][j], dp[i-1][b] + A[i][j])$$

Where a and b are index other than j from (0, 1, 2)

6. Ways to Decode

$$\text{Return valid}(A[1:]) + \text{valid}(A[2:])$$

7. Stairs

Can only take 1 or 2 steps. For each n, count the ways to reach n-2 and n-1 and add them.

$$A = [1, 1]$$

Then fib: $A.append(A[-1] + A[-2])$

8. LIS

At each step, increase the count by 1 with previous max element which is less than current element

$$Dp = [1] * \text{len}(A)$$

For i in range(1, A.len):

For j in range(0, i):

If $A_i > A_j$ and $dpi < dpj + 1$:

$$dpi = dpj + 1$$

Return max(dp)

9. Intersecting Chords in A Circle

Catalan Number

At any time, divide the remaining points into two sets, no point in S1 joins S2.

$$Ways(N) = \sum_{i=0}^{N-1} Ways(i) * Ways(N-1-i)$$

$$Ways(0) = 1, Ways(1) = 1$$

10.

Derived DP

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1. Chain of Pairs

Check by Ignoring current element.

If $\text{maxLimit} < \text{current start}$: Try to move forward by adding current element.

Return maxPossible

2. Max Sum Without Adjacent Elements

At each index i ,

$$dp[i] = \max(dp[i - 1], \max(A[i], B[i]) + dp[i - 2])$$

Find max element at i th position if we consider previous index or previous to previous index

3. Merge Elements

$Dp[i][j]$ contain the cost to merge all elements from index i to j .

Set $dp[i][j]$ and merge cost = INT_MAX , $\text{sum}(A[i:j+1])$

For index in $\text{range}(i+1, j+1)$:

$$Dp[i][j] = \min(\text{prev}, \text{merge_cost} + \text{merge}(i, \text{index}-1, A) + \text{merge}(\text{index}, j, A))$$

Knapsack

21 September 2021

9:47 PM

1. Flip Array

Make an dp array of size sum

For n in A:

For j in [sum//2, n]:

Dp[j] = min(dp[j], dp[j-i] + 1)

This creates a dp array which stores all possible sum in the dp. Dp also contains

the minimum number of elements to make the sumi

Now we need to check the sum nearest to the middle.

2. Tushar Birthday Party

Algorithm:

a. Find max_eating_capacity.

b. For cap in [1, max_cap]:

i. For dish in [1, dishes]:

1) If capacity >= Dishwt[dish]:

a) Dp[cap][dish] = min(dp[cap][dish-1] , dp[cap - dishwt][dish] + Cost[dish]

2) Else:

a) Dp[cap][dish] = dp[cap][dish-1]

For each capacity, find the minimum number of dish which can fill it. Above algorithm will fill
The minimum dishes for each capacity.

Then find the number of dishes required for each friend.

3. 0-1 Knapsack

```
def knapSack(W, wt, val, n):  
    dp = [[0 for x in range(W+1)] for x in range(n+1)]  
    # Build table dp[][] in bottom up manner  
    for i in range(n+1):  
        for w in range(W+1):  
            if i==0 or w==0:  
                dp[i][w] = 0  
            elif wt[i-1] <= w:  
                dp[i][w] = max(val[i-1] + dp[i-1][w-wt[i-1]], dp[i-1][w])  
            else:  
                dp[i][w] = dp[i-1][w]
```

Profit of zero capacity or no element = 0 (Row and column)

If weight of ith element is more than capacity,

Then max(profit with one less carrying capacity, cost of ith element + profit with carrying capacity
Decreased by wt of ith element)

For each capacity i, check if adding object w can increase the profit.

4. Equal Average Partition

Divide the array in two parts such that both parts are equal

Since $s_1 / n_1 = s_2 / n_2 = s / n$

$\rightarrow s_1 = s * n_1 / n$

Find n_1 such that s_1 is integer $\Rightarrow s * n_1 \% n == 0$

For those n_1 , apply subset sum with (0, sumCount, elementCount).

If subset exist. Make sorted disjoint sets. Return it.

Additional Problems

21 September 2021 11:09 PM

1. Best Time to buy and sell stocks 2.

Buy one sell one.

As soon as you get a higher stock than purchased one. Add it to profit, then update the purchase to current stock

DP OPTIMIZED BACKTRACK

1. Word Break 2

Given a string and a dictionary, find possible sentences in the string.

Solution:

Build the trie dictionary

```
def rec(self, A, N, res):
    for i in range(1, N+1):
        if self.trie.search(A[:i]):
            if i == N:
                self.ans.append(res + A[:i])
            self.rec(A[i:], N-i, res + A[:i] + ' ')
```

For every matching word in string A, recurse with string after matching word.

2. Word Break 1

Check if string can be segmented to words in dictionary. Same as above. Dont build the string

3. Palindrome Partitioning

```
def minCut(self, s):
    if s == s[::-1]:
        return 0
    else:
        x = sys.maxsize
        for i in range(1, len(s)):
            if s[:i] == s[:i][::-1]:
                x = min(x, 1 + self.minCut(s[i:]))
        return x
```

Test for every possible segmenet if it is a palindrome.

4. Count Permutations of BST

a. Build Combination (N)

Create 2D matrix Using $nCr(n, r) = nCr(n-1, r-1) + nCr(n-1, r)$

b. DP = [A][B] A is nodes, B is height

c. DP[0][0], DP[1][0] = 1, 1

d. For node in [2:A+1]

i. For ht in [1:B+1]

1) Total = 0

2) For i in [0: node]

a) L, r = i, nodes - i - 1

b) Curr = 0

c) For j in [0, ht-1]:

i) Curr += DP[L][j] + DP[r][ht-1]

ii) Curr += DP[R][j] + DP[L][ht-1]

d) Curr += DP[L][ht-1] + DP[r][ht-1]

e) Total += curr * nCr(L + r, r)

3) DP[nodes][ht] = total

e. Return DP[A][B]

$$F(N) = \sum_{x=0}^{N-1} {}^{N-1}C_x F(x) F(N-1-x)$$

5. Unique Binary Trees

Find structurally unique BST that ca store 1...A

```
def numTrees(self, A):
    dp = [1, 1] + [0] * A
    for i in range(2, A+1):
        for j in range(0, i):
            dp[i] += dp[j] * dp[i-j-1]
    return dp[A]
```

$$F(N) = \sum_{x=0}^{N-1} f(x) f(N-1-x)$$

UBT(0), UBT(1) = 1, 1

Greedy Or DP

21 September 2021 11:48 PM

1. Tushar Birthday Bombs

Maximize total number of kicks with total sum of kicks strenght \leq Bearing Limit.

Calclute maximum hits. Keep the elements in left less than limit.

Keep checking if using the element gives same number of hits as maximum hits. Then replace the element.

Algorithm():

- min_strength , min_index, max_hits = min(B), index(min), A // min_st
- Store the hit strength less than limit upto the min_index
- l, ans = []
- While i < len(S):
 - o Max_hit , Curr_hit = A // min_strength, 1 + (limit - S[i]) // min_strenght
 - o If limit \geq S[i] and max_hit == cur_hit :

Add the index to ans, decrease limit = limit - S[i]
- Return ans

2. Jump Game Array

```
For index i in [0: len(A) - 1]
    If i > max_jump : return 0
    Max_ump = max(max_jump, i + A[i])
Return 1
```

3. Min Jump Array

Find the min index on left which brings to i.

Tricky

22 September 2021 9:23 AM

1. Longest AP

Check in left, (max count where difference $A[i] - A[j]$) + 1 wherever exist.

```
sol = defaultdict(int)
n = len(a)
for i in range(n):
    for j in range(i):
        d = a[i] - a[j]
        sol[(i, d)] = max(sol[(i, d)], 1 + sol[(j, d)])
return max(sol.values(), default=0) + 1
```

```
Store the difference with index value, so next time when checking of difference with that element, if
difference match, increase the count by 1
```

2. N digits numbers with digit sum S

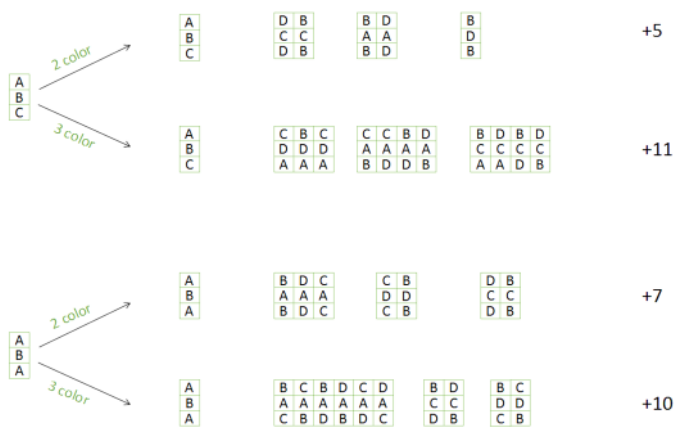
Recurse start with (1, 9)
If Number Limit becomes 0, return if Sum is Zero.
If Sum becomes 0, return 1 : ie possible
Else, check with all (0, 9) digits

3. Shortest Common Superstring

Bit Masking with DP
 Idea : Pick order for strings in S and construct superstring : Naive
 Pick highest overlap strings and merge them : Greedy

- Until the list is left with one element:
 - Find the pair with highest overlap,
 - Merge the strings in the list

4. Ways to Color 3xN board



```
def solve(self, A):
    c3 = 24
    c2 = 12
    for i in range(A-1):
        c3, c2 = ( 11*c3 + 10*c2 ) % 1000000007, ( 5*c3 + 7*c2 )
    return (c3+c2) % 1000000007
```

5. Kth manhattan Distance Neighborhood

For each $M_{i,j}$ find $M_{p,q}$ such that $|i - p| + |j - q| \leq K$

Run K times:

Update $M_{i,j}$ with max neighbor.

6. Best Time to buy and Sell Stocks atmost B times.

$dp[i][j]$ = maximum profit from most i transactions using prices[0..j]

A transaction is defined as one buy + sell.

On Day j :

a. Do nothing, profit is same : $dp[i][j] = dp[i][j-1]$

b. Sell the stock j, To sell stock j, must buy it on

$\sim t : [0, \dots, j-1] \quad \max(\text{prices}[j] - \text{prices}[t] + dp[i-1][t-1])$ buying on day t and selling on day j

Time complexity of this approach is $O(n^2 * k)$.

In order to reduce it to $O(n*k)$, we must find

$\sim t : [0, \dots, j-1] \quad \max(\text{prices}[j] - \text{prices}[t] + dp[i-1][t-1])$ in constant time

If you see carefully,

$\sim t : [0, \dots, j-1] \quad \max(\text{prices}[j] - \text{prices}[t] + dp[i-1][t-1])$ is same as

$\text{prices}[j] + \sim t : [0, \dots, j-1] \quad \max(dp[i-1][t-1] - \text{prices}[t])$

Track the max till T_{th} column.

```
def solve(self, price, B):
    B = min(len(price), B)
    profit = [ [0] * (len(price) + 1) for i in range(B + 1)]
    for i in range(1, B + 1):
        maxdiff = -sys.maxsize
        for j in range(1, len(price) ):
            maxdiff = max( maxdiff, profit[i-1][j-1] - price[j-1] )
            profit[i][j] = max( profit[i][j-1], price[j] + maxdiff)
    return profit[B][len(price)-1]
```

7. Coins in a Line

Execute Smarty,

If turn is yours, you try to maximize the coins,

Else minimize the coins.

```
def pick(self, l, r, turn):
    if l == r:
        return 0
    t1 = self.pick(l+1, r, 1 ^ turn)
    t2 = self.pick(l, r-1, 1 ^ turn)
    if turn == 1:
        return max(t1 + self.A[l], t2 + self.A[r])
    return min(t1, t2)
```

8. Evaluate Expression to True

Add all characters in one array, all symbols in one array.

Travel with gap of 2 character at once to 3 upto all character at once.

$T[i][j]$, $F[i][j]$ will contain true ways and false ways from $i \rightarrow j$

For each gap and with each character.

```
tt, ff, tf, ft = T[i][k] * T[k+1][j], F[i][k] * F[k+1][j], T[i][k] * F[k+1][j], F[i][k] * T[k+1][j]
    if ope[k] == '|':
        T[i][j] += tf + ft + tt
        F[i][j] += ff
    if ope[k] == '&':
        T[i][j] += tt
        F[i][j] += tf + ft + ff
    if ope[k] == '^':
        T[i][j] += tf + ft
        F[i][j] += tt + ff
```

9. Egg Drop Problem

Drop egg from floor x:

- Egg break : Check from remaining eggs and floor x - 1
- Egg survives : Check from all eggs and floor total - x

Take maximum of above two cases : as we need to minimize the problem

Iterative Solution:

Dp[i][j] to store minimum number of trials for i eggs and j floors.

Dp[i][1], dp[i][0] = 1, 0

Dp[1][j] = j

For index i, j:

For x -> [1, j+1]:

Res = 1 + max(dp[i-1][x-1] , dp[i][j-x])

Dp[i][j] = min Res

Easiest Solution:

L, R = 1, B

Apply binary search:

If sumBinaryCoeff(mid, A) < B:

L = Mid + 1

Else:

R = Mid

Return L

$$SumBinaryCoeff(N, R) = \sum_{i=1}^{i=R} nCr(N, i)$$

MaxFloor(x trials, n eggs) = MaxFloor(x-1 trials, n-1 eggs) + MaxFloor(x-1 trials, n eggs) + 1

MaxFloor(0, n) = 0

MaxFloor(x, 0) = 0

We need to find x such that

MaxFloor(x trials, n eggs) >= K floors

Above relation solves to :

$$Maxfloor = \sum_{i=1}^N nCr(x, i)$$

10. Best Time to buy and sell stocks 3

Only two transactions are allowed.

Dp = 0 * [stocks + 1] [2 + 1]

For i in range(1, 3):

Maxdiff = INT_MIN

For j in range(1, stocks):

Maxdiff = max(maxdiff, dp[i - 1][j - 1] - stocks[j - 1])

Dp[i][j] = max(dp[i][j - 1], stocks[j] + maxdiff)

Return dp[2][stocks]

11. Longest Valid Parenthesis

Dp[i] = longest set of parenthesis ending at i

If s[i] == '(': dp[i] = 0

If s[i] == ')': If s[i-1] == '(':

Dp[i] = dp[i-2] + 2

Elif s[i-1] == ')' and s[i-dp[i-1]-1] == '(':

Dp[i] = dp[i-1] + 2 + dp[i-dp[i-1]-2]

- 1) Create an empty stack and push -1 to it.
The first element of the stack is used to provide a base for the next valid string.
- 2) Initialize result as 0.
- 3) Add index of '(' to stack.
- 2) If `str[i] == ')'`,
We need to remove its equivalent '(' for stack if it exists.
 - a) Pop an item from the stack (Most of the time an opening bracket)
If there is still an element in stack, it is the left valid limit uptill now.
I - `Stack[-1]` is the current limit/
 - b) If the stack is not empty, then find the length of current valid substring by taking the difference between the current index and top of the stack. If current length is more than the result, then update the result.
If stack is empty, means the string in the left is invalid totally,
Add index of current ')' element to mark the start of valid index as the left is not valid anymore.
 - c) If the stack is empty, push the current index as a base for the next valid substring.
- 3) Return result.

Another Approach

Tree DP

22 September 2021 1:04 PM

1. Max Edge Queries

Find maximum weighted edge in a simple path from u to v .

Binary Lifting to pre compute the maximum weighted edge from every other node at a distance of 2^i

INIT:

- Make adjacency list

- $Dp[i][j]$ store parent of j at 2^i

- $Max[i][j]$ store the maximum edge from node j to parent of this node at 2^i

DFS:

- Update level of each node

- Update parent of each node in dp

- Update weight of each node in mx

Compute Ancestor

- For j in range(1, maxLevel):

 - For i in range(1, $N+1$):

 - $T = dp[i][j-1]$

 - If $t \neq -1$:

 - $Dp[i][j] = dp[t][j-1]$

 - $mx[i][j] = \max(mx[i][j], mx[t][j-1])$

Get LCA(u, v)

- If $level_u < level_v$: swap u, v

- $Diff = level_u - level_v$

- Move to parent :

 - If $diff$ and $1 \ll i$ is true;

- For remaining level:

 - Move to parent together, and check if they match.

 - If both become equal, return it as parent

Find_Max_Edge(u, v):

- $Lca = get_lca(u, v)$

- Travel in path from Lca to u and Lca to v to return max edge

2. Max Sum Path in binary Tree

Do a postorder traversal.

At the end of traversal of node, you will get path from both subtrees, return maximum path cost.

At every step update max value to contain all possible combinations $c, l+c, r+c, l+r+c$.

```
def traverse(self, R):
    if R == None: return 0
    l, c, r = self.traverse(R.left), R.val, self.traverse(R.right)
    self.ans = max(self.ans, c, l + c, c + r, l + c + r)
```



```
return max(c,          1 + c,          c + r)
```

Matrix DP

22 September 2021 1:50 PM

1. Kingdom War

Since the element in left is less or equal to right and element in up is less or equal to down.

$$dp[i, j] = A[i, j] + dp[i + 1, j] + dp[i, j + 1] - dp[i + 1, j + 1]$$

2. Maximum Path in Triangle

Keep updating the paths according to the maximum above.

3. Maximum Size square SubMatrix

$$dp[i, j] = \min(dp[i - 1, j], dp[i, j - 1], dp[i - 1, j - 1]) + 1$$

4. Increasing Path in Matrix

Update the cost if possible in the matrix in row order.

```
if i < len(A) - 1 and A[i][j] < A[i+1][j]:  
    dp[i+1][j] = max(dp[i+1][j], dp[i][j] + 1)  
if j < len(A[0]) - 1 and A[i][j] < A[i][j+1]:  
    dp[i][j+1] = max(dp[i][j+1], dp[i][j] + 1)
```

5. Minimum Difference Subsets

Use knapsack to store the possible sums.

Find the sum closest to sum//2. return sum - 2 * sumIndex

6. Subset Sum Problem

Recurse with adding the element or without adding the element. If sum becomes 0, subset sum is possible.

Top down:

Knapsack type, Try storing the sums.

If subset sum exist return 1.

7. Unique Paths in Grid

If $A[i][j] == 1$: leave as 0

Else : $dp[i][j] = dp[i-1][j] + dp[i][j-1]$

8. Dungeon Princess

Matrix Path, with life health dropper and potion to increase health

Traverse matrix in reverse order.

Set the bottom right value as 1 or (x if -x is there in the point)

For every point on boundary:

$$Dp[i][j] = \max(1, \text{nextBoundaryElement} - \text{current element})$$

For every other elements:

$$Dp[i][j] = \max(1, \min(\text{health below}, \text{health right}) - \text{current health})$$

9. Min Sum Path in Matrix

Easy Problem. Sum of left and top element

10. Min Sum Path in Triangle

Easy as above.

11. Max Rectangle in Binary Matrix

Make histogram at each row.

Find max histogram area at each row.

Use CleverStack to solve maxArea for histogram.

CleverStack:

Histogram Area:

Making Left and Right Smaller index --

While there is smaller element in stack than current element:

RightSmaller [Make index of stack element] = current index

LeftSmaller[currentIndex] = Index of stack top element

Direct CleverStack:

For each element in HISTORGRAM:

If current element is greater or equal to top element:

Add index to stack

Else Current Element is smaller top element:

Top_index = stack.pop()

Curr_Area = A[top_index] * (current_index - stack[-1] - 1)

Or Curr_Area = A[top_index] * current_index if stack is empty

Empty the stack:

Curr_area = A[top_index] * (max_i - stack[-1] - 1)

Or Curr_Area = A[top_index] * max_i

Here stack store immediate lower element index in the left.

12. Rod Cutting

Recursively,

try all points and divide and conquer left and right part separately.

Return leftcost, left seq, rightmin, rightseq

13. Queen Attack

For each queen:

Travel in each direction:

Keep increasing the count until a border arrives or other queen is found.

Suffix/ Prefix DP

22 September 2021 4:18 PM

1. Sub Matrix with sum Zero

```
For each start_row [0 : ROWS]
    M = [0] * N
    For i in [start_row : ROWS]
        For j in [0 : N]
            M[j] += A[i][j]
        Ans += countSubsetSumZero(M)
Return ans
```

```
Rows = [0, 1, 2, 3]
Start Rows to End Rows =
(0, 0), (0, 1), (0, 2), (0, 3)
(1, 1), (1, 2), (1, 3)
(2, 2), (2, 3)
(3, 3)
```

All possible combinations of rectangle. Count SubsetSumZero for each row.

2. Coins Sum Infinite

Same as count sums existence (Knapsack).

Try two ways, [Rec(A, Value - A[index], index) + Rec(A, Value, index-1)]
If value become zero return 1,
If value < 0 or index == -1 return 0

Iterative Solution:

```
def coinchange2(self, A, B):
    dp = [0] * (B + 1)
    dp[0] = 1
    for coin in A:
        for i in range(1, B + 1):
            if coin <= i:
                dp[i] = dp[i] + dp[i - coin]
    return dp[-1] % 1000007
```

3. Max Product Subarray

```
Set min, max, res = A[0], A[0], A[0]
For i in [1: len(A)] :
    Set min, max = max( A[i], max * A[i], min * A[i]), min( A[i], max * A[i], min * A[i])
    Res = max(res, max)
Return res
```

4. Best Time to buy and Sell stocks.

```
Update min_so_far at every index j.
Update res = max(res, price[j] - min_so_far)
```

5. Arrange 2

Try to put horses one by one in the stable. And recurse with next horses and one less stable.
Update cost if less than current cost.

Graph Traversal

22 September 2021 4:56 PM

1. Path in Directed Graph

Do dfs or bfs. If node explored return 1 else 0

2. Water Flow

Validity of BFS is if neighbor less than or equal to current: Allow the transfer

Do BFS for boundaries for blue lake.

Separately Do BFS for boundaries for red lake

Count the intersection

3. Stepping Numbers

Do BFS, neighbor can be $(\text{current} * 10 + \text{current} \% 10 \pm 1)$ if possible

4. Capture Regions on Board

Capture all regions covered by 'x'.

Change all '0' --> '_'.

Start with all boundary and do bfs. Make the '_' to '0'.

The nodes which are untouched or '_' are surrounded by 'x'. In the original matrix, mark the Untouched nodes to 'x'.

5. Word Search Board

Do DFS to check if letter exist. Neighbor is if it is in range and character matches.

DFS

22 September 2021 5:19 PM

1. Path with good nodes

DFS with goodcount.

If lead and goodcount < limit:

 Increase resultCounter

2. Largest Distance between nodes of a tree

a. DFS with start node. Capture the node farthest from root keeping a height counter.

b. DFS with node recieved from above. The maximum height reached will be max dist between two nodes of tree

3. Cycles in Directed Graph

DFS : if a visited + unclosed node is found, cycle is true.

4. Delete Edge.

Maximize the product of (sum of weights of nodes in tree 1 , sum of wts of nodes in tree 2)

Build the sum from leaf to root.

Store the sum from branches and current node value as NODE WEIGHT.

For each node in B:

 leftCost = min(NODEWT[edge[0]] , NODEWT[edge[1]])

 currVal = leftCost * (TotalCost - leftCost)

 Update maxVal

5. Two Teams

Check if all people can be separated into two teams.

Do Graph Coloring.

Apply colour 0 to root, for every edge switch colour. If the neighbor is found with same colour

Return 0

BFS

22 September 2021 6:03 PM

1. Valid Path

Prepare graph with circle conditions. Do graph search.

2. Snake Ladder

Make a dictionary to update snakes and ladder.

Do BFS while queue not empty:

 Add 0 to queue:

 Add next 6 neighbors into queue.

 Update with dictionary if snake or ladder is encountered.

Repeat till 100 is not reached.

3. Region in Binary Matrix

Multiple BFS with count of explored node by each starting point.

Return maximum count of explored nodes.

4. Level Order

Queue based Graph Traversal

5. Smallest Multiple with 0 and 1

Start with queue = ['1']

BFS, add '0' and '1' to end of each element of queue:

The first to be found as multiple is the result. Do the modulus and set parent accordingly.

6. Min Cost Path

Algorithm:

1. Start with cell (0,0) push it into the doubly-ended queue and also make its distance as 0.
2. Pop the front node from the queue.
3. You can go to four directions from the popped node so if you go to a direction that is written on the cell then mark $\text{dist}[\text{neighbour}] = \text{dist}[\text{current}] + 1$ else $\text{dist}[\text{neighbour}] = \text{dist}[\text{curr}]$
4. If direction in which you move is not same as the direction written on the cell so this implies you have to incur a cost of 1 so push it to the back of queue else push it to the front of the queue.
5. Repeat steps 2-4

Push the forward nodes in front. Push the reverse going nodes in the back.

7. Permutation Swaps:

Prepare the graph with good pairs.

Create a matrix for each element's store source positions and destination position.

Do DFS to check if path exist for all source to destination.

Graph Connectivity

22 September 2021 6:31 PM

1. Commutable Islands

Minimal Spanning Tree

```
def find(self, i):
    if self.parent[i] == i: return i
    return self.find( self.parent[i])

def union(self, x, y):
    xr, yr = self.find(x), self.find(y)
    if self.rank[xr] < self.rank[yr]: self.parent[xr] = yr
    elif self.rank[yr] < self.rank[xr]: self.parent[yr] = xr
    else: self.parent[yr], self.rank[xr] = xr, self.rank[xr] +
```

1

Kruskal Or Prims Algorithm

Kruskal Union Find:

- a. Sort edge with respect to weight.
- b. Take an edge, Check if it does not make a cycle. Add to output.
Increase edge count by 1. Union(u, v)

2. Possibility of finishing all courses given pre requisites

Detect Cycle in list. If cycle exist it it not possible

3. Cycle in a undirected graph

Cycle with more than two node.

Provide a variable as parent.

While exploring the neighbors, if the nbor is visited and parent != node :

Return cycle exists.

4. Black Shapes

Count connected componenets

Extra Problems

22 September 2021 6:52 PM

1. Convert Sorted List to BST

Count the number of nodes.

Work with inorder traversal.

Keep travelling left with half nodes,

After returning from left side,

Make the node with current head list.

Keep travelling right with other half of the list.

```
def sortedListToBSTRecur(self, n) :  
    if (n <= 0) :  
        return None  
    left = self.sortedListToBSTRecur( int(n/2) )  
    root = TreeNode( self.head.val)  
    root.left = left  
    self.head = self.head.next  
    root.right = self.sortedListToBSTRecur( n - int(n/2) - 1)  
    return root  
  
def sortedListToBST(self, A):  
    self.head = A  
    n, temp = 0, A  
    while temp != None:        n, temp = n + 1, temp.next  
    return self.sortedListToBSTRecur(n)
```

2. Clone Graph

Hard Problem

Traversal and create a copy of nodes and add it to dictionary

Retraverse and make nodes as in original graph

Shortest Path

22 September 2021 7:00 PM

1. Sum of Fibonacci Number

Build fibonacci number till A.
Do coin change.

2. Knight on Chess Board

Do a breath first search, if destination is reached count steps to reach there.

3. Useful Extra Edges

Recursively, use the edge only once. Keep flag to store this information.
Do dfs from src to dest as well as dest to src.

4. Word Ladder

Shortest Transformation of Word A to B using dictionary C
Store all characters at each position using the dictionary.
Do BFS.

For each position:

Try each character other than itself and if word is valid:

Add it to queue