HW6

Andrew Shao

2024-11-06

(a)

1. The model is:

$$brozek = -46.216 + 0.646 \cdot chest$$

Since the p-value is extremely small $(7.373 \cdot 10^{-39})$, we conclude that these two variables are associated.

2. Pearson's correlation coefficient is 0.703 between the two variables.

The calculated p-value for T_{obs} is extremely small and close to 0, so we conclude that the two variables are significantly correlated at the $\alpha = 0.05$ level. The value is the same as the value for the slope. The 95% confidence interval is [0.6344, 0.7604]

3. Spearman's correlation coefficient = 0.6731

Since the p-value is extremely close to 0, we can conclude that the two variables are significantly correlated at the $\alpha = 0.05$ level.

4. The two variables are correlated and the association between the two variables is positive and strong.

(b)

The model is:

$$brozek = -40.599 + 1.567 \cdot neck$$

Since the p-value is extremely small $(9.904 \cdot 10^{-17})$, we conclude that these two variables are associated.

Pearson's correlation coefficient is 0.491 between the two variables.

The calculated p-value for T_{obs} is extremely small and close to 0, so we conclude that the two variables are significantly correlated at the $\alpha = 0.05$ level. The value is the same as the value for the slope. The 95% confidence interval is [0.3917, 0.5798]

Spearman's correlation coefficient = 0.491

Since the p-value is extremely close to 0, we can conclude that the two variables are significantly correlated at the $\alpha = 0.05$ level.

The two variables are correlated and the association between the two variables is positive and weaker than between brozek and chest.

(c)

I think chest has a stronger association because it is highly significant and the R-squared value is larger and both the pearson and spearman correlation coefficients are much larger than those for neck.

(d)

- 1. The model has 13 predictors: age, weight, height, neck, chest, abdom, hip, thigh, knee, ankle, biceps, forearm, and wrist. The four significant predictors at the $\alpha=0.05$ level are neck, abdom, forearm, and wrist. The multiple R-squared value is 0.749 and the adjusted R-squared value is 0.7353. The F-statistic is 54.63 on 13 and 238 degrees of freedom with a p-value less than $2.2 \cdot 10^{-16}$.
- 2. The Breusch-Pagan p-value is 0.1107, meaning that there is not enough evidence to reject the null hypothesis at the $\alpha=0.05$ level suggesting that the constant variance assumption holds. The Q-Q plot residuals seem to generally follow the line which suggests that the residuals are indeed normally distributed. The Shapiro-Wilk normality test p-value is 0.2801 meaning there is not enough evidence to reject the null hypothesis at the $\alpha=0.05$ level suggesting that the residual normality assumption holds.
- 3. In this specific model, neck is significantly associated with brozek while chest is not, which differs from my answer in (c) that chest had the stronger association. This could be due to collinearity between the predictors including neck and chest.

(e)

- 1. Many of the correlation coefficients are very close to 1 or -1 which suggests collinearity between predictors, which affects the significance of individual predictors within the model.
- 2. Most of the condition numbers are greater than 30 which suggests a high level of collinearity in the model which could cause imprecision in the estimation of β .
- 3. The VIF values that are greater than 10 are weight, abdom, hip, and chest which confirms the theory that collinearity is present among the variables.

(f)

1. Minimum: 0

Q1: 12.8 Median: 19 Mean: 18.94 Q3: 24.6 Maximum: 45.1

Standard deviation: 7.75

- 2. The data looks mostly normal, but the Q-Q plot deviates from the normal line at the tails which could indicate non-normality.
- 3. The Shapiro-Wilk p-value is 0.2747 meaning there is not enough evidence to reject the null hypothesis at the $\alpha = 0.05$ level suggesting that brozek is normal.
- **4.** An error occurs because the some values for the response variable aren't positive (in this case, values of 0).
- 5. The plot shows that a lambda value close to 1 is within the 95% confidence interval, suggesting transformation might not be necessary since it is close to 1.
- **6.** I would not recommend transformation since the Q-Q plot and Box-Cox plot do not suggest a need to transform; the best fit lambda is close to 1 and the data seems to be normal.

(g)

- 1. Of the fourteen predictors in the model, age, abdom, abdom squared, and wrist are significant. The R-squared value is 0.7573 and the F-statistic p-value is extremely small.
- 2. Of the fifteen predictors in the model, only age and wrist are significant. The R-squared value is 0.758 and the F-statistic p-value is extremely small.
- 3. I think adding the quadratic term was beneficial since it increased both R-squared and adjusted R-squared values slightly with the added term being statistically significant at the $\alpha=0.05$ level. Adding the cubic term didn't change the R-squared values much and instead made both all the abdom terms insignificant. It seems the quadratic term captured some non-linearity within the data while adding the cubic term seem to add excess complexity to the model which could cause it to overfit.

Appendix

(a)

```
library(faraway)
## Warning: package 'faraway' was built under R version 4.3.3
head(fat)
##
     brozek siri density age weight height adipos free neck chest abdom
                                                                            hip
## 1
       12.6 12.3
                 1.0708
                          23 154.25
                                     67.75
                                             23.7 134.9 36.2
                                                               93.1
                                                                     85.2
## 2
       6.9 6.1
                 1.0853
                          22 173.25
                                     72.25
                                             23.4 161.3 38.5
                                                              93.6
                                                                     83.0
                                                                           98.7
## 3
       24.6 25.3
                 1.0414
                          22 154.00
                                     66.25
                                             24.7 116.0 34.0 95.8
                                                                     87.9
                                                                           99.2
       10.9 10.4
                 1.0751
                          26 184.75
                                     72.25
                                             24.9 164.7 37.4 101.8
## 4
                                                                     86.4 101.2
## 5
       27.8 28.7
                  1.0340
                          24 184.25
                                     71.25
                                              25.6 133.1 34.4 97.3 100.0 101.9
## 6
       20.6 20.9
                 1.0502 24 210.25
                                    74.75
                                             26.5 167.0 39.0 104.5 94.4 107.8
     thigh knee ankle biceps forearm wrist
     59.0 37.3
                 21.9
                        32.0
                                27.4
                                      17.1
## 1
     58.7 37.3
                 23.4
                        30.5
                                28.9
                                      18.2
## 3
     59.6 38.9
                24.0
                        28.8
                                25.2 16.6
## 4 60.1 37.3
                 22.8
                        32.4
                                29.4
                                      18.2
                        32.2
                                27.7
                                      17.7
## 5
     63.2 42.2
                 24.0
     66.0 42.0 25.6
                        35.7
                                30.6
                                      18.8
## (a)(1) simple linear regression
lma <- lm(brozek ~ chest, data=fat);</pre>
summary(lma)
##
## Call:
## lm(formula = brozek ~ chest, data = fat)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                             Max
                                        13.8989
## -13.8875 -3.8211 -0.2752
                                3.4950
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                            4.18460
                                     -11.04
                                               <2e-16 ***
## (Intercept) -46.21636
## chest
                 0.64622
                            0.04136
                                      15.62
                                               <2e-16 ***
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5.524 on 250 degrees of freedom
## Multiple R-squared: 0.494, Adjusted R-squared: 0.492
## F-statistic: 244.1 on 1 and 250 DF, p-value: < 2.2e-16
## Extract those information for the slope
summary(lma)$coefficients[2,]
##
       Estimate
                 Std. Error
                                  t value
                                              Pr(>|t|)
## 6.462223e-01 4.136018e-02 1.562426e+01 7.372549e-39
## or the t-statistics and p-value for the slope
## t-stat=1.562426e+01= 15.62426, p-value= 7.372549e-39
summary(lma)$coefficients[2,3:4]
        t value
                    Pr(>|t|)
## 1.562426e+01 7.372549e-39
## (a)(2) Pearson's correlation
# (i) Pearson's correlation
r1 = cor(fat$brozek, fat$chest);
## [1] 0.7028852
# (ii) hypothesis testing via Pearson's correlation
n= dim(fat)[1];
t.obs1 = r1* sqrt((n-2)/(1-r1^2));
t.obs1 ### compare with (i)
## [1] 15.62426
# p-value
pvalue1 = 2*(1-pt(abs(t.obs1), df = n-2));
pvalue1
## [1] 0
# (iii) 95% CI on Pearson's correlation
alpha = 0.05;
cutoffvalue = qnorm(1- alpha/2);
Zr1 = 0.5*log((1+r1)/(1-r1));
ZCI = Zr1 + c(-1, 1)* cutoffvalue / sqrt(n-3);
rho1.CI = (exp(2*ZCI) -1) / (exp(2*ZCI) +1);
rho1.CI
## [1] 0.6344161 0.7604106
### (a)(3) Spearman's Correlation
## (i) point estimate
rs1= cor(fat$brozek, fat$chest, method= "spearman");
```

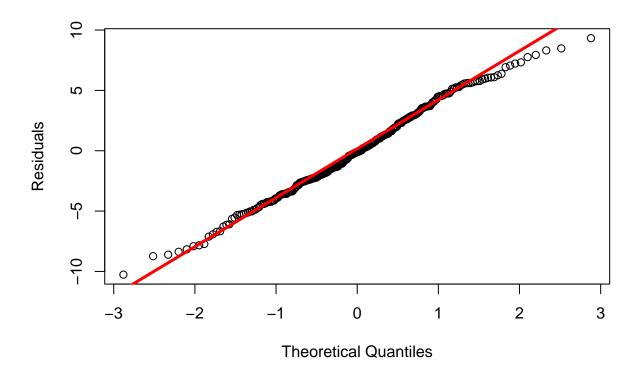
[1] 0.6730803

```
## (ii) hypothesis testing
n= dim(fat)[1];
t.obs2 = rs1* sqrt((n-2)/ (1-rs1^2));
t.obs2
## [1] 14.38991
# p-value based on Spearman's correlation
pvalue2 = 2*(1-pt(abs(t.obs2), df = n-2));
pvalue2
## [1] 0
(b)
# (b)(1) Simple Linear Regression Model for `brozek` and `neck`
lmb <- lm(brozek ~ neck, data=fat)</pre>
summary(lmb)
##
## Call:
## lm(formula = brozek ~ neck, data = fat)
## Residuals:
##
                1Q Median
       Min
                                   3Q
                                           Max
## -14.0076 -4.9450 -0.2405 5.0321 21.1344
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -40.5985 6.6857 -6.072 4.66e-09 ***
## neck
                1.5671
                           0.1756 8.923 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.764 on 250 degrees of freedom
## Multiple R-squared: 0.2416, Adjusted R-squared: 0.2385
## F-statistic: 79.62 on 1 and 250 DF, p-value: < 2.2e-16
# Extract information for the slope of `neck`
summary(lmb)$coefficients[2,]
       Estimate
                 Std. Error
                                 t value
                                             Pr(>|t|)
## 1.567090e+00 1.756186e-01 8.923259e+00 9.904320e-17
# t-statistics and p-value for the slope
summary(lmb)$coefficients[2, 3:4]
        t value
                   Pr(>|t|)
## 8.923259e+00 9.904320e-17
# (b)(2) Pearson's Correlation
# (i) Pearson's correlation coefficient
r2 <- cor(fat$brozek, fat$neck)
r2
```

```
## [1] 0.4914889
# (ii) Hypothesis testing for Pearson's correlation
n <- dim(fat)[1]</pre>
t.obs2 \leftarrow r2 * sqrt((n - 2) / (1 - r2^2))
t.obs2
## [1] 8.923259
# p-value
pvalue2 \leftarrow 2 * (1 - pt(abs(t.obs2), df = n - 2))
pvalue2
## [1] 0
# (iii) 95% Confidence Interval for Pearson's correlation
alpha <- 0.05
cutoffvalue <- qnorm(1 - alpha / 2)</pre>
Zr2 \leftarrow 0.5 * log((1 + r2) / (1 - r2))
ZCI2 \leftarrow Zr2 + c(-1, 1) * cutoffvalue / sqrt(n - 3)
rho2.CI \leftarrow (exp(2 * ZCI2) - 1) / (exp(2 * ZCI2) + 1)
rho2.CI
## [1] 0.3917062 0.5798451
# (b)(3) Spearman's Correlation
# (i) Spearman's correlation coefficient
rs2 <- cor(fat$brozek, fat$neck, method = "spearman")
rs2
## [1] 0.4913248
# (ii) Hypothesis testing for Spearman's correlation
t.obs3 \leftarrow rs2 * sqrt((n - 2) / (1 - rs2^2))
t.obs3
## [1] 8.919331
# p-value for Spearman's correlation
pvalue3 \leftarrow 2 * (1 - pt(abs(t.obs3), df = n - 2))
pvalue3
## [1] 0
(d)
######Part (d) ########
### Lily's Model
modLily <- lm(brozek ~ age + weight+ height+ neck+ chest + abdom+ hip+
                 thigh+ knee+ ankle+ biceps+ forearm+ wrist, data=fat);
summary(modLily)
##
## Call:
## lm(formula = brozek ~ age + weight + height + neck + chest +
##
       abdom + hip + thigh + knee + ankle + biceps + forearm + wrist,
       data = fat)
##
```

```
##
## Residuals:
      Min
               1Q Median
                              3Q
                                    Max
## -10.264 -2.572 -0.097
                           2.898
                                  9.327
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -15.29255
                         16.06992 -0.952 0.34225
                                  1.895 0.05929 .
## age
               0.05679
                         0.02996
## weight
              -0.08031
                          0.04958 -1.620 0.10660
## height
              -0.06460
                          0.08893 -0.726 0.46830
                          0.21533 -2.032 0.04327
## neck
              -0.43754
## chest
              -0.02360
                         0.09184 -0.257 0.79740
## abdom
                          0.08008 11.057 < 2e-16 ***
              0.88543
              -0.19842
                          0.13516 -1.468 0.14341
## hip
## thigh
               0.23190
                          0.13372
                                   1.734 0.08418 .
                          0.22414 -0.052 0.95850
## knee
              -0.01168
## ankle
               0.16354
                          0.20514
                                  0.797 0.42614
               0.15280
                                  0.964 0.33605
## biceps
                          0.15851
## forearm
               0.43049
                          0.18445
                                  2.334 0.02044 *
                          0.49552 -2.980 0.00318 **
## wrist
              -1.47654
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.988 on 238 degrees of freedom
## Multiple R-squared: 0.749, Adjusted R-squared: 0.7353
## F-statistic: 54.63 on 13 and 238 DF, p-value: < 2.2e-16
### model diagnostic
### (i) check equal variance assumption
library("lmtest")
## Warning: package 'lmtest' was built under R version 4.3.2
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
      as.Date, as.Date.numeric
bptest(modLily)
##
   studentized Breusch-Pagan test
##
## data: modLily
## BP = 19.418, df = 13, p-value = 0.1107
### If you want to go above and beyond,
    you can check the p-value of F-test when regressing
    the absolute value of residuals on all X variables again
## If p-value >= 5%, then it is okay to accept the equal variance assumption
## If p-value < 5%, then we can run the weighted least square regression
\hookrightarrow hip+
```

```
thigh+ knee+ ankle+ biceps+ forearm+ wrist, data=fat);
summary(lm.weight)
##
## Call:
## lm(formula = abs(residuals(modLily)) ~ age + weight + height +
      neck + chest + abdom + hip + thigh + knee + ankle + biceps +
##
      forearm + wrist, data = fat)
##
## Residuals:
     Min
##
            1Q Median
                         3Q
                               Max
## -3.781 -1.730 -0.285 1.393 6.470
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -10.09069
                         8.80802 -1.146 0.2531
                         0.01642 1.112 0.2671
## age
               0.01827
## weight
              -0.04476
                         0.02718 -1.647 0.1009
## height
              0.06278
                         0.04874 1.288 0.1990
                         0.11803 2.136
## neck
               0.25208
                                         0.0337 *
## chest
             -0.06308 0.05034 -1.253 0.2114
## abdom
              0.02454 0.04389 0.559 0.5766
              ## hip
## thigh
              -0.03278 0.07329 -0.447 0.6551
## knee
              -0.19103 0.12285 -1.555
                                         0.1213
## ankle
                         0.11244 2.252
              0.25326
                                         0.0252 *
                         0.08688 1.617
## biceps
               0.14049
                                          0.1072
              -0.11631
                         0.10110 -1.150
                                          0.2511
## forearm
## wrist
              -0.17917
                         0.27160 -0.660 0.5101
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.186 on 238 degrees of freedom
## Multiple R-squared: 0.0839, Adjusted R-squared: 0.03386
## F-statistic: 1.677 on 13 and 238 DF, p-value: 0.06664
### (ii) Check the normality assumption
qqnorm(residuals(modLily),ylab="Residuals",main="")
qqline(residuals(modLily), lwd=3,col="red")
```



```
shapiro.test(residuals(modLily))
##
   Shapiro-Wilk normality test
## data: residuals(modLily)
## W = 0.99297, p-value = 0.2801
(e)
######Part (e): Collinearity ########
### (e)(1) Pairwise correlation
## any pairs that have large correlation?
     Say >= 0.90? >= 0.80? >= 0.70?
### There are two ways to extract X matrix
### The first one is to use "model.matrix" function in the regression model
## here we assume to exclude the intercept for collinearity analysis
Lily.X <- model.matrix(modLily)[,-1];</pre>
round(cor(Lily.X),2)
##
             age weight height neck chest abdom
                                                  hip thigh knee ankle biceps
            1.00 -0.01 -0.17 0.11 0.18 0.23 -0.05 -0.20 0.02 -0.11 -0.04
## age
```

1.00 0.25 0.13 0.09

0.31 0.83 0.89 0.89 0.94 0.87 0.85 0.61

0.25 1.00 0.78 0.75 0.73 0.70 0.67 0.48

0.17 0.15 0.29 0.26

0.80

0.21

0.73

weight -0.01

height -0.17

0.11

neck

1.00

0.31

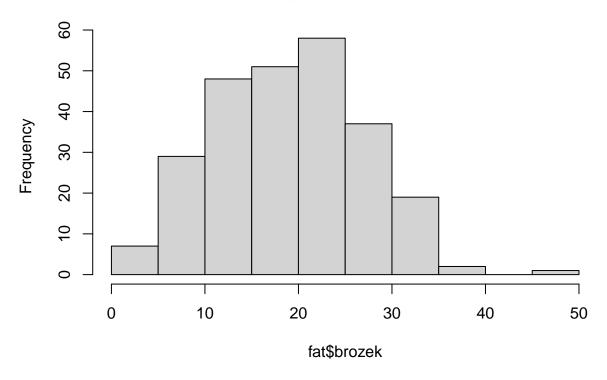
0.83

```
## chest
           0.18
                   0.89
                          0.13 0.78 1.00 0.92 0.83 0.73 0.72 0.48
                                                                         0.73
## abdom
           0.23
                   0.89
                          0.09 0.75
                                    0.92
                                           1.00
                                                0.87
                                                       0.77 0.74
                                                                  0.45
                                                                         0.68
## hip
           -0.05
                   0.94
                          0.17 0.73
                                    0.83
                                           0.87
                                                 1.00
                                                       0.90 0.82
                                                                  0.56
                                                                         0.74
           -0.20
                                                 0.90
## thigh
                   0.87
                          0.15 0.70
                                    0.73
                                           0.77
                                                       1.00 0.80
                                                                  0.54
                                                                         0.76
## knee
           0.02
                   0.85
                          0.29 0.67
                                    0.72
                                           0.74
                                                 0.82
                                                       0.80 1.00
                                                                  0.61
                                                                         0.68
## ankle
                  0.61
                          0.26 0.48
                                    0.48
                                          0.45
                                                 0.56
                                                       0.54 0.61 1.00
                                                                         0.48
           -0.11
## biceps -0.04
                   0.80
                          0.21 0.73
                                    0.73
                                                 0.74
                                                       0.76 0.68
                                                                         1.00
                                           0.68
                                                                  0.48
## forearm -0.09
                   0.63
                          0.23 0.62
                                    0.58
                                           0.50
                                                 0.55
                                                       0.57 0.56
                                                                  0.42
                                                                         0.68
## wrist
            0.21
                   0.73
                          0.32 0.74 0.66 0.62
                                                0.63
                                                      0.56 0.66 0.57
                                                                         0.63
##
           forearm wrist
## age
            -0.09 0.21
             0.63 0.73
## weight
## height
             0.23 0.32
             0.62 0.74
## neck
## chest
             0.58 0.66
## abdom
             0.50
                   0.62
             0.55
                   0.63
## hip
## thigh
              0.57 0.56
## knee
              0.56 0.66
## ankle
              0.42 0.57
             0.68 0.63
## biceps
## forearm
              1.00 0.59
## wrist
             0.59 1.00
### The second one is to create the X matrix by ourselves from the raw data
        based on those 13 predictor variables
head(fat);
     brozek siri density age weight height adipos free neck chest abdom
##
                                                                           hip
## 1
       12.6 12.3 1.0708 23 154.25
                                    67.75
                                             23.7 134.9 36.2
                                                             93.1
                                                                    85.2
                                                                          94.5
       6.9 6.1 1.0853 22 173.25
                                    72.25
## 2
                                             23.4 161.3 38.5
                                                             93.6
                                                                    83.0
                                                                          98.7
## 3
       24.6 25.3
                 1.0414
                         22 154.00
                                    66.25
                                             24.7 116.0 34.0 95.8
                                                                    87.9
## 4
      10.9 10.4
                                    72.25
                                             24.9 164.7 37.4 101.8 86.4 101.2
                 1.0751
                         26 184.75
       27.8 28.7
                 1.0340
                         24 184.25
                                    71.25
                                             25.6 133.1 34.4 97.3 100.0 101.9
## 6
       20.6 20.9 1.0502 24 210.25 74.75
                                             26.5 167.0 39.0 104.5 94.4 107.8
     thigh knee ankle biceps forearm wrist
## 1 59.0 37.3 21.9
                        32.0
                                27.4 17.1
## 2 58.7 37.3 23.4
                                28.9 18.2
                        30.5
## 3 59.6 38.9 24.0
                        28.8
                                25.2 16.6
## 4 60.1 37.3 22.8
                        32.4
                                29.4 18.2
## 5 63.2 42.2 24.0
                        32.2
                                27.7 17.7
## 6 66.0 42.0 25.6
                        35.7
                                30.6 18.8
Lily.X2 \leftarrow fat[,c(4:6,9:18)]
round(cor(Lily.X2),2)
##
            age weight height neck chest abdom
                                                  hip thigh knee ankle biceps
## age
                        -0.17 0.11 0.18 0.23 -0.05 -0.20 0.02 -0.11
            1.00
                 -0.01
                   1.00
                          0.31 0.83
                                          0.89
                                                0.94 0.87 0.85 0.61
                                                                         0.80
## weight
          -0.01
                                    0.89
## height
          -0.17
                   0.31
                          1.00 0.25
                                    0.13
                                          0.09
                                                 0.17
                                                       0.15 0.29
                                                                  0.26
                                                                         0.21
## neck
            0.11
                   0.83
                          0.25 1.00
                                    0.78
                                           0.75
                                                 0.73
                                                      0.70 0.67
                                                                  0.48
                                                                         0.73
## chest
                  0.89
                          0.13 0.78
                                    1.00
                                           0.92
                                                 0.83
                                                       0.73 0.72
                                                                  0.48
            0.18
                                                                         0.73
                  0.89
## abdom
            0.23
                          0.09 0.75
                                    0.92
                                          1.00
                                                 0.87
                                                       0.77 0.74 0.45
                                                                         0.68
## hip
           -0.05
                   0.94
                          0.17 0.73 0.83
                                           0.87
                                                 1.00
                                                      0.90 0.82 0.56
                                                                         0.74
                          0.15 0.70 0.73 0.77 0.90 1.00 0.80 0.54
## thigh
           -0.20
                  0.87
                                                                         0.76
```

```
0.29 0.67 0.72 0.74 0.82 0.80 1.00 0.61
## knee
           0.02
                  0.85
                                                                        0.68
                  0.61
## ankle
          -0.11
                         0.26 0.48 0.48 0.45 0.56 0.54 0.61 1.00
                                                                        0.48
                  0.80
                         0.21 0.73 0.73 0.68 0.74 0.76 0.68 0.48
                                                                        1.00
## biceps -0.04
## forearm -0.09
                  0.63
                         0.23 0.62 0.58 0.50 0.55
                                                     0.57 0.56 0.42
                                                                        0.68
## wrist
           0.21
                  0.73
                         0.32 0.74 0.66 0.62 0.63 0.56 0.66 0.57
                                                                       0.63
##
          forearm wrist
## age
            -0.09 0.21
             0.63 0.73
## weight
## height
             0.23 0.32
             0.62 0.74
## neck
## chest
             0.58 0.66
## abdom
             0.50 0.62
## hip
             0.55 0.63
## thigh
             0.57 0.56
## knee
             0.56 0.66
## ankle
             0.42 0.57
## biceps
             0.68 0.63
## forearm
             1.00 0.59
## wrist
             0.59 1.00
## these two methods should yield to same answers!
### (e)(2) Condition Numbers
Lily.X <- model.matrix(modLily)[,-1]</pre>
Lily.e <- eigen(t(Lily.X) %*% Lily.X)</pre>
Lily.e$val
   [1] 1.959256e+07 6.418499e+04 3.059739e+04 5.704341e+03 2.803947e+03
## [6] 1.934715e+03 1.030340e+03 6.376692e+02 5.280964e+02 4.318186e+02
## [11] 3.763758e+02 2.723663e+02 6.345357e+01
sqrt(Lily.e$val[1]/Lily.e$val)
         1.00000 17.47144 25.30482 58.60610 83.59121 100.63222 137.89717
## [8] 175.28623 192.61449 213.00748 228.15747 268.20620 555.67072
### (e)(3) VIF values
### There are two ways. The first one is to use the function "vif" in the package
→ "faraway"
require(faraway)
vif(Lily.X)
##
        age
               weight
                         height
                                     neck
                                              chest
                                                        abdom
                                                                    hip
                                                                            thigh
##
   2.250450 33.509320 1.674591 4.324463 9.460877 11.767073 14.796520 7.777865
##
       knee
                ankle
                         biceps
                                 forearm
                                              wrist
  4.612147 1.907961 3.619744 2.192492 3.377515
max(vif(Lily.X))
## [1] 33.50932
mean(vif(Lily.X))
## [1] 7.790078
```

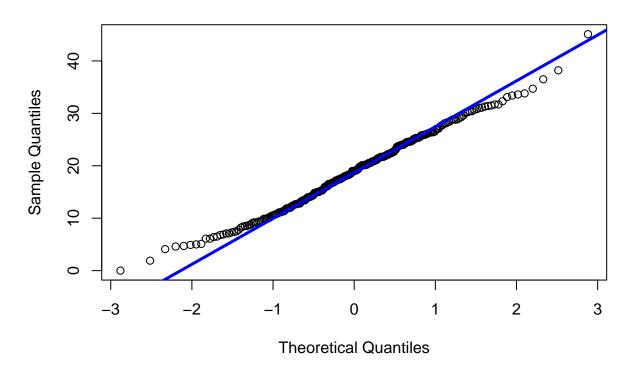
```
### The second one is to compute VIF on your own
p = dim(Lily.X)[2];
VIF1 <- NULL;</pre>
for (i in 1:p){
Rsqure.tmp <- summary(lm(Lily.X[,i] ~ Lily.X[,-i]))$r.squared;</pre>
VIF1 <- cbind(VIF1, 1/(1-Rsqure.tmp));</pre>
}
VIF1
##
           [,1]
                    [,2]
                             [,3]
                                       [,4]
                                                [,5]
                                                         [,6]
                                                                  [,7]
                                                                            [,8]
## [1,] 2.25045 33.50932 1.674591 4.324463 9.460877 11.76707 14.79652 7.777865
##
            [,9]
                    [,10]
                             [,11]
                                       [,12]
                                                [,13]
## [1,] 4.612147 1.907961 3.619744 2.192492 3.377515
colnames(VIF1) <- colnames(Lily.X);</pre>
VIF1
##
            age weight
                           height
                                      neck
                                               chest
                                                        abdom
                                                                          thigh
                                                                   hip
## [1,] 2.25045 33.50932 1.674591 4.324463 9.460877 11.76707 14.79652 7.777865
                    ankle biceps forearm
            knee
                                               wrist
## [1,] 4.612147 1.907961 3.619744 2.192492 3.377515
## Check whether this is the same as the "vif" function
vif(Lily.X)
##
         age
                weight
                          height
                                      neck
                                                chest
                                                          abdom
                                                                      hip
                                                                              thigh
## 2.250450 33.509320 1.674591 4.324463 9.460877 11.767073 14.796520 7.777865
##
        knee
                 ankle
                          biceps
                                  forearm
                                                wrist
## 4.612147 1.907961 3.619744 2.192492 3.377515
(f)
######Part (f): Transforming the response ########
require(MASS)
## Loading required package: MASS
### 1. summary statistics for the response variable
summary(fat$brozek)
##
      Min. 1st Qu. Median
                                              Max.
                              Mean 3rd Qu.
##
           12.80
                    19.00
                             18.94
                                     24.60
                                              45.10
c(mean(fat$brozek), sd(fat$brozek) )
## [1] 18.938492 7.750856
### 2. plots
hist(fat$brozek)
```

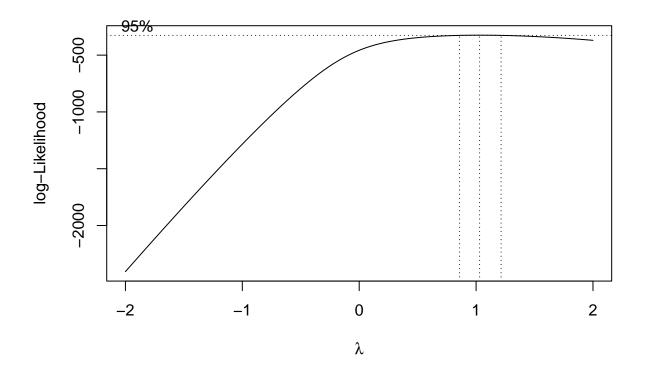
Histogram of fat\$brozek



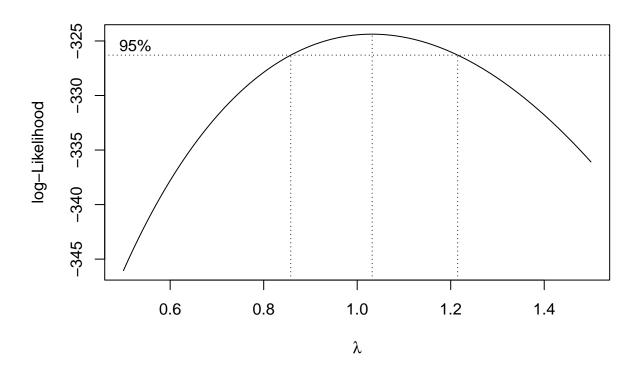
```
qqnorm(fat$brozek)
qqline(fat$brozek, lwd=3, col="blue")
```

Normal Q-Q Plot





boxcox(modLily1, lambda= seq(0.5, 1.5, by=0.001))



(g)

```
######Part (g): Transforming the predictor ########
### 1. add quadatic function of "abdom"
modLily2 <- lm( brozek ~ age + weight+ height+ neck+ chest + abdom+ I(abdom^2) +</pre>
                  hip+thigh+ knee+ ankle+ biceps+ forearm+ wrist, data=fat);
summary(modLily2)
##
## Call:
  lm(formula = brozek ~ age + weight + height + neck + chest +
##
       abdom + I(abdom^2) + hip + thigh + knee + ankle + biceps +
##
       forearm + wrist, data = fat)
##
## Residuals:
##
        Min
                       Median
                                    3Q
                  1Q
                                            Max
## -10.0626 -2.8326 -0.0641
                                2.5456
                                         8.9499
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -40.062052 18.064852 -2.218 0.02753 *
## age
                 0.059107
                            0.029538
                                       2.001
                                              0.04652 *
## weight
                -0.042509
                            0.050625
                                     -0.840
                                              0.40193
## height
                -0.117154
                            0.089551 -1.308 0.19206
## neck
                -0.401973
                            0.212552 -1.891 0.05982 .
```

```
## chest
               -0.051016
                           0.091007 -0.561 0.57562
## abdom
               1.581316 0.256695
                                     6.160 3.09e-09 ***
## I(abdom^2)
               -0.003852
                          0.001352 -2.849 0.00477 **
               -0.119470
                           0.136033 -0.878 0.38070
## hip
## thigh
                0.162969
                          0.133966
                                     1.217
                                            0.22500
## knee
               -0.167375
                          0.227527
                                    -0.736 0.46268
## ankle
                0.172261
                           0.202167
                                     0.852 0.39503
## biceps
                0.136916
                           0.156294
                                     0.876 0.38191
## forearm
                0.303322
                           0.187156
                                     1.621 0.10641
## wrist
               -1.574766
                           0.489489 -3.217 0.00148 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.93 on 237 degrees of freedom
## Multiple R-squared: 0.7573, Adjusted R-squared: 0.743
## F-statistic: 52.82 on 14 and 237 DF, p-value: < 2.2e-16
### 2. add both quadatic and cubic function of "abdom"
modLily3 <- lm( brozek ~ age + weight+ height+ neck+ chest + abdom+ I(abdom^2) +
                 I(abdom^3) + hip+thigh+ knee+ ankle+ biceps+ forearm+ wrist, data=fat);
summary(modLilv3)
##
## Call:
## lm(formula = brozek ~ age + weight + height + neck + chest +
      abdom + I(abdom^2) + I(abdom^3) + hip + thigh + knee + ankle +
##
      biceps + forearm + wrist, data = fat)
##
## Residuals:
                      Median
                                   3Q
       Min
                 1Q
                                          Max
                               2.5369
                                       9.0815
## -10.0071 -2.8404 -0.1842
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.061e+00 5.558e+01
                                     0.055 0.95613
## age
               6.226e-02 2.981e-02
                                     2.089 0.03780 *
## weight
              -4.106e-02 5.069e-02 -0.810 0.41871
## height
              -1.135e-01 8.973e-02 -1.264 0.20733
              -3.743e-01 2.154e-01 -1.738 0.08350
## neck
## chest
              -6.274e-02 9.218e-02 -0.681 0.49679
## abdom
              2.627e-01 1.628e+00
                                    0.161 0.87191
## I(abdom^2)
             9.046e-03 1.578e-02
                                     0.573 0.56698
## I(abdom^3) -4.139e-05 5.045e-05 -0.820 0.41278
## hip
              -1.079e-01 1.369e-01 -0.788 0.43128
## thigh
              1.705e-01 1.344e-01
                                     1.269 0.20572
## knee
              -1.815e-01 2.283e-01
                                    -0.795 0.42756
## ankle
               1.873e-01 2.031e-01
                                     0.922 0.35735
                                    0.911 0.36302
## biceps
              1.427e-01 1.566e-01
## forearm
               2.779e-01 1.898e-01
                                     1.464 0.14452
              -1.590e+00 4.902e-01 -3.243 0.00135 **
## wrist
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.932 on 236 degrees of freedom
```

Multiple R-squared: 0.758, Adjusted R-squared: 0.7426 ## F-statistic: 49.28 on 15 and 236 DF, p-value: < 2.2e-16