Problem Set 4

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Due Dec 13, 2023

This homework must be turned in on Brightspace by Dec. 13 2023. It must be your own work, and your own work only – you must not copy anyone's work, or allow anyone to copy yours. This extends to writing code. You may consult with others, but when you write up, you must do so alone.

Your homework submission must be written and submitted using Rmarkdown. No handwritten solutions will be accepted. No zip files will be accepted. Make sure we can read each line of code in the pdf document. You should submit the following:

- 1. A compiled PDF file named yourNetID_solutions.pdf containing your solutions to the problems.
- 2. A .Rmd file containing the code and text used to produce your compiled pdf named your-NetID solutions.Rmd.

Note that math can be typeset in Rmarkdown in the same way as Latex. Please make sure your answers are clearly structured in the Rmarkdown file:

- 1. Label each question part
- 2. Do not include written answers as code comments.
- 3. The code used to obtain the answer for each question part should accompany the written answer. Comment your code!

Problem 1 (100 points)

Despite the heated political and media rhetoric, there are a few causal estimates of the effect of expanded health insurance on healthcare outcomes. One landmark study, the Oregon Health Insurance Experiment, covered new ground by utilizing a randomized control trial implemented by the state of Oregon. To allocate a limited number of eligible coverage slots for the state's Medicaid expansion, about 30,000 low-income, uninsured adults (out of about 90,000 wait-list applicants) were randomly selected by lottery to be allowed to apply for Medicaid coverage. Researchers collected observable measure of health (blood pressure, cholesterol, blood sugar levels, and depression), as well as hospital visitations and healthcare expenses for 6,387 selected adults and 5,842 not selected adults.

For this problem, we will use the OHIE.dta file.

- treatment selected in the lottery to sign up for Medicaid (instrument)
- ohp_all_ever_admin Ever enrolled in Medicaid after notification of lottery results (compliance)
- tab2bp_hyper Outcome: Binary indicator for elevated blood pressure (1 indicates a high blood pressure)
- tab2phqtot_high Outcome: Binary indicator for depression
- tab4_catastrophic_exp_inp Outcome: Indicator for catastrophic medical expenditure (1 if their total out-of-pocket medical expenses are larger than 30% of their household income)
- tab5_needmet_med_inp Outcome: Binary indicator of whether the participant feels that they received all needed medical care in past 12 months

```
# Load in the data
data <- haven::read_dta("OHIE.dta")</pre>
```

Hint: This was an experiment with imperfect compliance. Instead of creating a "participated" or "complied" variable, simply use "treatment" as the instrument and "ohp_all_ever_admin" (enrollment in Medicaid) as the main independent variable of interest.

Question A (25 points)

Estimate the intent-to-treat effects of being selected to sign up for Medicaid on each of the four outcomes (elevated blood pressure, depression, catastrophic medical expenditure, and whether respondents had their health care needs met). Provide 95% confidence intervals for each estimate and interpret your results. (Use lm_robust)

```
# Estimate the ITT on elevated blood pressure
itt_bp <- lm_robust(tab2bp_hyper ~ treatment, data = data)
tidy(itt_bp)</pre>
```

```
##
            term estimate std.error statistic
                                                  p.value conf.low conf.high
                                                                                 df
## 1 (Intercept)
                   0.1591
                             0.00480
                                        33.182 3.21e-231
                                                            0.1497
                                                                       0.1685 12186
                  -0.0016
## 2
                             0.00662
                                        -0.242 8.09e-01
                                                           -0.0146
                                                                       0.0114 12186
       treatment
##
          outcome
## 1 tab2bp_hyper
## 2 tab2bp_hyper
```

The estimated effect is -0.0016 with a confidence interval of [-0.0146, 0.0114]. This interval includes 0, so we do not reject the null hypothesis of no effect since this result is not statistically significant. We conclude that being selected to sign up for Medicaid has no effect on elevated blood pressure.

```
# Estimate the ITT on depression
itt_dep <- lm_robust(tab2phqtot_high ~ treatment, data = data)
tidy(itt_dep)</pre>
```

```
##
            term estimate std.error statistic p.value conf.low conf.high
## 1 (Intercept)
                                         50.33 0.00e+00
                                                            0.292
                   0.3037
                             0.00603
                                                                     0.3155 12159
                  -0.0349
                             0.00821
                                         -4.26 2.09e-05
                                                           -0.051
                                                                    -0.0188 12159
## 2
       treatment
##
             outcome
## 1 tab2phqtot_high
## 2 tab2phqtot_high
```

The estimated effect is -0.0349 with a confidence interval of [-0.051, -0.0188]. This interval doesn't include 0, so we reject the null hypothesis of no effect since this result is statistically significant. We conclude that being selected to sign up for Medicaid makes it less likely to be depressed.

```
# Estimate the ITT on catastrophic expenditures
itt_exp <- lm_robust(tab4_catastrophic_exp_inp ~ treatment, data = data)
tidy(itt_exp)</pre>
```

```
##
            term estimate std.error statistic p.value conf.low conf.high
## 1 (Intercept)
                                        17.92 6.77e-71
                                                          0.0479
                   0.0538
                            0.00300
                                                                   0.05971 11793
## 2
       treatment -0.0153
                            0.00388
                                         -3.94 8.34e-05 -0.0229 -0.00766 11793
##
                       outcome
## 1 tab4_catastrophic_exp_inp
## 2 tab4_catastrophic_exp_inp
```

The estimated effect is -0.0153 with a confidence interval of [-0.0229, -0.00766]. This interval doesn't include 0, so we reject the null hypothesis of no effect since this result is statistically significant. We conclude that being selected to sign up for Medicaid makes it less likely to have catastrophic medical expenditure.

```
# Estimate the ITT on "needs met"
itt_needs <- lm_robust(tab5_needmet_med_inp ~ treatment, data = data)
tidy(itt_needs)</pre>
```

```
##
            term estimate std.error statistic p.value conf.low conf.high
                                         96.02 0.00e+00
                                                                     0.6249 12214
## 1 (Intercept)
                   0.6124
                             0.00638
                                                           0.5999
## 2
       treatment
                   0.0345
                             0.00875
                                          3.94 8.19e-05
                                                           0.0173
                                                                     0.0516 12214
##
                  outcome
## 1 tab5_needmet_med_inp
## 2 tab5 needmet med inp
```

The estimated effect is 0.0345 with a confidence interval of [0.0173, 0.0516]. This interval doesn't include 0, so we reject the null hypothesis of no effect since this result is statistically significant. We conclude that being selected to sign up for Medicaid makes it more likely for patients feel their medical needs are met.

Question B (25 points)

Suppose that researchers actually wanted to estimate the effect of Medicaid enrollment (ohp_all_ever_admin) on each of the four outcomes. Suppose they first used a naive regression of each of the the outcomes on the indicator of Medicaid enrollment. Report a 95% confidence interval for each of your estimates and interpret your results. Why might these be biased estimates for the causal effect of Medicaid enrollment?

```
# Estimate the Naive OLS effect on elevated blood pressure
ols_bp <- lm_robust(tab2bp_hyper ~ ohp_all_ever_admin, data = data)
tidy(ols_bp)</pre>
```

```
##
                   term estimate std.error statistic p.value conf.low conf.high
## 1
            (Intercept)
                          0.1634
                                    0.00397
                                                41.21 0.0000
                                                                0.1557
                                                                          0.17122
## 2 ohp all ever admin
                         -0.0181
                                    0.00716
                                                -2.52 0.0117
                                                               -0.0321
##
        df
                outcome
## 1 12186 tab2bp hyper
## 2 12186 tab2bp_hyper
```

The estimated effect is -0.0181 with a confidence interval of [-0.0321, -0.00401]. This interval doesn't include 0, so we reject the null hypothesis of no effect since this result is statistically significant. We conclude that being enrolled in Medicaid makes it less likely to have elevated blood pressure.

```
# Estimate the Naive OLS effect on depression
ols_dep <- lm_robust(tab2phqtot_high ~ ohp_all_ever_admin, data = data)
tidy(ols_dep)</pre>
```

```
##
                   term estimate std.error statistic p.value conf.low conf.high
## 1
                                                                             0.2806
                                    0.00477
                                                 56.83 0.00e+00
                                                                  0.2619
            (Intercept)
                           0.2713
                                    0.00924
                                                  5.34 9.52e-08
                                                                  0.0312
                                                                             0.0674
## 2 ohp_all_ever_admin
                           0.0493
        df
                   outcome
## 1 12159 tab2phqtot_high
## 2 12159 tab2phqtot_high
```

The estimated effect is 0.0493 with a confidence interval of [0.0312, 0.0674]. This interval doesn't include 0, so we reject the null hypothesis of no effect since this result is statistically significant. We conclude that being enrolled in Medicaid makes it more likely to be depressed.

```
# Estimate the Naive OLS effect on catastrophic expenditures
ols_exp <- lm_robust(tab4_catastrophic_exp_inp ~ ohp_all_ever_admin, data = data)
tidy(ols_exp)</pre>
```

```
##
                   term estimate std.error statistic p.value conf.low conf.high
## 1
            (Intercept)
                                   0.00235
                                                20.81 1.66e-94
                                                                 0.0443
                                                                          0.05355
                          0.0489
## 2 ohp_all_ever_admin
                         -0.0107
                                   0.00405
                                                -2.65 8.13e-03 -0.0187
                                                                         -0.00278
##
        df
                             outcome
## 1 11793 tab4_catastrophic_exp_inp
## 2 11793 tab4_catastrophic_exp_inp
```

The estimated effect is -0.0107 with a confidence interval of [-0.0187, -0.00278]. This interval doesn't include 0, so we reject the null hypothesis of no effect since this result is statistically significant. We conclude that being enrolled in Medicaid makes it less likely to have catastrophic medical expenditure.

```
# Naive OLS estimate on needs met
ols_needs <- lm_robust(tab5_needmet_med_inp ~ ohp_all_ever_admin, data = data)
tidy(ols_needs)</pre>
```

```
##
                   term estimate std.error statistic p.value conf.low conf.high
## 1
                                    0.00522
                                               117.40 0.00e+00
                                                                  0.6026
            (Intercept)
                           0.6128
                                                                            0.6230
                                                                            0.0799
## 2 ohp all ever admin
                          0.0613
                                    0.00948
                                                 6.46 1.08e-10
                                                                  0.0427
##
        df
                        outcome
## 1 12214 tab5_needmet_med_inp
## 2 12214 tab5_needmet_med_inp
```

The estimated effect is 0.0613 with a confidence interval of [0.0427, 0.0799]. This interval doesn't include 0, so we reject the null hypothesis of no effect since this result is statistically significant. We conclude that being enrolled in Medicaid makes it more likely for patients feel their medical needs are met.

These might be biased estimates because unobserved confounders may be present since enrollment is not done randomly. These confounders would affect both patient outcome and the ability for patients to enroll in Medicaid. For example, there may be socioeconomic factors (such as poverty) that make certain people more eligible to enroll in Medicaid, that also generally negatively affect peoples' health outcomes.

Question C (25 points)

Suppose we were to use assignment to treatment as an instrument for actually receiving Medicaid coverage.

Consider that not everyone who was selected to apply for Medicaid actually ended up applying and receiving coverage. Likewise, some applicants who were not selected to receive the treatment nevertheless were eventually covered. What were the compliance rates (the level of Medicaid enrollment) for subjects who were selected and subjects who were not selected? Use a "first stage" regression to estimate the effect of being selected on Medicaid enrollment to estimate the compliance rates. Is the instrument of assignment-to-treatment a strong instrument for actual Medicaid enrollment?

```
# First Stage OLS
linreg <- lm_robust(ohp_all_ever_admin ~ treatment, data = data)</pre>
tidy(linreg)
##
            term estimate std.error statistic p.value conf.low conf.high
                                                                              df
## 1 (Intercept)
                    0.145
                            0.00347
                                          42.0
                                                     0
                                                          0.139
                                                                    0.152 20743
## 2
       treatment
                    0.236
                            0.00589
                                          40.1
                                                     0
                                                          0.225
                                                                     0.248 20743
##
                outcome
## 1 ohp all ever admin
## 2 ohp_all_ever_admin
# null model (compliance given an intercept only model)
null_mod<-lm_robust(ohp_all_ever_admin ~ 1, data=data)</pre>
# F - Stat for Instrument Strength (use waldtest)
waldtest(linreg, null_mod, test = 'F')
## Wald test
## Model 1: ohp_all_ever_admin ~ treatment
## Model 2: ohp_all_ever_admin ~ 1
     Res.Df Df
                  F Pr(>F)
     20743
## 1
## 2 20744 -1 1610 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

14.5% of participants who weren't selected still enrolled in the Medicaid program. Being selected in the lottery increased participants' chances of enrollment in Medicaid by 23.6% for a total of 38.1% of participants who were selected. This implies that 23.6% of the subjects were compliers who would enroll if selected and would not otherwise. Since the estimated effect of being selected and the sample size is large, this instrument is strong. The calculated F-statistic was 1610, which is very high, with an extremely small p-value of less than $2 \cdot 10^{-16}$.

Question D (25 points)

Now estimate the effect of Medicaid enrollment on each of the four outcomes using an instrumental variables strategy. Report a 95% confidence interval for your estimates and interpret your results. Compare the estimates to those you obtained in Question B.

```
# Estimate the IV effect on elevated blood pressure (use iv_robust())
iv_bp <- iv_robust(tab2bp_hyper ~ ohp_all_ever_admin|treatment, data = data)
tidy(iv_bp)</pre>
```

```
##
                   term estimate std.error statistic p.value conf.low conf.high
## 1
            (Intercept)
                           0.1601
                                    0.00818
                                               19.567 5.71e-84
                                                                  0.1440
                                                                            0.1761
## 2 ohp_all_ever_admin
                         -0.0063
                                    0.02606
                                               -0.242 8.09e-01
                                                                -0.0574
                                                                            0.0448
        df
                outcome
## 1 12186 tab2bp_hyper
## 2 12186 tab2bp hyper
```

The IV estimate for the effect of Medicaid enrollment on elevated blood pressure is -0.0063. The 95% confidence interval for this estimate is [-0.0574, 0.0448]. Since 0 falls within this interval, we fail to reject the null hypothesis of no effect since the result is not statistically significant. This result differs from the previous naive OLS result, which suggested that enrollment in Medicaid does negatively affect participants' chances of elevated blood pressure. The IV estimate suggests that enrollment in Medicaid doesn't affect participants' chances of elevated blood pressure and the previously observed effect was due to unobserved confounders.

```
# Estimate the IV effect on depression
iv_dep <- iv_robust(tab2phqtot_high ~ ohp_all_ever_admin|treatment, data = data)
tidy(iv_dep)</pre>
```

```
##
                    term estimate std.error statistic
                                                         p.value conf.low conf.high
## 1
                            0.325
                                     0.0104
                                                 31.26 2.38e-206
                                                                     0.304
                                                                              0.3452
            (Intercept)
## 2 ohp_all_ever_admin
                           -0.138
                                     0.0329
                                                 -4.19 2.84e-05
                                                                    -0.202
                                                                             -0.0732
        df
                    outcome
## 1 12159 tab2phqtot high
## 2 12159 tab2phqtot high
```

The IV estimate for the effect of Medicaid enrollment on depression is -0.138. The 95% confidence interval for this estimate is [-0.202, -0.0732]. Since 0 doesn't fall within this interval, we reject the null hypothesis of no effect since the result is statistically significant. This result differs from the previous naive OLS result, which suggested that enrollment in Medicaid increases participants' chances of depression. The IV estimate suggests that enrollment in Medicaid decreases participants' chances of depression.

```
##
                   term estimate std.error statistic p.value conf.low conf.high
## 1
            (Intercept)
                                    0.00508
                                                12.43 3.03e-35
                          0.0631
                                                                  0.0532
  2 ohp_all_ever_admin
                         -0.0604
                                                -3.91 9.16e-05
                                                                -0.0906
                                                                           -0.0301
                                    0.01543
##
        df
                              outcome
## 1 11793 tab4_catastrophic_exp_inp
## 2 11793 tab4_catastrophic_exp_inp
```

The IV estimate for the effect of Medicaid enrollment on catastrophic expenditures is -0.0604. The 95% confidence interval for this estimate is [-0.0906, -0.0301]. Since 0 doesn't fall within this interval, we reject the null hypothesis of no effect since the result is statistically significant. This result agrees with the previous naive OLS result, which suggested that enrollment in Medicaid decreases participants' chances of having catastrophic medical expenditure. The IV estimated effect is larger, with a larger standard error as well.

```
# IV estimate on needs met
iv_needs <- iv_robust(tab5_needmet_med_inp ~ ohp_all_ever_admin|treatment, data = data)
tidy(iv_needs)</pre>
```

```
##
                   term estimate std.error statistic p.value conf.low conf.high
                                                 54.45 0.00e+00
## 1
            (Intercept)
                            0.592
                                     0.0109
                                                                    0.570
                                                                              0.613
## 2 ohp_all_ever_admin
                            0.135
                                     0.0344
                                                  3.94 8.35e-05
                                                                    0.068
                                                                              0.203
        df
                         outcome
## 1 12214 tab5_needmet_med_inp
## 2 12214 tab5_needmet_med_inp
```

The IV estimate for the effect of Medicaid enrollment on medical needs met is 0.135. The 95% confidence interval for this estimate is [0.068, 0.203]. Since 0 doesn't fall within this interval, we reject the null hypothesis of no effect since the result is statistically significant. This result agrees with the previous naive OLS result, which suggested that enrollment in Medicaid increases participants' chances of feeling that their medical needs are met. The IV estimated effect is larger, with a larger standard error as well.