Q1.

The pixels in an image are scanned from left to the right and from the top to the bottom. Each new pixel is predicted by the average of the pixel above and the one to the left. Let f and F represent the original and the predicted values, and e = f - F is the prediction error. The prediction error is quantized to "0", "B", or "-B" according to:

Find the optimum weights while predicting the image such that mean square error is minimum. Repeat the process if you use all nearest neighbor to predict the pixel value. Repeat the process on any image of your choice

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new pixel is predicted by the average of the pixel above and the one to the left. Let f and F
represent the original and the predicted values, and e = f - F is the prediction error. The prediction
error is quantized to "0", "B", or "-B" according to:

$$\hat{e} = \begin{cases} -B & e < -T & 0 & 0 & 1 \\ 0 & -T \le e \le T & 2 & 2 & 2 \\ B & e > T & 6 & 6 & 5 \end{cases}$$



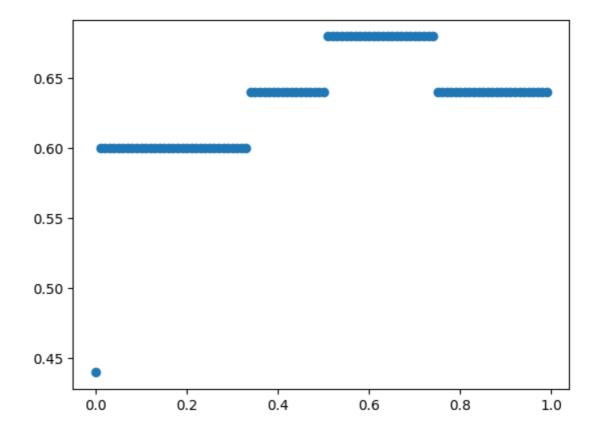
Find the optimum weights while predicting the image such that mean square error is minimum. Repeat the process if you use all nearest neighbor to predict the pixel value.

Repeat the process on any image of your choice

```
In [1]: import numpy as np
        import cv2 as cv
        from matplotlib import pyplot as plt
In [2]: img = np.array([
           [0,0,1,5,6],
           [0,0,1,5,6],
           [2,2,4,7,8],
            [3,3,7,4,2],
            [6,6,5,1,0]
        ])
In [3]: pad = np.pad(img,1)
        pad
Out[3]: array([[0, 0, 0, 0, 0, 0],
               [0, 0, 0, 1, 5, 6, 0],
               [0, 0, 0, 1, 5, 6, 0],
               [0, 2, 2, 4, 7, 8, 0],
               [0, 3, 3, 7, 4, 2, 0],
               [0, 6, 6, 5, 1, 0, 0],
               [0, 0, 0, 0, 0, 0, 0]])
In [4]: w = pad[1:-1, :-2]
        e = pad[1:-1, 2:]
```

n = pad[:-2, 1:-1]s = pad[2:, 1:-1]

```
nw = pad[:-2, :-2]
        ne = pad[:-2, 2:]
        se = pad[2:, 2:]
        sw = pad[2:, :-2]
In [5]: def average(arrays, weights):
            shape = arrays[0].shape
            out = np.zeros(shape)
            norm = np.sum(np.array(weights))
            for a,w in zip(arrays, weights):
                out += a*w/norm
            return out
In [6]: def error(orig, pred, B=1, T=1):
            e = orig - pred
            r1 = e < -T
            r2a = -T <= e
            r2b = e \ll T
            r3 = T < e
            e[r2a] = 0
            e[r2b] = 0
            e[r1] = -B
            e[r3] = B
            return e
In [7]: def mse(arr):
            return np.mean(np.square(arr))
In [8]: def find2optimum():
            x = []
            y = []
            for weight in np.arange(start=0, stop=1, step=0.01):
                pred = average([n,w], [weight, 1-weight])
                E = error(img, pred)
                e = mse(E)
                x.append(weight)
                y.append(e)
            plt.scatter(x,y)
In [9]: find2optimum()
```



Result (left and top)

We obtain that the optimal weight is 0 for top and 1 for left. The MSE will be 0.4, taking B=1 and T=1

```
In [10]: def find8optimum(start=0, stop=1, step=0.25):
             err_Arr = []
             weight\_Arr = []
             for w1 in np.arange(start, stop, step):
                 for w2 in np.arange(start, stop, step):
                     for w3 in np.arange(start, stop, step):
                          for w4 in np.arange(start, stop, step):
                              for w5 in np.arange(start, stop, step):
                                  for w6 in np.arange(start, stop, step):
                                      for w7 in np.arange(start, stop, step):
                                          for w8 in np.arange(start, stop, step):
                                              pred = average([n, ne, e, se, s, sw,
                                              E = error(img, pred)
                                              err = mse(E)
                                              if not np.isnan(err):
                                                  err_Arr.append(err)
                                                  weight_Arr.append([w1,w2,w3,w4,w5
             min_idx = np.argmin(err_Arr)
             min_val = err_Arr[min_idx]
             min weight = weight Arr[min idx]
             print(f"Minimum error is {min_val} with weights {min_weight}")
```

In [11]: find8optimum(step=0.5)

Minimum error is 0.36 with weights [0.0, 0.0, 0.0, 0.0, 0.0, 0.5, 0.0, 0.0]

/var/folders/v_/7h9hf8f91m9cxmhg0xrmbstr0000gn/T/ipykernel_25892/249885976
3.py:6: RuntimeWarning: invalid value encountered in divide
 out += a*w/norm

In [12]: find8optimum(step=0.25)

/var/folders/v_/7h9hf8f91m9cxmhg0xrmbstr0000gn/T/ipykernel_25892/249885976
3.py:6: RuntimeWarning: invalid value encountered in divide
 out += a*w/norm

Minimum error is 0.32 with weights [0.0, 0.0, 0.0, 0.0, 0.25, 0.0, 0.5, 0.0]

In [13]: find8optimum(step=0.2)

/var/folders/v_/7h9hf8f91m9cxmhg0xrmbstr0000gn/T/ipykernel_25892/249885976
3.py:6: RuntimeWarning: invalid value encountered in divide
 out += a*w/norm

Minimum error is 0.32 with weights [0.0, 0.0, 0.0, 0.0, 0.2, 0.0, 0.4, 0.0]

In [14]: find8optimum(step=0.15)

/var/folders/v_/7h9hf8f91m9cxmhg0xrmbstr0000gn/T/ipykernel_25892/249885976
3.py:6: RuntimeWarning: invalid value encountered in divide
 out += a*w/norm

Minimum error is 0.32 with weights [0.0, 0.0, 0.0, 0.0, 0.15, 0.0, 0.3, 0.0]

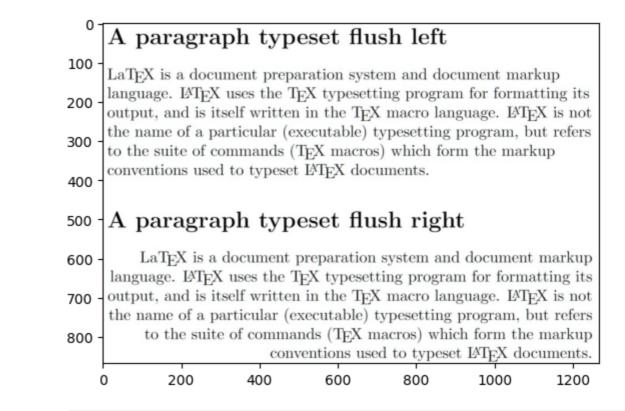
Result (all nearest neighbors)

Minimum error is 0.32 with weights [0.0, 0.0, 0.0, 0.0, 0.15, 0.0, 0.3, 0.0]

We are following OpenCV's format for run-length encoding where tuples are (start_col, end_col, row)

```
In [1]: def runlength(mat):
            a = []
            for r in range(len(mat)):
                 arr=mat[r]
                 start=0
                 end=0
                 isCounting=False
                 for i in range(len(arr)):
                     if arr[i] == 255 and isCounting == False:
                         isCounting=True
                         start=i
                           print("starting",i)
                     if arr[i] == 0 and isCounting == True:
                         end=i-1
                         isCounting=False
                           print("ending", i)
                         a.append((start,end,r))
                 if arr[len(arr)-1] == 255:
                     end=len(arr)-1
                     a.append((start,end,r))
            return a
In [2]: import cv2 as cv
        import numpy as np
        import matplotlib.pyplot as plt
In [3]: img = cv.imread("img.jpeg")
        _, b = cv.threshold(img, 30, 255, cv.THRESH_BINARY)
In [6]: plt.imshow(img)
```

Out[6]: <matplotlib.image.AxesImage at 0x17db05610>



In [4]: b = np.mean(b,axis=-1,dtype=int)

In [5]: runlength(b)

```
Out[5]:
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In [ ]:
In [ ]:
```

Huffman coding is a variable-length prefix coding technique. It relies on creating a variable-length code for each symbol (in this case, pixel values) based on their frequency of occurrence in the image. It does not involve any mathematical transforms.

```
In [60]: import heapq
         import collections
         from PIL import Image
         image_path = r"img.jpeg"
         image = Image.open(image_path)
         image = image.resize((1024, 1024))
         pixel_values = list(image.getdata())
         frq = collections.Counter(pixel_values)
         heap = [[weight, [pixel, ""]] for pixel, weight in frq.items()]
         heapq.heapify(heap)
         while len(heap) > 1:
             lo = heapq.heappop(heap)
             hi = heapq.heappop(heap)
             for pair in lo[1:]:
                 pair[1] = '0' + pair[1]
             for pair in hi[1:]:
                 pair[1] = '1' + pair[1]
             heapq.heappush(heap, [lo[0] + hi[0]] + lo[1:] + hi[1:])
         huffman_dict = dict(heap[0][1:])
         encoding = ''.join(huffman_dict[pixel] for pixel in pixel_values)
         original_size = len(pixel_values) * 8 # Assuming 8 bits per pixel
         compressed_size = len(encoding)
         huffman_compression_ratio = original_size / compressed_size
         print(f"Huffman Compression Ratio: {huffman_compression_ratio:}")
```

Huffman Compression Ratio: 2.488950814740001

DCT is a mathematical transform that converts image data into a frequency-domain representation. It is widely used in JPEG compression. DCT captures the frequency components of an image, allowing for efficient compression by quantizing high-frequency components.

```
In [65]: import numpy as np
    from scipy.fftpack import dct
    from PIL import Image

    image_path = r'img.jpeg'
    image = Image.open(image_path)
    # print(image.size)
    image = image.resize((1024, 1024))

gray = image.convert("L")
```

```
imarr = np.array(gray)
# print(imarr.shape)
block_size = 8
quantmat = np.array([[16, 11, 10, 16, 24, 40, 51, 61],
                                [12, 12, 14, 19, 26, 58, 60, 55],
                                [14, 13, 16, 24, 40, 57, 69, 56],
                                [14, 17, 22, 29, 51, 87, 80, 62],
                                [18, 22, 37, 56, 68, 109, 103, 77],
                                [24, 35, 55, 64, 81, 104, 113, 92],
                                [49, 64, 78, 87, 103, 121, 120, 101],
                                [72, 92, 95, 98, 112, 100, 103, 99]])
def quantize(k, Q):
    return np.round(k / Q)
def dequantize(l, Q):
    return l * Q
height, width = imarr.shape
dctb = np.zeros_like(imarr)
for i in range(0, height, block_size):
    for j in range(0, width, block_size):
        block = imarr[i:i + block_size, j:j + block_size]
        dct_block = dct(dct(block, axis=0), axis=1)
        qb = quantize(dct_block, quantmat)
        dctb[i:i + block_size, j:j + block_size] = qb
original = height * width * 8
compressed = dctb.size * np.log2(quantmat.max())
compression_ratio = original / compressed
print(f"Compression Ratio: {compression_ratio:}")
```

Compression Ratio: 1.1562593052715515

KL transform (Karhunen-Loève transform) is a linear transformation that converts data into a set of uncorrelated variables (principal components). It is used for decorrelation and dimensionality reduction.

```
image_path = r'img.jpeg'
image = Image.open(image_path)
image = image.resize((1024, 1024))

gray = image.convert("L")
imarr = np.array(gray)
covariance_matrix = np.cov(imarr.astype(float))
e1, e = np.linalg.eigh(covariance_matrix)

ind = np.argsort(e1)[::-1]
e1 = e1[ind]
e = e[:, ind]

compression_ratio = 0.1
```

```
eign = int(compression_ratio * len(e1))
sel = e[:, :eign]
compressed_image = np.dot(sel.T, imarr.T).T
newimage = np.dot(compressed_image, sel.T)

original = imarr.size * 8
compressed = eign * (len(e1) + 1) * 64

compression_efficiency = original / compressed

print(f"Compression Efficiency: {compression_efficiency:.2f}")

# matplotlib.pyplot.imshow(image, cmap='gray')
# matplotlib.pyplot.imshow(newimage, cmap='gray')
```

Compression Efficiency: 1.25

Haar wavelet transform is a mathematical technique that decomposes an image into wavelet coefficients representing different levels of detail.

```
In [64]: import numpy as np
         from PIL import Image
         import pywt
         import sys
         image_path = r'img.jpeg'
          image = Image.open(image_path)
          image = image.resize((1024, 1024))
         gray = image.convert("L")
         imarr = np.array(gray)
         coeffs = pywt.dwt2(imarr, 'haar')
         threshold = 15.0
         qc = [np.where(np.abs(coef) < threshold, 0, coef) for coef in coeffs]</pre>
          reconstructed_image = pywt.idwt2(qc, 'haar')
         original_size_bits = imarr.size * 8
         compressed_size_bits = sum([np.sum(np.abs(coef) > 0) * np.ceil(np.log2(np.abs(coef) > 0))
         compression_efficiency = original_size_bits / compressed_size_bits
         print(f"Compression Efficiency: {compression_efficiency:.2f}")
```

Compression Efficiency: 2.79

Conclusion:

Huffman Coding: Huffman coding is typically used for lossless compression, so it preserves image quality but may not achieve very high compression ratios.

DCT Coding: DCT coding is often used for lossy compression. The trade-off between image quality and compression ratio can be adjusted by varying the quantization step size.

KL Transform-Based Coding: KL transform can be used for both lossless and lossy compression, offering a flexible trade-off between image quality and compression

ratio.

Haar Wavelet Compression: Haar wavelet compression can also be used for both lossless and lossy compression, providing control over image quality and compression ratio.