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R0 = 6 378 137;
μ = 3.9860047 * 1014;

h0 = 1 000 000;
R = R0 + h0;
h[x_, y_] :=  $\sqrt{x^2 + y^2} - R0$ 
T[R_] :=  $2 * \pi * \sqrt{R^3 / \mu}$ ;
Vx0 =  $\sqrt{\mu / R}$ ;
Rcube[x_, y_] :=  $\left(\sqrt{x^2 + y^2}\right)^3$ ;
crkamat = {{1/2}, {0, 1/2}, {0, 0, 1}};
crkbvec = {1/6, 1/3, 1/3, 1/6};
crkcvec = {1/2, 1/2, 1};
ClassicalRungeKuttaCoefficients[4, p_] := N[{crkamat, crkbvec, crkcvec}, p];
benchmarkTest[tStart_, tEnd_, tStep_, printOutput_, rungeKutta4_] :=
Module[{},
system := {
x'[t] == Vx[t],
y'[t] == Vy[t],
Vx'[t] == -μ / Rcube[x[t], y[t]] * x[t],
Vy'[t] == -μ / Rcube[x[t], y[t]] * y[t],
x[0] == 0,
y[0] == R,
Vx[0] == Vx0,
Vy[0] == 0
};
solution := If[rungeKutta4,
First@NDSolve[system, {x, y, Vx, Vy}, {t, 0, 10 000},
Method → {"ExplicitRungeKutta", "DifferenceOrder" → 4, "Coefficients" →
ClassicalRungeKuttaCoefficients}, StartingStepSize → tStep]
,
First@NDSolve[
system, {x, y, Vx, Vy}, {t, 0, 10 000}, PrecisionGoal → 10
]
];
{Vx1, Vy1, x1, y1} = {Vx, Vy, x, y} /. solution;
Print[Vx1[10 000 - tStep] - -6314.591];
Print[Vy1[10 000 - tStep] - 3761.713];
Print[x1[10 000 - tStep] + 3 776 042];
Print[y1[10 000 - tStep] - -6 338 645];

Print[Vx1[10 000 - 1]];
Print[Vy1[10 000 - 1]];
Print[x1[10 000 - 1]];
Print[y1[10 000 - 1]];

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];

steps = {1, 0.1, 0.01};

times = ConstantArray[0, 12];

For[i = 3, i <= Length[steps], i++,
  times[[i]] =
    First@AbsoluteTiming[benchmarkTest[0, 10 000, steps[[i]], False, False]];
  times[[i + 6]] = First@AbsoluteTiming[
    benchmarkTest[0, 10 000, steps[[i]], False, True]];
]

times

-0.0000300461
-0.000377808
0.279127
0.467148
-6318.3
3755.48
-3.76979 × 106
-6.34237 × 106
-0.0000369835
-0.000393715
0.297848
0.456064
-6318.3
3755.48
-3.76979 × 106
-6.34237 × 106
{0, 0, 0.011001, 0, 0, 0, 0, 0, 4.773273, 0, 0, 0}

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