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# GSURE Denoising enables training of higher quality generative priors for accelerated Multi-Coil MRI Reconstruction

Asad Aali<sup>1</sup>, Marius Arvinte<sup>1,2</sup>, Sidharth Kumar<sup>1</sup>, Yamin Ishraq Arefeen<sup>1</sup>, and Jonathan I. Tamir<sup>1</sup>

<sup>1</sup>*Chandra Family Department of Electrical and Computer Engineering, The University of Texas at Austin, Austin, TX, United States*, <sup>2</sup>*Intel Corporation, Hillsboro, OR, United States*

Asad Aali  
MS Student  
Electrical & Computer Engineering  
The University of Texas at Austin



# UT Computational Sensing and Imaging Lab

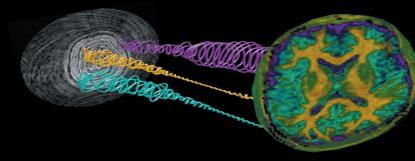
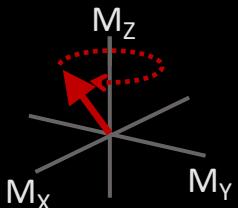
- Joint design of imaging system and software
- Particular focus on application to MRI
- Work with clinicians to translate work to hospital



Jon Tamir, PhD  
Assistant Professor, ECE, UT Austin  
<http://www.jtsense.com/>    <https://github.com/utcsilab>

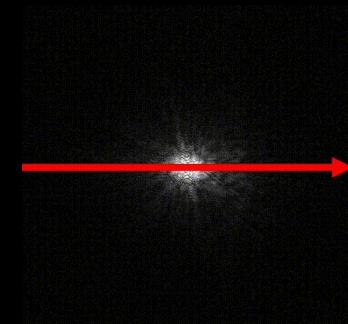
# Computational MRI

## Imaging physics

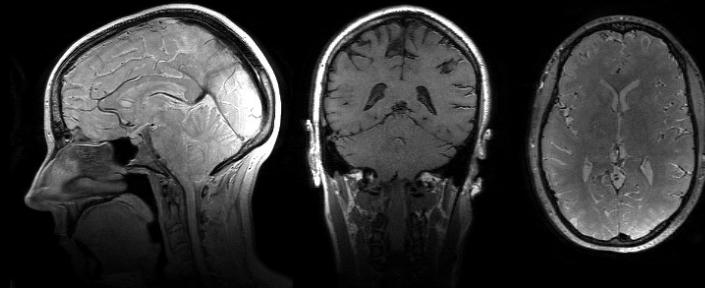


Prior knowledge

Acquisition

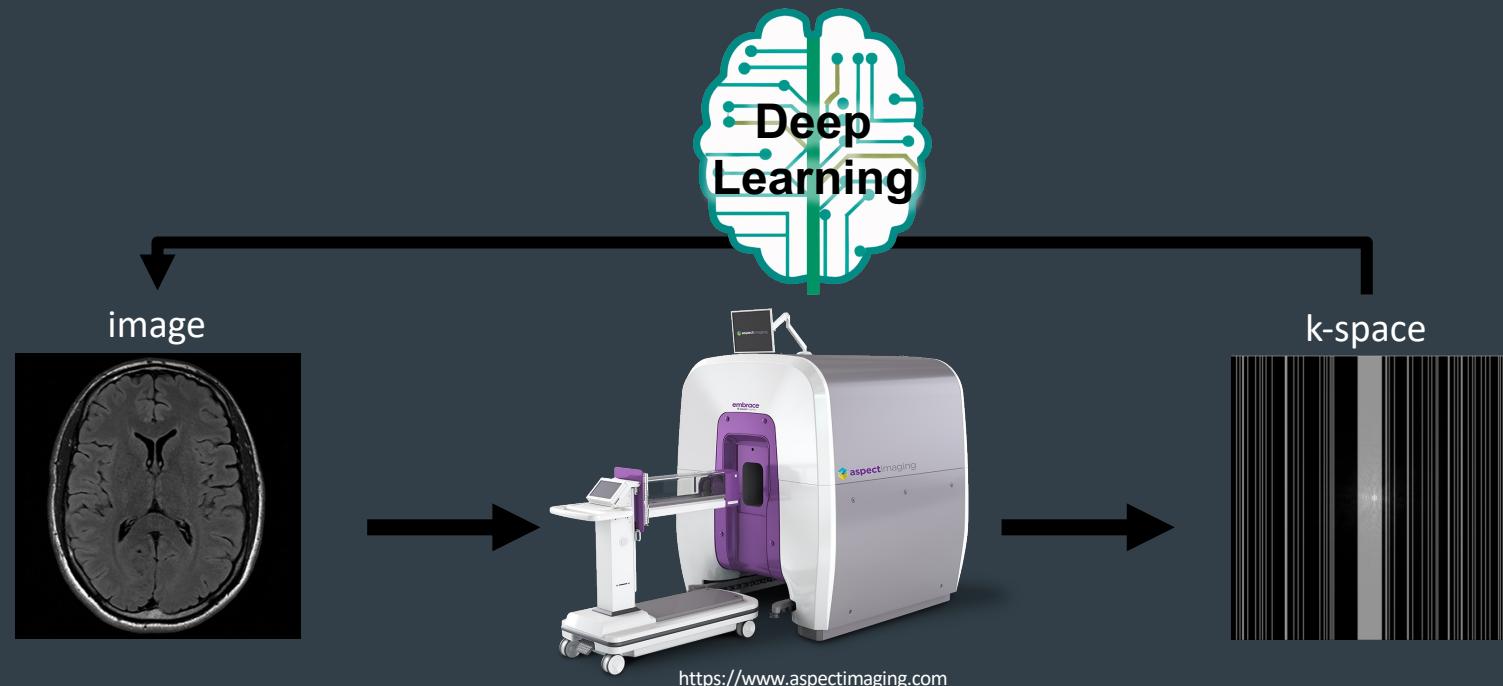


Reconstruction



# Deep learning inversion for MRI

1. End-to-end supervised training
2. Distribution learning / generative modeling



# Generative models are powerful image generators

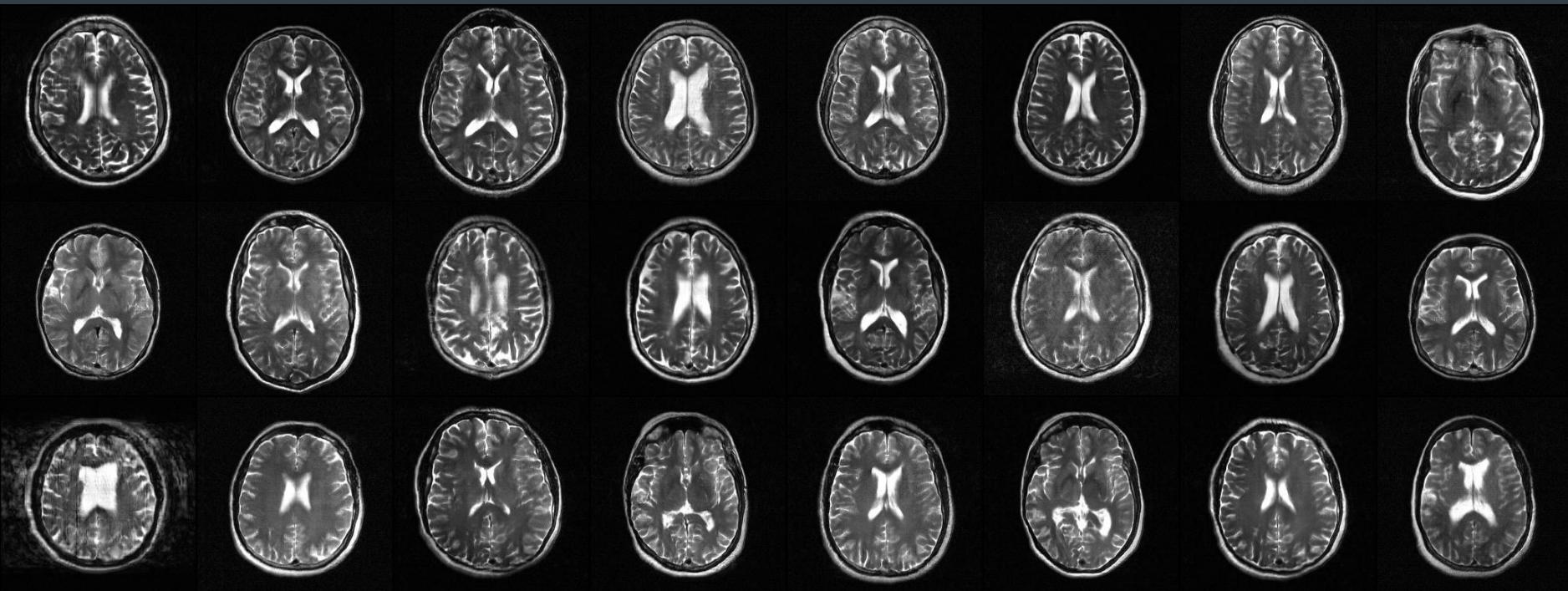


# Generative models are powerful image generators



<https://thiscatdoesnotexist.com/>

# Generative models are powerful image generators

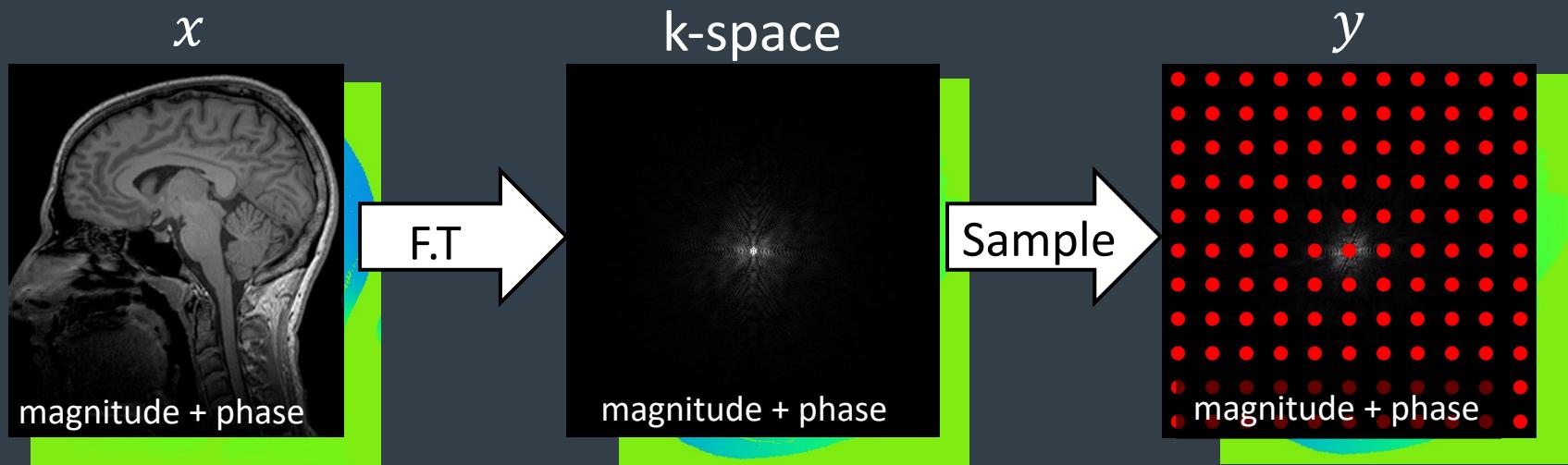


Generative model trained on FastMRI data

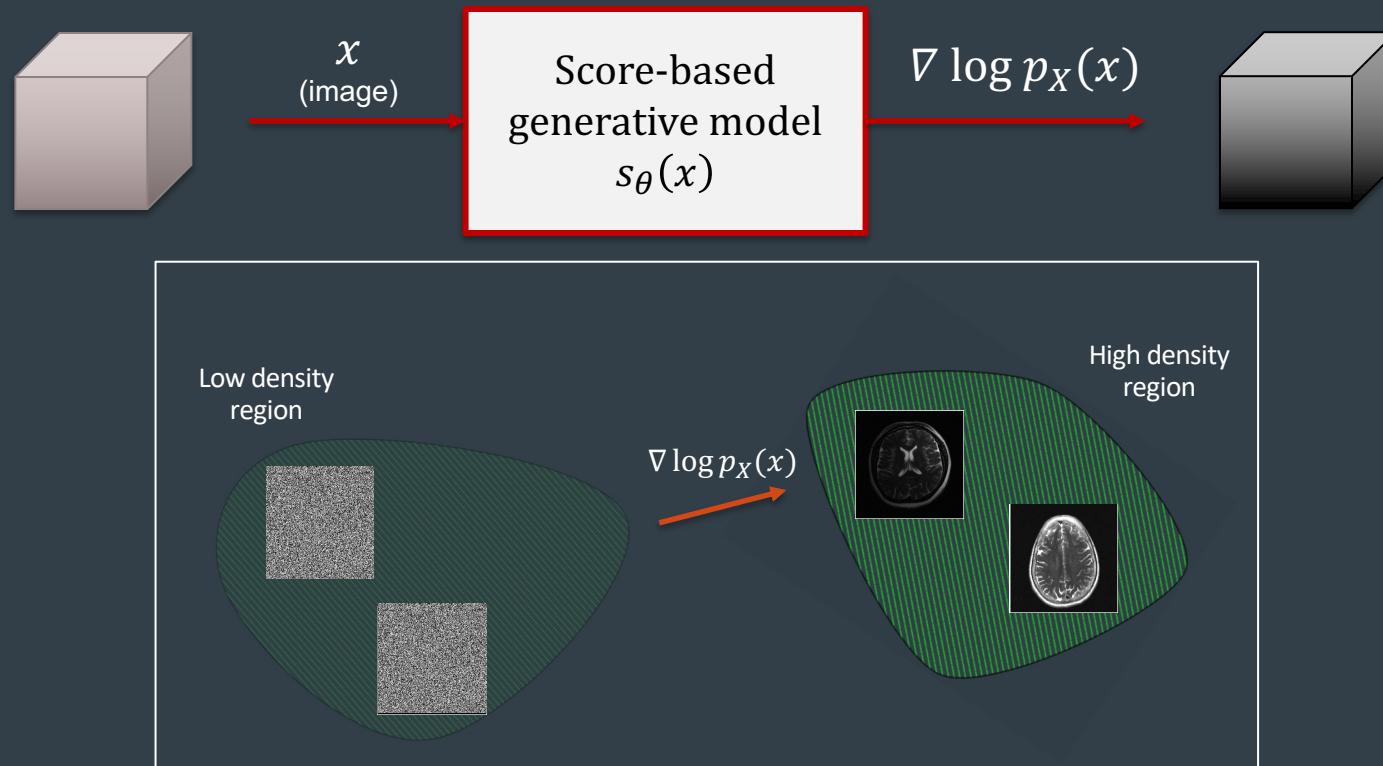
# MRI: Problem Formulation

Signal is the Fourier transform of the image

$$y = Ax + \text{noise}$$



# Score-based generative models

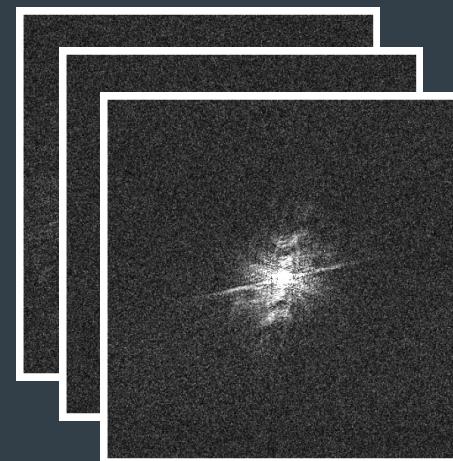


# MRI Samples are inherently noisy

Goal is to learn the **clean distribution** using *noisy* data (i.i.d Gaussian, with known power  $\sigma_w^2$ ).

$$y = Ax + \text{noise}$$

$y$

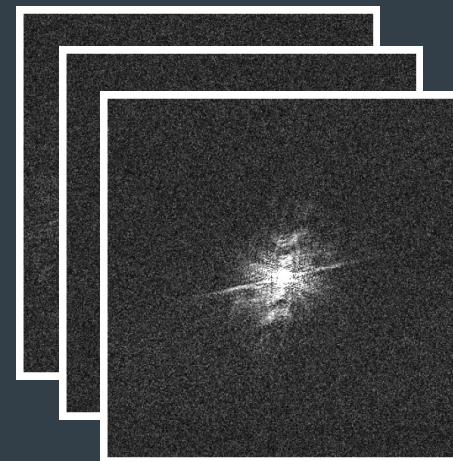


Original K-Space

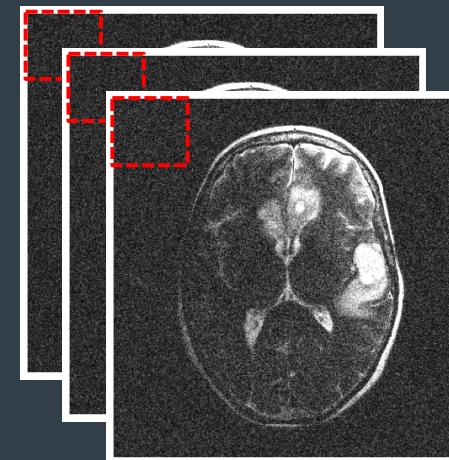
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$$y = Ax + \text{noise}$$

 $y$  $F^H y$ 

Original K-Space

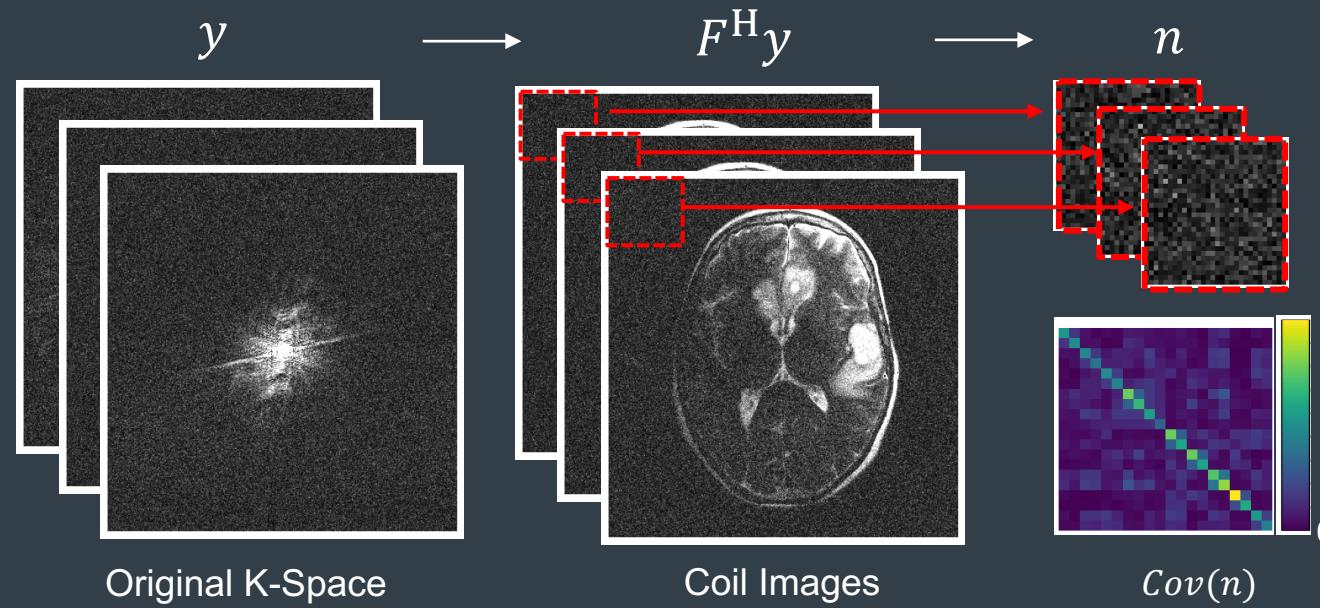


Coil Images

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Goal is to learn the **clean distribution** using *noisy* data (i.i.d Gaussian, with known power  $\sigma_w^2$ ).

$$y = Ax + \text{noise}$$

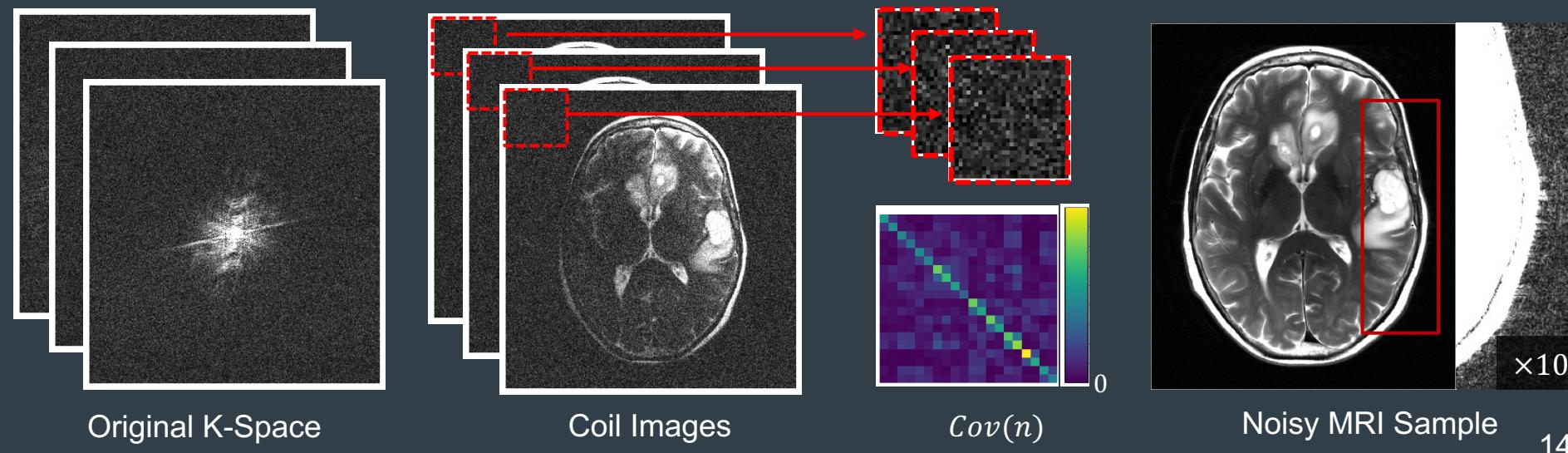


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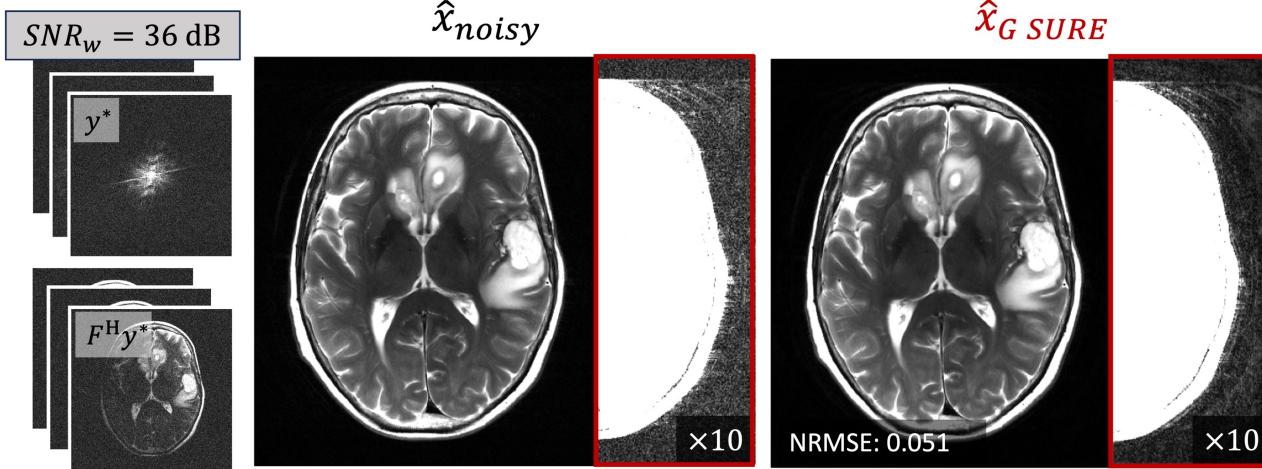
$$y = Ax + \text{noise}$$

$$y \longrightarrow F^H y \longrightarrow n \longrightarrow \hat{x}_{\text{noisy}} = A^H y^*$$



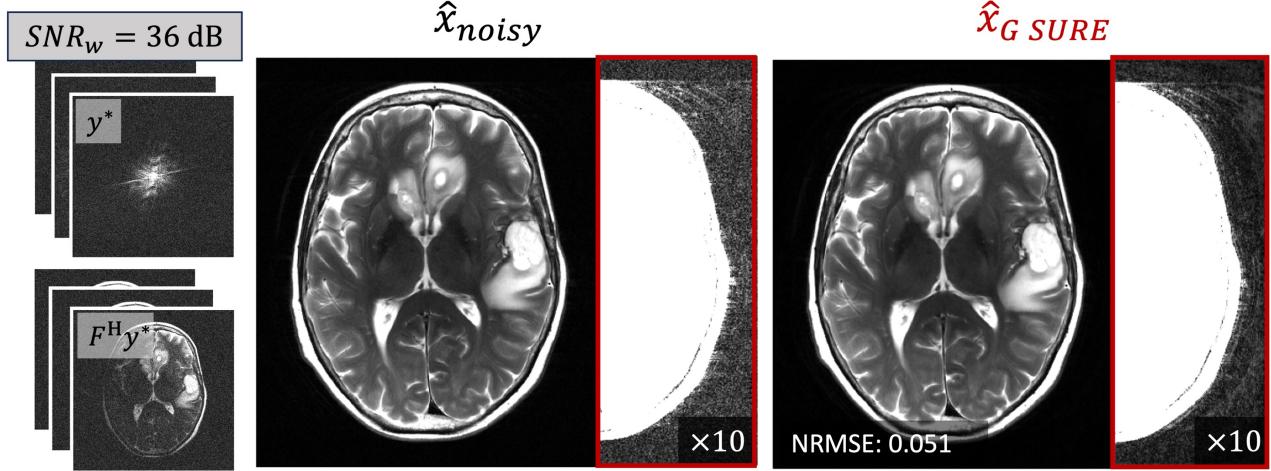
# Denoising with GSURE

Original FastMRI



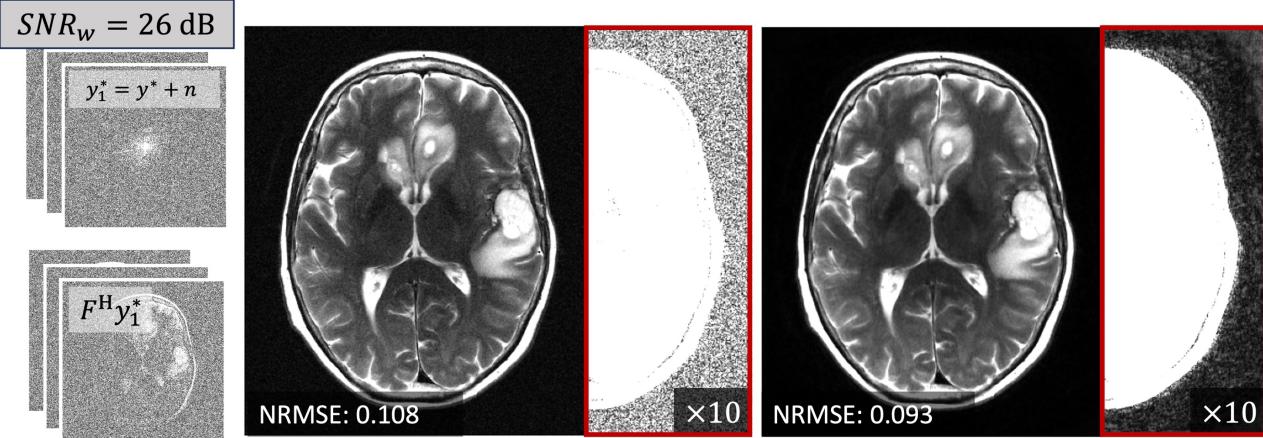
# Denoising with GSURE

Original FastMRI



Original FastMRI

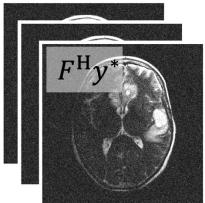
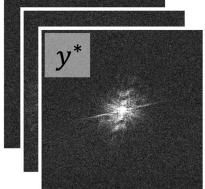
+  
Additive Gaussian Noise



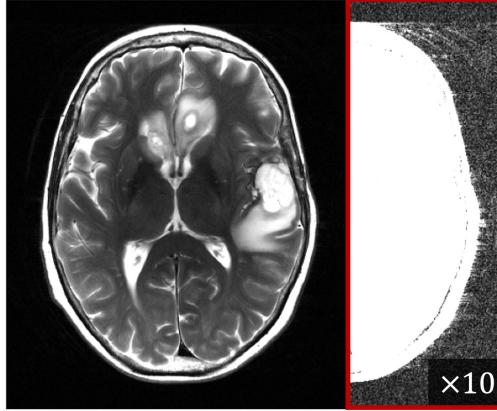
# Denoising with GSURE

Original FastMRI

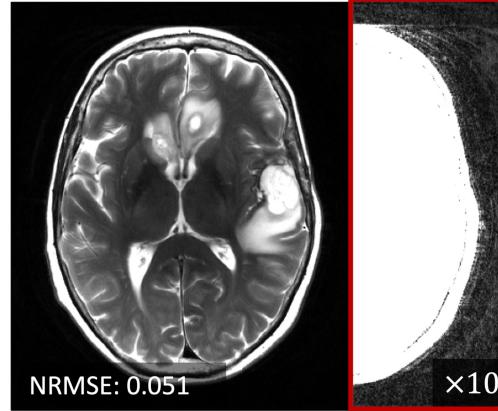
$$SNR_w = 36 \text{ dB}$$



$$\hat{x}_{noisy}$$



$$\hat{x}_{G \text{ SURE}}$$

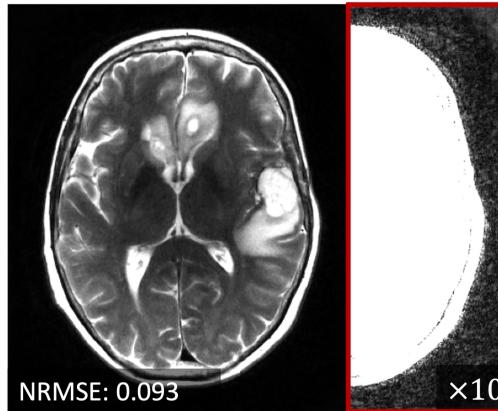
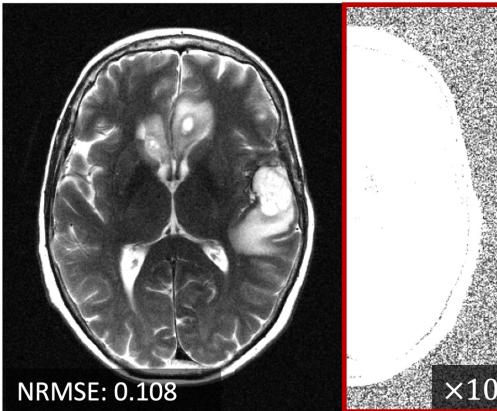
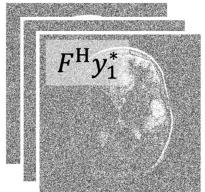
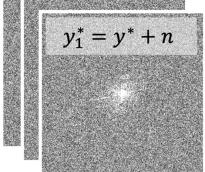


Original FastMRI

+

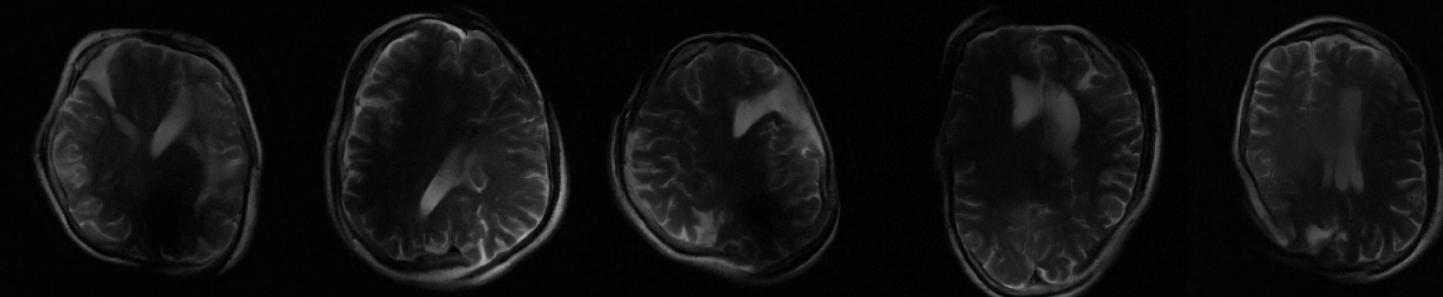
Additive Gaussian Noise

$$SNR_w = 26 \text{ dB}$$



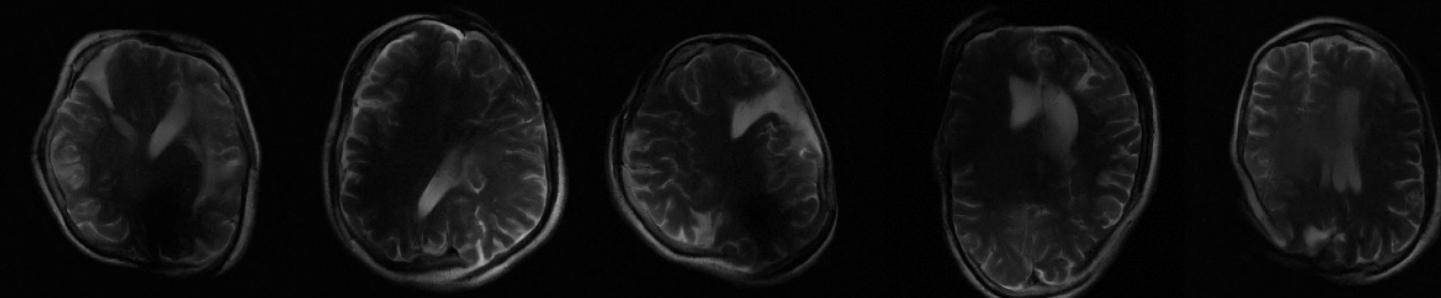
# Learning Priors using Generative Models – $p(x)$

Naive Score

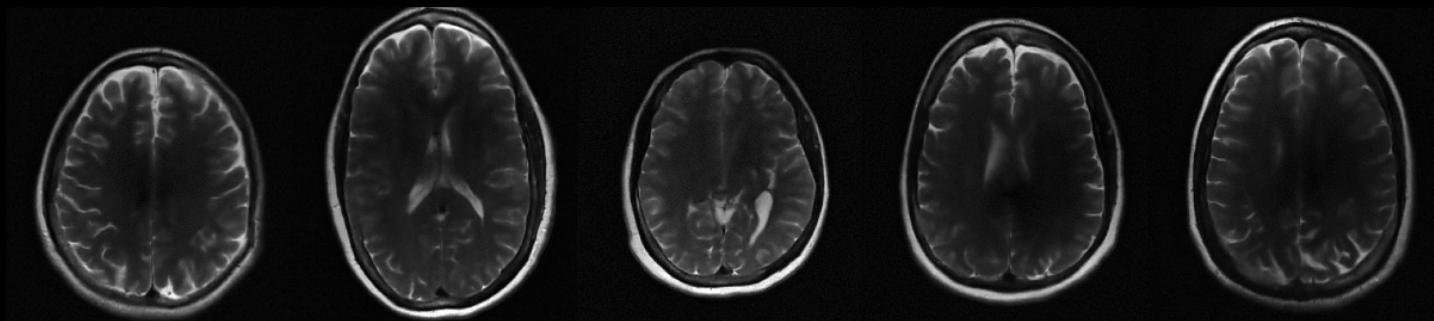


# Learning Priors using Generative Models – $p(x)$

Naive Score

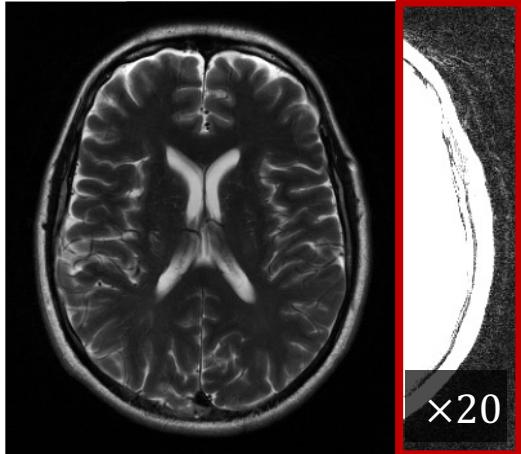


GSURE-Score

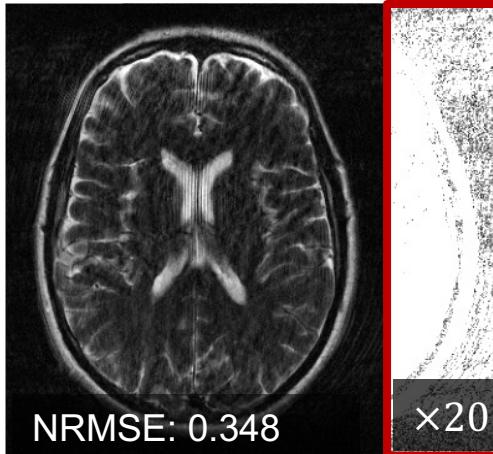


# Inverse Problems using Generative Models $x \sim p(x|y)$

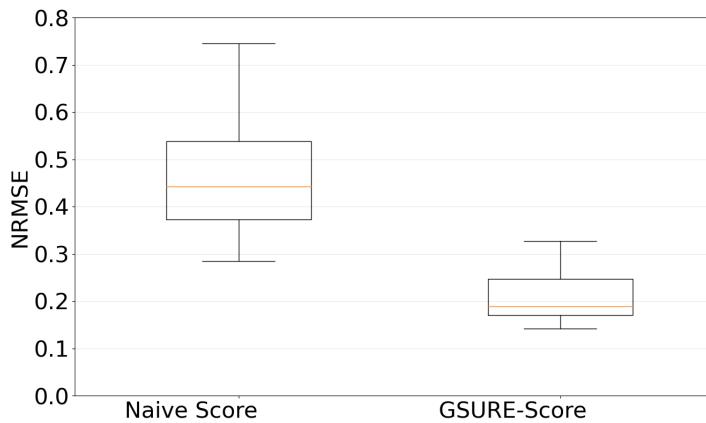
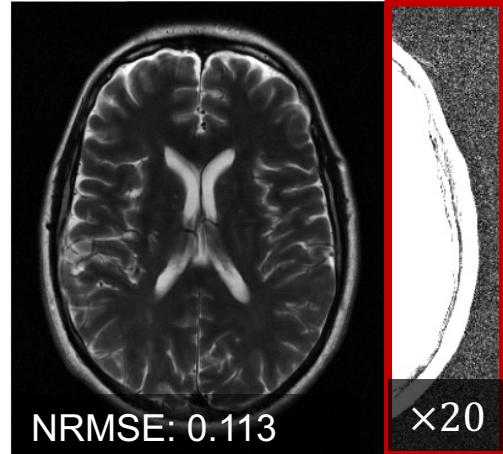
Fully Sampled



Naive Score



GSURE-Score



# Conclusions

1. Self-supervised techniques like GSURE can successfully remove noise
2. Denoising as a pre-processing step, severely improves the quality of generative priors
3. Priors trained on denoised FastMRI are better inverse problem solvers than naive training

# Thank you!

Asad Aali

[asad.aali@utexas.edu](mailto:asad.aali@utexas.edu)

<https://www.linkedin.com/in/asadaali/>

<https://asad-aali.github.io/>

MS ECE Student

The University of Texas at Austin

