Repairing Multiline Syntax Errors Using the Levenshtein-Bar-Hillel Construction

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Overview

Formal Language Theory

2 Algebraic Parsing

3 Decoding

Original code	Human repair
newlist = [] i = set([5, 3, 1)] z = set([5, 0, 4)]	

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```
(1) v = df.iloc(5:, 2, 0) (3) v = df.iloc(5[:, 2:]) (5) v = df.iloc[5:, 2:]
```

(2)
$$v = df.iloc(5)$$
, $2()$ (4) $v = df.iloc(5:, 2:)$ (6) $v = df.iloc(5[:, 2])$

Original code	Valid repairs	

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High-level architecture overview

This process can be depicted as series of staged transformations lowering the CFL intersection problem onto a finite automaton. Below, we consider a simplified version based on the language of balanced parentheses.

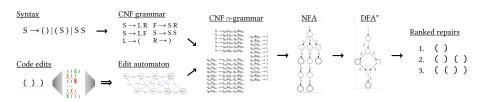


Figure: Simplified dataflow of the language intersection pipeline. Given a grammar and broken code fragment, we (1) create a automaton generating the language of small edits, then (2) construct a grammar representing the intersection of the two languages. This grammar can be (3) converted into a finite automaton, (4) determinized, then (5) decoded to produce a list of repairs.

Parsing for linear algebraists

Given a CFG $\mathcal{G} \coloneqq \langle V, \Sigma, P, S \rangle$ in Chomsky Normal Form, we can construct a recognizer $R_{\mathcal{G}} : \Sigma^n \to \mathbb{B}$ for strings $\sigma : \Sigma^n$ as follows. Let 2^V be our domain, 0 be \emptyset , \oplus be \cup , and \otimes be defined as follows:

$$s_1 \otimes s_2 := \{ C \mid \langle A, B \rangle \in s_1 \times s_2, (C \to AB) \in P \}$$

$$\mathsf{e.g.},\ \{\mathsf{A}\to\mathsf{BC},\ \mathsf{C}\to\mathsf{AD},\ \mathsf{D}\to\mathsf{BA}\}\subseteq\!\!\mathsf{P}\vdash\!\!\{\mathsf{A},\ \mathsf{B},\ \mathsf{C}\}\otimes\!\{\mathsf{B},\ \mathsf{C},\ \mathsf{D}\}=\{\mathsf{A},\ \mathsf{C}\}$$

If we define $\sigma_r^{\uparrow} \coloneqq \{ w \mid (w \to \sigma_r) \in P \}$, then initialize $M_{r+1=c}^0(\mathcal{G}',e) := \sigma_r^{\uparrow}$ and solve for the fixpoint $M^* = M + M^2$,

$$M^0 := \begin{pmatrix} \varnothing & \sigma_1^{\rightarrow} & \varnothing & \cdots & \varnothing \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ \vdots & \ddots & \ddots$$

$$S \Rightarrow^* \sigma \iff \sigma \in \mathcal{L}(\mathcal{G}) \text{ iff } S \in \Lambda_{\sigma}^*, \text{ i.e., } \mathbb{1}_{\Lambda_{\sigma}^*}(S) \iff \mathbb{1}_{\mathcal{L}(\mathcal{G})}(\sigma).$$

$\mathsf{Satisfiability} + \mathsf{holes}$

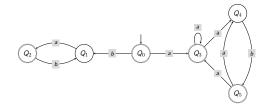
Let us consider an example with two holes, $\sigma=1$ _ _ , and the grammar being $G:=\{S\to NON, O\to +\mid \times, N\to 0\mid 1\}$. This can be rewritten into CNF as $G':=\{S\to NL, N\to 0\mid 1, O\to \times\mid +, L\to ON\}$. Using the algebra where $\oplus=\cup$, $X\otimes Z=\{w\mid \langle x,z\rangle\in X\times Z, (w\to xz)\in P\}$, the fixpoint $M'=M+M^2$ can be computed as follows:

	2^V	$\mathbb{Z}_2^{ V }$	$\mathbb{Z}_2^{ V } o \mathbb{Z}_2^{ V }$
M ₀	$ \begin{pmatrix} & \{N\} \\ & \{N,O\} \\ & \{N,O\} \end{pmatrix} $		$egin{pmatrix} V_{0,1} & & & & & & & & & & & & & & & & & & &$
<i>M</i> ₁	$ \begin{pmatrix} N & \emptyset \\ \{N,O\} & \{L\} \\ \{N,O\} \end{pmatrix} $		$\begin{pmatrix} & V_{0,1} & V_{0,2} \\ & V_{1,2} & V_{1,3} \\ & & V_{2,3} \end{pmatrix}$
M_{∞}	$ \begin{pmatrix} N & \emptyset & \{S\} \\ \{N,O\} & \{L\} \\ \{N,O\} \end{pmatrix} $		$ \begin{pmatrix} V_{0,1} & V_{0,2} & V_{0,3} \\ V_{1,2} & V_{1,3} & V_{2,3} \end{pmatrix} $

Background: Regular grammars

A regular grammar (RG) is a quadruple $\mathcal{G}=\langle V,\Sigma,P,S\rangle$ where V are nonterminals, Σ are terminals, $P:V\times (V\cup\Sigma)^{\leq 2}$ are the productions, and $S\in V$ is the start symbol, i.e., all productions are of the form $A\to a$, $A\to aB$ (right-regular), or $A\to Ba$ (left-regular). e.g., the following RG and NFA correspond to the language defined by the $\operatorname{regex}_{(a(ab)*)*(ba)*}$:

$$\begin{split} S &\to Q_0 \mid Q_2 \mid Q_3 \mid Q_5 \\ Q_0 &\to \varepsilon \\ Q_1 &\to Q_0 b \mid Q_2 b \\ Q_2 &\to Q_1 a \\ Q_3 &\to Q_0 a \mid Q_3 a \mid Q_5 a \\ Q_4 &\to Q_3 a \mid Q_5 a \\ Q_5 &\to Q_4 b \end{split}$$





Levenshtein automaton customization

Consider the string $\sigma=($)) and the alphabet $\Sigma=\{$),($\}$. Every string within one edit of σ is recognized by an NFA with the following structure:

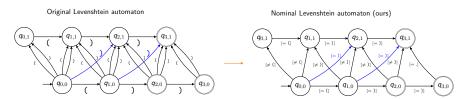


Figure: Automaton recognizing every single patch of the broken string () within Levenshtein distance 1. We nominalize the original Levenshtein automaton, ensuring upward arcs denote a mutation, and replace terminals with a symbolic predicate, which deduplicates parallel arcs in large alphabets.

https://fulmicoton.com/posts/levenshtein/#observations-lets-count-states

Levenshtein reachability

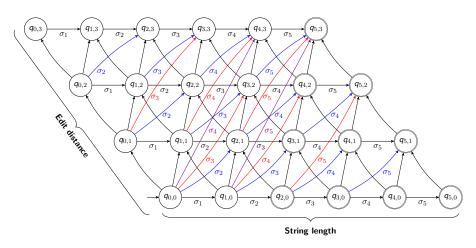


Figure: Bounded Levenshtein reachability from $\sigma: \Sigma^n$ is expressible as an NFA populated by accept states within radius k of $S=q_{n,0}$, which accepts all strings σ' within Levenshtein radius k of σ .

Geometrically interpreting the edit calculus

Each arc plays a specific role. \uparrow handles insertions, \checkmark handles substitutions and \checkmark handles deletions of ≥ 1 tokens. Consider some illustrative cases:

```
f.[x) f. x) f.(x) .+(x) f.(x;
f.(x) f.(x) f.() (x) f* x;
```

Note that the same $\langle \sigma, \sigma' \rangle$ pair can have multiple Levenshtein alignments:

```
[,xy] [,xy] [x,y]
```

Non-uniqueness of geodesics has implications for CFG \cap L-NFA ambiguity.

The nominal Levenshtein automaton

The original Levenshtein automaton (Schulz & Stoyan, 2002):

$$\frac{s \in \Sigma \quad i \in [0, n] \quad j \in [1, k]}{(q_{i,j-1} \xrightarrow{s} q_{i,j}) \in \delta} \uparrow \qquad \frac{s \in \Sigma \quad i \in [1, n] \quad j \in [1, k]}{(q_{i-1,j-1} \xrightarrow{s} q_{i,j}) \in \delta} \checkmark$$

$$\frac{s = \sigma_i \quad i \in [1, n] \quad j \in [0, k]}{(q_{i-1,j} \xrightarrow{s} q_{i,j}) \in \delta} \Rightarrow \qquad \frac{s = \sigma_i \quad i \in [2, n] \quad j \in [1, k]}{(q_{i-2,j-1} \xrightarrow{s} q_{i,j}) \in \delta} \checkmark \checkmark$$

$$\frac{q_{i,j} \quad |n - i + j| \le k}{q_{i,j} \in F} \text{ Done}$$

We modify the original automaton with a nominal predicate:

$$\frac{i \in [0, n] \quad j \in [1, k]}{(q_{i,j-1} \stackrel{[\neq \sigma_{i+1}]}{\rightarrow} q_{i,j}) \in \delta} \uparrow \qquad \frac{i \in [1, n] \quad j \in [1, k]}{(q_{i-1,j-1} \stackrel{[\neq \sigma_{i}]}{\rightarrow} q_{i,j}) \in \delta} \checkmark$$

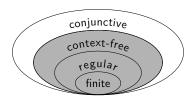
$$\frac{i \in [1, n] \quad j \in [0, k]}{(q_{i-1,j} \stackrel{[=\sigma_{i}]}{\rightarrow} q_{i,j}) \in \delta} \rightarrow \frac{d \in [1, d_{\max}] \quad i \in [d+1, n] \quad j \in [d, k]}{(q_{i-d-1,j-d} \stackrel{[=\sigma_{i}]}{\rightarrow} q_{i,j}) \in \delta} \checkmark \checkmark$$

Background: Context-free grammars

In a context-free grammar $\mathcal{G}=\langle V,\Sigma,P,S\rangle$ all productions are of the form $P:V\times (V\cup\Sigma)^+$, i.e., RHS may contain any number of nonterminals, V. Recognition decidable in $\mathcal{O}(n^\omega)$, n.b. CFLs are **not** closed under \cap !

For example, consider the grammar $S \to SS \mid (S) \mid ()$. This represents the language of balanced parentheses, e.g. (), ()(), (()), (()), (()), (()))...

Every CFG has a normal form $P^*: V \times (V^2 \mid \Sigma)$, i.e., every production can be refactored into either $v_0 \to v_1 v_2$ or $v_0 \to \sigma$, where $v_{0...2}: V$ and $\sigma: \Sigma$, e.g., $\{S \to SS \mid (S) \mid ()\} \Leftrightarrow^* \{S \to XR \mid SS \mid LR, L \to (,R \to), X \to LS\}$



Background: Closure properties of formal languages

Formal languages are not always closed under set-theoretic operations, e.g., CFL \cap CFL is not CFL in general. Let \cdot denote concatenation, * be Kleene star, and \complement be complementation:

	\cup	\cap	•	*	C
Finite ¹	1	1	1	1	√
$Regular^1$	1	1	1	1	✓
Context-free 1,2	1	$oldsymbol{\mathcal{X}}^\dagger$	1	1	X
Conjunctive 1,2	1	1	1	1	?
Context-sensitive 2	1	✓	1	+	✓
Recursively Enumerable 2		1	1	1	X

We would like a language family that is (1) tractable, i.e., has polynomial recognition and search complexity and (2) reasonably expressive, i.e., can represent syntactic properties of real-world programming languages.

[†] However, CFLs are closed under intersection with regular languages.

The Bar-Hillel construction and its specialization

The original Bar-Hillel construction provides a way to construct a grammar for the intersection of a regular and context-free language.

$$\frac{q \in I \quad r \in F}{\left(S \to qSr\right) \in P_{\cap}} \sqrt{-} \frac{(A \to a) \in P \quad (q \stackrel{a}{\to} r) \in \delta}{\left(qAr \to a\right) \in P_{\cap}} \uparrow \frac{\left(w \to xz\right) \in P \quad p, q, r \in Q}{\left(pwr \to (pxq)(qzr)\right) \in P_{\cap}} \bowtie$$

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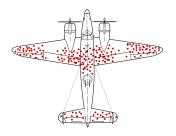
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Observation: too many (q, v, q') triples! Three low-hanging optimizations:

- Only consider (q, q') where $q \Longrightarrow^* q'$.
- Filter impossible (q, v, q') triples based on path length.
- Remove unreachable states from the Levenshtein automaton.

Edit location refinement: intuition

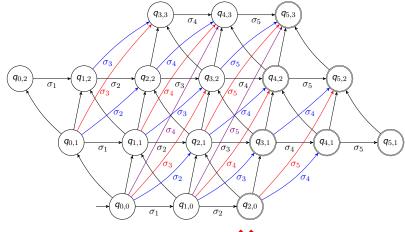
But do we really need $|\sigma| \times d_{\rm max}$ states? Can we somehow narrow down the edit range? Where should we make the edits?

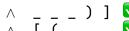


Often, it is easier to determine where *not* to make the edits. Certain regions, no matter their contents, will never yield a viable repair.

Edit location refinement: example

Let's prune states absorbing obviously impossible repair trajectories.





Grammar refinement: Parikh interval maps

If we're reusing the CFG, it would make sense to precompute some statistics. For example, the total tokens each nonterminal can parse.

e.g., if ${\it R}$ is a unit nonterminal that maps to one value, then $[{\it R}]=[1,1].$

Can be parameterized by Σ ., e.g.,: $[R] = \{a: [1,1], b: [0,0] \ldots \}$

We call this the Parikh interval. We can compute it for each string length, e.g., $[R, a, 1] = \{a : [1, 1], b : [0, 0] \dots\}, [R, a, 2] = \dots$

Now when we have a new automaton, we can check whether (q, v, q') is compatible by checking whether the Parikh range for q, q' and v overlaps.

This optimization is not specific to LBH intersections, and can be applied to any CFG/FSA intersection.

Potential ambiguity of Levenshtein-Bar-Hillel grammars

The previous technique enumerates parse trees in a given \mathbb{T}_2 , but does not guarantee string uniqueness since the CFG may be ambiguous.

Lemma

If the FSA, α , is ambiguous, the intersection CFG, G_{\cap} , can be ambiguous.

Proof.

Let ℓ be the language defined by $G=\{S\to LR, L\to (R\to)\}$, where $\alpha=L(\varrho,2)$, the broken string ϱ is)(, and $\mathcal{L}(G_\cap)=\ell\cap\mathcal{L}(\varrho)$. Then, $\mathcal{L}(G_\cap)$ contains the following two identical repairs:)() with the parse $S\to q_{00}Lq_{21}\ q_{21}Rq_{22}$, and () with the parse $S\to q_{00}Lq_{11}\ q_{11}Rq_{22}$.

We can eliminate ambiguity and thereby improve the rate of convergence for natural syntax repair by first translating \mathbb{T}_2 into an FSA.

Existence of an FSA that generates $\mathcal{L}(G_{\cap})$

There is an FSA generating $\mathcal{L}(G_{\cap})$. We first show this non-constructively:

Lemma

The intersection grammar, G_{\cap} , is acyclic.

Proof.

Assume G_{\cap} is cyclic. Then $\mathcal{L}(G_{\cap})$ must be infinite. But since G_{\cap} generates $\ell \cap \mathcal{L}(\alpha)$ by construction and α is acyclic, $\mathcal{L}(G_{\cap})$ is necessarily finite. Therefore, G_{\cap} must not be cyclic.

Since G_{\cap} is acyclic and thus finite, it must be representable as an FSA. Using an FSA for decoding has many advantages, notably, it can be efficiently minimized and decoded in order of n-gram likelihood using a Markov chain or standard pretrained autoregressive language model.

Translating from T_2 to a DFA

Let $+,*:\mathcal{A}\times\mathcal{A}\to\mathcal{A}$ be automata operators satisfying the property $\mathcal{L}(A_1+A_2)=\mathcal{L}(A_1)\cup\mathcal{L}(A_2)$, and $\mathcal{L}(A_1*A_2)=\mathcal{L}(A_1)\times\mathcal{L}(A_2)$. We can translate \mathbb{T}_2 to \mathcal{A} , as follows, recalling FSAs are closed over +,*:

$$\mathcal{Y}(T:\mathbb{T}_2) \mapsto \begin{cases} \alpha \mid \mathcal{L}(\alpha) = \{T\} & T:\Sigma, \\ \sum_{\langle T_1, T_2 \rangle \in \mathsf{children}(T)} \mathcal{Y}(T_1) * \mathcal{Y}(T_2) & T: \mathit{VL}\big(\mathit{V}^2\mathit{P}(\mathsf{a})^2\big) \end{cases}$$

In the case of LBH intersections, $\mathcal{Y}(\mathcal{G}'_{\cap})$ yields $\alpha: \mathcal{A} \mid \mathcal{L}(\alpha) = \ell \cap \mathcal{L}(\alpha, d)$, which can be minimized via Brzozowski's algorithm then decoded:

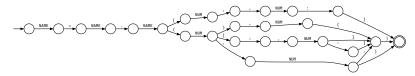


Figure: $L({\sf NAME} = {\sf NAME}$. NAME (NUM : , NUM :), $2) \cap \ell_{\rm Python}$

Decoding the DFA in order of normalized log likelihood

Algorithm Steerable DFA walk

11: return $\left[\sigma_{|\sigma|...1} \mid \langle \sigma, q, \gamma \rangle = T \in \mathcal{T}\right]$

```
Require: \mathcal{A} = \langle Q, \Sigma, \delta, I, F \rangle DFA, P_{\theta} : \Sigma^{d} \to \mathbb{R} Markov chain
  1: \mathcal{T} \leftarrow \emptyset total trajectories, \mathcal{P} \leftarrow [\langle \varepsilon, i, 0 \rangle \mid i \in I] partial trajectories
  2: repeat
               let \langle \sigma, q, \gamma \rangle = \text{head}(\mathcal{P}) in
  3:
                      \mathbf{T} = \{ \langle s\sigma, q', \gamma - \log P_{\theta}(s \mid \sigma_{1-d-1}) \rangle \mid (q \stackrel{s}{\to} q') \in \delta \}
  4.
               for \langle \sigma, q, \gamma \rangle = T \in \mathbf{T} do
  5:
                      if \exists s : \Sigma, q' : Q \mid (q \xrightarrow{s} q') \in \delta then
  6:
                             \mathcal{P} \leftarrow \mathsf{tail}(\mathcal{P}) \oplus \mathcal{T} \qquad \qquad \triangleright \mathsf{Add} \mathsf{\ partial\ trajectory\ to\ PQ}.
  7:
                      if q \in F then
  8:
                             \mathcal{T} \leftarrow \mathcal{T} \oplus \mathcal{T}
  9:
                                                                    ▶ Accepting state reached, add to queue.
10: until interrupted or \mathcal{P} = \emptyset.
```

Characteristics of the repair dataset

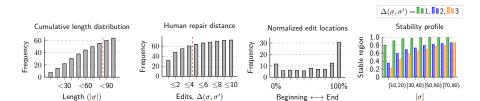


Figure: Repair statistics across the StackOverflow dataset, of which Tidyparse can handle about half in under ${\sim}30s$ and ${\sim}150$ GB. Larger repairs and edit distances are possible, albeit requiring additional time and memory. The stability profile measures the average fraction of all edit locations that were never altered by any repair in the $L({\sigma}, \Delta({\sigma}, {\sigma}'))$ -ball across repairs of varying length and distance.

Ranked repair

We train on lexical n-grams using the standard MLE for Markov chains. To score the repairs, we use the conventional length-normalized NLL:

$$NLL(\sigma) = -\frac{1}{|\sigma|} \sum_{i=1}^{|\sigma|} \log P_{\theta}(\sigma_i \mid \sigma_{i-1} \dots \sigma_{i-n})$$
 (1)

For each retrieved set $\hat{A}\subseteq A$ drawn before a predetermined timeout and each $\sigma\in\hat{A}$, we score the repair and return \hat{A} in ascending order. To evaluate the quality of our ranking, we use the Precision@k statistic. Specifically, given a repair model, $R:\Sigma^*\to 2^{\Sigma^*}$ and a parallel corpus, $\mathcal{D}_{\mathsf{test}}$, of errors (σ^\dagger) and repairs (σ') , we define Precision@k as:

$$\mathsf{Precision@k}(R) = \frac{1}{|\mathcal{D}_{\mathsf{test}}|} \sum_{\langle \sigma^{\dagger}, \sigma' \rangle \in \mathcal{D}_{\mathsf{test}}} \mathbb{1} \left[\sigma' \in \underset{\boldsymbol{\sigma} \subset R(\sigma^{\dagger}), |\boldsymbol{\sigma}| \leq k}{\operatorname{argmax}} \sum_{\sigma \in \boldsymbol{\sigma}} \mathsf{NLL}(\sigma) \right] \tag{2}$$

Precision and latency comparison

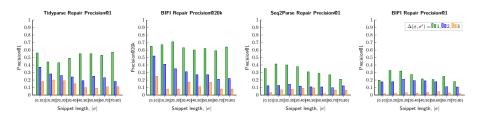


Figure: Tidyparse, Seq2Parse and BIFI repair precision across length and edits.

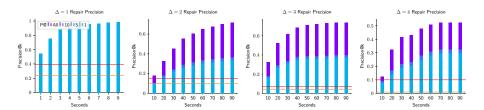
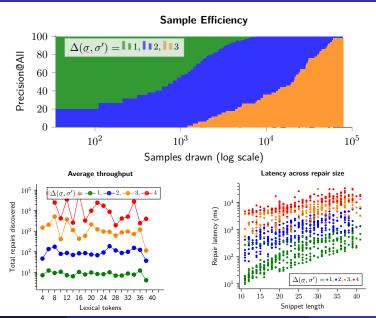


Figure: Latency benchmarks. Note the varying y-axis ranges. The red line marks Seq2Parse and the orange line marks BIFI's Precision@1 on the same repairs.

Results from sample efficiency experiments



Outcomes in the syntax repair pipeline

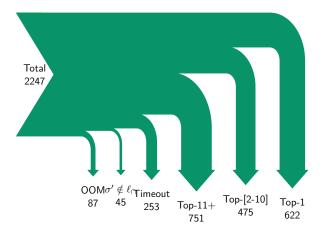


Figure: Sankey diagram of 967 total repair instances sampled uniformly from the StackOverflow Python dataset balanced acrost snippet lengths and edit distances $(\lfloor |g|/10 \rfloor \in [0,8], \Delta(\varrho,\sigma') < 4)$ with a sampling timeout of 30s per repair.

Feature comparison matrix

	Sound	Complete	Natural	Theory		Tool
Tidyparse	✓	✓	✓	CFG∩	1	IDE-ready
Seq2Parse	√ †	×	✓	CFG	X	Python
BIFI	X	×	✓	Σ^*	X	Python
OrdinalFix	✓	×	X	CFG+	X	Rust
$Outlines^1$	√ †	√ †	✓	EBNF	X	Python
$SynCode^1$	✓	✓	✓	EBNF	X	Python
Aho/Irons	1	×	X	CFG	X	None

Sound = generated repairs always syntactically valid.

Complete = all valid repairs are eventually generated.

 $\textbf{Natural} \approx \text{statistically likely } / \text{ designed to model human preferability}.$

 $\mid\mid$ = Trivially parallelizable, i.e., designed to be executed on multiple cores.

¹ Not specifically intended for syntax repair, but can be adapted.

[†] Claimed by the authors, but counterexamples known to exist.

Abbreviated history of algebraic parsing

- ullet Chomsky & Schützenberger (1959) The algebraic theory of CFLs
- Cocke–Younger–Kasami (1961) Bottom-up matrix-based parsing
- Brzozowski (1964) Derivatives of regular expressions
- Valiant (1975) first realizes the Boolean matrix correspondence
 - Naïvely, has complexity $\mathcal{O}(n^4)$, can be reduced to $\mathcal{O}(n^\omega)$, $\omega < 2.763$
- ullet Lee (1997) Fast CFG Parsing \Longleftrightarrow Fast BMM, formalizes reduction
- ullet Might et al. (2011) Parsing with derivatives (Brzozowski \Rightarrow CFL)
- Bakinova, Okhotin et al. (2010) Formal languages over GF(2)
- Bernady & Jansson (2015) Certifies Valiant (1975) in Agda
- Cohen & Gildea (2016) Generalizes Valiant (1975) to parse and recognize mildly context sensitive languages, e.g. LCFRS, TAG, CCG
- Considine, Guo & Si (2022) SAT + Valiant (1975) + holes
- Considine, Guo & Si (2024) Levenshtein Bar-Hillel repairs

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Learn more at:

https://tidyparse.github.io