

An Edit Calculus for Probabilistic Program Repair

Breandan Considine



School of Computer Science
McGill University
Montreal, Quebec, Canada

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Abstract

We introduce an edit calculus for correcting syntax errors in arbitrary context-free languages, and by extension, any programming language with a context-free grammar. Syntax errors with a small repair seldom have many unique small repairs, which can usually be enumerated up to a small edit distance then quickly reranked. Our work places a heavy emphasis on precision: the enumerated set must contain every possible repair within a given radius and no invalid repairs. To do so, we construct a grammar representing the language intersection between a Levenshtein automaton and a context-free grammar, then decode it in order of probability. This produces an ordered set of repairs that contains with high probability the intended revision.

Abrégé

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Contribution

The work presented in this thesis is the sole result of the author’s original research, except where otherwise indicated. The author has made the following contributions to the work presented in this thesis:

- The conception of syntax repair as a language intersection task.
- The adaptation and specialization of the Bar-Hillel construction to probabilistic program repair.
- The formalization of the program repair objective as a pragmatic language game between a human and a machine.
- The design and implementation of the probabilistic program repair system called Tidyparse.

Acknowledgements

Official McGill Guidelines: Among other acknowledgements, the student is required to declare the extent to which assistance (paid or unpaid) has been given by members of staff, fellow students, research assistants, technicians, or others in the collection of materials and data, the design and construction of apparatus, the performance of experiments, the analysis of data, and the preparation of the thesis (including editorial help).

- In addition, it is appropriate to recognize the supervision and advice given by the thesis supervisor(s) and advisors.

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Terminology

Technical and vernacular collisions induce a strange semantic synesthesia, e.g., complete, consistent, kernel, reflexive, regression, regular, sound. The intension may be distantly related to standard English, but if one tries to interpret such jargon colloquially, there is no telling how far astray they will go. For this reason, we provide a glossary of terms to help the non-technical reader navigate the landscape of this thesis.

- **Automaton:** A mathematical model of computation that can occupy one of a finite number of states at any given time, and makes transitions between states according to a set of rules.
- **Deterministic:** A property of a system that, given the same input, will always produce the same output.
- **Grammar:** A set of rules that define the syntax of a language.
- **Language:** A set of words generated by a grammar. For the purposes of this thesis, the language can be finite or infinite.
- **Word:** A member of a language, consisting of a sequence of terminals. For the purposes of this thesis, words are always finite.
- **Terminal:** A single token from an alphabet. For the purposes of this thesis, the alphabet is always finite.
- **Intersection:** The set of elements common to two or more sets.
- **Probabilistic:** A property of a system that, given the same input, may produce different outputs.
- **Theory:** A set of sentences in a formal language.



Related Literature

Translating ideas into computer programs demands a high degree of precision, as computers have strict criteria for admitting valid programs. These constraints act as a failsafe against faulty programs and runtime errors, but can be tedious to debug. During the editing process, these constraints are invariably violated by the hasty or inexperienced programmer, requiring manual repair. To assist with this task, automated program repair (APR) attempts to generate possible revisions from which the author may choose. This subject has been closely investigated by programming language research and treated in a number of existing literature reviews [Mon18, LGPRC21]. We direct our attention primarily towards syntax repair, which attempts to fix parsing errors, the earliest stage in program analysis.

0.1 Syntax Repair

Spellchecking is an early precursor to syntax repair that originates from word processing and seeks to find, among a finite dictionary, the most likely intended revision of a misspelled word [KCG90]. Akin to spellchecking, syntax repair considers the case where this dictionary is not necessarily finite, but rather generated by a grammar representing a potentially infinite collection of words called a language. In the case of programming language syntax, the language and corresponding grammar is typically context-free [CS59].

Various methods have been proposed to handle syntactic program errors, which have been a longstanding open problem since the advent of context-free languages. In 1972, Aho and Peterson [AP72] introduce an algorithm that returns a syntactically valid sequence whose distance from the original sequence is minimal. Their method guarantees that a valid repair will be

found, but only generates a single repair and does attempt to optimize the naturalness of the generated solution.

While algorithmically elegant, this approach is problematic because source code has both formal and natural characteristics. A pragmatic solution must not merely suggest valid repairs, but also generate suggestions a human is likely to prefer in practice. To model coding conventions and stylistic patterns, researchers have borrowed techniques from natural language processing, but often sacrifice validity, precision or latency as these techniques are prone to misgeneralize and hallucinate syntactically invalid repairs.

Recent work Yasunaga et al. [YL21] and Sakkas et al. [SEG⁺22] use natural language models to generate probable fixes, but do not attempt to sample from the space of all and only valid repairs. As a consequence, they have difficulty with inference scaling, where additional test time compute does not translate into improved precision. Furthermore, the generated samples may not even be syntactically valid, as we observe in practice.

Our work addresses all of these concerns. We try to generate every nearby valid program and prioritize the solutions by naturalness, while ensuring response time is tolerable. In other words, we attempt to satisfy soundness, completeness, naturalness and latency simultaneously.

1

Introduction

Pray, Mr. Babbage, if you put
into the machine wrong figures,
will the right answers come out?

—Charles Babbage (1791–1871)

Computer programs are instructions for performing a chore that humans would rather avoid doing ourselves. In order to persuade the computer to do them for us, we must communicate our intention in a way that is plain and unambiguous. Programming languages are protocols for this dialogue, designed to enable programmers to conveniently express their intent and facilitate the exchange of information between programmers and computers.

Programs are seldom written from left-to-right in one fell swoop. During the course of writing a program, the programmer often revisits and revises code as they write, sharing additional information and receiving feedback. Often, during this process, the programmer makes a mistake, causing the program to behave in an unexpected manner. These mistakes can manifest as a simple typographic or syntactic error, or a more subtle logical error.

To intercept these errors, programming language designers have adopted a convention for specifying valid programs, called a grammar, which serves two essential purposes. The first is to reject obviously ill-formed programs, and the second is to parse the source code into an intermediate representation that can be handled by a compiler. We will focus on the first case.

When a parser enters an invalid state, a chain of unfortunate events occurs. The compiler halts, raising an error message. To rectify this situation,

the programmer must pause their work, inspect the message, plan a fix, apply it, then try to remember what they were doing beforehand. The cognitive overhead of this simple but repetitive chore can be tiresome. To make matters worse, the error message may be unhelpful or challenging to diagnose.

Program repair attempts to address such errors by inferring the author’s intent from an approximate solution. We can think of this as playing a kind of language game. Given an invalid piece of source code for some programming language, the objective of this game is to modify the code to satisfy the language specification. The game is won when the proposed solution is both valid and the author is satisfied with the result. We want to play this game as efficiently as possible, with as little human feedback as possible.

Prior work on program repair focuses on approximate or semidecision procedures. These methods are heuristic and often brittle, relying on statistical guarantees to locate probable repairs. Furthermore, they rely on a handcrafted set of often language-specific rules, which may not generalize to other programming languages. To our knowledge, no existing approach can repair programs in a language-agnostic way, or guarantee (1) soundness (2) naturalness and (3) completeness in a unified framework. Most are based on software engineering compromises, rather than formal language theory.

Our goal in this thesis is to introduce an edit calculus of program repair. Broadly, our approach is to repair faulty programs by combining probabilistic language models with exact combinatorial methods. We do so by reformulating the problem of program repair in the parlance of formal language theory. In addition to being a natural fit for syntax repair, this also allows us to encode and compose static analyses as grammatical specifications.

Program repair is a highly underdetermined problem, meaning that the validity constraints do not uniquely determine a solution. A proper theory of program repair must be able to resolve this ambiguity to infer the user’s intent from an incomplete specification, and incrementally refine its guess as more information becomes available from the user.

This calculus we propose has a number of desirable properties. It is highly compositional, meaning that users can manipulate constraints on programs while retaining the algebraic closure properties, such as union, intersection, and differentiation. It is well-suited for probabilistic reasoning, meaning we can use any probabilistic model of language to guide the repair process. It is also amenable to incremental repair, meaning that we can repair programs in a streaming fashion, while the user is typing.

2

Formal Language Theory

In computer science, it is common to conflate two distinct notions for a set. The first is a collection sitting on some storage device, e.g., a dataset. The second is a lazy construction: not an explicit collection of objects, but a representation that allows us to efficiently determine membership on demand. This lets us represent infinite sets without requiring an infinite amount of storage. Inclusion then, instead of being simply a lookup query, becomes a decision procedure. This is the basis of formal language theory.

The representation we are chiefly interested in is called a *grammar*, a common metanotation for specifying the syntactic constraints on programs, shared by nearly every programming language. Programming language grammars are overapproximations to the true language, but provide a reasonably detailed specification for rejecting invalid programs and parsing valid ones.

Formal languages are arranged in a hierarchy of containment, where each language family strictly contains its predecessors. On the lowest level of the hierarchy are finite languages. Type 3 contains finite and infinite languages generated by a regular grammar. Type 2 contains context-free languages, which admit parenthetical nesting. Supersets, such as the recursively enumerable sets, are Type 0. There are other kinds of formal languages, such as logics and circuits, which are incomparable with the Chomsky hierarchy.

Most programming languages leave level 2 after the parsing stage, and enter the realm of type theory. At this point, compiler authors layer additional semantic refinements on top of syntax, but must deal with phase ordering problems related to the sequencing of such analyzers, breaking commutativity and posing challenges for parallelization. This lack of compositionality is a major obstacle to the development of modular static analyses.

The advantage of dealing with formal language representations is that we can reason about them algebraically. Consider the context-free grammar: the arrow \rightarrow becomes an $=$ sign, $|$ becomes $+$ and AB becomes $A \times B$. The ambiguous Dyck grammar, then, can be seen as a system of equations.

$$S \rightarrow () \mid (S) \mid SS \iff f(x) = x^2 + x^2 f(x) + f(x)^2 \quad (2.1)$$

We will now solve for $f(x)$, giving us the generating function for the language:

$$0 = f(x)^2 + x^2 f(x) - f(x) + x^2 \quad (2.2)$$

Now, using the quadratic equation, where $a = 1, b = x^2 - 1, c = x^2$, we have:

$$f(x) = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-x^2 + 1 \pm \sqrt{x^4 - 6x^2 + 1}}{2} \quad (2.3)$$

Note there are two solutions, but only one where $\lim_{x \rightarrow 0} = 1$. From the ordinary generating function (OGF), we also have that $f(x) = \sum_{n=0}^{\infty} f_n x^n$. Expanding $\sqrt{x^4 - 6x^2 + 1}$ via the generalized binomial theorem, we have:

$$f(x) = (1 + u)^\alpha = \sum_{k=0}^{\infty} \binom{\alpha}{k} u^k \quad (2.4)$$

$$= \sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} (x^4 - 6x^2)^k \text{ where } u = x^4 - 6x^2 \quad (2.5)$$

Now, to obtain the number of ambiguous Dyck trees of size n , we can extract the x^n -th coefficient using the binomial series:

$$[x^n]f(x) = [x^n] \frac{-x^2 + 1}{2} + \frac{1}{2} [x^n] \sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} (x^4 - 6x^2)^k \quad (2.6)$$

$$[x^n]f(x) = \frac{1}{2} \binom{\frac{1}{2}}{n} [x^n](x^4 - 6x^2)^n = \frac{1}{2} \binom{\frac{1}{2}}{n} [x^n](x^2 - 6x)^n \quad (2.7)$$

We can use this technique, first described by Flajolet & Sedgewick [Fla09], to count the number of trees of a given size or distinct words in an unambiguous CFG. This lets us understand grammars as a kind of algebra, which is useful for enumerative combinatorics on words and syntax-guided synthesis.

Naturally, like algebra, there is also a kind of calculus to formal languages. Janusz Brzozowski [Brz64] introduced the derivative operator for regular languages, which can be used to determine membership, and extract subwords from the language. This operator has been extended to CFLs by Might et al. [MDS11], and is the basis for a family of elegant parsing algorithms.

The Brzozowski derivative has an extensional and intensional form. Extensionally, we have $\partial_a L = \{b \in \Sigma^* \mid ab \in L\}$. Intensionally, we have an induction over generalized regular expressions (GREs), which are a superset of regular expressions that also support intersection and negation.

$\partial_a(\ \emptyset\) = \emptyset$	$\delta(\ \emptyset\) = \emptyset$
$\partial_a(\ \varepsilon\) = \emptyset$	$\delta(\ \varepsilon\) = \varepsilon$
$\partial_a(\ a\) = \varepsilon$	$\delta(\ a\) = \emptyset$
$\partial_a(\ b\) = \emptyset$ for each $a \neq b$	$\delta(\ R^*\) = \varepsilon$
$\partial_a(\ R^*\) = (\partial_a R) \cdot R^*$	$\delta(\ \neg R\) = \varepsilon$ if $\delta(R) = \emptyset$
$\partial_a(\ \neg R\) = \neg \partial_a R$	$\delta(\ \neg R\) = \emptyset$ if $\delta(R) = \varepsilon$
$\partial_a(\ R \cdot S\) = (\partial_a R) \cdot S \vee \delta(R) \cdot \partial_a S$	$\delta(\ R \cdot S\) = \delta(R) \wedge \delta(S)$
$\partial_a(\ R \vee S\) = \partial_a R \vee \partial_a S$	$\delta(\ R \vee S\) = \delta(R) \vee \delta(S)$
$\partial_a(\ R \wedge S\) = \partial_a R \wedge \partial_a S$	$\delta(\ R \wedge S\) = \delta(R) \wedge \delta(S)$

Similar to sets, it is possible to combine languages by manipulating their grammars, mirroring the setwise notions of union, intersection, complementation and difference over languages. These operations are convenient for combining, for example, syntactic and semantic constraints on programs. For example, we might have two grammars, G_a, G_b representing two properties that are desirable or necessary for a program to be considered valid.

Like all representations, grammars are themselves a trade-off between expressiveness and efficiency. It is possible to represent the same finite set with multiple representations of varying complexity. For example, the set of strings containing ten or fewer balanced parentheses can be expressed as a finite automaton containing millions of states, or a simple conjunctive grammar containing a few productions, $\mathcal{L}(S \rightarrow () \mid (S) \mid SS) \cap \Sigma^{[0,10]}$.

The choice of representation is heavily usage-dependent. For example, if we are interested in recognition, we might favor a disjoint representation, allowing properties to be checked independently without merging, whereas if we are interested in generation or deciding non-emptiness, we might prefer a

unified representation which can be efficiently sampled without rejection.

Union, concatenation and repetition are all mundane in the theory of formal languages. Intersection and negation are more challenging concepts to borrow from set theory, and do not translate naturally into the Chomsky hierarchy. For example, the intersection of two CFLs is Turing Complete, but the intersection of a CFL and a regular language is a CFL.

Deciding intersection non-emptiness (INE) of a finite collection of finite automata is known to be PSPACE-complete [Koz77]. It is still unknown whether a faster algorithm than the product construction exists for deciding INE of just two finite automata.

The textbook algorithm proceeds as follows: create an automaton containing the cross-product of states, and simulate both automata in lockstep, creating arcs between states that are co-reachable. If a final state is reachable in the product automaton, then the intersection is non-empty. This requires space proportional to the Cartesian product of the two states.

Figure 2.1: TODO: depict product construction for finite automata here.

The goal of this thesis is to speed up the product construction by leveraging (1) parameterized complexity (2) pruning and (3) parallelization to speed up the wallclock runtime of the product construction and generalize it to CFG-REG intersections. We show it is possible to decide intersection non-emptiness in realtime for Levenshtein automata and build a tool to demonstrate it on real-world programming languages and grammars.

Finally, we show a probabilistic extension of the REG-CFL product construction, which can be used to decode the top-K most probable words in the intersection of two languages. This is useful for applications in natural language processing, where we might want to find the most natural word that satisfies multiple constraints, such as being a valid repair with fewer than k edits whose probability is maximized.

3

Deterministic Program Repair

Parsimony is a guiding principle in program repair that comes from the 14th century Franciscan friar named William of Ockham. In keeping with the Franciscan minimalist lifestyle, Ockham’s principle basically says that when you have multiple hypotheses, the simplest one is the best. It is not precisely clear what “simple” ought to mean in the context of program repair, but a first-order approximation is to strive for the smallest number of changes required to transform an invalid program into a valid one.

Levenshtein distance is one such metric for measuring the minimum number of changes between two strings. First proposed by the Soviet scientist Vladimir Levenshtein, it quantifies how many insertions, deletions, and substitutions are required to transform one string into another. Conveniently, there is an automaton, called the Levenshtein automaton [SM02], that recognizes all strings within a given edit distance of a given string. We can use this automaton to locate the positions and contents of the most likely repair consistent with the observed program and the grammar.

The closure of CFLs under intersection with regular languages was first established in 1961 by Bar-Hillel, implying the existence of a context-free grammar representing the conjunction of any finite automaton and context-free grammar. Such a construction was given by Salomaa in 1973, who provides a direct, but inefficient, construction. In our work, we refine this construction to intersections with Levenshtein automata, which recognize all and only strings within a given edit distance of a reference string. Using this refinement, we demonstrate it is feasible to repair multiline syntax errors in practical programming languages.

Given the source code for a computer program σ and a grammar G , our goal is to find every valid string σ consistent with the grammar G and within a certain edit distance. Consider the language of valid strings within a certain Levenshtein distance from a reference string σ . We can intersect the language given by the Levenshtein automaton with the language of all valid programs given by the grammar G . The resulting language will contain all possible repairs within a small edit distance.

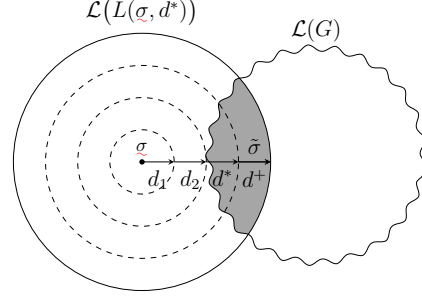


Figure 3.1: CFL intersection.

3.1 Levenshtein Automata

Levenshtein automata are finite automata that recognize all and only strings within a given edit distance of a reference string by permitting insertions, deletions, and substitutions. For example, suppose we have a string , and wish to find nearby repairs. To represent the language of small edits, there is an automaton, called the Levenshtein automaton, recognizing every single string that can be formed by inserting, substituting or deleting a parenthesis. We depict this automaton in Figure 3.2.

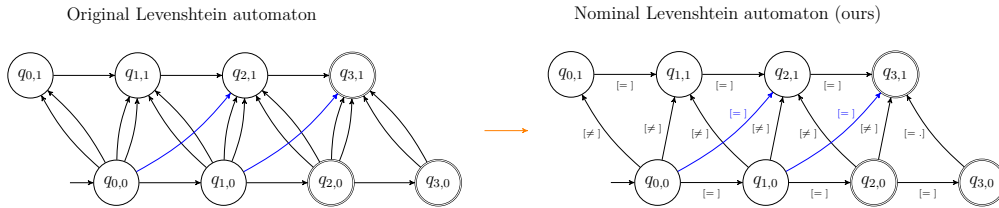


Figure 3.2: Automaton recognizing every 1-edit patch. We nominalize the original automaton, ensuring upward arcs denote a mutation, and use a symbolic predicate, which deduplicates parallel arcs in large alphabets.

The original automaton is nondeterministic, containing an upward arc for each token. This can be avoided with a simple modification that matches an inequality predicate. The machine enters at $q_{0,0}$ and at each step, accepts the labeled token. Final states are encircled twice, denoting that any trajectory ending at such a state is considered valid. When the edit distance grows larger, we introduce some additional arcs to handle multi-token deletions,

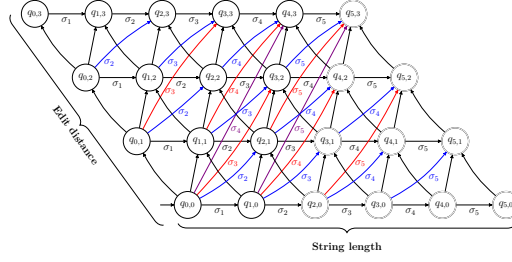


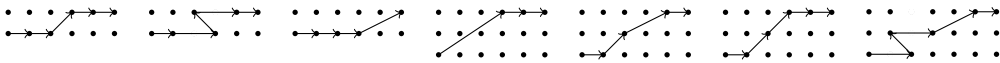
Figure 3.3: NFA recognizing Levenshtein $L(\sigma : \Sigma^5, 3)$.

but the overall picture remains unchanged. We depict a 3x5 automaton recognizing 3-edit patches of a length-5 string in Figure 3.3.

Here, a pattern begins to emerge: the automaton is a grid of states, with each horizontal arc consuming a token in the original string, and upwards arcs recognizing mutations. Traversing a vertical arc corresponds to an insertion or substitution, and a diagonal arc corresponds to a deletion. Levenshtein automata can also be defined as a set of inference rules, which generalize this picture to arbitrary length strings and edit distances. The indices are a bit finicky, but the rules are otherwise straightforward.

$$\begin{array}{c}
\frac{s \in \Sigma \quad i \in [0, n] \quad j \in [1, d_{\max}]}{(q_{i,j-1} \xrightarrow{s} q_{i,j}) \in \delta} \nwarrow \quad \frac{s \in \Sigma \quad i \in [1, n] \quad j \in [1, d_{\max}]}{(q_{i-1,j-1} \xrightarrow{s} q_{i,j}) \in \delta} \nearrow \\
\\
\frac{i \in [1, n] \quad j \in [0, d_{\max}]}{(q_{i-1,j} \xrightarrow{\sigma_i} q_{i,j}) \in \delta} \rightarrow \quad \frac{d \in [1, d_{\max}] \quad i \in [d+1, n] \quad j \in [d, d_{\max}]}{(q_{i-d-1,j-d} \xrightarrow{\sigma_i} q_{i,j}) \in \delta} \nearrow \\
\\
\frac{}{q_{0,0} \in I} \text{INIT} \quad \frac{q_{i,j} \in Q \quad |n - i + j| \leq d_{\max}}{q_{i,j} \in F} \text{DONE}
\end{array}$$

Each rule recognizes a specific type of edit. \nwarrow handles insertions, \nearrow handles substitutions and \nearrow handles deletions of one or more terminals. Let us consider some illustrative cases depicting the edit trajectory with specific Levenshtein alignments. Note that the trajectory may not be unique.



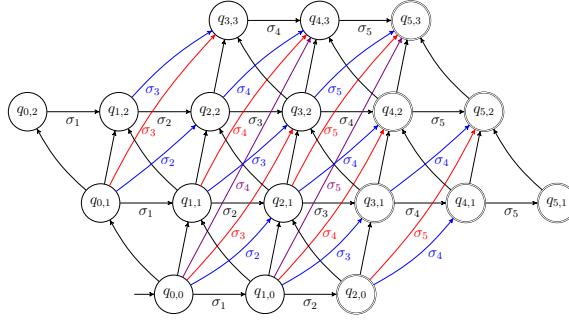
3.2 The Bar-Hillel Construction

The Bar-Hillel construction is a method for conjoining a context-free grammar with a finite automaton. First proposed by Bar-Hillel in 1961, and later realized by Salomaa in 1973, this construction is based on the idea of a product automaton, generalized to a grammar. It consists of three rules:

$$\frac{q \in I \quad r \in F}{(S \rightarrow qSr) \in P_\cap} \sqrt{\quad} \quad \frac{(A \rightarrow a) \in P \quad (q \xrightarrow{a} r) \in \delta}{(qAr \rightarrow a) \in P_\cap} \uparrow$$

$$\frac{(w \rightarrow xz) \in P \quad p, q, r \in Q}{(pwr \rightarrow (pxq)(qzr)) \in P_\cap} \bowtie$$

The \bowtie rule has a strong dependency on the number of states. Every reduction in the number of states will have a cubic impact on the size of the product automaton. So, the primary target is to first reduce the number of states in the Levenshtein automaton. We can reduce the number of states without compromising the integrity of the Bar-Hillel construction by pruning states which are obviously inaccessible. For example, let us consider the following scenario:



$G: \rightarrow$

$\sigma:$	✗
✗	\wedge ✓
✗	\wedge ✓

We can determine the monoedit bounds by conducting a binary search for the rightmost and leftmost states with an empty porous completion problem, and remove all states from the automaton which absorb trajectories that are incompatible. Similar bounds can be established for multi-edit locations.

Now, let us consider the Parikh constraints.

3.3 Parikh Refinements

To identify superfluous q, v, q' triples, we define an interval domain that soundly overapproximates the Parikh image, encoding the minimum and maximum number of terminals each nonterminal must and can generate, respectively. Since some intervals may be right-unbounded, we write $\mathbb{N}^* = \mathbb{N} \cup \{\infty\}$ to denote the upper bound, and $\Pi = \{[a, b] \in \mathbb{N} \times \mathbb{N}^* \mid a \leq b\}^{|\Sigma|}$ to denote the Parikh image of all terminals.

[Parikh mapping of a nonterminal] Let $p : \Sigma^* \rightarrow \mathbb{N}^{|\Sigma|}$ be the Parikh operator [Par66], which counts the frequency of terminals in a string. We define the Parikh map, $\pi : V \rightarrow \Pi$, as a function returning the smallest interval such that $\forall \sigma : \Sigma^*, \forall v : V, v \Rightarrow^* \sigma \vdash p(\sigma) \in \pi(v)$.

The Parikh mapping computes the greatest lower and least upper bound of the Parikh image over all strings in the language of a nonterminal. The infimum of a nonterminal's Parikh interval tells us how many of each terminal a nonterminal *must* generate, and the supremum tells us how many it *can* generate. Likewise, we define a similar relation over NFA state pairs:

[Parikh mapping of NFA states] We define $\pi : Q \times Q \rightarrow \Pi$ as returning the smallest interval such that $\forall \sigma : \Sigma^*, \forall q, q' : Q, q \xRightarrow{\sigma} q' \vdash p(\sigma) \in \pi(q, q')$.

Next, we will define a measure on Parikh intervals representing the minimum total edits required to transform a string in one Parikh interval to a string in another, across all such pairings.

[Parikh divergence] Given two Parikh intervals $\pi, \pi' : \Pi$, we define the divergence between them as $\pi \parallel \pi' = \sum_{n=1}^{|\Sigma|} \min_{(i, i') \in \pi[n] \times \pi'[n]} |i - i'|$.

We know that if the Parikh divergence between two intervals is nonzero, those intervals must be incompatible as no two strings, one from each Parikh interval, can be transformed into the other with fewer than $\pi \parallel \pi'$ edits.

[Parikh compatibility] Let q, q' be NFA states and v be a CFG nonterminal. We call $\langle q, v, q' \rangle : Q \times V \times Q$ *compatible* iff their divergence is zero, i.e., $v \triangleleft qq' \iff (\pi(v) \parallel \pi(q, q')) = 0$.

Finally, we define the modified Bar-Hillel construction for nominal Levenshtein automata as:

$$\frac{(A \rightarrow a) \in P \quad (q \xrightarrow{\textcolor{brown}{a}} r) \in \delta \quad \textcolor{brown}{a}[\cdot]}{(qAr \rightarrow a) \in P_{\cap}} \hat{\uparrow}$$

$$\frac{\textcolor{brown}{w} \triangleleft pr \quad \textcolor{brown}{x} \triangleleft pq \quad \textcolor{brown}{z} \triangleleft qr \quad (w \rightarrow xz) \in P \quad p, q, r \in Q}{(pwr \rightarrow (pxq)(qzr)) \in P_{\cap}} \hat{\bowtie}$$

4

Probabilistic Program Repair

As we have seen, the problem of program repair is highly underdetermined. To resolve this ambiguity, we will use a probabilistic model to induce a distribution over the language of valid programs. This distribution will guide the repair process by assigning a likelihood to each possible repair. Then, taking the maximum over all possible repairs, we can find the most likely repair consistent with the constraints and the observed program.

Specifically, we will define an ordering over strings by their likelihood under the probabilistic model. We then define a repair as the most likely string consistent with the observed program and the grammar. We factorize the probability of a string as the product of the probability of each token in the string, conditioned on its predecessors. This allows us to compute the joint probability in a left-to-right fashion.

This probabilistic model will generally admit programs that are locally probable, but globally inconsistent with the grammar. To enforce syntactic validity, we will use the probabilistic language model to “steer” a generative sampler through the automaton representing the repair language. This has two advantages: first, it allows us to sample from the repair language incrementally, and second, it ensures that subsequences with high probability are retrieved first, and all trajectories are syntactically valid.

We will consider two kinds of probabilistic models: a constrained Markov model and an unconstrained transformer-based neural network trained on program repair, then evaluate the performance of these models on a syntax repair benchmark consisting of pairwise program transformations. As we will show, the constrained Markov model is able to achieve state-of-the-art precision on blind prediction of the lexical sequence.

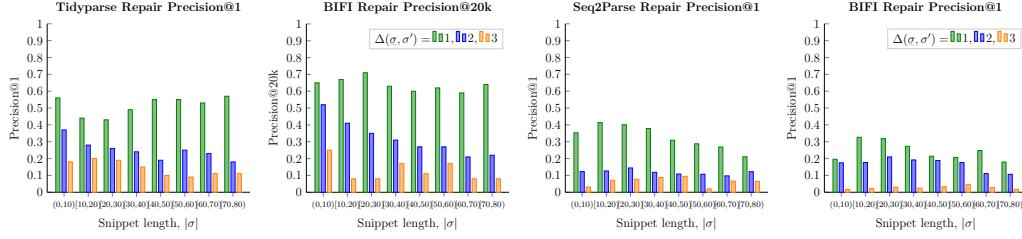


Figure 4.1: Tidyparse, Seq2Parse and BIFI repair precision across length and edits.

If we give it an equivalent number of samples, the constrained Markov model attains an even wider margin.

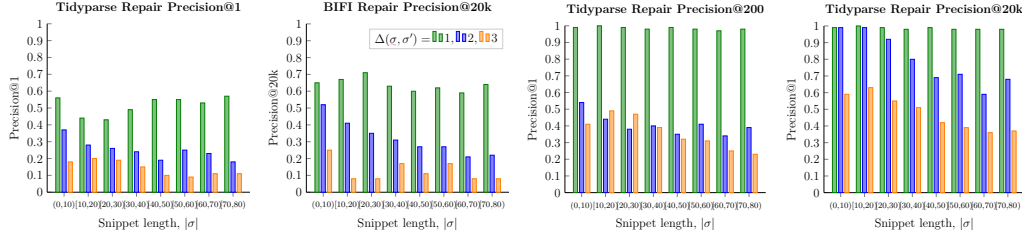


Figure 4.2: Tidyparse, Seq2Parse and BIFI repair precision across length and edits.

Now, we measure latency.

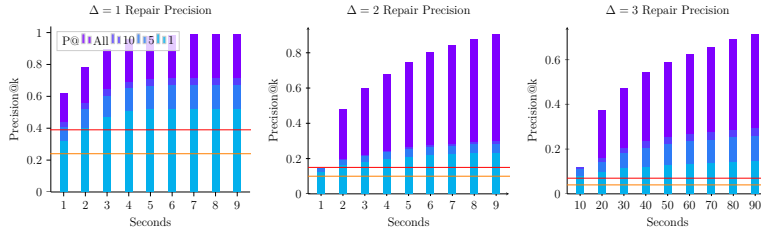


Figure 4.3: Latency benchmarks. Note the varying axis ranges. The red line marks Seq2Parse and the orange line marks BIFI's Precision@1 on the same repairs.

5

Discussion

Official McGill Guidelines: The discussion of findings must be in line with disciplinary expectations. A comprehensive discussion is expected to be a minimum of 10 pages, double-spaced for doctoral students and a minimum of 5 pages, double-spaced for Master's students (including figures, images, and tables). It pertains to the entirety of a thesis. The discussion of findings should provide an final, overarching summary of study themes, limitations, and future directions.

In the case of a manuscript-based thesis, the comprehensive discussion should encompass all of the chapters of the thesis and should not be a repetition of the individual chapters. This section can be used to address issues not sufficiently covered in the preceding chapters or papers (e.g., critiques raised by reviewers that could not be incorporated into published works, or reintroducing discussion arguments removed from published papers upon reviewer request). This section can also be used to elaborate on the practical/applied aspects of published findings in a manner that is more accessible to less expert readers.

6

Conclusions and Future Work

Official McGill Guidelines: Clearly state how the objectives of the research were met and discuss implications of findings.

Publications

This part is optional, but it gives a nice touch to list all the publications (official venues down to poster sessions) throughout your PhD.

Keep this in the same style as publications in your academic CV: Conference / Year - Title - Authors. And here comes a sample ref for the bibliography: [Con23]

- Under Review (2024) – Syntax Repair as Language Intersection
- Midwest PL Summit (2024) – Let’s wrap this up! Incremental structured decoding with resource constraints
- POPL, LAFI (né PPS) (2024) – A Tree Sampler for Bounded Context-Free Languages
- Doctoral Symposium at SPLASH (2023) – A Pragmatic Approach to Syntax Repair
- TEACH Workshop at ICML (2023) – Idiolect: A Reconfigurable Voice Coding Assistant
- BotSE Workshop at ICSE (2023) – Idiolect: A Reconfigurable Voice Coding Assistant
- LIVE Workshop at SPLASH (2022) – Tidyparse: Real-Time Context Free Error Correction
- ARRAY Workshop at PLDI (2022) – Probabilistic Array Programming on Galois Fields
- ICLR (2021) – ∇ Sim: Differentiable simulation for system identification and visuomotor control

Acronyms

Below are a list of acronyms used in the construction of this thesis:

- **NFA**: Nondeterministic **F**inite **A**utomaton
- **DFA**: Deterministic **F**inite **A**utomaton
- **CFG**: Context **F**ree **G**rammar
- **CFL**: Context **F**ree **L**anguage
- **CNF**: Chomsky Normal **F**orm
- **GRE**: Generalized **R**egular **E**xpression
- **OGF**: Ordinary **G**enerating **F**unction

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