

## DYNAMIC PROGRAMMING

Dynamic programming is mainly an optimisation over plain recursion. It means simplifying a complicated problem which has recursion in it by breaking it down into simpler sub-problems.

### EXAMPLES

**Dijkstra's Algorithm:** Dijkstra's algorithm for shortest path problem is a successive approximation scheme that solves the dynamic programming functional equation for shortest path problem by "Reaching" method.

**Fibonacci Sequence:** Original algorithm for getting  $n$ -th Fibonacci number

function fib( $n$ )

if  $n \leq 1$  return  $n$

return fib( $n-1$ ) + fib( $n-2$ )

Using the technique "memoization" of dynamic programming, the above function's performance can be improved drastically. The algorithm of

Fibonacci sequence using "memoization" and bottom-up approach would be

```
function fib(n)
  if n = 0
    return 0
  else
    var previous_fib := 0, current_fib := 1
    repeat n-1 times
      . var new_fib := previous_fib + current_fib
      previous_fib := current_fib
      current_fib := new_fib
    return current_fib
```

Time Complexity for this is  $O(n)$  and space complexity is  $O(1)$  or constant.