

## Answer to the question no-01

Advantage of BFS:

1. Shortest path: when we have to determine shortest route from source to destination in an unweighted graph, it is very useful.
2. Level traversal: when we have to determine a node's level from source node, it works perfectly.
3. Optimization: when there are many solutions for a problem , BFS helps to find the optimal solution.

Advantage of DFS:

1. Topological sorting: when we have to do topological sorting in a directed acyclic graph(DAG), it is more helpful.
2. Single solution: if there is only one solution for a problem DFS performs properly.
3. Memory : DFS runs on path, there is no need to store the nodes. So, it takes less Memory.

Disadvantage of BFS:

1. It stores nodes. For that it needs much more memory than DFS.
2. We can not find the longest path from source node to destination.

Disadvantage of DFS:

1. In an unweighted cyclic graph, it can not perform the shortest path from source to destination.
2. It can not determine the level properly.

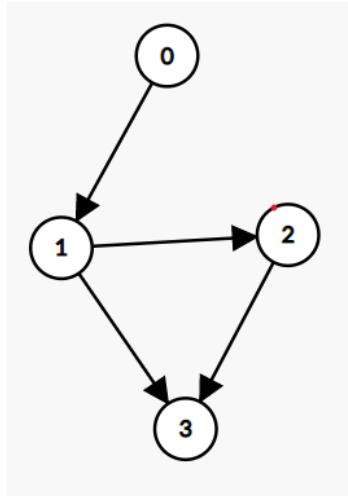
## Answer to the question no-02

There are 3 ways to represent the graph to a computer.

1.Adjacency Matrix:

Expression of a graph by 2D Matrix.

If the adjacency matrix is  $M[\text{node}][\text{node}]$ , then  $M[i][j]==1$  if there is direct connection between i to j using only 1 edge.



This is a directed graph.

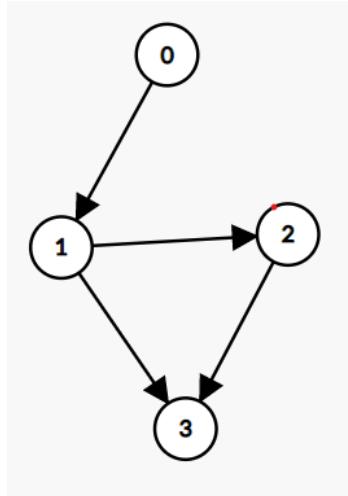
If we want to express it using adjacency matrix then it will look like:

0	1	0	0
0	0	1	1
0	0	0	1
0	0	0	0

If it were a weighted graph then we can write the weight instead of writing 1.

## 2. Adjacency List:

Expression of a graph by linked list or vector. It is a separate list of every node.



For this unweighted directed graph, we can write the list and it will look like:

0->1

1->2,3

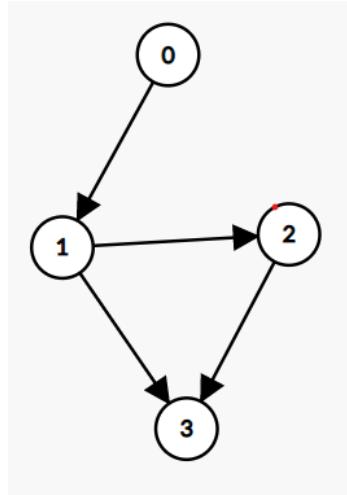
2->3

3->

If it were weighted, we can pair the node and value together.

### 3. Edge List:

Expression of a graph by set.



For this unweighted directed graph, we can write the set and it will look like:

```
[  
    [0,1]  
    [1,2]  
    [2,3]  
    [1,3]  
]
```

If it were a weighted graph then we can add the weight after the 2 nodes in the cell.  
So, in this way we can represent all types of graphs.

## Answer to the question no-03

```
#include<bits/stdc++.h>
```

```
using namespace std;
```

```
const int N=1e5+10;
```

```
int visited[N];
```

```
vector<int>adj_list[N];
```

```
int n;
```

```
bool DFS(int node)
```

```
{
```

```
    visited[node]=1;
```

```
    for(int adj_node:adj_list[node])
```

```
{
```

```
        if(visited[adj_node]==0)
```

```
{
```

```
            bool run=DFS(adj_node);
```

```
            if(run)
```

```
{
```

```
                return true;
```

```
}
```

```
}
```

```
        else if(visited[adj_node]==2)
```

```
{
```

```
            return true;
```

```
}
```

```
}
```

```
    visited[node]=2;
```

```
    return false;
```

```
}
```

```
int main()
```

```
{
```

```
    int e;
```

```
    cin>>n>>e;
```

```
    for(int i=1; i<=e; i++)
```

```
{
```

```
    int u,v;
```

```
    cin>>u>>v;
```

```

adj_list[u].push_back(v);
adj_list[v].push_back(u);
}
bool run;
for(int i=1; i<=n; i++)
{
    if(visited[i]==0)
    {
        run=DFS(i);
        if(run)
        {
            cout<<"Cycle Exist\n";
            break;
        }
    }
}
if(!run)
{
    cout<<"No Cycle\n";
}
}
}

```

### Answer to the question no-04

```

#include<bits/stdc++.h>
using namespace std;
int array_sum(int b,int a,int A[])
{
    if(a==0)
    {
        return A[a];
    }
    b+=A[a]+array_sum(b,--a,A);
    return b;
}
int main()
{
    int n;

```

```

cin>>n;
int A[n];
for(int i=0;i<n;i++)
{
    cin>>A[i];
}
cout<<array_sum(0,n-1,A)<<endl;
}

```

### Answer to the question no-05

```

#include<bits/stdc++.h>
using namespace std;
const int N=1e5 +5;
vector<int>adj_list[N];
int visited[N],level[N],parent[N];
void DFS(int node)
{
    visited[node]=1;
    for(auto adj_node:adj_list[node])
    {
        if(visited[adj_node]==0)
        {
            parent[adj_node]=node;
            level[adj_node]=level[node]+1;
            DFS(adj_node);
        }
    }
}
int main()
{
    int nodes,edges;
    cin>>nodes>>edges;
    for(int i=1;i<=edges;i++)
    {
        int u,v;
        cin>>u>>v;
        adj_list[u].push_back(v);
    }
}

```

```

        adj_list[v].push_back(u);
    }
    int src=1;
    DFS(src);
    if(visited[nodes]==0)
    {
        cout<<"NO"<<endl;
    }
    else
    {
        cout<<"YES"<<endl;
    }
}

```

### **Answer to the question no-06**

```

#include<bits/stdc++.h>
using namespace std;
const int N=1005;
int maze[N][N];
int level[N][N];
int dx[] = {0,0,-1,1}, dy[] = {1,-1,0,0};
int visited[N][N];
int n,m,a,b;
int parent[N][N];
deque<char>r;
char c[] = {'R','L','U','D'};
bool path()
{
    for(int i=0; i<m; i++)
    {
        if(visited[0][i]==1)
        {
            a=0;
            b=i;
            return true;
        }
    }
}

```

```

    }
    for(int i=0; i<n; i++)
    {
        if(visited[i][0]==1)
        {
            a=i;
            b=0;
            return true;
        }
    }
    for(int i=1; i<n; i++)
    {
        if(visited[i][m-1]==1)
        {
            a=i;
            b=m-1;
            return true;
        }
    }
    for(int i=1; i<m-1; i++)
    {
        if(visited[n-1][i]==1)
        {
            a=n-1;
            b=i;
            return true;
        }
    }
    return false;
}
bool is_inside(pair<int,int>coord)
{
    int x=coord.first;
    int y=coord.second;
    if(x>=0&&x<n && y>=0 && y<m)
    {
        return true;
    }
}

```

```

        }
        return false;
    }
bool is_safe(pair<int,int>coord)
{
    int x=coord.first;
    int y=coord.second;
    if(maze[x][y]==-1)
    {
        return false;
    }
    return true;
}
void BFS(pair<int,int>src)
{
    queue<pair<int,int>>q;
    visited[src.first][src.second]=1;
    level[src.first][src.second]=0;
    parent[src.first][src.second]=0;
    q.push(src);
    while(!q.empty())
    {
        pair<int,int>head=q.front();
        q.pop();
        int x=head.first,y=head.second;
        for(int i=0; i<4; i++)
        {
            int new_x=x+dx[i];
            int new_y=y+dy[i];
            pair<int,int>adj_node= {new_x,new_y};
            if(is_inside(adj_node) && is_safe(adj_node) && visited[new_x][new_y]==0)
            {
                visited[new_x][new_y]=1;
                level[new_x][new_y]=level[x][y]+1;
                parent[new_x][new_y]=i;
                q.push(adj_node);
            }
        }
    }
}

```

```

        }
    }
}
int main()
{
    cin>>n>>m;
    pair<int,int>src,dst;
    memset(level,-1,sizeof(level));
    memset(visited,0,sizeof(visited));
    for(int i=0; i<n; i++)
    {
        string input;
        cin>>input;
        for(int j=0; j<m; j++)
        {
            if(input[j]=='#'||input[j]=='M')
            {
                maze[i][j]=-1;
            }
            else if(input[j]=='A')
            {
                src= {i,j};
            }
        }
    }
    BFS(src);
    if(!path())
    {
        cout<<"NO\n";
        return 0;
    }
    cout<<"YES\n";
    dst.first=a;dst.second=b;
    cout<<level[a][b]<<endl;
    while(1)
    {
        int d=parent[dst.first][dst.second];

```

```
if(src==dst)
{
    break;
}
r.push_front(c[d]);
dst.first-=dx[d];
dst.second-=dy[d];
}
for(auto i:r)
{
    cout<<i;
}
}
```

## **Answer to the question no-07**

The Dijkstra algorithm is used for determining the shortest path on a weighted graph. So, the steps are follow:

1. First of all we determine the distance from source to destination is infinity.

2. As our source node is E , so explore the node from E and write down the distance from it.

- E is a done node. Now choose the smallest distance which is node G and explore it. Here exploring G we get node E but we cannot update the value as  $0 < 5$ .

4. G is a done node. Now the smallest is node F. Exploring node F we get B,H. as  $13+6 < 20$  so we update the distance of B and write down the distance of H.

5. F is done. Now the smallest is node C. when exploring C we get B . As  $16 < 19$  so, we update the distance and write down the distance of A.

6. C is done. A is now the smallest. When exploring A we get B,I,J. Here  $12 < 16$  so we update the distance of B and write down the distance of I and J.

7. A is done. Now the smallest is node B. From node B we can explore A,C,E,F,G,H. Distance of H is the same, so we do not need to update the value. So write down the values.

	A	B	C	D	E	F	G	H	I	J
	-	-	-	-	-	-	-	-	-	-
E	-	20	9	-	0	-	5	-	-	-
G	-	20	9	-	0	6	5	-	-	-
F	-	19	9	-	0	6	5	27	-	-
C	10	16	9	-	0	6	5	27	-	-
A	10	12	9	-	0	6	5	27	28	15
B	10	12	9	-	0	6	5	27	28	15

8. B is done. Now the smallest is J. we get A,B,I. Here  $21 < 28$ , so we update the distance of I and write down the others.

	A	B	C	D	E	F	G	H	I	J
	-	-	-	-	-	-	-	-	-	-
E	-	20	9	-	0	-	5	-	-	-
G	-	20	9	-	0	6	5	-	-	-
F	-	19	9	-	0	6	5	27	-	-
C	10	16	9	-	0	6	5	27	-	-
A	10	12	9	-	0	6	5	27	28	15

<b>B</b>	10	12	9	-	0	6	5	27	28	15
<b>J</b>	10	12	9	-	0	6	5	27	21	15

9. J is done. Now the smallest is I. we get A,H,J. As the value becomes large , we don't need to update it.

	<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>	<b>F</b>	<b>G</b>	<b>H</b>	<b>I</b>	<b>J</b>
	-	-	-	-	-	-	-	-	-	-
<b>E</b>	-	20	9	-	0	-	5	-	-	-
<b>G</b>	-	20	9	-	0	6	5	-	-	-
<b>F</b>	-	19	9	-	0	6	5	27	-	-
<b>C</b>	10	16	9	-	0	6	5	27	-	-
<b>A</b>	10	12	9	-	0	6	5	27	28	15
<b>B</b>	10	12	9	-	0	6	5	27	28	15
<b>J</b>	10	12	9	-	0	6	5	27	21	15
<b>I</b>	10	12	9	-	0	6	5	27	21	15

10. 'I' is done. Last one is H. There is no scope to update any value. So, write down the previous row.

	<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>	<b>F</b>	<b>G</b>	<b>H</b>	<b>I</b>	<b>J</b>
	-	-	-	-	-	-	-	-	-	-
<b>E</b>	-	20	9	-	0	-	5	-	-	-

<b>G</b>	-	20	9	-	0	6	5	-	-	-
<b>F</b>	-	19	9	-	0	6	5	27	-	-
<b>C</b>	10	16	9	-	0	6	5	27	-	-
<b>A</b>	10	12	9	-	0	6	5	27	28	15
<b>B</b>	10	12	9	-	0	6	5	27	28	15
<b>J</b>	10	12	9	-	0	6	5	27	21	15
<b>I</b>	10	12	9	-	0	6	5	27	21	15
<b>H</b>	10	12	9	-	0	6	5	27	21	15

11. After performing the dijkstra algorithm we get the distance from E to all nodes.

	<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>	<b>F</b>	<b>G</b>	<b>H</b>	<b>I</b>	<b>J</b>
	-	-	-	-	-	-	-	-	-	-
<b>E</b>	-	20	9	-	0	-	5	-	-	-
<b>G</b>	-	20	9	-	0	6	5	-	-	-
<b>F</b>	-	19	9	-	0	6	5	27	-	-
<b>C</b>	10	16	9	-	0	6	5	27	-	-
<b>A</b>	10	12	9	-	0	6	5	27	28	15
<b>B</b>	10	12	9	-	0	6	5	27	28	15
<b>J</b>	10	12	9	-	0	6	5	27	21	15
<b>I</b>	10	12	9	-	0	6	5	27	21	15
<b>H</b>	10	12	9	-	0	6	5	27	21	15

From E node

A->10  
B->12  
C->9  
E->0  
F->6  
G->5  
H->27  
I->21  
J->15

### **Answer to the question no-08**

Recursive case:

It is a part of a recursive function. When a function calls itself ,it is called a recursive case and the recursive case will run until the termination condition is met.

Base case:

It is a very important part of a recursive function. Because it is the termination condition of a recursive function. If we do not write a base case the program will fall in infinite position.

The relation between base case and recursive base is very important. Because base case can not terminate the function itself, when a recursive case calls the base case then it terminates the recursion.

If we see an example:

```
int Pow(int n,int m)
{
if(m==1)
{
return n;
}
return n*Pow(n,m-1);
}
```

Here the recursive case is Pow(n,m-1) and the base case is m==1.

The function Pow is calling itself by lessening the number by 1.

As a result when m==1 then it terminates the function , does the calculation and returns the value to the main function.

This is how a recursive function works.