### Final Syllabus Stats

### 1. Normal Dist.

Find the value of z according to this formula if X is given. And then find area by seeing corresponding value of z.

$$Z = \frac{X - \mu}{\sigma}$$

#### Normal dist in reverse:

- If area is above then write + with value of z.
- If area is below then write with value of z.

#### **Binomial:**

- If less than X: find prob. till X-0.5 e.g X=30 then  $P(x \le 29.5)$
- If less than equal to X: Find prob till X+0.5 e.g X=30 then P(x<=30.5)
- If greater than X: then X+0.5 e.g, X=60 then P(x>=60.5)
- If at least X: then X-0.5 e.g, X=60 then P(x>=59.5)
- If in between X1 and X2: X1-0.5 and X2+0.5 e.g, X1=40 and X2=60 P(39.5<=X<=60.5)
- Exactly X: make X1=X-0.5 and X2=X+0.5 e.g, X=50 then find P(49.5 <= X <= 50.5)

### 2. Linear Regression:

• Co-eff. Of Correlation "r":

$$r = \frac{\sum xy - \frac{(\sum x)(\sum y)}{n}}{\sqrt{\left[\sum x^2 - \frac{(\sum x)^2}{n}\right]\left[\sum y^2 - \frac{(\sum y)^2}{n}\right]}}$$

Or 
$$r = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sqrt{\sum (x - \bar{x})^2 \cdot \sum (y - \bar{y})^2}}$$

Y on X:

$$Y = \alpha + \beta x$$

$$\alpha = \bar{y} - \beta \bar{x}$$

$$\beta_{yx} = \frac{\sum xy - \frac{(\sum x)(\sum y)}{n}}{[\sum x^2 - \frac{(\sum x)^2}{n}]}$$
Or 
$$\beta_{yx} = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$

• X on Y:

$$x = \alpha + \beta y$$

$$\alpha = \bar{x} - \beta \bar{y}$$

$$\beta_{xy} = \frac{\sum xy - \frac{(\sum x)(\sum y)}{n}}{[\sum y^2 - \frac{(\sum y)^2}{n}]}$$

$$\text{Or } \beta_{xy} = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (y - \bar{y})^2}$$

### • Properties:

$$Rxy = \sqrt{\beta_{xy} * \beta_{yx}}$$

• **SSE**:

$$\sum e^2 = \sum (y - \hat{y})^2$$

• Co-eff. Of determination:

$$R^2 = \frac{\sum (y - \hat{y})^2}{\sum (y - \bar{y})^2}$$

It is percentage that x% times our estimation is right.

### 3. Testing and Hypothesis:

### 1. General Procedure of Testing Mean (for large data):

If  $n \ge 30$ . And population is known.

$$Z = \frac{\bar{X} - \mu}{\frac{\sigma}{\sqrt{n}}}$$

And

$$Z = \frac{\bar{X} - \mu}{\frac{S}{\sqrt{n}}}$$

X bar = Sample Mean.

 $\mu = Population Mean$ 

 $\sigma = Population S.D$ 

 $\sigma^2 = Pop. Variance$ 

S<sup>2</sup>= Sample Variance

s<sup>2</sup>= Unbiased Sample Variance

N= Population

N=Sample Size

Note:

if there is discussion of equality in question then put this in H0.

If there is not discussion of equality in question then put in H1.

### 2. Testing of Mean for Small Data:

If pop. Is unknown and n<30.

Apply t-test.

$$t = \frac{\bar{x} - \mu}{\frac{S}{\sqrt{n}}}$$

And  $s = \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}}$  and calculate s according to this formula in 5<sup>th</sup> step calculation.

# 3. Testing of Proportion: (don't apply t-test in this)

P= Proportion of Population

$$q=1-p$$

n= Sample Size

In this we change mu to P and P0. In 1st step

$$Z = \frac{X - np}{\sqrt{npq}} \text{ for } 5^{\text{th}} \text{ step calculation}$$

# 4. Testing of Difference of Two Means:

Use mu1 and mu2 in hyp.

$$Z = \frac{(\overline{x1} - \overline{x2})}{\sqrt{\frac{s1^2}{n1} + \frac{s2^2}{n2}}}$$

# 5. Testing of Difference of Two Proportions:

Use P1 and P2 in hyp.

$$Z = \frac{(\widehat{P1} - \widehat{P2})}{\sqrt{\frac{\widehat{P1}\widehat{q1}}{n_1} + \frac{\widehat{P2}\widehat{q2}}{n_2}}}$$

$$\widehat{P1} = X1/n1$$

$$\widehat{P2} = X2/n2$$

$$\widehat{q1} = 1 - \widehat{P1}$$

$$\widehat{q2} = 1 - \widehat{P2}$$