

In the name of God



**Sharif University of Technology**

School of Electrical Engineering

**Principles of Biomedical Engineering**

Dr. Ali Ghazizadeh

Fall Semester 1400

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## Homework 2 - Cell potential

*Note:*

- Please upload your assignment on CW.
  - You can either type or scan your answers but it should be legible.
  - Your file name should be in format of HW#\_Name\_Student ID.
  - Do not copy other students' answers.
  - If you have any questions regarding this assignment, message *@asadian\_ah* in Telegram or email *ahosseina98@gmail.com*.
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### ***Problem 1.***

Choose the correct answer.

1. Which of the following values is unnecessary when finding the equilibrium potential of an ion using the Nernst equation?
  - a) The temperature
  - b) The ratio of external and internal ion concentrations.
  - c) The charge of the ion
  - d) The permeability of the ion channel

2. The resting membrane potential is close in value to the Nernst equilibrium potential for ——— because ———.
- a)  $\text{Na}^+$  / there is a leakage of  $\text{Na}^+$  ions through the membrane channels
  - b)  $\text{K}^+$  / there is a leakage of  $\text{Ca}^{2+}$  ions through the membrane channels
  - c)  $\text{K}^+$  / the membrane is very permeable to  $\text{K}^+$  ions at rest
  - d)  $\text{Na}^+$  / due to its large driving force
  - e)  $\text{Cl}^-$  / because it's the only negatively charged ion
3. What effect does an intravenous injection of KCl have on behavior of neurons?
- a) Extracellular  $[\text{K}^+]$  decreases and therefore the membrane potential gets closer to  $\text{Na}^+$  equilibrium potential.
  - b) The membrane potential becomes more negative and it becomes more difficult to generate action potentials.
  - c) Extracellular  $[\text{K}^+]$  increases and therefore the membrane potential gets closer to  $\text{Na}^+$  equilibrium potential.
  - d) None of the above is true.
4. What would happen to the resting membrane potential of a neuron if sodium ( $\text{Na}^+$ ) channels were normally open in the membrane, but everything else was the same?
- a) Nothing much would happen, and it would remain at approximately -65 mV.
  - b) It would be less negative than the normal resting potential.
  - c) It would be more negative than the normal resting potential.
  - d) It would lose its polarization and stand at exactly 0 mV (no difference between inside and outside of the neuron).
  - e) None of the above.

## ***Problem 2.***

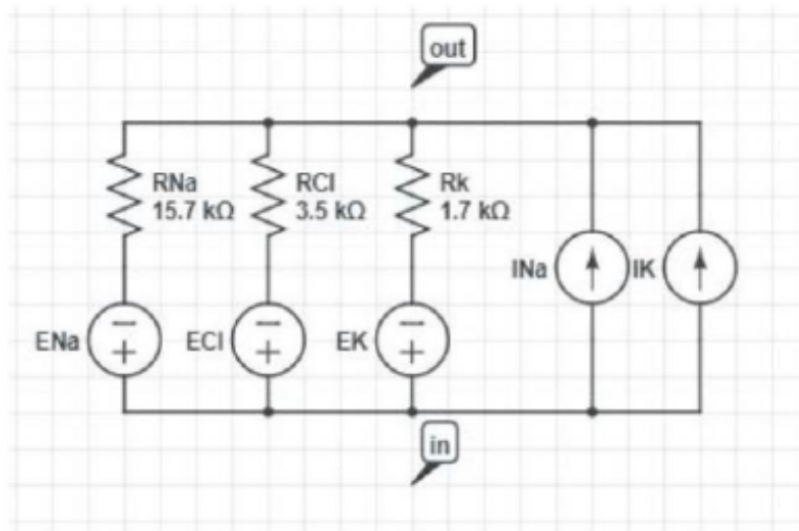
Derive Goldman equation when we have four ions of  $\text{Ca}^{2+}$ ,  $\text{Cl}^-$ ,  $\text{K}^+$ ,  $\text{Na}^+$ .

### Problem 3.

Consider the following values for concentration and membrane permeability of each ion and answer the following questions.

Ion	Relative Permeability	ICF	ECF
$K^+$	1	300	30
$Na^+$	0.1	20	500
$Cl^-$	0.15	40	400

$$R_k = 1.7 \text{ K}\Omega, R_{Na} = 15.7 \text{ K}\Omega, R_C = 3.5 \text{ K}\Omega$$

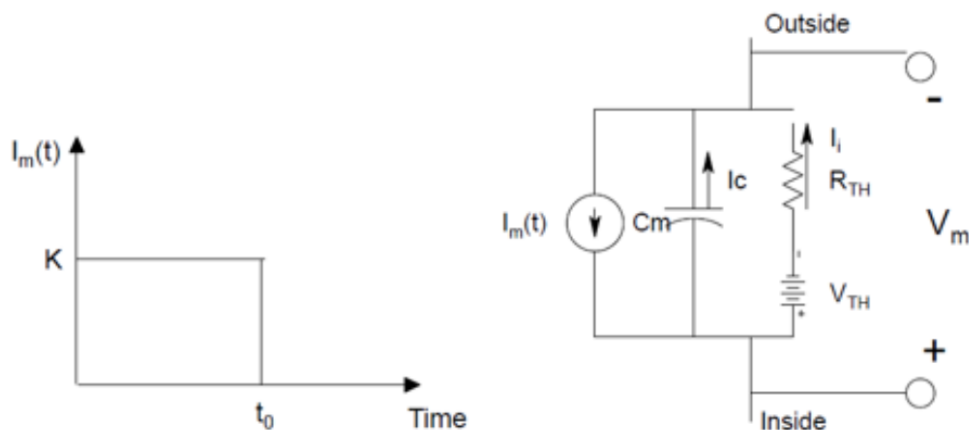


- If there were no active pump mechanism (i.e. the current sources were zero) what would be the resting membrane potential and ion currents according to parallel-conductance membrane model?
- Which Nernst potential is close to resting potential of membrane?
- If both pumps are active, can you use the Goldman equation with all ions to calculate the resting potential? Explain your answer.

## Problem 4.

Assume  $I_m(t)$  is applied to cell membrane. Calculate and plot cell membrane potential.  
( $t_0 = 6ms$ ,  $K = 15\mu A$ )

$R_k = 1.7\text{ K}\Omega$ ,  $R_{Na} = 15.67\text{ K}\Omega$ ,  $R_C = 3.125\text{ K}\Omega$   
 $E_k = 150\text{ mv}$ ,  $E_{Na} = 56\text{ mv}$ ,  $E_{Cl} = 150\text{ mv}$ ,  $C_m = 1\text{ }\mu\text{F}$



## Problem 5.

Equilibrium concentrations of intracellular and extracellular ions are shown for a ‘normal’ marine algal cell (*Valonia ventricosa*) in the table below. The reported membrane potential is  $-70\text{ mV}$  (negative-inside)<sup>1</sup>.

- a) For the four ions below, sort ions based on their predicted relative permeabilities, given the reported resting voltage. Then find a way to approximate the relative permeability of each ion with respect to the most permeable ion.

Ion	Extracellular(mM)	Intracellular(mM)
$\text{Na}^+$	490	40
$\text{K}^+$	10	435
$\text{Ca}^{2+}$	1.0	$< 10^{-4}$
$\text{Cl}^-$	560	140

<sup>1</sup>Gutknecht J (1966) Sodium, potassium, and chloride transport and membrane potentials in *Valonia ventricosa*. The Biological Bulletin 130:331–344.

- b) For the most permeable ion (in a), calculate the net concentration of imbalanced charge that would cause a potential of  $-100$  mV. Valonia is a spherical cell with a diameter of 1 centimeter.

(Equations and constants are provided. Please be sure that you show units.)

$$Q = C \cdot \Delta E, \quad (\text{coulombs}) = (\text{coulombs/volt}) (\text{volt})$$

$$\text{Charge (Q) for a spherical cell of radius } r : \quad Q = \text{Volume} \cdot c \cdot F$$

$c$  is the concentration of net charge and  $F$  is the Faraday constant.

$$\text{Capacitance of a spherical cell of radius } r : \quad C = \text{Area} \cdot C'$$

$C'$  is the capacitance per unit area. ( $\simeq 1 \frac{\mu F}{cm^2}$  for cells)

$$F = 9.649 \cdot 10^4 \text{ (coulombs} \cdot \text{mol}^{-1}\text{)}$$

## Problem 6. The Patch Clamp

The patch-clamp technique was developed in 1976 by Erwin Neher and Bert Sakmann to record current from single ion channels.

- a) Explain this technique briefly.
- b) It is 1976 and you developed the patch clamp technique. You obtained the following data from your first experiment. What does this tell you about the ion channel in this recording? Provide a rationale for your answer.  
(The patch pipette did not contain any neurotransmitters.)

