

## Lecture 1: August 31

*Lecturer: Vijay Garg**Scribe: Asad Malik*

## Introduction

Students in EE 382N are required to scribe lecture notes for one lecture. These lecture notes will be done using the document processing system called Latex. There is a sample *scribe.tex* file on the Canvas system which can be used as a template. You can run `pdflatex` on that file to generate *scribe.pdf*.

During each class, the professor will list the topics to be covered on the whiteboard. Once a topic has been completed, he will check it off the list. That's the time to ask questions.

**Textbook:** Elements of Distributed Computing

The textbook will cover roughly 50% of the course material. The rest will be covered by lectures and research papers. There will be 3 tests during the semester and **no** final exam. Test dates will be posted on canvas.

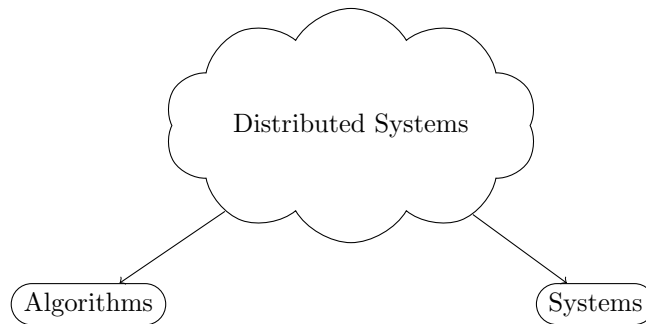
## Course Rules

- No cellphone or laptop use allowed during the lecture
- Tablets are permitted for the sole purpose of taking lecture notes
- Ask at least one question during the semester
- Limit yourself to 5 questions during a lecture
- No guns allowed in the office

## Course Info

- Prof. Garg Office: EER 7.884
- TA: Changyong Hu (colinhu9@gmail.com)
- Assignments done in groups of 2
- Term project done in teams of 3-4

## Goals of the Course



Both **Algorithms** and **Systems** are an important part of this course. We will be covering the theory as well as putting it into practice so expect to work on complex programming assignments.

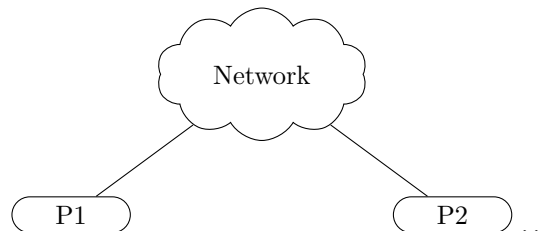
The term project is a very important part of the course. The goal is to produce something new instead of working on already solved problems. The term project is loosely based on a conference style of submission with each team submitting a paper (7-8 pages) which will be reviewed by their peers. Papers which are accepted by the reviewers will be presented at the end of the semester. The deadline for submission will be 2-3 weeks prior to the end of the semester (exact dates are TBD). You will be expected to study and work in groups as collaboration is a good way to learn the material.

## Happened-before, Posets & Lattices

**Source:** Lamport's paper '78 *Time, Clocks, and the Ordering of Events in a Distributed System*

**Definition** of Distributed Systems. There are 3 assumptions associated with what a distributed system is:

1. No shared clocks
2. No shared memory
3. Asynchronous



The only way for communication is through messages which may take an unbounded amount of time. There is no way to synchronize the clocks due to uncertainty of how long messages might take.

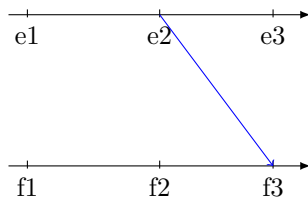
Lamport's paper discusses how to order events with asynchronous clocks.

Defining happened-before ( $\rightarrow$ ) without using clocks:

If we say  $e \rightarrow f$ , we must be 100% certain of the fact. Rules for  $\rightarrow$  relations.  $\rightarrow$  is the smallest relation such that:

- if  $e$  occurred before  $f$  in the same process, then  $e \rightarrow f$
- if  $e$  is send of a message and  $f$  is the receive of that message, then  $e \rightarrow f$
- if  $\exists g: e \rightarrow g \wedge g \rightarrow f$ , then  $e \rightarrow f$

**Example:**



From the example, we can infer the following:

1.  $e1 \rightarrow e2$ ,  $e2 \rightarrow e3$ , hence  $e1 \rightarrow e3$
2.  $f1 \rightarrow f2$ ,  $f2 \rightarrow f3$ , hence  $f1 \rightarrow f3$
3.  $e2 \rightarrow f3$  (message sent at  $e2$  received at  $f3$ ) hence  $e1 \rightarrow f3$

**Concurrent Events:**  $e \parallel f \implies (e \not\rightarrow f) \wedge (f \not\rightarrow e)$

$\rightarrow$  is transitive.

$\rightarrow$  is irreflexive; no event can happen before itself just like  $<$  "less than" relationship.

$\rightarrow$  defines relationships in the irreflexive partially ordered set.

Examples of **irreflexive asymmetric**

- $(E, \rightarrow)$
- $(N, <)$

where:

$E$  is the set of all relationships defined by  $\rightarrow$  relationship

$N$  is the set of all natural numbers defined by  $<$  relationship

Examples of **reflexive antisymmetric**

- $(E, \Rightarrow)$
- $(N, \leq)$

where:

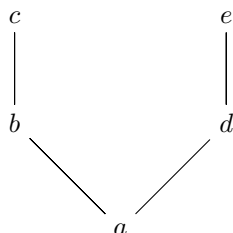
$E$  is the set of all relationships defined by  $\Rightarrow$  relationship

$N$  is the set of all natural numbers defined by  $\leq$  relationship

$$(e \Rightarrow f) \wedge (f \Rightarrow e) \implies e = f$$

## Posets

Hasse Diagram transitively reduced diagram



$a < b, a < c$

$a < d, a < e$

$b < c, d < e$

**Chain:**  $Y$  is a chain in  $X$  if

$\forall a, b \in Y: (a \leq b) \vee (b \leq a)$

**Example:** Longest chains are  $(a, b, c)$  and  $(a, d, e)$ . [Length is 3]

**Anti-Chain:**  $Y$  is an anti-chain in  $X$  if

$\forall a, b \in Y: (a \parallel b)$

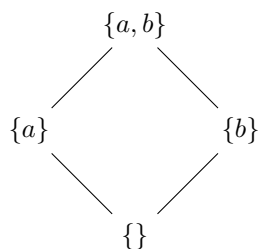
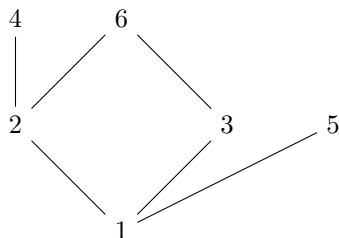
**Example:** Longest anti-chains are  $(b, d)$ ,  $(c, e)$ ,  $(c, d)$ ,  $(b, d)$ . [Width is 2]

**Note:**

1. Height of poset is the longest chain
2. Width of poset is longest anti-chain

### Some More Examples

Relation  $(\mathbb{N}, \text{divides})$ .  $a \leq b$  if  $a$  divides  $b$ , i.e  $b \% a = 0$



Set  $Y = a, b$  Subsets of  $Y$ :

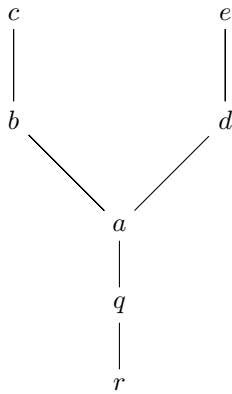
## Infimum and Supremum

### Infimum

Given  $(X, \leq)$  &  $Y \subseteq X$

$m \in X$  is the meet/infimum/"greatest lower bound" of  $Y$  if

1.  $\forall y \in Y: m \leq y$  { $m$  is a lower bound}
2.  $\forall m' : [\forall y \in Y: m' \leq y] \implies m' \leq m$



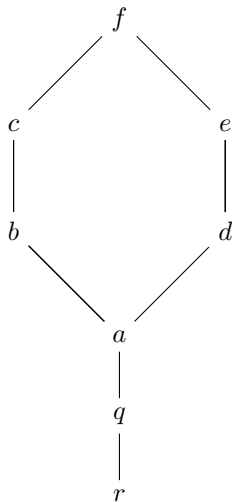
$\mathbf{inf}(b, d) = a = b \sqcap d$

$\mathbf{inf}$  is represented by the symbol  $(\sqcap)$

### Supremum

Supremum is the least upper bound and is represented by the symbol  $(\sqcup)$ . For the example above, the  $\mathbf{sup}(b, d)$  or  $b \sqcup d$  does not exist.

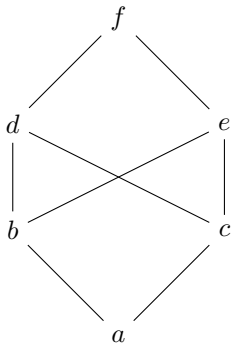
A poset  $(X, \leq)$  is a lattice if for all finite  $Y \subseteq X$ ,  $\mathbf{sup}(Y)$  and  $\mathbf{inf}(Y)$  exist.



The example above is a lattice as for all subsets,  $\mathbf{sup}$  and  $\mathbf{inf}$  exist.

$b \sqcup d = f$

$b \sqcap d = a$



The example above is **NOT** a lattice.

$b \sqcup c =$  does not exist

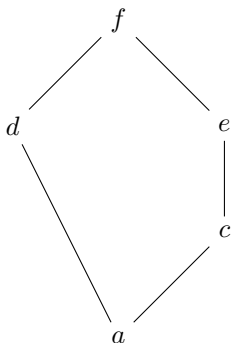
$b \sqcap c = a$

For  $(\mathbb{N}, \text{divides})$  poset,  $\text{GCD} = \inf$  and  $\text{LCM} = \sup$ .

**Distributive Property:**

1.  $a \sqcap (b \sqcup c) = (a \sqcap b) \sqcup (a \sqcap c)$
2.  $a \sqcup (b \sqcap c) = (a \sqcup b) \sqcap (a \sqcup c)$

**Pentagon Lattice**



The lattice above is not distributive.

**Diamond Lattice**

