Tiebreaking Strategies for A* Search: How to Explore the Final Frontier

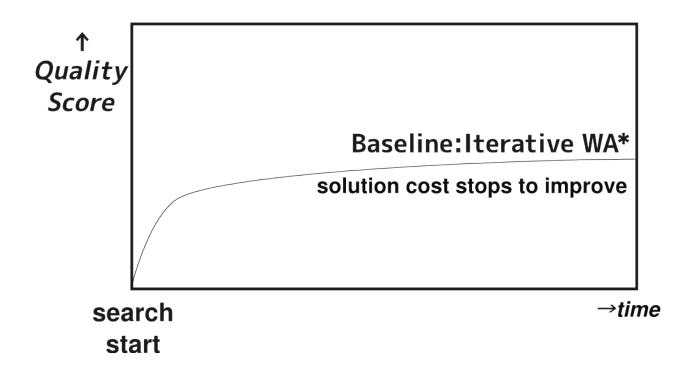
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Presentation available on

https://guicho271828.github.io/2016-6-13-hsdip/

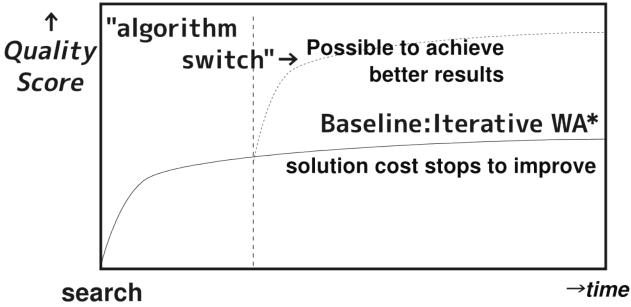
1 Satisficing Planning + Online Cost Refinements

Typical Characteristics of Anytime Algorithms



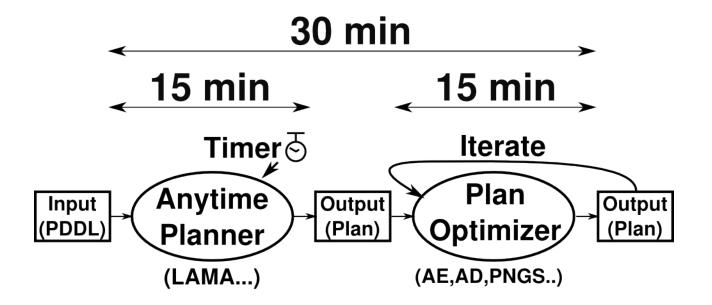
2 Satisficing Planning + Algorithm Switch

Typical Characteristics of Anytime Algorithms



start One major example: Plan Postprocessing

3 Main Topic of the paper: Plan Postprocessing



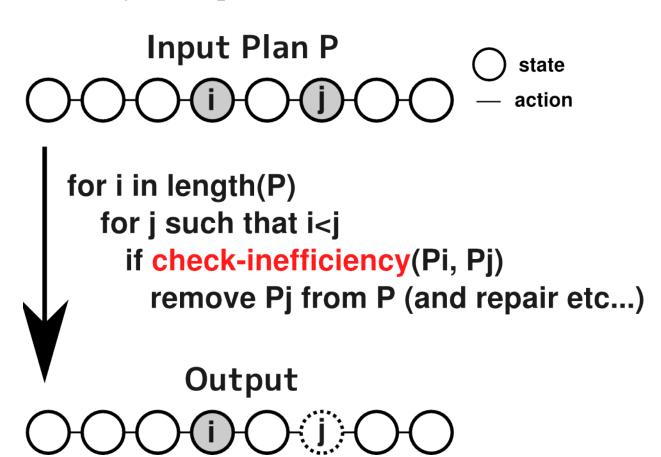
4 Various Postprocessing Systems

- Aras (Nakhost and Muller 2010)
 - Action Elimination(AE) remove trivially redundant actions
 - Plan Neighborhood Graph Search(PNGS) replan on neighborhood graph
- Action Dependency (AD) (Chrpa, McCluskey and Osborne 2012)
 - Remove actions of inverse effects etc.
- Block Deordering (BDPO2) (Siddiqui and Haslum 2013;2015)
 - convert the input to partial order blocks, replan each block
- Anytime Iterative Refinement of Solution (AIRS) (Estrem and Krebsbach 2012)

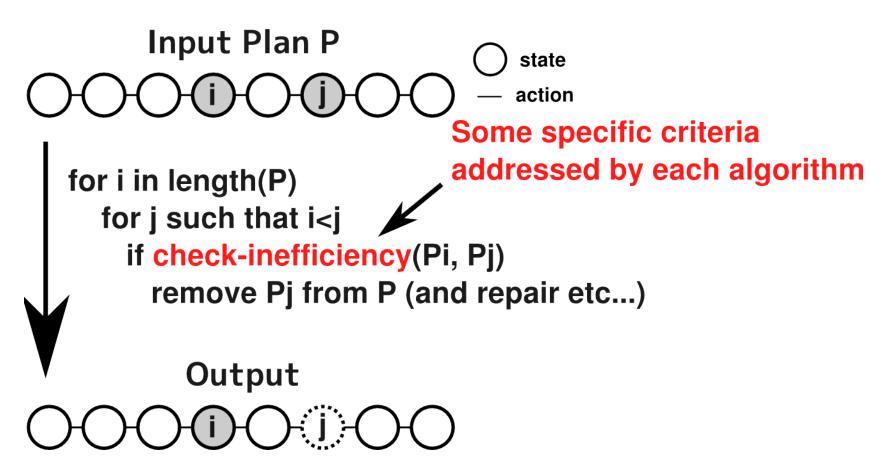
5 Two groups of Optimization Algorithms

Polytime Optimizer	Search-based Optimizer
Based on the direct	External solver refines
analysis of a given plan	a partial segment in a plan

5.1 Polytime Optimizers



5.2 Polytime Optimizers



5.3 Two groups of Optimization Algorithms

Polytime Optimizer

Based on the direct

External solver refines

analysis of a given plan

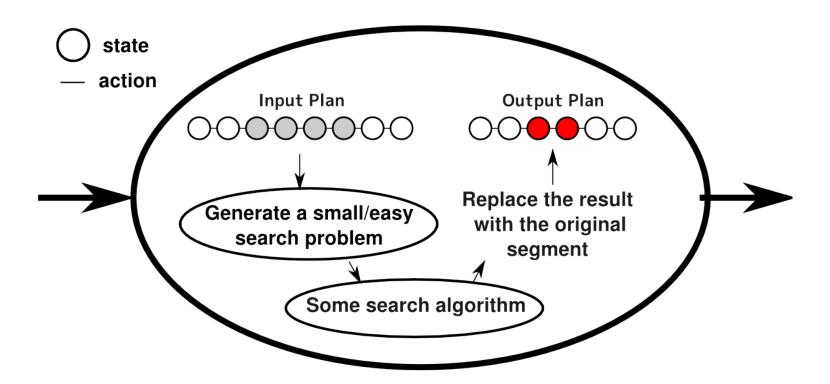
a partial segment in a plan

 $AE: O(n^2)$

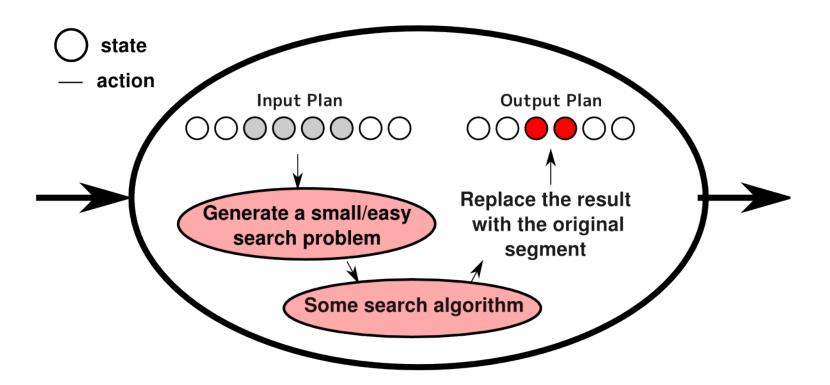
 $AD: O(n^2)$

n: plan length

5.4 Search-based Optimizers



5.5 Search-based Optimizers



5.6 Two groups of Optimization Algorithms

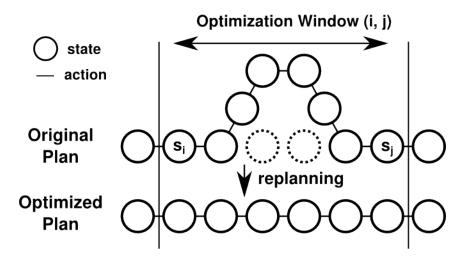
Polytime Optimizer	Search-based Optimizer			
Based on the direct	External solver refines			
analysis of a given plan	a partial segment in a plan			
$AE: O(n^2)$	PNGS			
$AD: O(n^2)$	AIRS			
n: plan length	BDPO2			

5.7 Search-based Optimizers Taxonomy

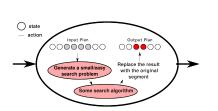
State		
— action Input Plan	Output Plan	
/0000000	000000	
	1 \ ~	
Generate a small/easy search problem	Replace the result with the original	
search problem	segment	
Some search a	lgorithm	

	Subproblems are based on	Subproblems are solved v
PNGS	neighborhood graph	
	(search space around the plan)	
AIRS	windows (ordered by $\Delta \cot/\Delta h$)	
BDPO2	windows (block decomposition)	

5.8 Window-based optimization



5.9 Search-based Optimizers Taxonomy



	Subproblems are based on	Subproblems are solved v
PNGS	neighborhood graph	Blind unit-cost A*
	(search space around the plan)	or Backward Breadths Fi
AIRS	windows (ordered by $\Delta \cos t/\Delta h$)	Blind Bidirectional
BDPO2	windows (block decomposition)	Admissible A*
		or PNGS (lavered approa

6 Open Questions

What is the baseline of various search-based optimizers?

i.e. Are these *complex* algorithms necessary?

How to combine Polytime and Search-based Optimizers?

Also, how effective is it to combine them?

7 Various Minor Differences in Search-based Optimizers

	Subproblems are based on	Subproblems are solved with
PNGS	neighborhood graph	Blind unit-cost A*
	(search space around the plan)	or Backward Breadths First
AIRS	windows (ordered by $\triangle \cot \Delta h$)	Blind Bidirectional
BDPO2	windows (block deordering)	Admissible A*
		or PNGS (layered approach)

→ The amount of observation from the experiments are limited

8 Simplest baseline of search-based optimizers: R-WIN

AIRS	(search space around the plan) windows (ordered by $\Delta \cot \Delta h$)	or Backward Breadths First Blind Bidirectional
	`	Blind Bidirectional Admissible A*
DDPU2	windows (block deordering)	
		or PNGS (layered approach)
R-WIN	windows (random)	Admissible A* + LMcut

9 Evaluate them in an "Equal Condition"

	Subproblems are based on	Subproblems are solved with
PNGS	neighborhood graph	Admissible A* + LMcut
	(search space around the plan)	
AIRS	windows (ordered by $\Delta \cot \Delta h$)	Admissible A* + LMcut
BDPO2	windows (block deordering)	Admissible A* + LMcut
R-WIN	windows (random)	Admissible A* + LMcut

10 Evaluation

	Algorithm	Harmonic Means
39 IPC domains		of Ratios
Optimize the 15 min, 2GB results of	LAMA(15min)	100%
LAMA	LAMA(30min)	%
Resource 15 min, 2GB	AE	%
Participants AD, AE, AIRS, PNGS,	AD	%
R-WIN	AIRS	%
(BDPO2 is not tested)	PNGS	%
	R-WIN	%

11 Results

	Algorithm	Harmonic Means
39 IPC domains		of Ratios
Optimize the 15 min, 2GB results of	LAMA(15min)	100%
LAMA	LAMA(30min)	99.3%
Resource 15 min, 2GB	AE	98.4%
Participants AD, AE, AIRS, PNGS,	AD	97.4%
R-WIN	AIRS	97.9%
(BDPO2 is not tested)	PNGS	96.0%
	R-WIN	95.9%

Complex tweaks did not outperform the simplest variant

Sadly "Improvements" did not outperform the simplest baseline

Now let's reliably improve upon the baseline

14 Improve AIRS to outperform R-WIN: CH-WIN

Why we chose AIRS?

→ Easy to implement, minimum diff from R-WIN

Problem in AIRS:

Original AIRS is tested only on

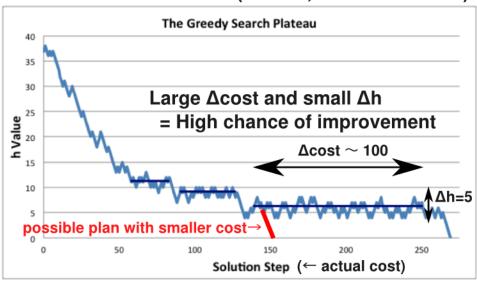
small-scale 15-puzzle/grid-pathfinding

< 0.1 sec replanning time

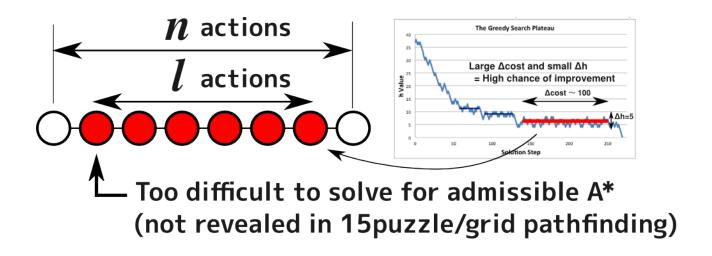
15 Window Priority Scheme in AIRS

Window priority: $\triangle cost(i,j) / \triangle h(i,j)$

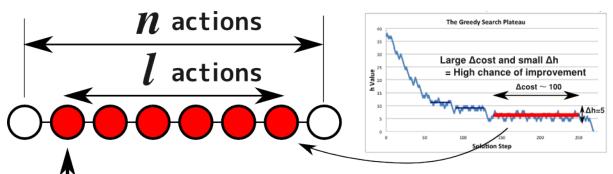
from (Estrem, Krebsbach 2012)



16 AIRS Pitfall 1: windows too long



16.1 AIRS Pitfall 1: windows too long



Too difficult to solve for admissible A* (not revealed in 15puzzle/grid pathfinding)

Dynamic Adjustment of $m{l}$ in CH-WIN:

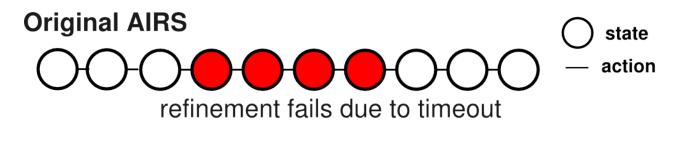
Adjust *l* by a binary search (helper variable: *L*)

Initial length: l=n/4, L=n

Replanning success: $l \leftarrow (l+L)/2$

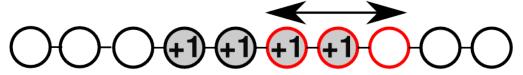
Replanning fail: $L \leftarrow l, l \leftarrow l/2$

17 AIRS Pitfall 2: Penalty could inhibit solving promising windoes





Shorter window w/ possible refinements, but not selected due to penalty



→ CH-WIN does not use penalty

(→ duplicated window detection)

18 AIRS pitfall 3 : Keep it simple

```
\label{eq:while x length (Sol) - 2 do} \begin{aligned} y \leftarrow x + 2; \\ \text{while y < Length (Sol) do} \\ \hline \text{Ratio} \leftarrow \frac{h_2 \left(\text{Sol}_x, \, \text{Sol}_y\right)}{g \left(\text{Sol}_y\right) - g \left(\text{Sol}_x\right) - p} + \\ \hline h_2 \left(\text{Sol}_x, \, \text{Sol}_y\right) \\ \hline \left(g \left(\text{Sol}_y\right) - g \left(\text{Sol}_x\right) - p\right) - \text{MaxOverlap}\left(x + 1, y - 1, \text{Sol,FS}\right)}; \\ \hline \textbf{if Ratio < Br then} \\ \hline \textbf{Br} \leftarrow \textbf{Ratio}; \\ \hline \left(\text{Bx,By}\right) \leftarrow \left(x,y\right); \\ \hline \left(\text{Bx,By}\right) \leftarrow \left(x,y\right); \\ \hline \\ \textbf{No explanation to} \end{aligned} \\ \begin{array}{c} y \leftarrow x + 2; \\ h_2 \left(\text{Sol}_x\right) + h_3 \left(\text{Sol}_y\right) + h_4 \left(\text{Sol}_y\right) + h_3 \left(\text{Sol}_y\right) + h_3
```

why these complications are necessary

→ Remove it

19 Result

CH-WIN achieved the **best performance**

Algorithm	Harmonic Means		
	of Ratios		
LAMA(15min)	100%		
LAMA(30min)	99.3%		
AE	98.4%		
AD	97.4%		
AIRS	97.9%		
PNGS	96.0%		
R-WIN	95.9%		
CH-WIN (proposed)	93.3%		

20 Open Questions

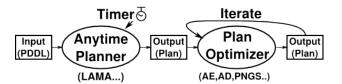
What is the *baseline* of various search-based optimizers?

i.e. Are these *complex* algorithms necessary? → Simple algorithms perform better

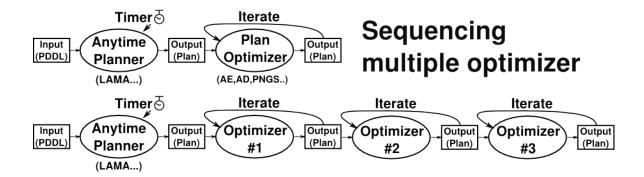
How to combine Polytime and Search-based Optimizers?

Also, how effective is it to combine them?

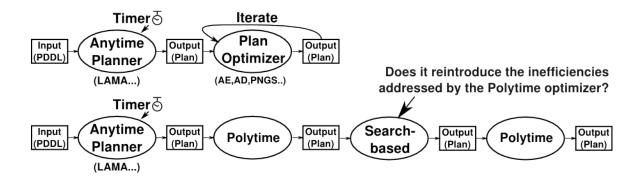
21 Multiple Optimizers



21.1 Multiple Optimizers



21.2 Polytime + Search-based Optimizers



21.3 Iterating Polytime Optimizer

	AD	AD	AD	AD	AE	AE	AE	ΑE
		AE	AE	AE		AD	AD	AD
			AD	AD			AE	ΑE
domain				AE				AD
mean(harmonic)	98.4	97.4	97.4	97.4	97.4	97.4	97.4	97.4

Table 4: Result of applying poly-time optimizers iteratively to plans obtained by 15-minute runs of LAMA. The harmonic means of the ratios over all instances are shown.

- Iterating AE and AD is not effective
- we can safely assume that we apply them at most once

22 Polytime + Search-based Result

Algorithm		
X	x only	AE+AD+x
LAMA(15min)	100%	-
LAMA(30min)	99.3%	-
AE	97.4%	
AD	98.4%	
AIRS	97.9%	95.6%
PNGS	96.0%	94.4%
R-WIN	95.9%	94.0%
CH-WIN (proposed)	93.3%	91.8%

23 Lessons Learned

- **Avoid** unnecessary complexity
- R-WIN, baseline, outperformed AIRS, PNGS etc.
- Use the simplest variant as a baseline, improve upon it
- CH-WIN, an improved AIRS variant, outperformed previous algorithms
- Reconfirmed poly+search effectiveness

Thank you for Listening!

Presentation available on

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https:
//guicho271828.github.io/2016-6-13-hsdip/
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