#### **Exploiting Search Space Structure** Masataro Asai, Graduate School of Arts and Sciences, in Classical Planning: Analyses and Algorithms The University of Tokyo 2 yrs remaining

### 0. Prior Work:

- 1st, 2nd paper: macro
- 3rd paper: A\*, tiebreaking, plateau
- →Weak connections of topics; Requires a unified story

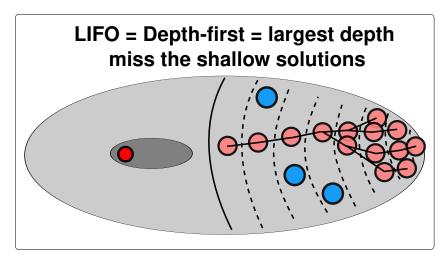
(macro ∩ plateau analysis) == search space

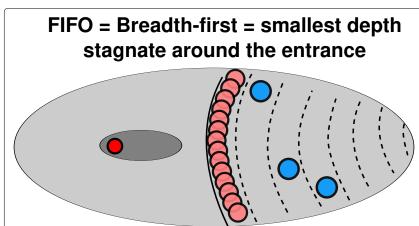
# 1. Effective search space (ESS)

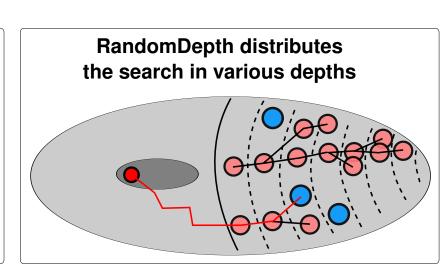
- The portion of the search space evaluated
- Search algorithm affects the ESS
- Heuristic function, tiebreaking, macro operators

#### Random-Depth Tiebreaking (3rd paper)

Search the plateau more uniformly

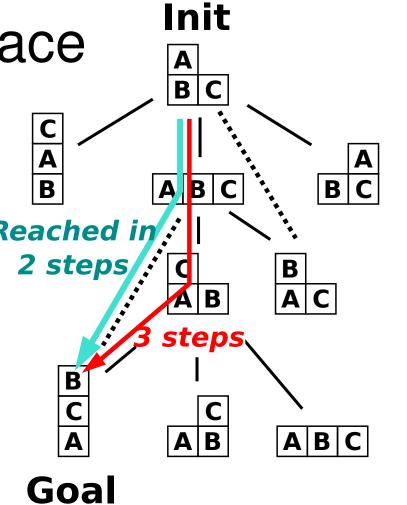




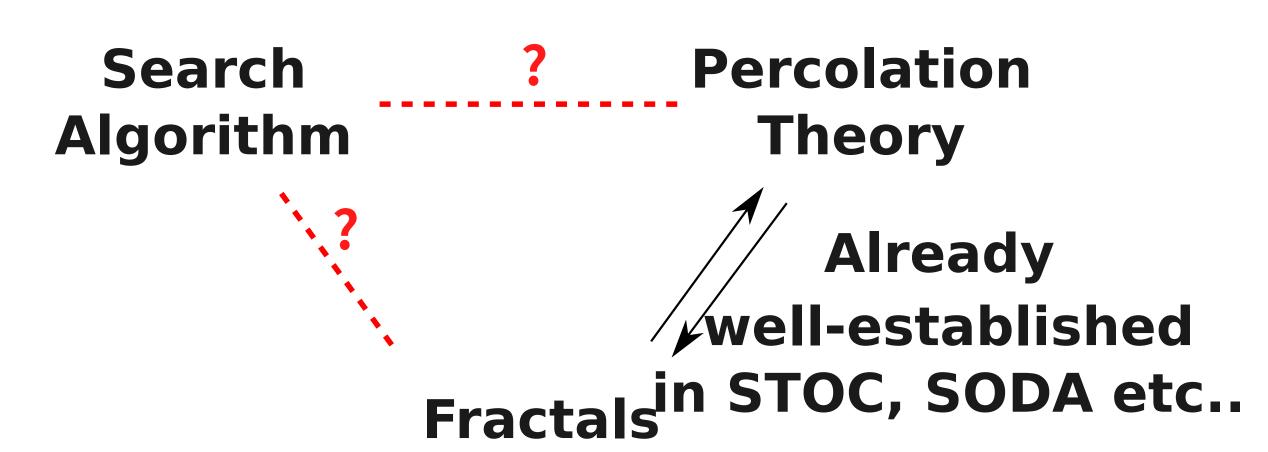


#### Macro operators (1st, 2nd papers)

- Creates shortcuts in the search space
- Useful when it guides the search
- Increases the branching factor in the search space
- Increases the branching factor in the ESS  $\rightarrow$  ?

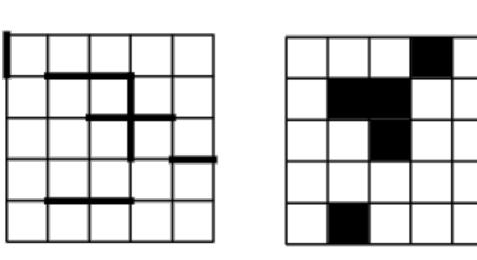


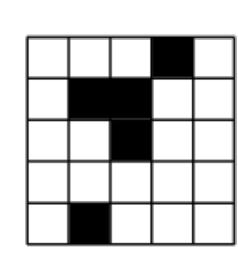
# 2. Framework for Analysing ESS



# 3. Percolation Theory (graph connectivity)

A node (edge) is occupied/unoccupied





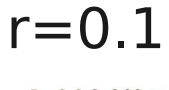
site percolation

Occupied node(edge): black Unoccupied node(edge): white

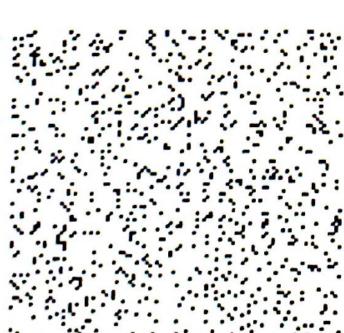
Occupation ratio *r* 

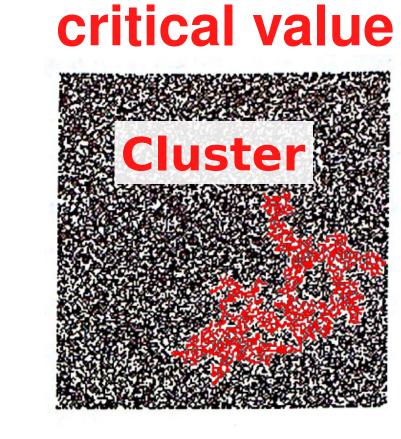
= #(occupied) / # (to\*

A non-percolated graph: Connectivity Obviously disconnected non-trivial everywhere  $r=r_c=0.5928$ 

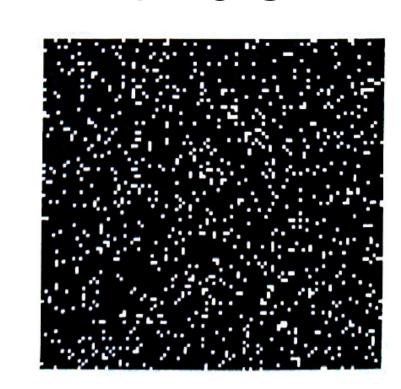


bond percolation





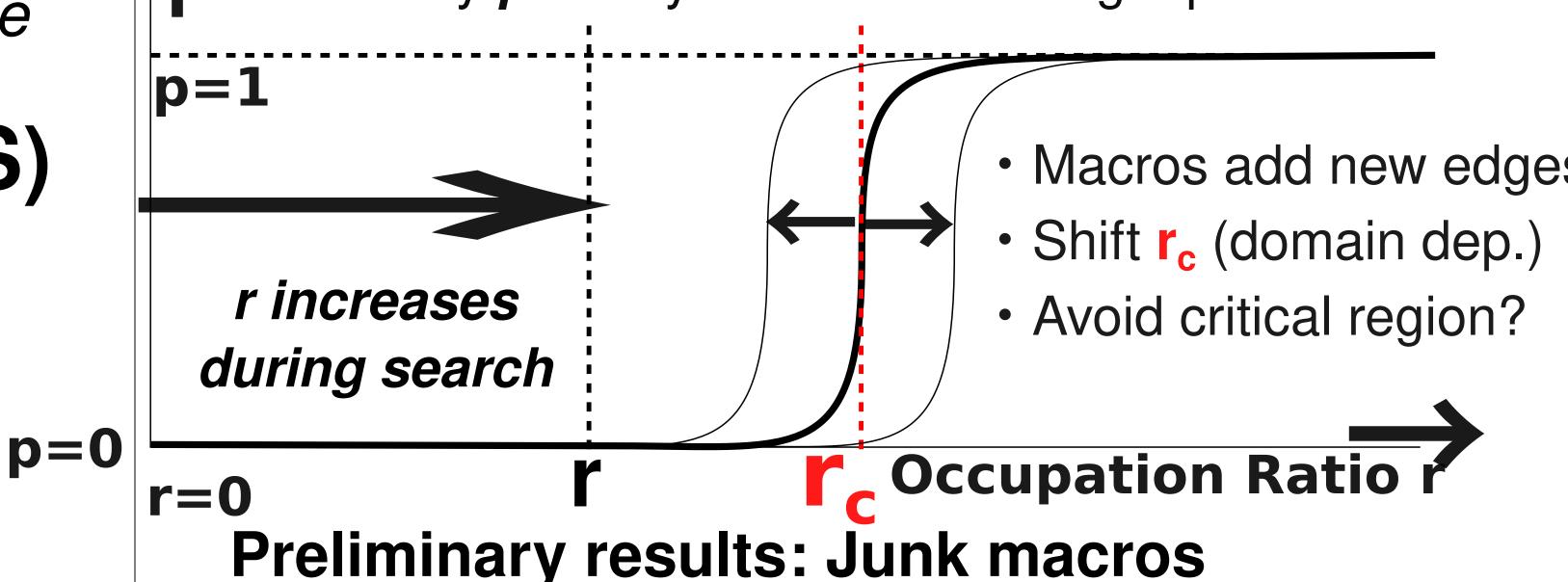
A percolated graph: Obviously connected everywhere r = 0.9



#### (cont.) Percolation = Phase Transition

Around r=r<sub>c</sub>, graph connectivity becomes increasingly difficult to answer (Similar to the phase transition in satisfiability)

Probability **p** of any two nodes having a path



(LAMA) Domain 280721 (.74) cybersec 190577 (.47) 179752 (.88) driverlog 2643 (.08) mystery 355576 (.89) pipesworld-t 87475 (.90) *331 (1.1)* 114 (.96) *445 (1.0)* 

transport-sat11 2 205 (1.3) 630 (2.0) 835 (1.8)

- Randomly generated junk macros
- · Conventionally considered harmfu
- Actually reduces evaluations in some domains

### Open Questions / new methods

How existing macros change ESS?

47244 (.47)

- r<sub>c</sub> of each planning domain? (e.g. Logistics=0.XX)
- When each algorithm finds a soltion? (e.g. r=0.YY)
  - e.g. Local search, lookaheads, type-GBFS
- Random restarts with randomly ignoring edges
  - Multiple incomplete runs • Shifts r<sub>c</sub>
    - → Probabilistically complete algorithm

# 4. Analyze ESS as Fractals

### Measuring the Fractal dimension of a graph

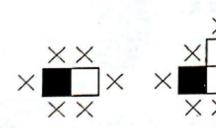
0-0-0 $dim = log_3(4) = 1.26$ dim=2 dim=1

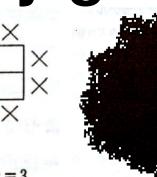
- e.g. Radius method
- Change the radius
- Count the nodes

New algorithm?

## Some fractals are defined by generative rules







A model for a cell culture

Nodes are randomly generated on the surface = ESS with random selection from the OPEN list

#### **Fractal Models** Eden Random Order Random Depth Fractal? $\leftrightarrow$ Ballistic Aggregation ↔ New algorithm?

## 5. Thesis Abstract

DLA (dim = 1.71)

- 1. Propose the framework
- 2. Propose paper 1,2,3
- 3. Analyze the ESS of paper 1,2,3 using the framework
  - → A deeper insight into why paper 1,2,3 is successful