# Questions/Keep in Mind

- T-type Cat channel: shift/scale gating variables? Corrently shifted/scaled only two parameters based on fit on data.
- → search for pacemaker neurons in drosophila. Which neurous do they project to? (R5?) Are they inhibitory, or excitatory? Inhibitory will be like a sugar on top:)
- What is the timescale of Car spikes? Googlay resulted in simplar shape.

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1	Ir	ntroduction
	Cti	We predict that $I_T$ should provide the inward current for the generation of low-threshold $a^{2+}$ spikes, with rapidly activating and inactivating $K^+$ current $I_A$ modulating the inial components of these $Ca^{2+}$ spikes. In contrast, the slower kinetics of activation and factivation of the $K^+$ current $I_{K2}$ suggest that this current may affect more the later ortions of low-threshold $Ca^{2+}$ spikes. The properties of $I_h$ suggest that it is critical to

 $\mathbf{2}$ 

firing; the rapidly inactivating and transient  $K^+$  current,  $I_A$ , which may fascilitate slow repetitive firing and may interact with  $I_T$  during  $Ca^{2+}$ -dependent burst firing; a slowly inactivating transient  $K^+$  current,  $I_{K2}$ , which may control repetitive firing rate; and a

• these currents include  $I_T$ , the low-threshold, transient  $Ca^{2+}$  current that underlines burst

modulation of the voltage-time course of the cell at hyperpolarized membrane potentials

and may provide a "pacemaker" potential for rhythmic burst generation [8].

hyperpolarization-activated, mixed cationic conductance with slow kinetics,  $I_h$ , which activates on hyperpolarization and which may generate a "pacemaker" potential for the generation of slow oscillations [8].

- The modeled currents were derived wither from Drosophila neurons (specify), or (e.g. rat thalamic neurons, etc)...
- We assumed that  $I_T$  was composed of a uniform populatio of channels whose inactivation could be ompletely described by the Boltzmann function.
- Current-Voltage relationship was better reproduced when constant-field equation was used instead of the ohmic one [8].
- T-Type:  $m^3h$  format [17]
- Model: slow deinactivation [17]
- T-Type Ca current together with the leakage current suffices to describe the low-threshold spike (LTS)... Outward currents are not required to reproduce the basic shape of the LTS...Each LTS trigerres a burst of fast action potentials that ride on its crest. As such, LTS plays a critical role in linking synaptic input to intrinsic membrane mechanisms of bursting in the relay cell and in supporting the slow membrane oscillations underlying the spondling rhythm [17].
- $I_T$  is de-inactivated by hyperpolarization, thus providing an ionic basis for the so-called post-inhibitory rebound excitation [18].
- This "3 Hz" bursting is primarily due to the interplay between a T-type calcium current  $I_T$ , and a non-specific cation "sag" current  $I_h$  which has much slower kinetics that  $I_T$  and is activated by hyperpolarization [18].
- Physiologists have been interested in the action of calcium on excitable tissues since the days of Ringer (1883). Some of the main facts established (see Brink, 1954) are that increasing the external calcium concentration raises the threshold, increases membrane resistance (Cole, 1949) and accelerates accommodation. Reducing the calcium concentration has the converse effects, and frequently leads to spontaneous oscillations or repetitive activity (e.g. Adrian & Gelfan, 1933; Arvanitaki, 1939). Other observations which may be less well known are that removal of calcium reduces rectification (Loligo nerve, Steinbach, Spiegelman & Kawata, 1944) and increases the fraction of the sodium carrying system which is in a refractory or inactive condition (Purkinje fibres, Weidmann, 1955). In connexion with the last observation, it is interesting that tissues which do not normally give an anode break response can be made to do so by reducing the concentration of calcium ions in the external medium (Frankenhaeuser, 1957) [5].

#### 2 T-Type Calcium Channel

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#### 2.1 Model

T-Type Ca<sup>2+</sup> current was modelled using constant-field equation [8]:

$$I_T(V) = m_T(V)^3 h_T(V) P z^2 \frac{VF^2}{RT} \frac{[Ca^{2+}]_{\text{inside}} - [Ca^{2+}]_{\text{outside}} \exp[-zFV/(RT)]}{1 - \exp[-zFV/(RT)]}$$
(1)

where  $m_T$  and  $h_T$  correspond to the activation and inactivation gates, P is the maximum permeability (scaled to either have the current amplitude observed during the electrophysiological experiments reported in [11] (Section 2.3), or to ), z is the valence of ion (= 2 for Ca<sup>2+</sup>), V is membrane potential in Volts, F is Faraday's constant ( $\approx 9.6485 \times 10^4 C \cdot \text{mol}^{-1}$ ), R is the universal gas constant ( $\approx 8.3145 J/K^{\circ} \cdot \text{Mol}$ ), T is temperature is Kelvin (here, 273.16 + 25 = 298.16°). [ $Ca^{2+}$ ]<sub>inside</sub> and [ $Ca^{2+}$ ]<sub>outside</sub> are the concentrations of  $Ca^{2+}$  inside and outside the membrane. The values were set to  $23 \times e^{-9}$  and  $0.5 \times e^{-3}$  correspondingly, from the motor neurons in Drosophila [5].

Another approach to model the T-Type Ca<sup>2+</sup> current is by Ohm's law [8, 17]:

$$I_T(V) = g_T m_T(V)^3 h_T(V) (V - V_{Ca})$$
(2)

 $g_T$  is the maximum value of the conductance of the T-Type Ca<sup>2+</sup> current, and  $V_{Ca}$  us the reversal potential for  $Ca^{2+}$ , which can be estimated given the ion concentrations inside and outside the membrane (see Section 2.1.1). However, the model with the Ohmic current did not reprocude the I-V relations in [11] correctly (see Sction ...). Similar issue was described in [8], where choosing equation 1 instead of 2 resulted in better fit of the I-V relationship to the experimental data.

#### 2.1.1 Reversal Potential

Reversal potential was estimated by Nernst equation [10]:

$$V_{\text{ion}} = \frac{RT}{zF} \ln \frac{[\text{Ion}]_{\text{outside}}}{[\text{Ion}]_{\text{inside}}}$$

where  $[\text{Ion}]_{\text{inside}}$ , and  $[\text{Ion}]_{\text{outside}}$  are concentrations of the ions (here,  $Ca^{2+}$ ) inside and outside of the cell. The values for  $[Ca^{2+}]_{inside}$  and  $[Ca^{2+}]_{outside}$  were taken to be 23nM, and 0.5mM correspondingly from the motor neurons in Drosophila [14]. R is the universal gas constant ( $\approx 8.3145 J/K^{\circ} \cdot \text{Mol}$ ), T is temperature is Kelvin (here,  $273.16 + 25 = 298.16^{\circ}$ ), F is Faraday's constant ( $\approx 9.6485 \times 10^4 C \cdot \text{mol}^{-1}$ ), z is the valence of the ion (z = 2 for  $Ca^{2+}$ ).

$$V_{Ca} \approx 128 mV$$

#### 2.1.2 Activation Gate

Dynamics of the activation variable  $m_T$  of T-Type  $Ca^{2+}$  channel is given by [17]:

$$\frac{dm_T(V)}{dt} = \frac{m_{T,\infty}(V) - m_T(V)}{\tau_{m_T}(V)}$$

where [2, 17]:

$$m_{T,\infty}(V) = \frac{1}{1 + \exp\left[-(V - V_{m_T,1/2})/k_{m_T}\right]}$$
(3)

and

$$\tau_{m_T}(V) = \sigma_{m_T}(V)\tau_{m_T}^-(V) + (1 - \sigma_{m_T}(V))\tau_{m_T}^+(V)$$
(4)

In the equations above,  $m_{T,\infty}$  and  $\tau_{m_T}$  are voltage-sensitive steady-state activation function and time constant, correspondingly.  $V_{m_T,1/2}$  is membrane potential at which the steady-state activation function is equal to its half-maximum (i.e. 0.5), and  $k_{m_T}$  is the slope factor.  $\tau_{m_T}^-(V)$  and  $\tau_{m_T}^+(V)$  describe the time constant below (deactivation) and above (activation) -50 mV correspondingly, and  $\sigma_{m_T}(V)$  defines smooth transition between the two at -50 mV. First, the following functions were fit to the values provided in [11]:

$$\tau_{m_T}^-(V) = 3(a_{m_T,1} + \exp\left[(V - b_{m_T,1})/k_{m_T,1}\right]) \tag{5}$$

$$\tau_{m_T}^+(V) = a_{m_T,2} + \exp\left[-(V - b_{m_T,2})/k_{m_T,2}\right]$$
 (6)

The scaling factor 3 for  $\tau_{m_T}^-(V)$  is related to the how deactivation time constant was measured in [11] (for the details see Section 2.2.2). As the equations 5 have discontinuity at V = -50 mV, after fitting the parameters of those equations, the following equation for  $\sigma_{m_T}(V)$  was chosen to model smooth transition between the two:

$$\sigma_{m_T}(V) = \frac{1}{1 + \exp\left[c_{\tau_{m,T}}(v+50)\right]} \tag{7}$$

where  $c_{\tau_{m,T}} > 0$  controls the sharpness of the transition and was fitted to the combined activation and deactivation time constants from [11] after fixing the parameters of equation 5.

#### 2.1.3 Inactivation Gate

Inactivation gate was modelled with first-order kinetic scheme [3, 4]:

$$\frac{dh_T(V)}{dt} = \frac{h_{T,\infty}(V) - h(V)}{\tau_{h_T}(V)}$$

where [3, 17]:

$$h_{T,\infty}(V) = \frac{1}{1 + \exp\left[(V - V_{h_T,1/2})/k_{h_T}\right]}$$
(8)

and [18]: 
$$\tau_{h_T}(V) = h_{T,\infty}(V)(a_{h_T} + \exp[(V - b_{h_T})/k_{h_T}]) \tag{9}$$

**Note 1.** Second order kinetic schemes have also been developed for the inactivation gates [17]. The derivation of the equations in the paper are provided in more detail in Section 2.4.3.

#### 2.2 Fitting Data

As the data from the article is not available online, the values were estimated by taking screenshot, importing the image in Coreldraw and estimating the values using visual inspection and coordinate system of Coreldraw. The fitting was performed using python function  $scipy.optimize.curve\_fit$ . The following plots show the estimated activation/inactivation variables, as well as time constants as a function of test potential V, as provided in [11]:

**Note 2.** The error due to the subjective visual inspection should not be large. I did not estimated the error, but with moving the manually placed dot over the image on the did not have considerable effect in the final values (within the moving range where the manually placed dots were not obviously not overlapping with the ones from the image).

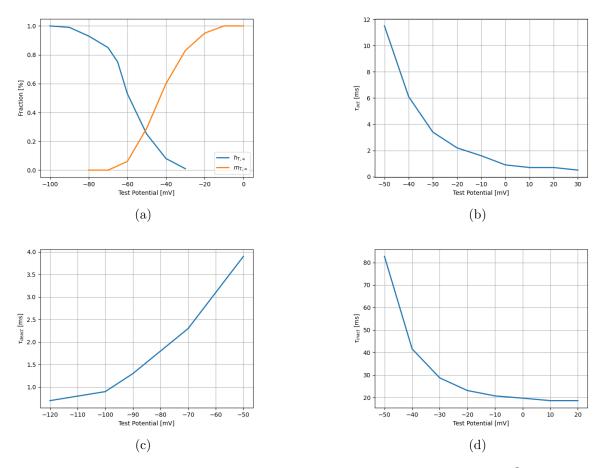
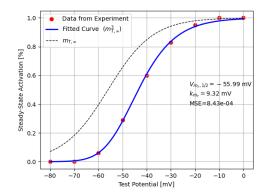


Figure 1: (a) Steady-state activation and inactivation functions of T-type Ca<sup>2+</sup> channel; (b) Activation, (b) deactivation and (c) inactivation as a functions of test potentials. Data adapted from [11].

The values of the resulted estimates (plotted in the figures above) are provided in Section 2.4.1.

#### 2.2.1 Estimating Steady-State Activation/Inactivation Function

Parameters for steady-state activation variable were estimated by fitting  $m_{T,\infty}^3(V)$  (see Equation 3) to the data from electrophysiological recordings presented in [11] (similar to the procedure described in [2]). The steady-state inactivation was estimated by fitting Equation 8 to the data from the same paper.



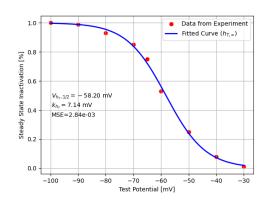


Figure 2: Fitted data to [11].

#### 2.2.2 Estimating Activation/Inactivation Time Constants

The data was taken from [11]. The paper provides information about the values for activation/inactivation variables, as well as time constants as a functions of membrane potentials.

#### Activation time constant

 $a_{T,1}$ ,  $b_{T,1}$ ,  $k_{T,1}$ ,  $a_{T,2}$ ,  $b_{T,2}$ ,  $k_{T,2}$  parameters were fit to the activation ( $V \ge -50 \text{ mV}$ ) and deactivation (V < -50 mV) time constants provided in [11] (equations 5). The initial guess for the parameters were chosen to be 0, -120, 1 for  $a_{T,1}$ ,  $b_{T,1}$ ,  $k_{T,1}$ , and 0, 50, 1 for  $a_{T,2}$ ,  $b_{T,2}$ ,  $k_{T,2}$ , correspondingly. The results are shown in Figure 3a.

[11] estimated the activation time constant (V > -50 mV) by fitting sum of two exponentials to the recorded current trace. As it is shown in Section 2.4.2, the fitted time constant does not need adjustment to account for the correspondingly time constant of activation. However, the deactivation time constant needs an adjustment.

The authors estimated deactivation time constant by measuring decay of the tail current  $(\tau_{\text{tail}})$ . As the model consists of three activation gates, and closing of each ion channel reuires only one activation gate to close, the deactivation time constant for one gate (out of the three) will be three times as large as  $\tau_{\text{tail}}$  [8]. For this reason,  $\tau_{m_t}$  for V < -50 mV was determined as  $3 \times \tau_{\text{tail}}$ .

As the set of equations 5 have jump discontinuity at V = -50 mV,  $\sigma_{m_T}$  was introduced to model a smooth transition between the functions describing the time constant below and above -50 mV (equation 7). The parameters of the exponentials modelling activation and deactivation time constants were fixed, and the parameter  $c_{\tau_m,T}$  of  $\sigma_{m_T}$  was fitted to the combined data of activation and deactivation time constants from [11] (Figure 3b).

Note 3. Original paper for the base model of the R5 neuron [18] did not model the activation time constant of T-Type Ca<sup>2+</sup> channels, as they replaced the activation variable by its steady state equation  $m_{t,\infty}(V)$ .

Note 4. [3] fitted activation time constant to double exponentials:

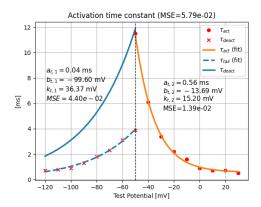
$$\tau_{m_T} = a_{\tau_{m_T}} + \frac{b_{\tau_{m_T}}}{\exp\left[(V - V_{\tau_{m_T}^1, 1/2})/k_{\tau_{m_T}^1}\right] + \exp\left[-(V - V_{\tau_{m_T}^2, 1/2})/k_{\tau_{m_T}^2}\right]}$$
(10)

However, MSE in case of double exponential fit was larger than with fitting the activation time constant with two exponential (see Fig. ), as described above.

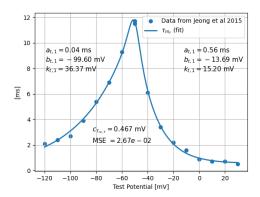
#### Inactivation time constant

[11] did not provide experimental values for  $\tau_{h_T}$  below -50 mV. Several authors reported recovery time constant for deinactivation to be much slower than the one of inactivation [3, 8, 9]. Equation 9 is a negative sigmoid, with a left asymtote at  $V \approx 216 \text{mV}$  (Figure 4).

Note 5. Another approach would be to fit the time constant only above -50 mV and take values below -50 mV from another source (e.g. [8]). However, as 1) the values for Drosophila T-Type channel are not available below -50 mV, 2) the fitted time constant has the same order of magnitude below -50 mV as described in the literature for deinactivation time constant, 3) given the previous comment, the exact velues will only affect time course of the current and is not very relevant for the neuronal model - continuous function was preferred for modelling the inactivation time constant.



(a) Fitted activation and deactivation time constants using exponential functions



(b) Smooth transition between activation and deactivation time constants

Figure 3: Fitted  $\tau_{m_T}$  to data from [11].

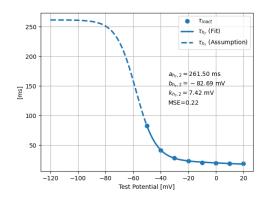


Figure 4: Fitted inactivation time constant

## 2.3 Simulations of T-Type $Ca^{2+}$ Current

Simulations were done using python package 'scipy.integrate.solve\_ivp' with zero initial conditions. Different integration methods were compared: RK45, BDF, and LSODA. Each solver is optimized for different problems (stiff, non-stiff, etc.). Simulations showed, that for some cases (e.g. simulating only t-type channel) it is best to use RK45. For the simulatins presented in this section, RK45 method was used.

#### 2.3.1 Ohmic Current vs Constant-Field Equation

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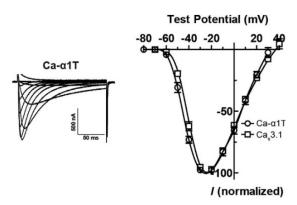


Figure 5: I-V relationship of T-Type  $Ca^{2+}$  current in Drosophila. Adapted from [11].

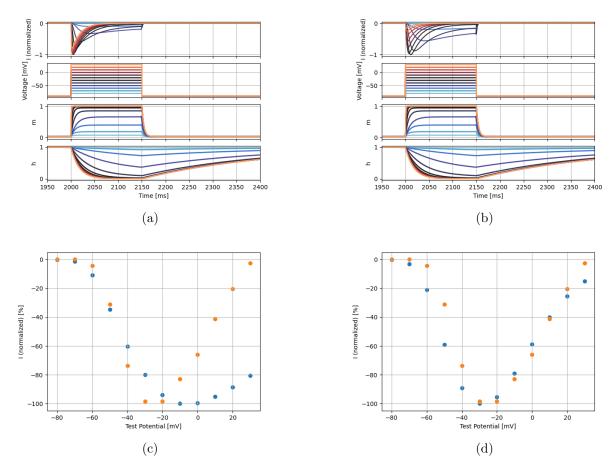
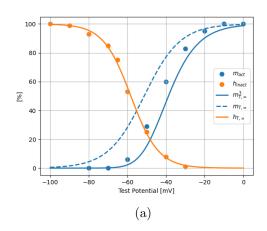


Figure 6: Ohm's low vs constant-field equation for T-Type  $Ca^{2+}$  current.

#### 2.3.2 Scaling/Shifting Gating Variables

- $[Ca]_{outside}$  affects gating constants.
- Shifted steady state activation and scaled tau activation (python function curve\_fit with initial guesses p0=[4, 0.5] for shift and scale correspondingly)
- m(v) to m(v-4.95)
- tau to tau\*0.45



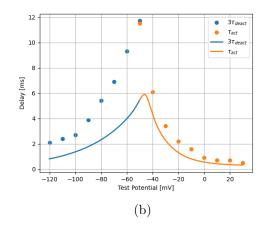
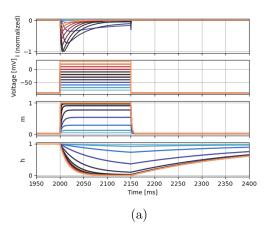


Figure 7: Add Text



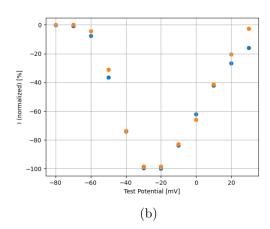


Figure 8: Add Text

# 2.4 Appendix

## ${\bf 2.4.1}\quad {\bf Estimates\ of\ Data\ in\ Jeong\ et\ al\ 2015}$

Inactivation						
Length	y1	y2	Perc	Round	Test Potential	
84.347	138.308	222.656	1.000011856	1	-100	
84.347	138.308	221.91	0.9911674393	0.99	-70	
84.347	138.308	216.864	0.931343142	0.93	-80	
					-70	
84.347	138.308	210.296	0.8534743382	0.85	-70	
84.347	138.308			0.75		
84.347	138.308	183.423	0.5348737952	0.53	-60	
84.347	138.308	159.321	0.2491256358	0.25	-50	
84.347	138.308	145.041	0.0798250086	0.08	-40	
84.347	138.308	139.015	0.008382040855	5 0.01	-30	
Activation Length	y1	y2	Perc	Round	Test Potential	
84.347	138.308	138.308	0	Round	-80	
			-	-		
84.347	138.308	138.308	0	0	-70	
84.347	138.308	143.029	0.05597116673	0.06	-60	
84.347	138.308	162.76	0.2898976846	0.29	-50	
84.347	138.308	189.012	0.6011357843	0.6	-40	
84.347	138.308	208.417	0.8311973159	0.83	-30	
84.347	138.308	218.852	0.954912445	0.95	-20	
84.347	138.308	222.256	0.9952695413	1	-10	
84.347	138.308	222.656	1.000011856	1	0	
Tau Activation Test Potential	length	k	y1	y2	Tau	Round
-50	94.853	10				11.5
			110.837	220.142	11.52362076	
-40	94.853	10	110.837	168.638	6.093745058	6.1
-30	94.853	10	110.837	143.507	3.444276934	3.4
-20	94.853	10	110.837	131.792	2.209207932	2.2
-10	94.853	10	110.837	126.028	1.60153079	1.6
0	94.853	10	110.837	119.373	0.8999188218	0.9
10	94.853	10	110.837	117.386	0.6904367811	0.7
20	94.853	10	110.837	117.187	0.6694569492	0.7
30	94.853	10	110.837	115.995	0.5437888101	0.5
Tau Inactivation						
Test Potential	length	k	y1	y2	Tau	Round
-50	122.173	100	120.28		82.73923044	82.7
-40	122.173	100	120.28	171.102	41.59838917	41.6
-30	122.173	100	120.28	155.338	28.69537459	28.7
-20	122.173	100	120.28	148.484	23.08529708	23.1
-10	122.173	100	120.28	145.514	20.65431806	20.7
0	122.173	100	120.28	144.372	19.71957798	19.7
10	122.173	100	120.28	143.001	18.59739877	18.6
20	122.173	100	120.28	143.001	18.59739877	18.6
Tau Deactivation						
Test Potential	length	k	y1	y2	Tau	Round
-120	130.684	. 5	125.975	143.595	0.6741452664	0.7
-110	130.684	5	125.975	146.32	0.7784043953	0.8
-110	130.684	5	125.975	149.948	0.7784043933	0.0
-100	130.684	5	125.975	158.758	1.254285146	1.3
		_				
-80	130.684	5	125.975	173.788	1.829336415	1.8
	130.684	5	125.975	186.399	2.311836185	2.3
-70						
-70 -60 -50	130.684 130.684	5	125.975 125.975	206.439 227.86	3.07857121 3.898143614	3.1

#### 2.4.2 From Current Trace to Sum of Exponentials

Sum of exponentials and gating time constants

$$\frac{dm}{dt} = \frac{m_{\omega} - m}{T_{m}}, \frac{dl}{dt} = \frac{l_{\omega} - l_{m}}{T_{l_{l_{m}}}} \qquad (1)$$

$$I(t) = g \, m^{p} \, l_{m} \, (v - E) \qquad (2)$$

$$n(0) = l_{m} \, (v - E) \qquad n(t) = m_{\omega} \, (1 - e^{-t/T_{m}}) \qquad = 0$$

$$l_{m} \, (1 - e^{-t/T_{m}}) \, l_{m} \, (1 - e^{-t/T_{m}}) \qquad = 0$$

$$l_{m} \, (1 - e^{-t/T_{m}}) \, l_{m} \, l_{m} \, (1 - e^{-t/T_{m}}) \, l_{m} \, l_{m$$

$$\begin{split} & = -3 g \, \text{m}_{\infty}^3 \, \text{f}_{\infty} \, (\text{V-E}) \\ & = -g \, \text{m}_{\infty}^3 \, \text{f}_{\infty} \, (\text{V-E}) \end{split}$$

#### 2.4.3 Derivation of equations in Wang 1991

$$\frac{\int_{1}^{R} dx}{dt} = \int_{1}^{1} (1 - R - J) - \beta_{1} J_{1} \qquad (1)$$

$$\frac{dx}{dt} = \beta_{1} (1 - R - J) - \delta_{2} J_{1} \qquad (2)$$

$$\frac{dx}{dt} = \beta_{1} (1 - R - J) - \delta_{2} J_{1} \qquad (2)$$

$$\frac{dx}{dt} = \beta_{1} (1 - R - J) - \delta_{2} J_{1} \qquad (2)$$

$$\beta_{2} (1 - R - J_{1}) = \beta_{1} J_{1} \qquad (2)$$

$$\int_{2}^{1} (1 - R - J_{1}) = \beta_{1} J_{1} \qquad (2)$$

$$\int_{2}^{1} (1 - R - J_{1}) = \beta_{1} J_{1} \qquad (2)$$

$$\int_{2}^{1} (1 - R - J_{1}) = \beta_{2} J_{1} \qquad (2)$$

$$\int_{2}^{1} (1 - R - J_{1}) = \beta_{2} J_{1} \qquad (2)$$

$$\int_{2}^{1} (1 - R - J_{1}) = \beta_{2} J_{1} \qquad (2)$$

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$$\int_{2}^{1} (1 - J_{2}) = J_{2} J_{2} J_{2} J_{2} \qquad (2)$$

$$\int_{2}^{1} (1 - J_{2}) = J_{2} J$$

$$R_{\infty} = \frac{J_{1}(1-J_{\infty})}{J_{1}+J_{3}} = \frac{J_{1}}{J_{1}+K_{1}J_{3}} \left(1 - \frac{K_{1}K_{2}}{1+K_{1}+K_{1}K_{2}}\right) = \frac{1}{1+K_{1}} \cdot \frac{1+K_{1}+K_{1}K_{2}-K_{1}K_{2}}{1+K_{1}+K_{1}K_{2}} = \frac{1}{1+K_{1}} \cdot \frac{1+K_{1}+K_{1}K_{2}}{1+K_{1}+K_{1}K_{2}} = \frac{1}{1+K_{1}(1+K_{2})}$$

$$k_{\infty} = \frac{1}{1 + \kappa_{1} (1 + \kappa_{2})} \qquad (A2\alpha)$$

$$d_{\infty} = \kappa_{1} \kappa_{2} k_{\infty} \qquad (A2\beta)$$

$$\frac{1}{2} \longrightarrow \frac{d}{dt} \begin{pmatrix} f_1 \\ d \end{pmatrix} = \begin{pmatrix} -d_1 - \beta_1 & -d_1 \\ -\beta_2 & -d_2 - \beta_2 \end{pmatrix} \begin{pmatrix} f_1 \\ d \end{pmatrix} + \begin{pmatrix} d_1 \\ \beta_2 \end{pmatrix}$$

Associated honogeneous equation:

$$\frac{d}{dt}\begin{pmatrix} f \\ d \end{pmatrix} = \begin{pmatrix} -d_1 - \beta_1 & -d_1 \\ -\beta_2 & -d_2 - \beta_2 \end{pmatrix}\begin{pmatrix} f \\ d \end{pmatrix} = \vec{X}$$

$$\begin{pmatrix} -d_1 - \beta_1 & -d_1 \\ -\beta_2 & -d_1 - \beta_2 \end{pmatrix} = A$$

$$det(A + \lambda I) = det\begin{pmatrix} -d_1 - \beta_1 + \lambda & -d_1 \\ -\beta_2 & -d_2 - \beta_2 + \lambda \end{pmatrix} =$$

$$= \left(-\lambda_{1} - \beta_{1} + \lambda\right) \left(-\lambda_{2} - \beta_{2} + \lambda\right) - \lambda_{1} \beta_{2} =$$

$$= \lambda_{1} \lambda_{2} + \lambda_{2} \beta_{2} - \lambda \lambda_{1} + \lambda_{2} \beta_{1} + \beta_{1} \beta_{2} - \lambda \beta_{1} - \lambda \lambda_{2} - \lambda \beta_{2} + \lambda^{2} - \lambda \beta_{2} =$$

$$= \lambda^{2} + \lambda \left(-\lambda_{1} - \beta_{1} - \lambda_{2} - \beta_{2}\right) + \lambda_{1} \lambda_{2} + \beta_{1} \left(\lambda_{2} + \beta_{2}\right) =$$

$$T_{c}$$

$$= \lambda^2 + \overline{1}_{\alpha} \cdot \lambda + D$$

$$T_r = -\left( +_1 + \beta_1 + \phi_2 + \beta_2 \right) = -\left( \frac{1}{\tau_1} + \frac{1}{\tau_2} \right)$$

$$\mathcal{D} = \lambda_1 \lambda_2 + \beta_1 (\lambda_2 + \beta_2) = \lambda_1 \lambda_2 + K \lambda_1 (\lambda_2 + K \lambda_2) = \lambda_1 \lambda_2 (1 + K (1+K))$$

$$K_{i} = \frac{\beta_{i}}{\beta_{i}} \quad j = 0 \quad f_{i} = K_{i} \delta_{i}$$

$$T_{i} = \frac{1}{\delta_{i} + \beta_{i}} \quad j = 0 \quad T_{i} = \frac{1}{\delta_{i} \left( 1 + K_{i} \right)} \quad j = 0 \quad \delta_{i} = \frac{1}{T_{i} \left( 1 + K_{i} \right)}$$

$$Sinilarly : \delta_{2} = \frac{1}{T_{2} \left( 1 + K_{2} \right)}$$

$$\begin{split} \lambda_{1},\lambda_{2} &= \frac{1}{2} \left[ -T_{r} + \sqrt{T_{r}^{2} - 4} \mathcal{D} \right] \\ T_{r}^{2} - 4 \mathcal{D} &= \left( \frac{1}{\tau_{1}} + \frac{1}{\tau_{2}} \right)^{2} - \frac{4 \left( 1 + K \left( 1 + K \right) \right)}{T_{1} T_{2} \left( 1 + K \right)^{2}} = \\ &= \left( \frac{1}{\tau_{1}} - \frac{1}{\tau_{2}} \right)^{2} + \frac{4}{\tau_{1} T_{2}} - \frac{4 \left( 1 + K \left( 1 + K \right) \right)}{T_{1} T_{2} \left( 1 + K \right)^{2}} = \left( \frac{1}{\tau_{1}} - \frac{1}{\tau_{2}} \right)^{2} + \frac{4 \left( 1 + K \right)^{2} - 4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} = \\ &= \left( \frac{1}{\tau_{1}} - \frac{1}{\tau_{2}} \right)^{2} + \frac{4 \left( 1 + K \right)^{2} - 4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4 \left( 1 + K \right)^{2}}{T_{1} T_{2} \left( 1 + K \right)^{2}} + \frac{4$$

Measurable time constants in experiments are  $\lambda_1^{-1}$  and  $\lambda_2^{-1}$  (i.e.  $\tau_0$  and  $\tau_r$ ).

general solution for d and 
$$k$$
:
$$A_{o}^{(l)} + A_{i}^{(l)} \exp(-\lambda_{i} t) + A_{i}^{(l)} \exp(-\lambda_{2} t)$$
where  $l = \{d, h\}$ 

Approximations:

$$\widetilde{l}_{2} \simeq \lambda_{2}^{-1} \left[ 1 + K(1+K) \right] / (1+K)^{2}$$

the state of the s

$$R = d_1(1-R-d) - \beta_1 R$$
 (1)

$$d = \beta_2 (1 - R - d) - b_2 d$$
 (2)

As (1) describes much faster process than (2), the authors used rapid equilibrium hypothesis on the former, assume steady state

$$l = \frac{dh}{dt} = 0, \quad l = 0$$

$$l = \frac{d_1(1-d)}{d_1+\beta_1}$$

$$(2)$$

$$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{$$

$$\frac{d}{dt} = \frac{d_{1}d_{2}K^{2}(1-d) - d_{1}d_{2}d - d_{1}d_{2}Kd}}{d_{1}+d_{1}K} = \frac{d_{2}K^{2}(1-d) - d_{2}d - d_{2}Kd}}{1+K} = \frac{d_{2}(K^{2}-K^{2}d-d-Kd)}{1+K} = \frac{d_{2}(K^{2}-d(1+K(1+K)))}{1+K} = -\frac{d_{2}(1+K(1+K))}{1+K} d + \frac{d_{2}K^{2}}{1+K} = \frac{d_{2}K^{2}}{1+K} = -\frac{d_{2}K^{2}}{1+K} = -\frac{d_{2}K^{2}}{$$

$$\frac{1+K}{J_{2}(1+K(1+K))} = \lambda_{2}^{-1}$$

$$J_{2}(1+K(1+K)) = \lambda_{2}^{-1}$$

$$J_{3}(1+K(1+K)) = \lambda_{4}^{-1}$$

$$J_{4}(1+K(1+K)) = \lambda_{4}^{-1}$$

$$J_{5}(1+K(1+K)) = \lambda_{5}^{-1}$$

$$J_{7}(1+K(1+K)) = \lambda_{7}^{-1}$$

$$J_{7}(1+K(1+K)) = \lambda_{7}^{-1}$$

$$J_{7}(1+K(1+K)) = \lambda_{7}^{-1}$$

$$\lambda_{2}^{-1} = \frac{1+K}{\lambda_{2}(1+K(1+K))}$$

$$\lambda_{2} = \frac{L}{T_{2}(1+K)}$$

$$= \sum_{k=1}^{\infty} \frac{\tilde{\iota}_{2}(1+K)^{2}}{1+K(1+K)}$$

$$= \sum_{k=1}^{\infty} \frac{\tilde{\iota}_{2}(1+K)^{2}}{1+K(1+K)}$$

$$= \sum_{k=1}^{\infty} \frac{\tilde{\iota}_{2}(1+K)^{2}}{1+K(1+K)}$$

#### 2.4.4 Overcoming Singularities in Constant-Field Equation

$$I_{T} = \hat{g} \rho_{z^{2}} \frac{E F^{2}}{RT} \frac{\left[C_{\alpha}^{2+}\right]_{i} - \left[C_{\alpha}^{2+}\right]_{o} e^{x} \rho\left(-zFE/RT\right)}{1 - e^{x} \rho\left(-zFE/RT\right)}$$

$$if - \frac{z^{FE}}{RT} >> 1 >> I_{T} = \hat{g} \rho_{z^{2}} \frac{EF^{2}}{RT} \cdot \frac{-\left[C_{\alpha}^{2+}\right]_{o}}{0 - L}$$

$$I_{T} = \hat{g} \rho_{z^{2}} \frac{EF^{2}}{RT} \left[C_{\alpha}^{2+}\right]_{o}$$

$$I_{T} = \hat{g} \rho_{z^{2}} \frac{EF^{2}}{RT} \frac{\left[C_{\alpha}^{2+}\right]_{i} - \left[C_{\alpha}^{2+}\right]_{o}\left(1 - \frac{zFE}{RT}\right)}{1 - \left[1 - \frac{zFE}{RT}\right]}$$

$$= \hat{g} \rho_{z^{2}} \frac{EF^{2}}{RT} \frac{\left[C_{\alpha}^{2+}\right]_{i} - \left[C_{\alpha}^{2+}\right]_{o}\left(1 - \frac{zFE}{RT}\right)}{\frac{zFE}{RT}}$$

$$I_{T} = \hat{g} \rho_{z} F \left(\left[C_{\alpha}^{2+}\right]_{i} - \left[C_{\alpha}^{2+}\right]_{o}\right)$$

#### 2.4.5 Additional Figures

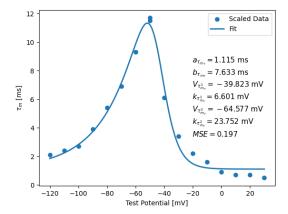


Figure 9: Fitting time constant of activation function for T-Type  $Ca^{2+}$  channel by double exponential function (Eq. 10). The fitting was done using the Python library  $scipy.optimize.curve\_fit$  with the following initial guesses for the parameters:  $a_{\tau_{m_T}}=2,\ b_{\tau_{m_T}}=1,\ V_{\tau_{m_T}^1}=-100,\ k_{\tau_{m_T}^1}=10,\ V_{\tau_{m_T}^2}=-40,\ k_{\tau_{m_T}^2}=10.$ 

#### 3 Sodium and Potassium Channels

#### 3.1 Sodium Channels

- Drosophila genome has two genes predicted to encode  $Na_v$  proteins: para, and 60E (NaCP60E). However, NaCP60E null mutants showed no loss in inward sodium current, suggesting that para is the putative  $Na_v$  channel [16].
- para has 60 predicted isoforms via alternative splicing [16]
- Para is only expressed in active neurons [16]
- Currently I chose vales from [19] where  $DmNa_v$  was expressed in Xenopus ooscyte (frog). The similar was done in [13], but the values are different.
- "heterologous expression indicates that the inclusion of specific exons imparts characteristic gating properties to individual splice variants of  $DmNa_v$  channels. These differences likely contribute to, and may even explain, the diversity in action potential firing between different neurons observed in the Drosophila CNS"
- [16] stated in Fig. 5 that 4th power exponential fit for activation resulted in time constant equal to 2.1. This means, that for one gate it should be 8.4.

The model and parameters for the transient and persistent Na channels, as well as fast and slow K currents were taken from [7]. All currents are modelled according to Ohm's law:

$$I_c(V, m, h) = g_c m_c^{p_c}(V) h_c(V) (V - V_c)$$

where c denotes the current type ( $c \in NaT, NaP, Kf, Ks$ ), where T, P, f, and s stand for 'Transient', 'Persistent', 'fast', and 'slow' correspondingly, p is the number of activation gates. Activation and inactivation variables are governed by ( $x \in m, h$ ):

$$\frac{dx}{dt}(V) = \frac{x_{c,\infty}(V) - x}{\tau_c(V)}$$

where the steady states  $x_{c,\infty}$  are defined as:

$$x_{c,\infty}(V) = \frac{1}{1 + \exp([V - V_{c,x,1/2}]/k_{c,x,1/2})}$$

The parameters are given in Table 1.

	Activation				Inactivation			
Current	$\overline{p}$	$V_{1/2,m}$	$k_m$	$ au_m$	$\overline{V_{1/2,h}}$	$k_h$	$ au_h$	
NaT	3	-29.13	-8.92	$0.13 + \frac{3.43}{1 + \exp((V + 45.35)/5.98)}$	-47	5	$0.36 + \exp\left(\frac{V + 20.65}{-10.47}\right)$	
NaP	1	-48.77		1	_	_	_	
Ks	4	-12.85	-19.91	$2.03 + \frac{1.96}{1 + \exp((V - 29.83)/3.32)}$	-	-	-	
Kf	4	-17.55	-7.27	$1.94 + \frac{2.66}{1 + \exp((V - 8.12)/7.96)}$	-45	6	$1.79 + \frac{515.8}{1 + \exp((V + 147.4)/28.66)}$	

Table 1: Channel parameters for activation and inactivation of sodium and potassium channels.

**Note 6.** Similar parameters (small differences) is also given in [12].

- 1. There is only one Ih channel gene [1, 6]
- $2.\,$  Also known as DMIH (drosophila homologue of HCN channels)

# 4 R5 Model

#### Contents

4.1 4.2	Model <td< th=""><th>24</th></td<>	24
• W	ang 1994 model simulations	
	- Blocking T-Type $Ca^{2+}$ channel destroys LTS	
	- Removing h current does not affect dynamics. H current is not necessary in the mode	el
• R	sting membrane potential of R5 is $\approx -49mV$ [15].	

## 4.1 Model

#### Appendix 4.2

#### Reverse Engineering Wang 1994 Model 4.2.1

Outword (I >0): I , I , (I,

IT - B, LTS

I, -?

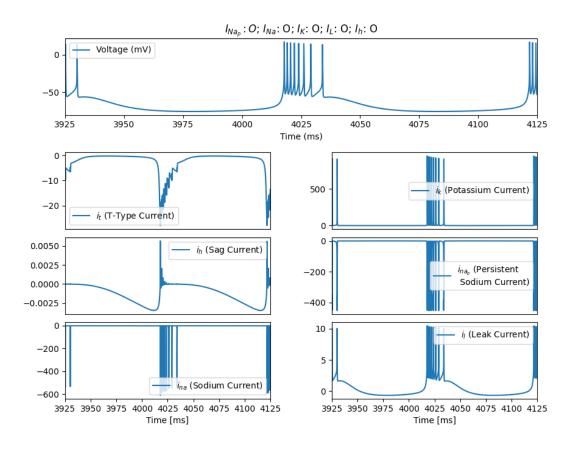
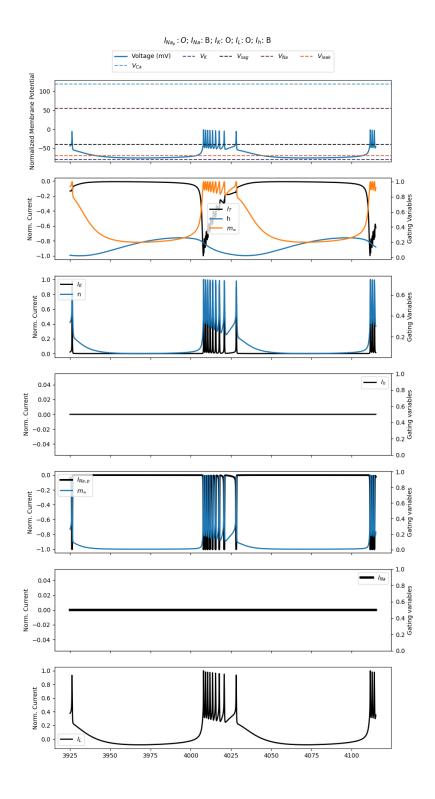


Figure 10



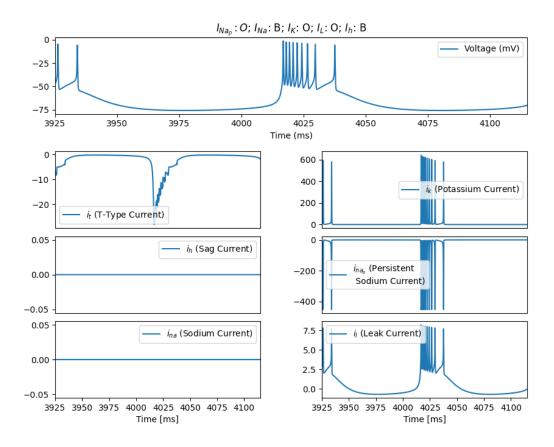


Figure 11

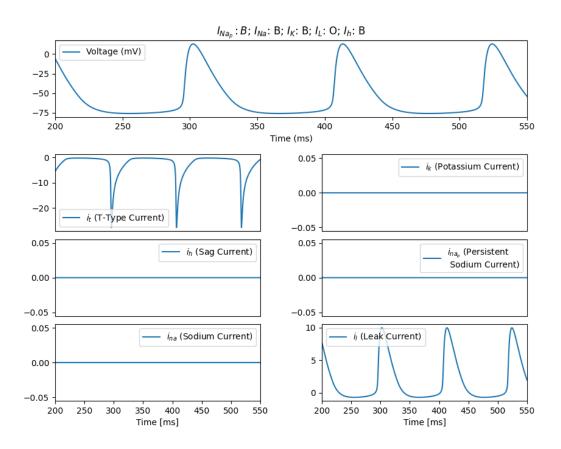


Figure 12

## 5 General Notes

#### Contents

5.1	Notes from Books/Papers	29
	Handwritten Notes	30

## 5.1 Notes from Books/Papers

**Note 7.** [In this equation...] the time evolution depends only on the present state of the system, and is defined entirely by knowledge of the set of transition probabilities. Such systems are called *Markovian systems*.

#### 5.2 Handwritten Notes

# Contents

Ion currents

L, T, N, and P-type Ca<sup>2+</sup> channels

Numerical simulations

4

Fig. 3.12-13 Parameters (Izhikevich bak) - 5

Ionic current

Inward currents (INA, Ica <0) increase the membrane potential (depolarization); Ontward currents ( $I_{K}$ ,  $I_{ce} > 0$ ) decrease it (hyperpolarization).  $I_{ce}$  is called ontwood current even though the flow of Cl ions is inward; the ions bring negative charge inside the membrane, which is equivalent to positively charged ions learny the cell, as in In.

$$C\dot{V} = I - I_{N_{\alpha}} - I_{c_{\alpha}} - I_{\kappa} - I_{c_{\ell}}$$

# L, T, N, and P type Cat hannels (Dayan & Albott)

- L-type Cat corrects are persistent as far as their voltage dependence is concerned, and they activate at a relatively high threshold. They inactivate due to a Cat-dependent rather than voltage-dependent process.

  (Dayan & Abbott). Slowly inactivating, high-voltage activated Isuzuh; et al 1989).
- -> T-type Cat currents have lower activation thresholds and are transient.

  (Dayan & Abbott). Rapidly inactivating, low-voltage activated. (Snanki et al 1989)
- N- and P-type Ca2+ conductances have intermediate thresholds and are transient and persistent, respectively. They may be responsible for the Ca2+ entry that causes the release of transmitter at presynaptic terminals (Dayan & Abbott). N-type channels are bu-threshold, rapidly inactivating (Snzuki et al 1989).

# Numerical Simulations

$$V(t+\Delta t) = V_{\infty} + (V(t) - V_{\infty}) \exp\left(-\frac{\Delta t}{\tau_{V}}\right)$$
 (1)

$$z (t+at) = z_{\infty} + (z(t)-z_{\infty}) \exp\left(-\frac{at}{T_{\infty}}\right)$$
 (2)

An efficient integration schene for conductance-bosed models is to alternate using rule (1) to update the membrane potential and rule (2) to update all the gating variables. It is important to alternate the updating of V with that of the gating variables, rather than doing them all simultaneously, as this keeps the method accurate to second order in At. If Cat-dependent conductances are included, the intracellular Cat concentration should be computed simultaneously with the membrane potential. By alternating the updating, we mean that the membrane potential is computed at times 0, At, 2At, while the gating variables are computed at times  $\Delta t/2$ ,  $\Delta t/2$ ,  $\Delta t/2$ , ... A discussion of the second-order accuracy of this scheme is given in Mascagni and Sherman (1998).

$$\frac{1}{10} \cdot \frac{1}{10} \cdot \frac{1}{10}$$

$$\dot{n} = (n_{\infty} - n)/\gamma(v) = £ 0.152$$
 $\dot{n}_{M} = (n_{M\infty} - n_{M})/\gamma_{M}(v) = 20$ 

$$m_{b} = \frac{1}{1 + \exp \left[ (V_{1/2}^{(n)} - V) / k^{(n)} \right]}$$

$$m_{b} = \frac{1}{1 + \exp \left[ (V_{1/2}^{(n)} - V) / k^{(n)} \right]}$$

$$m_{b} = \frac{1}{1 + \exp \left[ (V_{1/2}^{(n)} - V) / k^{(n)} \right]}$$

$$m_{b} = \frac{1}{1 + \exp \left[ (V_{1/2}^{(n)} - V) / k^{(n)} \right]}$$

$$n_{\infty} = \frac{1}{1 + \exp\left[\left(\frac{V_{1/2}^{(n)} - V}{V_{1/2}}\right) / k^{(n)}\right]}$$

$$\frac{1}{-25} \qquad \frac{1}{2}$$

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