

$$\frac{dh}{dt} = \alpha_1 (1 - h - d) - \beta_1 h ;$$

$$\frac{dd}{dt} = \beta_2 (1 - h - d) - \alpha_2 d$$

$$\frac{dh}{dt} = 0 \Rightarrow \alpha_1 (1 - h - d) = \beta_1 h$$

$$\alpha_1 - \alpha_1 h - \alpha_1 d = \beta_1 h$$

$$h = \frac{\alpha_1 (1 - d)}{\alpha_1 + \beta_1} = \frac{\alpha_1 (1 - d)}{\alpha_1 + \alpha_1 K}$$

$$h = \frac{1 - d}{1 + K}$$

$$\begin{aligned} \frac{dd}{dt} &= \alpha_2 K \left(1 - \frac{1 - d}{1 + K} - d \right) - \alpha_2 d = \alpha_2 K - \frac{\alpha_2 K (1 - d)}{1 + K} - \alpha_2 K d - \alpha_2 d = \\ &= \frac{\alpha_2 K (1 + K) - \alpha_2 K (1 - d) - (\alpha_2 K d + \alpha_2 d)(1 + K)}{1 + K} = \\ &= \frac{\cancel{\alpha_2 K} + \alpha_2 K^2 - \cancel{\alpha_2 K} + \alpha_2 K d - \cancel{\alpha_2 K d} - \alpha_2 K^2 d - \alpha_2 d - \alpha_2 K d}{1 + K} = \\ &= \frac{\alpha_2 (K^2 - (K^2 + K + 1)d)}{1 + K} \end{aligned}$$

$$\left. \begin{aligned} K &= \frac{\beta_2}{\alpha_2} \\ \tau_2 &= \frac{1}{\alpha_2 + \beta_2} \end{aligned} \right\} \Rightarrow \left. \begin{aligned} \beta_2 &= K \alpha_2 \\ \tau_2 &= \frac{1}{\alpha_2 (1 + K)} \end{aligned} \right\} \Rightarrow \alpha_2 = \frac{1}{\tau_2 (1 + K)}$$

$$\begin{aligned} \Rightarrow d &= \frac{K^2 - (K^2 + K + 1)d}{\tau_2 (1 + K)^2} = \frac{\frac{K^2}{K^2 + K + 1} - d}{h_{\infty} \tau_2 (1 + K)^2} = \\ &= \frac{h_{\infty} K^2 - d}{h_{\infty} \tau_2 (1 + K)^2} \end{aligned}$$

