

1 Bifurcations of Equilibria and Cycles

| Bifurcation of Equilibria | Behavior | Frequency | Amplitude | Operation |
|--|-----------|---------------------------|---------------------------|------------|
| Fold | bi-stable | nonzero | fixed | integrator |
| Saddle-node on Invariant Circle (SNIC) | excitable | zero ($\sqrt{\lambda}$) | fixed | integrator |
| Supercritical Hopf | excitable | nonzero | zero ($\sqrt{\lambda}$) | resonator |
| Subcritical Hopf | bi-stable | nonzero | arbitrary | resonator |

Table 1: Bifurcations of Equilibria (adapted from [1] with modifications)

| Bifurcation of Cycles | Behavior | Frequency | Amplitude |
|-------------------------------|-----------|----------------------------|---------------------------|
| SNIC | excitable | zero ($\sqrt{\lambda}$) | fixed |
| Supercritical Hopf | excitable | nonzero | zero ($\sqrt{\lambda}$) |
| Fold Limit Cycle* | bi-stable | nonzero | arbitrary |
| Saddle Homoclinic Orbit | bi-stable | zero ($1/ \ln \lambda $) | fixed |
| Saddle-Focus Homoclinic Orbit | bi-stable | zero ($1/ \ln \lambda $) | fixed |
| Focus-Focus Homoclinic Orbit | bi-stable | zero ($1/ \ln \lambda $) | fixed |
| Subcritical Flip** | bi-stable | nonzero | arbitrary |
| Subcritical Neimark-Sacker | bi-stable | nonzero | arbitrary |
| Blue-sky | excitable | zero ($\sqrt{\lambda}$) | fixed |

Table 2: Bifurcations of Cycles (Adapted from [1] with modifications). *Also called Saddle Node of Limit Cycles; **Also called period-doubling bifurcation;