## EXAM OF STATISTICS (DESCRIPTIVE STATISTICS AND REGRESSION)

2nd Physiotherapy Version A June, 06 2022

**Duration**: 1 hour.

(5 pts.) 1. The patients of a physiotherapy clinic were asked to assess their satisfaction in a scale from 0 to 10. The assessments are summarized in the table below.

Assessment	Patients
0 - 2	3
2 - 4	12
4 - 6	9
6 - 8	18
8 - 10	22

- (a) Compute the interquartile range of the assessment and interpret it.
- (b) If it is required an assessment greater than 5 in more than 50% of patients for the clinic to remain open, will the clinic remain open?
- (c) Is the assessment mean representative?
- (d) Compute the coefficient of kurtosis of the assessment and interpret it. Is the kurtosis normal?
- (e) If the assessment mean of another clinic is 6.8 and the standard deviation is 2.6, which assessment is relatively higher 6 in the first clinic or 6.2 in the second?

Use the following sums for the computations:

$$\sum x_i n_i = 408$$
,  $\sum x_i^2 n_i = 3000$ ,  $\sum (x_i - \bar{x})^3 n_i = -548.25$  and  $\sum (x_i - \bar{x})^4 n_i = 5140.45$ .

## Solution

Let X be the patient assessment.

- (a)  $Q_1 = 4.4444$ ,  $Q_3 = 9.0907$  and IQR = 4.6463, so the central dispersion is moderate.
- (b) F(5) = 0.2695, and the percentage of patients with an assessment greater than 5 is 73.05%.
- (c)  $\bar{x} = 6.375$ ,  $s_x^2 = 6.2344$ ,  $s_x = 2.4969$  and cv = 0.3917, thus the representativity of the mean is moderate
- (d)  $g_2 = -0.9335$  and the distribution is flatter than a Gauss bell, but normal, as  $g_2$  is between -2 and 2.
- (e) First clinic: z(6) = -0.1502

Second clinic: z(6.2) = -0.3077.

Thus, an assessment of 6 in the first clinic is relatively higher as its standard score is greater.

(5 pts.) 2. A study tries to determine the effectiveness a training program to increase the grip strength. The table below shows the grip strength in Kg in some weeks of the training program.

Week	1	3	6	9	14	17	21	24
Grip strength	15	22	29	34	36	39	40	41

(a) Compute the regression coefficient of the grip strength on the weeks and interpret it.

- (b) According to the logarithmic regression model, what is the expected grip strength after 5 and 25 weeks. Are these predictions reliable? Would these predictions be more reliable with the linear regression model?
- (c) According to the exponential regression model, how many weeks are required to have a grip strength of 25 Kg?
- (d) What percentage of the total variability of the weeks is explained by the exponential model?

## **Solution**

- (a)  $\overline{x}=11.875$  weeks,  $s_x^2=62.6094$  weeks<sup>2</sup>.  $\overline{y}=32$  Kg,  $s_y^2=76.5$  Kg<sup>2</sup>.  $s_{xy}=64$  weeks·Kg. Regression coefficient of Y on X:  $b_{yx}=1.0222$  Kg/week. The grip strength increases 1.0222
- Regression coefficient of Y on X:  $b_{yx} = 1.0222$  Kg/weeek. The grip strength increases 1.0222 Kg per week.
- (b)  $\overline{\ln(x)} = 2.0978 \ln(\text{weeks}), \ s_{\ln(x)}^2 = 1.05 \ln(\text{weeks})^2$  and  $s_{\ln(x)y} = 8.9226 \ln(\text{weeks}) \text{Kg}$ . Logarithmic regression model of Y on X:  $y = 14.1729 + 8.498 \ln(x)$ . Predictions: y(5) = 27.8499 Kg and y(25) = 41.5268 Kg. Logarithmic coefficient of determination:  $r^2 = 0.9912$ . The predictions are not reliable because the sample size is small. Linear coefficient of determination:  $r^2 = 0.8552$ . As the linear coefficient of determination is less than the logarithmic one, the predictions with the logarithmic model are more reliable.
- (c) Exponential regression model of X on Y:  $x = e^{-1.6345 + 0.1166y}$ . Prediction: x(25) = 3.6015 Weeks.
- (d) As  $r^2 = 0.9912$ , the exponential models explains 99.12% of the variability of the weeks.