## EXAM OF STATISTICS (PROBABILITY AND RANDOM VARIABLES)

2nd Physiotherapy	Version A	June, 18 2019
Name:	DNI:	Group:

**Duration**: 1 hour and 15 minutes.

- (2 pts.) 1. A study tries to determine the effectiveness of an occupational risk prevention program in jobs that require to be sit a lot of hours. A sample of 500 individuals between 40 and 50 years that spent more than 5 hours sitting was drawn. Half of the individuals followed the prevention program (treatment group) and the other half not (control group). After 5 years it was observed that 12 individuals suffered spinal injuries in the group following the prevention program while 32 individuals suffered spinal injuries in the group following 5 years it was observed that 21 individuals suffered spinal injuries in the group following the prevention program while 48 individuals suffered spinal injuries in the other group.
  - (a) Compute the cumulative incidence of spinal injuries in the total sample after 5 years and after 10 years.
  - (b) Compute the absolute risk of suffering spinal injuries in 10 years in the treatment and control groups.
  - (c) Compute the relative risk of suffering spinal injuries in 10 years in the treatment group compared to the control group. Interpret it.
  - (d) Compute the odds ratio of suffering spinal injuries in 10 years in the treatment group compared to the control group. Interpret it.
  - (e) Which statistics, the relative risk or the odds ratio, is more suitable in this study? Justify the answer.
- (3 pts.) 2. The table below shows the results of a study to evaluate the usefulness of a reactive strip to diagnose an urinary infection.

Outcome	Infection	No infection
Positive	60	80
Negative	10	200

- (a) Compute the sensitivity and the specificity of the test.
- (b) Compute the positive and the negative predictive values. Is this test better to confirm or to rule out the infection?
- (c) If another study has determined that the true prevalence of the infection is 2%, how does this affect to the predictive values?
- (5 pts.) 3. The time required to recover from an injury follows a normal distribution with variance 64 days. It is also known that 10% of people with this injury require more than 80 days to recover.
  - (a) What is the expected time required to recover from the injury? Remark: Use  $\mu = 70$  for the next part if you do not know how to compute it.
  - (b) What percentage of individuals will require between 60 and 75 days to recover?
  - (c) If we draw a random sample of 12 individuals with this injury, what is the probability of having between 9 and 11 individuals, both included, requiring less than 80 days to recover?
  - (d) If we draw a random sample of 500 individuals with this injury, what is the probability of having less than 4 requiring a time above the 99th percentile to recover?