

EXAM OF CALCULUS**Pharmacy/Biotechnology 1st year****Version A****January 18, 2021**

Name:

DNI:

Group:

Duration: 1 hour.

- (3.5 pts.) 1. A drug is administered intravenously at a speed of 15 mg/hour. At the same time, the body metabolizes the drug at a rate of 80% of the amount in the body per hour.
- (a) If the drug is administered continuously, what will the maximum amount of drug in the body be? Assume that there was no drug in the body at the beginning of the process.
 - (b) If administration is stopped when the amount administered is 150 mg, how long from that point will it take for the patient to have only 10 mg of drug in the body?
- (3.5 pts.) 2. The function $T(x, y) = \ln(3xy + 2x^2 - y)$ gives the temperature of the surface of a mountain at latitude x and longitude y . Some mountaineers are lost at position $(1, 2)$ and are at risk of freezing to death.
- (a) In which direction should they move to avoid the risk of freezing as fast as possible?
 - (b) If they are in the wrong direction and move so that the longitude decreases half of the increase of the latitude, will the risk of hypothermia increase or decrease?
 - (c) In which direction should they move to keep constant the temperature?
- (3 pts.) 3. A beach ball has a volumen of 50 dm^3 at the time when we start to pump air into it at a rate of $2 \text{ dm}^3/\text{min}$.
- (a) What is the speed at which the radius is changing?
 - (b) About when will the surface of the ball be twice its initial value?

Remark: The volume of a sphere is $V(r) = \frac{4}{3}\pi r^3$ and the surface is $S(r) = 4\pi r^2$.