#### SC42025 FILTERING AND IDENTIFICATION

# TURBULENCE MODELING FOR ADAPTIVE OPTICS

Aniket Ashwin Samant, Snehal Jauhri (Student IDs: 4838866, 4772202)

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# Introduction

This assignment deals with modeling an *Adaptive Optics* (AO) system in which three different data-driven turbulence modeling methods are used to achieve optimal control performances, viz.

- a random-walk process
- a Vector-Auto-Regressive model
- a stochastic state-space model

Each model has some questions associated with it, and we solve them in chronological sequence taking one model at a time.

### 1. RANDOM WALK MODEL

### **Question 1**

We know from the assignment's equation (2) that:

$$s_o(k) = G\phi(k) + e(k)$$

We have the values of the wavefront sensor data in open-loop,  $s_o(k)$ , and also the value of the matrix G. To compute the value of  $\phi(k)$ , given no prior information on it, we follow the linear least-squares approach:

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# **Question 2**

We are provided with some prior information about the wavefront, viz.:

- $E[\phi(k)] = 0$
- $E[\phi(k)\phi(k)^T] = C_{\phi}(0)$
- noise variance =  $\sigma_e^2$

Based on equation (8) from the assignment, we approximate the value of  $C_{\phi}(0)$  as:

$$C_{\phi}(0) = \frac{1}{N} \sum_{i=1}^{N} \phi(i) \phi(i)^{T}$$

WE HAVE THE REQUIRED DATA NOW WE JUST NEED TO COMPUTE THE EXPRESSIONS. Pg 113 in book

For questions 3 to 5, we assume  $E[\epsilon(k)] = 0$  and  $E[\epsilon(k)\epsilon(k)^T] = C_{\phi}(0)$ 

### **Question 3**

Similar to previous question but with now closed loop expression for s(k).

# **Question 4**

Use an expression similar to Kalman Gain to get ideal predictor.

# **Question 5**

Find Optimal Increment.

### 2. VAR MODEL

### **Question 1**

We know from the assignment's equation (2) that:

$$s_o(k) = G\phi(k) + e(k)$$

We have the values of the wavefront sensor data in open-loop,  $s_o(k)$ , and also the value of the matrix G. To compute the value of  $\phi(k)$ , given no prior information on it, we follow the linear least-squares approach:

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# **Question 3**

Similar to previous question but with now closed loop expression for s(k).

# **Question 4**

Use an expression similar to Kalman Gain to get ideal predictor.

# **Question 5**

Find Optimal Increment.

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