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MOVA/MOSS: Two integrated software solutions for comprehensive Structural Health Monitoring of structures

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Abstract

Recent ground-breaking advances in sensing technologies, data processing, and structural identification have made Structural Health Monitoring (SHM) occupy a central place in Structural Engineering. Although the technological transfer to the industry is still in the early development stages, there is clear evidence that SHM-enabled condition-based maintenance of structures will soon supersede traditional periodic maintenance strategies. Among the existing solutions, ambient vibration-based SHM has become particularly popular owing to its minimum intrusiveness and global damage assessment capabilities. Nevertheless, it is well documented that local pathologies with limited impact over the stiffness of structures can be hardly detected by such techniques. As a solution, recent studies advocate the use of integrated monitoring systems, where data from heterogeneous sensor networks are simultaneously processed to achieve a comprehensive structural assessment. Despite the great advances of these systems reported by researchers, practitioners still find many difficulties to bring them to practice. In this light, this paper reports the development of two novel software solutions for long-term SHM of structures, MOVA and MOSS, that are intended to bridge this gap while also introducing new methodological and scientific advances. The developed software enables the online system identification and damage detection of structures, including vibration-based SHM and data fusion of heterogeneous sensing systems with an innovative automated anomaly detection algorithm. A case study of a permanent static/dynamic/environmental monitoring system installed in a monumental masonry palace, the Consoli Palace in Gubbio (Italy), is presented to illustrate the capabilities of MOVA/MOSS.

Keywords: Data fusion, Novelty Analysis, Operational Modal Analysis, Damage detection, Structural Health Monitoring, Unsupervised Learning

1. Introduction

In the last two decades, SHM has gained a leading role in the field of Structural Engineering. Recent tragic events, such as the Genoa bridge collapse in 2018, have highlighted the need to prioritize the maintenance of civil infrastructure in the political agenda. Civil engineering infrastructures are inevitably subjected to ageing degradation, as well as to a number of adverse external actions (e.g. extreme weather, earthquakes, or accidental loads). In particular, the last Infrastructure Report Card of the American Society of Civil Engineers (ASCE) released in 2017 [1] estimated that 39% of the 614387 American bridges are over 50 years old, and classified 9.1% of the bridges as structurally deficient or in poor conditions. Moreover, the ASCE's report estimated the corresponding rehabilitation costs at \$123 billion. A similar picture emerges across Europe, where many of the bridges were built during the economic growth of the 1950s and, for instance, about 30% of the railway bridges exceed 100 years of age [2]. Nevertheless, despite large financial efforts have been dedicated to R&D actions in this field, the technology transfer has not been fully or successfully completed and SHM is still sparsely implemented in practice. Indeed, the last report of the European Joint Research Centre (JRC) [3] warned about the weak link between research and the wide-scale adoption of SHM technologies. To address these deficiencies, it is of pivotal importance to develop reliable and easy-to-use SHM solutions that facilitate practitioners' use of research breakthroughs.

Structural Health Monitoring aims to perform a diagnosis of the integrity of materials, structural components and assemblies constituting a structure [4]. This encompasses the application of Non-Destructive Testing (NDT) and damage identification tools and allows infrastructure managers to perform preventive condition-based maintenance, promote safety and maximize life expectancy. In essence, SHM involves long-term monitoring in order to track deviations in the structural response with respect to engineering-design specifications and past structural

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22 performance. In this framework, ambient vibration-based SHM has received most attention owing to its minimal
23 intrusiveness and fully non-destructive character [5]. These techniques exploit ambient acceleration records under
24 normal operating conditions to extract the modal features of a system through output-only (Operational) Modal
25 Analysis (OMA), namely natural frequencies, mode shapes, and damping ratios [6, 7]. The basic premise is that,
26 since modal features are functions of the mass, stiffness, and energy dissipation mechanisms, damage in a structure
27 can be inferred by tracking permanent variations in its modal parameters [8, 9]. Numerous recent works report
28 the successful application of this technology to diverse structural typologies, including bridges [10], dams [11],
29 buildings [12], stadiums [13], naval vessels [14], or aircraft structures [15]. Vibration-based SHM is also be-
30 coming increasingly popular for preventive conservation of Cultural Heritage (CH) structures. The monitoring
31 of such structures must have a minimum impact on their architectural and cultural value, for which OMA-based
32 SHM represents an ideal solution. In this context, plenty of successful applications can be found in the literature,
33 including CH bridges [16, 17], towers [18, 19], churches [20], and buildings [21, 22].

34 Considerable research has been devoted to the development of automated OMA procedures [23–25]. These
35 enable early detection of damage by tracking anomalies in time series of continuously identified modal features.
36 Nonetheless, numerous papers have reported about the striking dependence of modal features on environmental
37 (e.g. temperature, humidity, wind) and operational conditions (e.g. traffic level). For instance, Peeters and De
38 Roeck [26] found variations up to 18% in the first four resonant frequencies of the well-known case study of the
39 Z24-Bridge. This translates into daily and seasonal modal fluctuations that mask early stage damages. It fol-
40 lows that environmental effects must be filtered out through statistical pattern recognition and machine learning
41 techniques [27]. In this context, the Z24 Bridge constitutes an important benchmark on which intensive research
42 efforts have been exerted. The bridge was monitored during a nine-month period and, afterwards, artificial damage
43 was introduced. Peeters and De Roeck [26] successfully detected the artificial damage by analysing the residu-
44 als between experimental resonant frequencies and statistical predictions obtained by an autoregressive model.
45 Kullaa [28] and Yan and co-authors [29, 30] also worked on the Z24 Bridge and showed that damage can be
46 also detected through control charts and Principal Component Analysis (PCA). Ubertini *et al.* [9] reported the
47 damage detection of the bell-tower of the Basilica of San Pietro in Perugia during the 2016 Central Italy seismic
48 sequence through long-term vibration-based SHM. To do so, the environmental effects were filtered out using
49 Multiple Linear Regression (MLR) analysis and PCA, and the damage-induced anomalies in the residuals were
50 analysed through control charts. Hu *et al.* [31] reported the vibration-based SHM of a prestressed-concrete box
51 girder bridge in Berlin over 14 years. Through MLR filtering of the environmental effects, those authors found
52 a progressive increase in the number of outliers in the control charts from 1.35% in 2000/2001 to 21.58% after
53 2008. Such reductions were consistent with measured decreases in the strain of the main pre-stressed tendon, what
54 demonstrates the usefulness of vibration-based SHM for assessing progressive structural deterioration.

55 While highly effective in global structural assessment, vibration-based SHM may fail at detecting local de-
56 fects with a limited impact on the stiffness. Hence, the use of integrated monitoring systems comprising diverse
57 sensing solutions (e.g. dynamic, static, chemical) becomes imperative for effective local/global damage detection.
58 Moreover, the assessment of environmental conditions is often critical for efficient data fusion and extraction of
59 damage-sensitive features. The effects of environmental factors may dramatically vary depending on the type
60 of construction material and the structural typology, so sensor layouts must be tailored for every specific case
61 study. For instance, in masonry structures, positive correlations between environmental temperature and resonant
62 frequencies are often observed [9, 32]. This is conceivably explained as the effect of the closing of superficial
63 cracks or micro-cracks induced by thermal expansion of masonry. However, some other works such as the one
64 by Gentile *et al.* [33] report the opposite behaviour. Those authors reported the SHM of the Milan Cathedral in
65 Italy using both static (tilt meters and vibrating wire extensometers), environmental (hygrometers and temperature
66 sensors) and dynamic sensors (seismometers). Their results showed a negative correlation between resonant fre-
67 quencies and temperature, which was ascribed to the actions exerted by metallic tie-rods in the building. Negative
68 frequency-temperature correlations are also common in reinforced-concrete and steel structures (see e.g. [34, 35]),
69 which is usually ascribed to decreases in the material Young's modulus with increasing temperature. Neverthe-
70 less, likewise masonry structures, varying effects can be found depending on the specific structural typology, solar
71 radiation, and temperature distribution (see e.g. [36, 37]).

72 Despite the advanced state of research, the number of software solutions that allow implementing SHM sys-
73 tems in practice is considerably limited. The most popular software programs for vibration-based SHM of struc-
74 tures are MACEC, LMS Test.Lab, and ARTeMIS. MACEC [38] is a MATLAB toolbox for OMA of structures
75 developed by the Structural Mechanics Section of KU Leuven. This offers an extensive gallery of system identifi-
76 cation methods for Ambient Vibration Testing (AVT) of structures, including, among others, Frequency Domain
77 Decomposition (FDD), data-based and covariance-based Stochastic Subspace Identification (SSI), and Polyref-
78 erence Least Squares Complex Frequency Domain method (p-LSCF). Nonetheless, this software does not allow
79 performing continuous OMA and, therefore, cannot be directly applied to long-term vibration-based SHM. The

80 LMS Test.Lab Modal Analysis software [39] implements a very robust version of the p-LSCF method under
81 the commercial name of PolyMAX although, alike MACEC, this software does not permit the implementation
82 of long-term SHM systems. ARTeMIS [40] was developed by the company Structural Vibration Solutions A/S,
83 funded in 1999 as a spin-off from Aalborg University in Denmark. This software is particularly well-suited for
84 AVT of structures and, unlike the previous software programs, the most recent versions include a Damage Detec-
85 tion Plug-in with automated SSI and Hotelling's control charts. Nevertheless, ARTeMIS lacks the possibility of
86 using statistical pattern recognition methods to filter out environmental effects and, therefore, it may be difficult to
87 detect early-stage damage using this tool.

88 In view of the reported gap between research and professional practice, this paper introduces two new software
89 programs for integrated SHM of structures, called MOVA and MOSS, Italian acronyms of "MONitoraggio delle
90 Vibrazioni Ambientali" (AVT) and "MONitoraggio dello Stato di Salute" (SHM), respectively. MOVA focuses on
91 AVT, while MOSS is dedicated to the online management of permanent integrated SHM systems. The latter in-
92 cludes automated OMA, frequency tracking, filtering of environmental effects, and fusion of heterogeneous sensor
93 data. The data fusion capability of MOSS specifically lies in the possibility of performing pattern recognition us-
94 ing arbitrary combinations of predictors and estimators, including vibration and non-vibration data. Furthermore,
95 an original algorithm for automated anomaly detection is introduced. In this way, once set up, the user has online
96 access to a number of control charts assessing the performance of all those desired damage-sensitive features, and
97 the system triggers an alarm (visual, sound, and/or by e-mail) when an anomaly is detected in any of them. Central
98 to the development of MOVA/MOSS is the attention to ease of use and interpretability. Originally developed using
99 MATLAB environment, MOVA and MOSS have been implemented in C++ providing a compact graphical user
100 interface (GUI). In order to highlight the capabilities of MOVA/MOSS, this paper presents an application case
101 study of the static/dynamic SHM of a monumental masonry palace, the Consoli Palace in Gubbio (Italy).

102 The remaining of the paper is organised as follows: Section 2 concisely describes the case study of the Consoli
103 Palace. Section 3 outlines the theoretical background of vibration-based SHM. Section 4 describes the software
104 architecture of MOVA/MOSS through an application case study of the Consoli Palace and, finally, Section 5
105 concludes the paper.

106 **2. Application case study: The Consoli Palace in Gubbio, Italy**

107 The Consoli Palace is the most emblematic monument of the city of Gubbio in Italy (Fig. 1 (a)). Erected
108 between 1332 and 1349 to house the official courts, the Consoli Palace has hosted the Civic Museum of Gubbio
109 since 1901. Including a bell-tower and a panoramic loggia, the building is 60 m high and has a rectangular plan of
110 about 40×20 m. The palace features a Gothic style design with calcareous stone masonry, including an articulated
111 internal distribution of volumes with thick masonry bearing walls and vaults as horizontal elements. Erected on
112 the slope of the Ingino Mountain, the palace foundations are placed on two different levels with a drop of about
113 10 m. From the architectural point of view, the main façade is characterized by a distinctive fan-shaped staircase
114 entrance and an arched portal.

115 As an exceptional example of a stiff historic building, the Consoli Palace has become the benchmark case
116 study of several recent research projects. These include the Horizon 2020 European HERACLES project (2016-
117 2018) devoted to enhancing resilience of historic buildings against harmful events, with emphasis on climate-
118 change related effects. Within this project, a wide research programme was developed including diverse SHM
119 methodologies and protocols for application to historic masonry palaces (see e.g. [22, 41, 42]). More recently, the
120 Consoli Palace has also become the benchmark case study of a national Italian research project entitled "DETECT-
121 AGING" and devoted to the monitoring of degradation effects on the structural safety of CH constructions. From
122 these experiences, a considerable amount of monitoring data from different types of sensors has been collected,
123 making the Consoli Palace an ideal example to illustrate the capabilities of MOVA/MOSS.

124 In this work, we focus on the static/dynamic/environmental monitoring of the Consoli Palace. Firstly, in
125 order to characterize the modal features of the palace, an AVT with a moderately dense accelerometer network
126 sketched in Fig. 1 (c) was conducted on May 4th 2017. This consisted of 9 uni-axial high sensitivity piezoelectric
127 accelerometers (model PCB 393B12, ±0.50 g, and 10 V/g sensitivity) deployed on the three main floors of the
128 palace at heights of 4.64, 18.89, and 29.77 m (labelled from TS1 to TS9). Afterwards, a permanent integrated SHM
129 system has been installed in the Consoli Palace since July 2017, including 3 accelerometers, 2 crack meters, and
130 2 temperature sensors. Specifically, three PCB 393B12 accelerometers, labelled from PS1 to PS3, were deployed
131 on the roof level of the palace. Two linear variable transducers (LVDTs) denoted as LVDT1 and LVDT2 (S-
132 Series, measurement range 0-50 mm, resolution <0.3 μm) were installed across two major vertical cracks located
133 on the second floor of the building. Finally, two K-type thermocouples were also installed close to each LVDTs.
134 The sensors are connected to a NI CompactDAQ-9132 data acquisition system (processor 1.33 GHz Dual-Core
135 Atom, 2 GB RAM, 16 GB SD storage, 4-Slot, Windows Embedded Standard 7 operating system) with a NI

136 9234 acceleration acquisition module (24-bit resolution, 102-dB dynamic range, and anti-aliasing filters) and a
 137 NI 9219 crack amplitude and temperature acquisition module (24-bit resolution, +/-60V range, 100 S/s). The
 138 monitoring data were locally acquired and preliminarily processed through an in-house LabVIEW code, and
 139 stored in consecutive separate files containing 30 min-long recordings. Ambient accelerations were sampled at
 140 100 Hz, while crack amplitudes and temperature values were sampled at 0.1 Hz. The data files were sent online
 141 through the Internet to a remove server located in the Laboratory of Structural Health Monitoring and Earthquake
 142 Engineering, where MOSS was used for automated SHM of the palace.

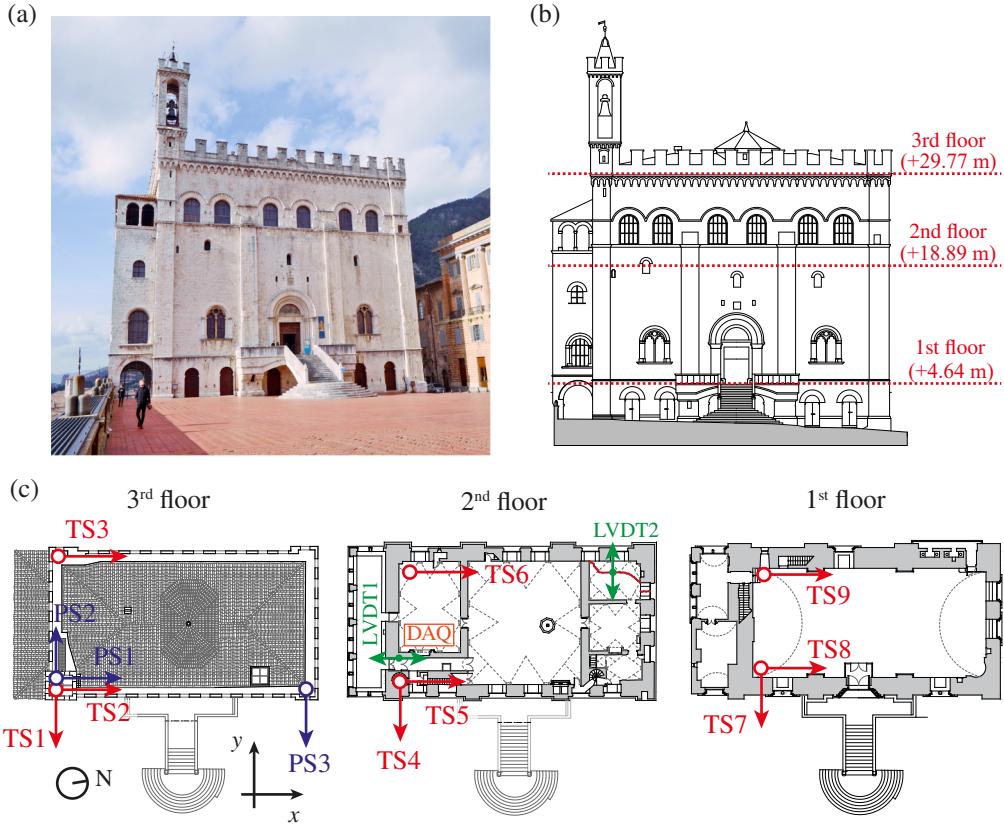


Figure 1: View of the Consoli Palace (a), elevation (b), and sketch of the structural monitoring system (c).

143 3. Theoretical background

144 MOVA and MOSS combine the experience on SHM of civil engineering structures accumulated by the re-
 145 search group during the last ten years. Some of the included routines have been previously tested in different
 146 structural typologies, specially bridges [24, 43] and CH structures [9, 22, 44].

147 3.1. Fundamentals of time-domain OMA methods

148 The differential equation of equilibrium of a dynamic system discretized into a finite element model (FEM)
 149 with n_2 degrees of freedom (DOFs) can be written in continuous state-space form as follows:

$$\begin{aligned} \dot{\mathbf{x}}(t) &= \mathbf{A}_C \mathbf{x}(t) + \mathbf{B}_C \mathbf{u}(t), \\ \dot{\mathbf{y}}(t) &= \mathbf{C}_C \mathbf{x}(t) + \mathbf{D}_C \mathbf{u}(t), \end{aligned} \quad (1)$$

150 where $\mathbf{A}_C \in \mathbb{R}^{2n_2 \times 2n_2}$, $\mathbf{B}_C \in \mathbb{R}^{2n_2 \times n_i}$, $\mathbf{C}_C \in \mathbb{R}^{l \times 2n_2}$, and $\mathbf{D}_C \in \mathbb{R}^{l \times n_i}$ are designated the state matrix, input matrix,
 151 output matrix, and direct transmission matrix, respectively. Vectors $\mathbf{x}(t) \in \mathbb{R}^{2n_2}$ and $\mathbf{y}(t) \in \mathbb{R}^l$ denote the state and
 152 observation vectors, respectively. The state vector $\mathbf{x}(t)$ contains the displacements and velocities of the DOFs of
 153 the system, while the observation vector $\mathbf{y}(t)$ contains a subset of l measured outputs. The first line in Eq. (1),
 154 called the state equation, relates n_i inputs (loads) applied to the system and contained in vector $\mathbf{u}(t) \in \mathbb{R}^{n_i}$ to the
 155 state vector $\mathbf{x}(t)$. On the other hand, the second line in Eq. (1) is called the observation equation and establishes
 156 a relation between the observation vector $\mathbf{y}(t)$ and the state vector $\mathbf{x}(t)$. The modal features of the system can

157 be extracted from the eigenvalue decomposition of the state matrix \mathbf{A}_C as $\mathbf{A}_C = \Psi \Lambda_C \Psi^{-1}$. Matrices Λ_C and Ψ
 158 containing the eigenvalues and eigenvectors of \mathbf{A}_C , respectively, present the following structure [45]:

$$\begin{aligned} \Lambda_C &= \begin{bmatrix} \Lambda & 0 \\ 0 & \Lambda^* \end{bmatrix}, \quad \Psi = \begin{bmatrix} \Theta & \Theta^* \\ \Theta \Lambda & \Theta^* \Lambda^* \end{bmatrix}, \\ \Lambda &= \begin{bmatrix} \ddots & & \\ & \lambda_k & \\ & & \ddots \end{bmatrix}, \quad \Theta = [\dots \ \phi_k \ \dots], \quad k = 1, \dots, n_2 \end{aligned} \quad (2)$$

159 where \bullet^* denotes complex conjugate. Parameters λ_k are related to the resonant frequencies (ω_k - natural frequencies
 160 in rad/s) and the modal damping ratios (ζ_k) of the system as:

$$\lambda_k = -\zeta_k \omega_k + i \sqrt{1 - \zeta_k^2} \omega_k, \quad (3)$$

161 with i denoting the imaginary unit. The mode shapes are represented in Eq. (2) by $\phi_k \in \mathbb{R}^{n_2}$. However, since only
 162 a subset of l DOFs is measured, the observable modal matrix $\Phi \in \mathbb{R}^{l \times n_2}$ is given by:

$$\Phi = \mathbf{C}_C \Psi. \quad (4)$$

163 In practice, recorded analogue signals are digitalized by an analogue-to-digital converter (A/D), so the available
 164 information is discrete in time. Such a process is conducted by sampling the signals at a certain sampling
 165 frequency $f_s = 1/\Delta t$, with Δt being the adopted sampling interval. Therefore, the time functions $\mathbf{x}(t)$ and $\mathbf{y}(t)$ in
 166 Eq. (1) must be replaced by their values at discrete time instants $k\Delta t$ with k being an integer, i.e. $\mathbf{y}_k = \mathbf{y}(k\Delta t)$,
 167 $\mathbf{x}_k = \mathbf{x}(k\Delta t)$. In addition, in the context of OMA, the system inputs in $\mathbf{u}(t)$ are unknown (unmeasured) and must
 168 be represented through stochastic processes. On this basis, the discrete stochastic state-space model reads:

$$\begin{aligned} \mathbf{x}_{k+1} &= \mathbf{A}\mathbf{x}_k + \mathbf{w}_k, \\ \mathbf{y}_k &= \mathbf{C}\mathbf{x}_k + \mathbf{v}_k, \end{aligned} \quad (5)$$

169 here, vectors $\mathbf{w}_k \in \mathbb{R}^{2n_2}$ and $\mathbf{v}_k \in \mathbb{R}^l$ represent white noise processes accounting for the effect of unknown outputs
 170 as well as the effects of process noise (modelling inaccuracies) and measurement noise, respectively. Both noise
 171 vectors are assumed to be zero-mean realizations of stochastic processes with the following correlation matrices:

$$E \left(\begin{bmatrix} \mathbf{w}_p \\ \mathbf{v}_p \end{bmatrix} \begin{bmatrix} \mathbf{w}_q^T & \mathbf{v}_q^T \end{bmatrix} \right) = \begin{bmatrix} \mathbf{Q} & \mathbf{S} \\ \mathbf{S}^T & \mathbf{R} \end{bmatrix} \delta_{pq}, \quad (6)$$

172 where sub-indexes p and q denote generic time instants, δ_{pq} is the Kronecker delta, and E is the expected value
 173 operator.

174 It can be demonstrated that the eigenvectors of matrix \mathbf{A} coincide with those of the continuous counterpart \mathbf{A}_C
 175 and, since \mathbf{C} equals \mathbf{C}_C , the modal matrix is given by Eq. (4) [46]. In addition, the eigenvalues of the discrete
 176 model μ_k are related to those of the continuous model λ_k as [46]:

$$\mu_k = e^{\lambda_k \Delta t} \Leftrightarrow \lambda_k = \frac{\ln(\mu_k)}{\Delta t}, \quad (7)$$

177 Therefore, the natural frequencies and model damping ratios can be readily obtained from the eigenvalues of
 178 matrix \mathbf{A} using Eqs. (3) and (7).

179 An important property of stochastic state-space models regards the relation between the correlation matrix of
 180 the measurement records and the state-space matrices [45]:

$$\mathbf{R}_j = \mathbf{C}\mathbf{A}^{j-1}\mathbf{G}, \quad (8)$$

181 with \mathbf{R}_j being the output correlation matrix for a time lag $\tau = j\Delta t$, and \mathbf{G} being the next state-output covariance
 182 matrix given by:

$$\mathbf{G} = E \left[\mathbf{x}_{k+1} \mathbf{y}_k^T \right]. \quad (9)$$

183 3.2. System identification

184 The software MOVA/MOSS offers four different system identification techniques, including two frequency-
 185 domain (EFDD and p-LSCF) and two time-domain identification techniques (COV-SSI and DATA-SSI).

186 3.2.1. Enhanced Frequency Domain Decomposition (EFDD)

187 The Frequency Domain Decomposition (FDD) method is based on the input/output relationship of linear time-
 188 invariant systems as [47]:

$$\mathbf{G}_{yy}(\omega) = \mathbf{H}(\omega)\mathbf{G}_{uu}(\omega)\mathbf{H}(\omega)^H, \quad (10)$$

189 where \bullet^H denotes complex conjugate (Hermitian) transpose. Matrices $\mathbf{G}_{uu}(\omega) \in \mathbb{C}^{r_c \times r_c}$ and $\mathbf{G}_{yy}(\omega) \in \mathbb{C}^{l \times l}$ represent
 190 the Power Spectral Density (PSD) matrices of the inputs and outputs, respectively, with r_c being the number of
 191 inputs (references), and $\mathbf{H}(\omega) \in \mathbb{C}^{r_c \times l}$ is the Frequency Response Function (FRF) matrix. In practice, the PSDs
 192 are commonly computed using the Welch's method. Then, the singular value decomposition (SVD) of \mathbf{G}_{yy} is
 193 performed as:

$$\mathbf{G}_{yy}(\omega_j) = \mathbf{U}_j \mathbf{S}_j \mathbf{U}_j^H, \quad (11)$$

194 where \mathbf{U}_j is an orthonormal matrix ($\mathbf{U}_j \mathbf{U}_j^H = \mathbf{I}$) containing the singular vectors of $\mathbf{G}_{yy}(\omega_j)$, and \mathbf{S}_j is a diagonal
 195 matrix holding the corresponding singular values (SVs). On this basis the resonant frequencies can be estimated
 196 by picking the peaks of the first SV, while the mode shapes are obtained as the first singular vector evaluated at
 197 the formerly picked frequency values.

198 The EFDD method represents an improved version of the FDD that allows to identify damping ratios and
 199 more accurate estimates of resonant frequencies. To do so, the singular value data around the resonance peaks
 200 are selected, typically according to a limit modal assurance criterion (MAC) value. Once selected, these spectrum
 201 segments are converted to the time domain in order to get auto-correlation functions for each mode. Finally, the
 202 corresponding resonant frequencies and damping ratios can be obtained by fitting the expression for the impulse
 203 response of a single-degree-of-freedom system. Alternatively, MOVA and MOSS implement the Single-Input-
 204 Multiple-Output (SIMO) version of the Ibrahim Time Domain (ITD) technique to extract the natural frequencies
 205 and damping ratios from the computed auto-correlation functions [48].

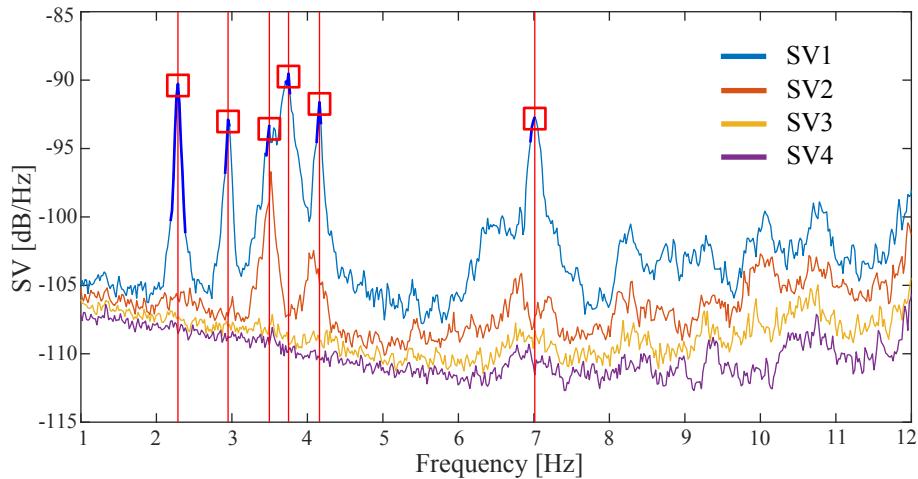


Figure 2: Dynamic identification of the Consoli Palace using EFDD in MOVA (SV plots and selected peaks).

206 Figure 2 presents the first four SVs of the spectral matrix calculated from the acceleration time-series recorded
 207 during the AVT of the Consoli Palace. These were calculated with the Welch's method using time segments with
 208 2048 points, and Hanning windows with an overlapping of 50%. The application of the SVD decomposition to the
 209 spectral matrix evaluated at all the discrete frequencies between 0 and 12 Hz produces 9 SVs for each frequency.
 210 The spectrum of the first singular values exhibits six peaks that are associated with main modes of the Consoli
 211 Palace within the frequency band under analysis as further investigated in Section 4. The points of the singular
 212 value spectra are selected for the application of the ITD method using a limit for the MAC of 0.8.

213 3.2.2. Polyreference Least Squares Complex Frequency Domain method (p-LSCF)

214 The Polyreference Least Squares Complex Frequency Domain method (p-LSCF) is a parametric frequency-
 215 domain method developed by Peeters and Van der Auweraer [49]. The p-LSCF models the positive half-spectrum

216 matrix using a right-matrix fraction model as:

$$\mathbf{G}_{yy}^+(\omega_j) = \mathbf{B}(\omega_j) [\mathbf{A}(\omega_j)]^{-1} = \left[\sum_{r=0}^p \mathbf{B}_r \Omega_r(\omega_j) \right] \left[\sum_{r=0}^p \mathbf{A}_r \Omega_r(\omega_j) \right]^{-1}, \quad (12)$$

217 where matrices $\mathbf{B}_r, \mathbf{A}_r \in \mathbb{R}^{l \times l}$ are model parameter matrices to be determined, $\Omega_r(\omega_j)$ are polynomial basis
218 functions, and p is the polynomial order. The p-LSCF model is expressed in the discrete z -domain (i.e. a
219 frequency-domain model derived from a discrete-time model), so the polynomial basis functions take the form
220 $\Omega_r(\omega_j) = e^{i\omega_j \Delta t r}$. The method seeks matrices \mathbf{B}_r and \mathbf{A}_r that minimize in a non-linear least-squares sense the error
221 matrix $\mathbf{E}^{NLS}(\omega_j) = \mathbf{G}_{yy}^+(\omega_j) - \hat{\mathbf{G}}_{yy}^+(\omega_j)$, which involves the difference between \mathbf{G}_{yy}^+ and the half-spectrum matrix
222 $\hat{\mathbf{G}}_{yy}^+$ estimated from the measurement records. Nevertheless, the right multiplication of $\mathbf{E}^{NLS}(\omega_j)$ by matrix $\mathbf{A}(\omega_j)$
223 leads to more convenient linear least-squares equation errors as:

$$\mathbf{E}^{LS}(\omega_j) = \left[\sum_{r=0}^p \mathbf{B}_r \Omega_r(\omega_j) \right] - \hat{\mathbf{G}}_{yy}^+(\omega_j) \left[\sum_{r=0}^p \mathbf{A}_r \Omega_r(\omega_j) \right], \quad (13)$$

224 where $\mathbf{E}^{LS}(\omega_j) \in \mathbb{C}^{l \times l}$ contains the errors (E_{ij}) to be minimized. The minimization problem can be written in
225 a more compact form after some transformations. In particular, an arbitrary line o of the error matrix at all the
226 discrete frequency values from ω_1 to ω_{N_f} can be stacked in a matrix $\mathbf{E}_o^{LS} \in \mathbb{C}^{N_f \times l}$:

$$\mathbf{E}_o^{LS}(\beta_o, \alpha) = \begin{bmatrix} E_{o1}(\omega_1) & \dots & E_{ol}(\omega_1) \\ E_{o1}(\omega_2) & \dots & E_{ol}(\omega_2) \\ \vdots & \ddots & \vdots \\ E_{o1}(\omega_{N_f}) & \dots & E_{ol}(\omega_{N_f}) \end{bmatrix} = [\mathbf{X}_o \quad \mathbf{Y}_o] \begin{bmatrix} \beta_o \\ \alpha \end{bmatrix}, \quad (14)$$

227 with

$$\begin{aligned} \Omega(\omega_j) &= [\Omega_0(\omega_j) \Omega_1(\omega_j) \dots \Omega_p(\omega_j)] \in \mathbb{C}^{p+1}, \\ \mathbf{Y}_o &= \begin{bmatrix} \Omega_0(\omega_1) \hat{\mathbf{S}}_{yyo}^+ & \Omega_1(\omega_1) \hat{\mathbf{S}}_{yyo}^+ & \dots & \Omega_p(\omega_1) \hat{\mathbf{S}}_{yyo}^+ \\ \vdots & \ddots & & \vdots \\ \Omega_0(\omega_{N_f}) \hat{\mathbf{S}}_{yyo}^+ & \Omega_1(\omega_{N_f}) \hat{\mathbf{S}}_{yyo}^+ & \dots & \Omega_p(\omega_{N_f}) \hat{\mathbf{S}}_{yyo}^+ \end{bmatrix} \in \mathbb{C}^{N_f \times l(p+1)}, \\ \mathbf{X}_o &= \begin{bmatrix} \Omega(\omega_1) \\ \vdots \\ \Omega(\omega_{N_f}) \end{bmatrix} \in \mathbb{C}^{N_f \times (p+1)}, \quad \beta_o = \begin{bmatrix} \mathbf{B}_{0o} \\ \mathbf{B}_{1o} \\ \vdots \\ \mathbf{B}_{po} \end{bmatrix} \in \mathbb{R}^{(p+1) \times l}, \quad \alpha = \begin{bmatrix} \mathbf{A}_0 \\ \mathbf{A}_1 \\ \vdots \\ \mathbf{A}_p \end{bmatrix} \in \mathbb{R}^{l(p+1) \times l}, \end{aligned} \quad (15)$$

228 where $\hat{\mathbf{S}}_{yyo}^+$ and \mathbf{B}_{ro} represent the o lines of matrices $\hat{\mathbf{S}}_{yy}^+$ and \mathbf{B}_r , respectively. Finally, a scalar cost function can be
229 constructed as the sum of the squared elements of the error matrix as:

$$\varepsilon(\beta_o, \alpha) = \sum_{o=1}^l \text{tr} \{ \mathbf{E}_o(\beta_o, \alpha)^H \mathbf{E}_o(\beta_o, \alpha) \} = \sum_{o=1}^l \text{tr} \left\{ [\beta_o^T \quad \alpha^T] [\mathbf{R}_o \quad \mathbf{S}_o] [\beta_o \quad \alpha] \right\}, \quad (16)$$

230 with $\mathbf{R}_o = \text{Re}(\mathbf{X}_o^H \mathbf{X}_o) \in \mathbb{R}^{(p+1) \times (p+1)}$, $\mathbf{S}_o = \text{Re}(\mathbf{X}_o^H \mathbf{Y}_o) \in \mathbb{R}^{(p+1) \times l(p+1)}$, $\mathbf{T}_o = \text{Re}(\mathbf{Y}_o^H \mathbf{Y}_o) \in \mathbb{R}^{l(p+1) \times l(p+1)}$, and
231 tr denoting the trace operator. The unknown model parameters in \mathbf{B}_r and \mathbf{A}_r can be obtained by forcing the
232 derivatives of the cost function with respect to α and β_o to be zero. This leads to the following reduced system of
233 equations:

$$\begin{aligned} 2(\mathbf{R}_o \beta_o + \mathbf{S}_o \alpha) &= \mathbf{0} \Leftrightarrow \beta_o = -\mathbf{R}_o^{-1} \mathbf{S}_o \alpha, \\ 2 \sum_{o=1}^l (\mathbf{T}_o - \mathbf{S}_o^T \mathbf{R}_o^{-1} \mathbf{S}_o) \alpha &= 0 \Leftrightarrow \mathbf{M} \alpha = 0, \end{aligned} \quad (17)$$

234 where matrix $\mathbf{M} \in \mathbb{C}^{l(p+1) \times l(p+1)}$ can be computed from the output half-spectrum matrix estimated from the mea-
235 surement records. In order to avoid the trivial solution of the previous equation ($\alpha = \mathbf{0}$), a constraint has to be
236 imposed. This is typically conducted by forcing either \mathbf{A}_o or \mathbf{A}_p to be the identity matrix. In particular, clearer

237 stabilization diagrams have been reported to be found when $\mathbf{A}_o = \mathbf{I}$ [6]. Then, the resolution of the system of
 238 equations reads:

$$\mathbf{M}\alpha = \mathbf{0} \Leftrightarrow \left[\begin{array}{c|c} \mathbf{M}_{aa} & \mathbf{M}_{ab} \\ \hline \mathbf{M}_{ba} & \mathbf{M}_{bb} \end{array} \right] \left[\begin{array}{c} \mathbf{I} \\ \alpha_b \\ \vdots \\ \mathbf{0} \end{array} \right] = \left[\begin{array}{c} \mathbf{0} \\ \mathbf{0} \\ \vdots \\ \mathbf{0} \end{array} \right] \Leftrightarrow \alpha_b = -\mathbf{M}_{bb}^{-1}\mathbf{M}_{ba} \Leftrightarrow \alpha = \left[\begin{array}{c} \mathbf{I} \\ -\mathbf{M}_{bb}^{-1}\mathbf{M}_{ba} \end{array} \right], \quad (18)$$

239 where \mathbf{M}_{ba} contains the first l columns and the last pl lines of \mathbf{M} , \mathbf{M}_{bb} contains the last pl columns and rows of
 240 \mathbf{M} , and α_b contains the last pl rows of α . Once matrix α is determined, matrix β_o is directly obtained using the
 241 relation between α and β_o in Eq. (17). With this step, the model parameter matrices \mathbf{A}_r and \mathbf{B}_r are determined and
 242 the identification problem is solved. Then, the modal features can be obtained through the transposition equations
 243 from right matrix-fraction models to state-space models, leading to the following state-space matrices [50]:

$$\mathbf{A}_C = \left[\begin{array}{ccccc} -\mathbf{A}_p^{-1} - \mathbf{A}_{p-1} & -\mathbf{A}_p^{-1} - \mathbf{A}_{p-2} & \dots & -\mathbf{A}_p^{-1} - \mathbf{A}_1 & -\mathbf{A}_p^{-1} - \mathbf{A}_0 \\ \mathbf{I} & \mathbf{0} & \dots & \mathbf{0} & \mathbf{0} \\ \vdots & \ddots & \dots & \vdots & \vdots \\ \mathbf{0} & \mathbf{0} & \dots & \mathbf{I} & \mathbf{0} \end{array} \right], \quad (19)$$

$$\mathbf{B}_C = \left[\begin{array}{c} \mathbf{A}_p^{-1} \\ \mathbf{0} \end{array} \right],$$

$$\mathbf{C}_C = \left[\begin{array}{ccc} \mathbf{B}_{p-1} - \mathbf{B}_p \mathbf{A}_p^{-1} \mathbf{A}_{p-1} & \dots & \mathbf{B}_0 - \mathbf{B}_p \mathbf{A}_p^{-1} \mathbf{A}_0 \end{array} \right],$$

$$\mathbf{D}_C = \mathbf{B}_p \mathbf{A}_p^{-1}.$$

244 Finally, the modal features can be readily determined through the eigenvalue decomposition of matrix \mathbf{A} . At
 245 this point, separation of physical and spurious modes becomes crucial. This is commonly performed through
 246 stabilization diagrams representing the modal parameters estimated considering p-LSCF models with increasing
 247 polynomial orders p . Figure 3 shows the stabilization diagram obtained using the p-LSCF method in MOVA for
 248 the ambient vibration dataset recorded during the AVT of the Consoli Palace. To do so, the cross half-spectra
 249 of the nine time series of ambient vibrations were obtained using the Welch's method considering time segments
 250 with 2048 points and 50% overlap. Afterwards, the model conversion in Eq. (19) was constructed by adopting
 251 polynomial orders between 20 and 120. It is noted in Fig. 3 that six clear columns of stable poles are found at
 252 frequency values corresponding to the main natural frequencies of the Consoli Palace in the considered frequency
 253 range. These results exemplify one of the main advantages of the p-LSCF method, which regards the generation of
 254 very clear stabilization diagrams. Indeed, it has been previously reported in the literature that most of the spurious
 255 poles appear with negative damping ratios when using the p-LSCF method, thereby they are directly eliminated
 256 before constructing the stabilization diagram [45].

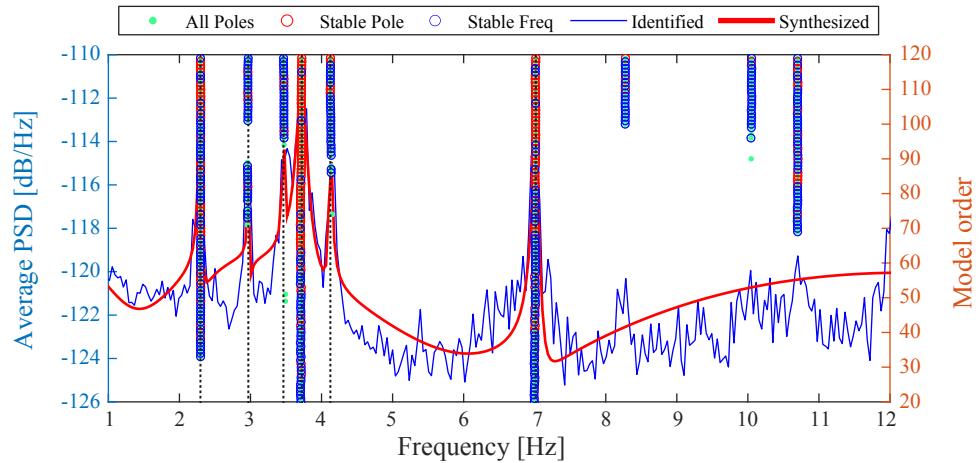


Figure 3: Dynamic identification of the Consoli Palace using p-LSCF in MOVA (stabilization diagram).

257 3.2.3. Stochastic Subspace Identification

258 The developed software includes two time-domain SSI methods, namely the Covariance driven SSI method
 259 (SSI-COV) and the data-driven SSI method (SSI-DATA).

260 **SSI-COV**

261 The SSI-COV method identifies a stochastic state-space model from the output covariance matrix (or corre-
 262 lation, as the mean of the signals is assumed to be zero). It starts by computing the output correlation matrix for
 263 positive time lags varying from Δt to $(2j_b - 1)\Delta t$ represented by \mathbf{R}_1 to \mathbf{R}_{2j_b-1} . Afterwards, the covariance matrix
 264 is organized in a $l j_b$ -by- $l j_b$ block Toeplitz matrix (sketched in Fig. 4) as:

$$\mathbf{T}_{1|j_b} = \begin{bmatrix} \mathbf{R}_{j_b} & \mathbf{R}_{j_b-1} & \dots & \mathbf{R}_1 \\ \mathbf{R}_{j_b+1} & \mathbf{R}_{j_b} & \dots & \mathbf{R}_2 \\ \dots & \dots & \dots & \dots \\ \mathbf{R}_{2j_b-1} & \mathbf{R}_{2j_b-2} & \dots & \mathbf{R}_{j_b} \end{bmatrix}. \quad (20)$$

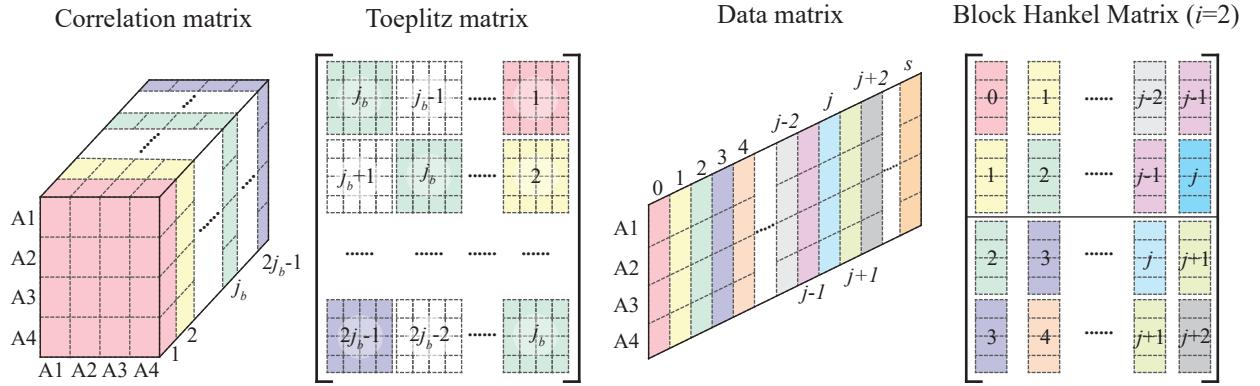


Figure 4: Schematic representation of the construction of the Toeplitz matrix and block Hankel matrix for SSI-COV and SSI-DATA, respectively.

265 Applying the factorization property of the correlation matrix in Eq. (8) to all the R_j matrices stored in the
 266 Toeplitz matrix, $T_{1|j_b}$ can be decomposed in the product of the following matrices:

$$\mathbf{T}_{1|j_b} = \begin{bmatrix} \mathbf{C} \\ \mathbf{CA} \\ \dots \\ \mathbf{CA}^{j_b-1} \end{bmatrix} \begin{bmatrix} \mathbf{A}^{j_b-1}\mathbf{G} & \dots & \mathbf{AG} & \mathbf{G} \end{bmatrix} = \mathbf{O}\mathbf{\Gamma}. \quad (21)$$

267 The second equality in Eq. (21) defines the following matrices: \mathbf{O} - extended observability matrix; and $\mathbf{\Gamma}$ -
 268 reversed extended stochastic controllability matrix. The first one is a column of j_b blocks with dimensions l -by- n
 269 (n is the dimension of the state-space model). The second one is formed by j_b n -by- l matrices organized in a row.
 270 According to the previous equation, the Toeplitz matrix results from the product of a matrix with n columns by
 271 a matrix with n rows. Therefore, if $n < l j_b$, the rank of $T_{1|j_b}$ is equal to n . Then, the SVD of the block Toeplitz
 272 matrix is calculated:

$$\mathbf{T}_{1|j_b} = \mathbf{USV}^T = [\mathbf{U}_1 \quad \mathbf{U}_2] \begin{bmatrix} \mathbf{S}_1 & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{V}_1^T \\ \mathbf{V}_2^T \end{bmatrix} = \mathbf{U}_1 \mathbf{S}_1 \mathbf{V}_1^T. \quad (22)$$

273 The number of non-zero SVs gives the rank of the decomposed matrix, which, in this case, coincides with
 274 n (assuming $n < l j_b$), the dimension of the state-space matrix \mathbf{A} . The comparison of Eqs. (21) and (22) shows
 275 that the observability and the controllability matrices can be calculated from the outputs of the SVD using the
 276 following partition of the singular values matrix:

$$\begin{aligned} \mathbf{O} &= \mathbf{U}_1 \mathbf{S}_1^{1/2}, \\ \mathbf{\Gamma} &= \mathbf{S}_1^{1/2} \mathbf{V}_1^T. \end{aligned} \quad (23)$$

Once the observability and controllability matrices are obtained, the identification of the state-space model matrices \mathbf{A} and \mathbf{C} is straightforward. On one hand, matrix \mathbf{C} can be extracted from the first l lines of the observability matrix. On the other hand, the state matrix \mathbf{A} can be computed according to different approaches. The developed software utilizes the Balanced Realization (BR) method which exploits the shift structure of the observability matrix, that is [45]:

$$\begin{bmatrix} \mathbf{C} \\ \mathbf{CA} \\ \vdots \\ \mathbf{CA}^{j_b-2} \end{bmatrix} \mathbf{A} = \begin{bmatrix} \mathbf{CA} \\ \mathbf{CA}^2 \\ \vdots \\ \mathbf{CA}^{j_b-1} \end{bmatrix} \Leftrightarrow \mathbf{A} = \begin{bmatrix} \mathbf{C} \\ \mathbf{CA} \\ \vdots \\ \mathbf{CA}^{j_b-2} \end{bmatrix}^\dagger \begin{bmatrix} \mathbf{C} \\ \mathbf{CA}^2 \\ \vdots \\ \mathbf{CA}^{j_b-1} \end{bmatrix} = \mathbf{O}^{to\dagger} \mathbf{O}^{bo}, \quad (24)$$

where \mathbf{O}^{to} contains the first $l(j_b - 1)$ lines of \mathbf{O} , and \mathbf{O}^{bo} contains the last $l(j_b - 1)$ lines of \mathbf{O}_{jb} . The symbol \dagger represents the Moore-Penrose pseudo-inverse.

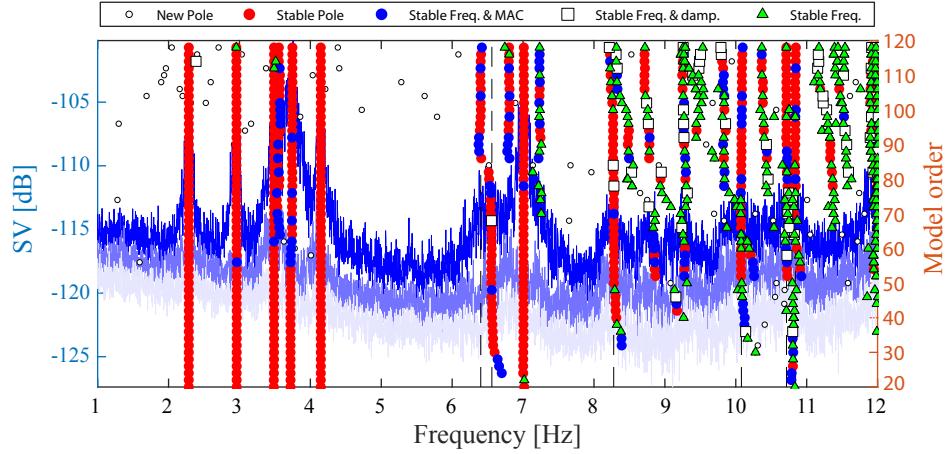


Figure 5: Dynamic identification of the Consoli Palace using SSI-COV in MOVA (stabilization diagram).

Figure 5 shows the stabilization diagram obtained using the SSI-COV method in MOVA for the ambient vibration dataset recorded during the AVT of the Consoli Palace. To do so, j_b has been assumed as 70, resulting in a $70 \cdot 9 \times 70 \cdot 9$ Toeplitz matrix. Then, matrices \mathbf{O} , Γ , \mathbf{A} and \mathbf{C} and then the modal parameters are estimated considering an odd number of singular values and vectors varying from 20 to 120. Similarly to the previous analyses, it is noted in Fig. 5 that six clear columns of stable poles are found at frequency values corresponding to the main natural frequencies of the Consoli Palace in the considered frequency range.

SSI-DATA

Data-driven stochastic subspace identification (SSI-DATA) is similar to SSI-COV, but identifies the state sequence before the estimation of the state-space matrices. Data-driven SSI consists of the following steps: (a) construction of the block Hankel matrix of the measurements, H_i ; (b) computation of the projection matrix, P_i ; (c) estimation of the observability matrix, Γ_i ; and (d) extraction of the modal parameters estimates from matrix Γ_i . The block Hankel matrix (sketched in Fig. 4) is defined as:

$$\mathbf{H}_i = \frac{1}{\sqrt{j}} \begin{bmatrix} \mathbf{y}(0) & \mathbf{y}(1) & \dots & \mathbf{y}(j-1) \\ \mathbf{y}(1) & \mathbf{y}(2) & \dots & \mathbf{y}(j) \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{y}(i-1) & \mathbf{y}(i) & \dots & \mathbf{y}(i+j-2) \\ \mathbf{y}(i) & \mathbf{y}(i+1) & \dots & \mathbf{y}(i+j-1) \\ \mathbf{y}(i+1) & \mathbf{y}(i+2) & \dots & \mathbf{y}(i+j) \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{y}(2i-1) & \mathbf{y}(2i) & \dots & \mathbf{y}(2i+j-2) \end{bmatrix} = \begin{bmatrix} \mathbf{Y}_{0|i-1} \\ \mathbf{Y}_{i|2i-1} \end{bmatrix} = \begin{bmatrix} \mathbf{Y}_p \\ \mathbf{Y}_f \end{bmatrix}, \quad (25)$$

where $2i$ and j , with $j \leq s - 2i + 1$, are user-defined quantities representing the number of output block rows and the number of columns of matrix \mathbf{H}_i , respectively. The block Hankel matrix in Eq. (25) is subdivided into two

298 sub-matrices, named as \mathbf{Y}_p and \mathbf{Y}_f , which are usually referred to as past and future output block matrices. The
 299 identification of the Kalman filter state sequences and, as a consequence, of the state-space matrices is based on
 300 the orthogonal projection of the row space of the future outputs on the row space of the past outputs:

$$\mathbf{P}_i = \mathbf{Y}_f / \mathbf{Y}_p = \mathbf{Y}_f \mathbf{Y}_p^T (\mathbf{Y}_p \mathbf{Y}_p^T)^\dagger \mathbf{Y}_p, \quad (26)$$

301 which can be efficiently computed by the LQ factorization of the block Hankel matrix of the outputs. The main
 302 theorem of DATA-SSI states that the projection matrix \mathbf{P}_i can be factorized into the product of the observability
 303 matrix \mathbf{O}_i and the Kalman filter state sequence $\hat{\mathbf{S}}_i$:

$$\mathbf{P}_i = \mathbf{O}_i \hat{\mathbf{S}}_i, \quad (27)$$

304 where $\hat{\mathbf{S}}_i$ is a matrix containing Kalman filter estimates of the state vector at different time steps. Similarly, the
 305 projection matrix \mathbf{P}_{i-1} can be obtained as:

$$\begin{bmatrix} \mathbf{Y}_{0|i-1} \\ \mathbf{Y}_{i|i} \\ \vdots \\ \mathbf{Y}_{i+1|2i-1} \end{bmatrix} = \begin{bmatrix} \mathbf{Y}_{0|i} \\ \vdots \\ \mathbf{Y}_{i+1|2i-1} \end{bmatrix} = \begin{bmatrix} \mathbf{Y}_p^+ \\ \mathbf{Y}_f^- \end{bmatrix} \Leftrightarrow \mathbf{P}_{i-1} = \mathbf{Y}_f^- / \mathbf{Y}_p^+, \quad (28)$$

306 where \mathbf{Y}_p^+ is the past output with one extra block row, while \mathbf{Y}_f^- is the future output matrix without the first block
 307 row $\mathbf{Y}_{i|i}$. The observability matrix \mathbf{O}_i can be estimated from the SVD of matrix $\mathbf{W}_1 \mathbf{P}_i \mathbf{W}_2$:

$$\mathbf{W}_1 \mathbf{P}_i \mathbf{W}_2 = \begin{bmatrix} \mathbf{U}_1 & \mathbf{U}_2 \end{bmatrix} \begin{bmatrix} \mathbf{\Sigma}_1 & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{V}_1^T \\ \mathbf{V}_2^T \end{bmatrix} = \mathbf{U}_1 \mathbf{\Sigma}_1 \mathbf{U}_1^T \quad (29)$$

308 According to the Canonical Variate Analysis (CVA) method, the weighting matrices \mathbf{W}_1 and \mathbf{W}_2 take the form
 309 $\mathbf{W}_1 = ((1/j) \mathbf{Y}_f \mathbf{Y}_f^T)^{-1/2}$ and $\mathbf{W}_2 = \mathbf{I}$. Then, the observability matrix \mathbf{O}_i and the Kalman filter state sequence $\hat{\mathbf{S}}_i$
 310 can be computed as:

$$\begin{aligned} \mathbf{O}_i &= \mathbf{U}_1 \mathbf{\Sigma}_1^{1/2}, \\ \hat{\mathbf{S}}_i &= \mathbf{O}_i^\dagger \mathbf{P}_i. \end{aligned} \quad (30)$$

311 A similar factorization can be applied to \mathbf{P}_{i-1} :

$$\mathbf{P}_{i-1} = \mathbf{O}_i^\dagger \hat{\mathbf{S}}_{i-1} \Leftrightarrow \hat{\mathbf{S}}_{i+1} = (\mathbf{O}_i^\dagger)^\dagger \mathbf{P}_{i-1}, \quad (31)$$

312 where \mathbf{O}_i^\dagger can be directly obtained from \mathbf{O}_i by deleting the last l rows. Finally, the state-space matrices \mathbf{A} and \mathbf{C}
 313 are obtained in a least squares sense as [51]:

$$\begin{bmatrix} \mathbf{A} \\ \mathbf{C} \end{bmatrix} = \begin{bmatrix} \hat{\mathbf{S}}_{i+1} \\ \mathbf{Y}_{i|i} \end{bmatrix} \hat{\mathbf{S}}_i^\dagger. \quad (32)$$

3.3. Automated system identification

314 The current version of MOSS allows performing automated system identification using SSI. To do so, the code
 315 includes the automation procedure introduced in reference [24] and concisely overviewed herein. This comprises
 316 the following steps: (a) modal identification for different values i and j of the number of rows and columns of the
 317 Toeplitz/Hankel matrices, respectively; (b) noise modes elimination; and (c) clustering analysis.

(a) Iterative modal identification

318 A total number of N SSI analyses are performed considering values of j and i varying within certain user-
 319 defined intervals $[j_{min}, j_{max}]$ and $[i_{min}, i_{max}]$ and steps Δj and Δi , respectively. Specific rules for setting adequate
 320 values of i_{min} , i_{max} , j_{min} , j_{max} , Δi and Δj can be found in reference [24], and are included as default parameters
 321 in MOSS. This procedure results in a set of M poles, whose modal information can be organized in matrix
 322 form as:

$$\begin{aligned} \mathbf{f} &= [f_1 \ f_2 \ \dots \ f_M]^T, \\ \boldsymbol{\zeta} &= [\zeta_1 \ \zeta_2 \ \dots \ \zeta_M]^T, \\ \boldsymbol{\Theta} &= [\boldsymbol{\Theta}_1 \ \boldsymbol{\Theta}_2 \ \dots \ \boldsymbol{\Theta}_M], \end{aligned} \quad (33)$$

323 where f_m , ζ_m , and $\boldsymbol{\Theta}_m$ denote the frequency, damping, and mode shape vector of an arbitrary m -th mode,
 324 $m = 1, 2, \dots, M$.

327 (b) Noise modes elimination

328 Noise modes elimination is performed by a similar approach to the interpretation of stabilization diagrams,
329 but accounting for variations of both j and i . To discern between noise modes and physical ones, a vector
330 $\mathbf{c} = [c_1 \ c_2 \ \dots \ c_M]^T$ is computed with components c_m , $m = 1, 2, \dots, M$, given by:

$$c_m = \begin{cases} -1 + \sum_{l=1}^M \delta_{lm}, & \text{if } \zeta_m \in [0 \ \zeta_{max}] \\ 0, & \text{if } \zeta_m \notin [0 \ \zeta_{max}] \end{cases} \quad (34)$$

331 with

$$\delta_{lm} = \begin{cases} 1, & \text{if } \Delta f_{lm} \leq \epsilon_f, \Delta \zeta_{lm} \leq \epsilon_\zeta, 1 - MAC_{lm} \leq \epsilon_{MAC} \\ 0, & \text{otherwise} \end{cases} \quad (35)$$

$$\Delta f_{lm} = \frac{|f_l - f_m|}{f_m}, \Delta \zeta_{lm} = \frac{|\zeta_l - \zeta_m|}{\zeta_m}, MAC_{lm} = MAC(\Theta_l, \Theta_m),$$

332 where ζ_{max} is the maximum reasonable value for the damping ratio of the physical modes ($\approx 5\text{-}10\%$ depending
333 on the structural typology), $MAC(\Theta_l, \Theta_m)$ is the MAC value between modes Θ_l and Θ_m , and ϵ_f , ϵ_ζ , and ϵ_{MAC}
334 are user-defined tolerances. An arbitrary component c_m represents the number of modes, among all the M
335 identified ones, which have similar modal features to those of the m -th mode. Therefore, the m -th mode is said
336 to be stable when it is similar in terms of frequency, damping, and mode shape to a minimum number N_{min}
337 of other modes, i.e. $c_m \geq N_{min}$. A value of $N_{min} = N/10$ is selected as a compromise for eliminating most of
338 the noise modes without cancelling the physical ones [24]. Then, the number of stable poles can be readily
339 obtained computing a vector \mathbf{S} :

$$\mathbf{S} = [S_1 \ S_2 \ \dots \ S_M]^T, \quad (36)$$

$$S_m = \begin{cases} 1, & \text{if } c_m \geq N_{min} \\ 0, & \text{otherwise} \end{cases}$$

340 whose components assign 0 and 1 to unstable and stable modes, respectively. Hence, the total number of stable
341 modes, P , simply reads $P = \sum_{l=1}^M S_l$. The vectors of stable frequencies \mathbf{f}^s and damping ratios ζ^s , and the matrix
342 of stable mode shapes Θ^s can be extracted as:

$$\mathbf{f}^s = \mathbf{H}\mathbf{E}\mathbf{f} = [f_1 \ f_2 \ \dots \ f_P]^T, \quad (37)$$

$$\zeta^s = \mathbf{H}\mathbf{E}\zeta = [\zeta_1 \ \zeta_2 \ \dots \ \zeta_P]^T,$$

$$\Theta^s = (\mathbf{H}\mathbf{E}\Theta^T)^T = [\Theta_1 \ \Theta_2 \ \dots \ \Theta_P],$$

343 where $\mathbf{H}\mathbf{E}$ is a $P \times M$ matrix whose non-zero components are $H\mathbf{E}_{p,\pi_p} = 1$, $p = 1, 2, \dots, P$, with $\pi_1, \pi_2, \dots, \pi_p$
344 being the positions of the non-zero terms of vector \mathbf{S} .

345 (c) Clustering analysis

346 An agglomerate hierarchical clustering algorithm is implemented to automate the interpretation of the SSI
347 outputs from the previous steps. Such an analysis is aimed at grouping the P stable modes into a set of homog-
348 enous data clusters pertaining to the same structural mode. The algorithm starts by generating a permutation
349 vector $\mathbf{v} = [v_1, v_2, \dots, v_P]^T$, containing the elements of vector $\mathbf{p} = [1, 2, \dots, P]^T$ in a random order. There
350 follows an iterative procedure composed of P steps sketched in Fig. 6. At the first step, the v_1 -th mode is
351 considered as the first cluster seed $C_1^1 = \{v_1\}$, where C_1^1 represents cluster C_1 evaluated at step number 1 (su-
352 perscript 1). The next $P - 1$ steps work in a similar way. Let us focus on a generic q -th step, at which a certain
353 number r of clusters will already exist. In order to compare the v_q -th mode and a cluster C_j , $j \in [1, \dots, r]$, a
354 similarity rule is defined as:

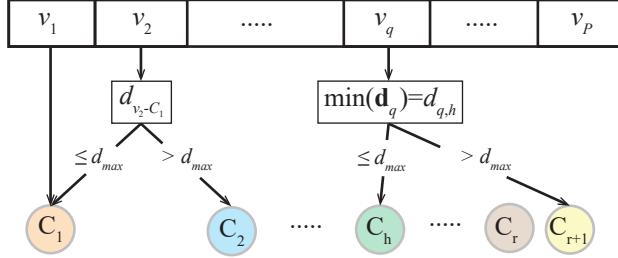


Figure 6: Graphical sketch of the hierarchical clustering approach.

$$d_{v_q-C_j} = \frac{|f_{v_q}^s - \bar{f}_{C_j}|}{\bar{f}_{C_j}} + 1 + MAC(\Theta_{v_q}^s, \bar{\Theta}_{C_j}), \quad (38)$$

where \bar{f}_{C_j} and $\bar{\Theta}_{C_j}$ denote the mean values of the frequencies and mode shapes of the poles composing cluster C_j , respectively, while $f_{v_q}^s$ and $\Theta_{v_q}^s$ are the frequency and the mode shape of the v_q -th mode, respectively. Then, the similarities between the v_q -th mode and the r clusters are arranged in a similarity vector \mathbf{d}_q as:

$$\mathbf{d}_q = [d_{v_q-C_1}, d_{v_q-C_2}, \dots, d_{v_q-C_r}]^T, \quad (39)$$

and the following rule is applied:

$$\begin{aligned} \text{if } d_{q,h} = \min(\mathbf{d}_q) \leq d_{max} \Rightarrow C_h^q = C_h^{q-1} \cup \{v_q\}, \\ \text{if } d_{q,h} = \min(\mathbf{d}_q) > d_{max} \Rightarrow C_h^q = C_h^{q-1}, C_{r+1}^1 = \{v_q\}, \end{aligned} \quad (40)$$

meaning that the v_q -th mode is assigned to cluster C_h (which is the closest one in terms of frequency and mode shape) if the similarity value $d_{q,h}$ is smaller than an user-defined threshold d_{max} ; otherwise a new cluster C_{r+1} is created containing the v_q -th mode. At the end of the procedure, a certain number nc of clusters defined by their centroids (average value of frequencies, damping ratios, and mode shapes) and cluster sizes (number of poles contained within the clusters) are obtained, and a minimum cluster size can be defined to disregard all those that are not populated enough to be considered as representative samples.

3.4. Damage detection

By applying the automated system identification procedure previously outlined in Section 3.3 to every measurement data, it is possible to obtain the time series of modal features of the structure. Such a process, often called “Frequency tracking”, is performed by tracking a reference set of resonant frequencies (typically obtained from an initial AVT) over the dataset of identified modal features. To do so, the poles of every dataset whose frequency values come closest to the reference ones (complying with a user-defined maximum relative tolerance and a minimum MAC value between the corresponding mode shapes) are collected in an observation matrix $\mathbf{Y} \in \mathbb{R}^{n \times N}$, where n is the number of identified frequencies and N is the number of observations. Then, any change in the dynamic behaviour of the structure, possibly related to developing damage, can be detected by the application of statistical process control tools to \mathbf{Y} . Nevertheless, as stated earlier in Section 1, environmental/operational factors usually mask the effects of early-stage damage and need to be removed. Therefore, damage detection typically comprises the following two steps: (a) removal of environmental effects, and (b) novelty analysis. Additionally, (c) automated anomaly detection algorithms can be implemented for online damage detection. The implementation of these steps within MOSS is briefly outlined hereafter.

3.4.1. Removal of environmental effects: regression models

Given the masking effects of environmental/operational factors on modal frequencies, the quantities contained in \mathbf{Y} cannot be directly used as damage-sensitive features. Instead, a proper residual error matrix, $\mathbf{E} \in \mathbb{R}^{n \times N}$, is used for this purpose and computed as:

$$\mathbf{E} = \mathbf{Y} - \widehat{\mathbf{Y}}, \quad (41)$$

383 where $\widehat{\mathbf{Y}}$ contains predictions of the time series of resonant frequencies computed from a baseline in-control
 384 population. This in-control population, usually referred to as the *training period*, contains a set of identified
 385 modal features that statistically represent the healthy condition of the structure. This must be long enough to
 386 cover the full range of environmental conditions (both daily and seasonal fluctuations), and typically a one-year
 387 period is assumed adequate. MOSS includes six different regression models to construct $\widehat{\mathbf{Y}}$, three input-output
 388 models and three input-only models, namely:

- 389 • Input-Output regression models: Multiple Linear Regression (MLR), AutoRegressive with eXogenous input
 390 model (ARX), and coupled MLR and Principal Component Analysis (MLR/PCA).
- 391 • Input-only regression models: Principal Component Analysis (PCA), Factor Analysis (FA), and Autoassociative
 392 Neural Networks (ANN).

393 In addition, MOSS also includes a Gaussian Mixture Model (GMM) for clustering analysis and detection of
 394 freezing conditions. Because of space constraints, the theoretical description of each of these models is omitted in
 395 this paper, and interested readers may refer to references [52, 53].

396 Under the assumption that $\widehat{\mathbf{Y}}$ reproduces the part of the variance of the resonant frequencies corresponding to
 397 changes in environmental/operational conditions, \mathbf{E} only contains the residual variance stemming from identifica-
 398 tion errors and un-modelled environmental/operational effects. If certain damage develops, this only affects the
 399 data contained in \mathbf{Y} , while $\widehat{\mathbf{Y}}$ remains unaltered. Therefore, \mathbf{E} concentrates the damage-induced variance apt for
 400 being used for damage detection purposes.

401 3.4.2. Novelty analysis

402 Once the residual error matrix \mathbf{E} is computed, the presence of damage is investigated using control charts as
 403 sketched in Fig. 7. These furnish in time a certain statistical distance accounting for disturbances in the distribution
 404 of the residuals contained in \mathbf{E} . By defining an in-control region, the appearance of out-of-control processes, pos-
 405 sibly associated to damage, is detected in the shape of data points violating the in-control region. MOSS includes
 406 three different control charts that are overviewed hereafter, namely the Hotelling, Multivariate Cumulative Sum
 407 (MCUSUM), and Multivariate Exponentially Weighted Moving Average (MEWMA) control charts. The statisti-
 408 cal distances assessed by these control charts are positive by definition, so the in-control region is defined by an
 409 interval $[0, UCL]$. The upper control limit (UCL) is computed as the value of the statistical distance corresponding
 410 to a certain confidence level α for the distribution of data within the training population.

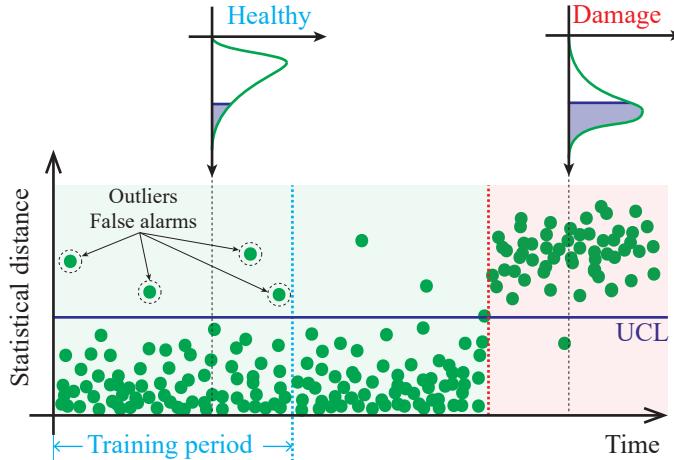


Figure 7: Control chart of a permanent SHM system.

- 411 • **Hotelling's T^2 :** The Hotelling's T^2 control chart [54] is defined as:

$$412 T_i^2 = r \left(\bar{\mathbf{E}} - \bar{\bar{\mathbf{E}}} \right)^T \Sigma_0^{-1} \left(\bar{\mathbf{E}} - \bar{\bar{\mathbf{E}}} \right), i = 1, 2, \dots, N/r, \quad (42)$$

413 where r is an integer parameter referred to as subgroup size, $\bar{\mathbf{E}}$ is the mean of the residuals in the subgroup
 414 of the last r observations, while $\bar{\bar{\mathbf{E}}}$ and Σ_0 are the mean values and the covariance matrix of the residuals
 415 statistically estimated in the training period.

- 415 • *Multivariate Cumulative Sum (MCUSUM)*: This control chart appears as an improvement of the sensitivity
 416 of the T^2 control chart to detect small shifts in the mean of the statistical process, and it is based upon
 417 the principle of accumulating information of past observations. Among the different versions of this control
 418 chart that can be found in the literature, MOSS includes one of the most commonly used MCUSUM methods
 419 proposed by Crosier [55] as:

$$CUSUM_i = \left(r \mathbf{S}_i^T \Sigma_0^{-1} \mathbf{S}_i \right)^{1/2}, \quad i = 1, 2, \dots, N/r, \quad (43)$$

420 with

$$\begin{aligned} C_i &= \left[r \left(\mathbf{S}_{i-1} + \bar{\mathbf{E}} - \bar{\bar{\mathbf{E}}} \right)^T \Sigma_0^{-1} \left(\mathbf{S}_{i-1} + \bar{\mathbf{E}} - \bar{\bar{\mathbf{E}}} \right) \right]^{1/2}, \\ \mathbf{S}_0 &= \mathbf{0}, \\ \mathbf{S}_i &= \begin{cases} \mathbf{0}, & \text{if } C_i \leq k, \\ \left(\mathbf{S}_{i-1} + \bar{\mathbf{E}} - \bar{\bar{\mathbf{E}}} \right) (1 - k/C_i), & \text{if } C_i > k, \end{cases} \end{aligned} \quad (44)$$

421 where k is a constant parameter. Specific expressions for setting k can be found in reference [55]. MOSS
 422 imposes a default value of $k = 0.5$.

- 423 • *Multivariate Exponentially Weighted Average (MEWMA)*: Originally proposed by Lowry *et al.* [56],
 424 the MEWMA control chart represents an intermediate solution between the T^2 and the MCUSUM control
 425 charts. Alike the MCUSUM control chart, the MEWMA method also accounts for the information from
 426 past observations, although it gives weights decreasing in a geometric progression from the most recent
 427 observation to the first one. The statistical distance used in the MEWMA control chart reads:

$$MEWMA_i = \left(r \mathbf{z}_i^T \Sigma_{z_i}^{-1} \mathbf{z}_i \right)^{1/2}, \quad i = 1, 2, \dots, N/r, \quad (45)$$

428 with

$$\begin{aligned} \mathbf{z}_i &= \lambda \left(\bar{\mathbf{E}} - \bar{\bar{\mathbf{E}}} \right) + (1 - \lambda) \mathbf{z}_{i-1}, \\ \Sigma_{z_i} &= \lambda \frac{1 - (1 - \lambda)^{2i}}{2 - \lambda} \Sigma_0, \end{aligned} \quad (46)$$

429 where λ is a smoothing constant with $0 \leq \lambda \leq 1$. Practically, the most often used value of λ is 0.1.

430 3.4.3. Automated damage detection

431 An alarm system based upon the detection of outliers in the control chart would result in an excessive number
 432 of false alarms. Note that the control limit UCL is defined for a certain confidence level α , so such a system would
 433 signal a proportion of $1 - \alpha$ alerts even when the structure remains in healthy condition (see Fig. 7). Therefore,
 434 it is necessary to implement a detection algorithm based upon variations in the statistical distribution of statistical
 435 distances. To do so, MOSS implements a simple but efficient approach based upon the pruned exact linear time
 436 (PELT) method proposed by Killick and co-authors [57]. This algorithm searches for a change-point or time
 437 instant at which some statistical property of a signal changes abruptly. In particular, we focus on the detection of
 438 mean shifts in the time series of residuals in \mathbf{E} . Considering a certain row of the error residual matrix \mathbf{E} as a signal
 439 x_1, x_2, \dots, x_N , the algorithm finds a position cp in a time series that minimizes the following cost function:

$$J = \sum_{i=1}^{cp-1} \left(x_i - \frac{1}{cp-1} \sum_{r=1}^{cp-1} x_r \right)^2 + \sum_{i=cp}^N \left(x_i - \frac{1}{N-cp+1} \sum_{r=cp}^N x_r \right)^2 \quad (47)$$

440 To do so, the PELT algorithm iteratively segments the time series until finding the optimal solution. Through
 441 the use of dynamic programming and pruning, it can be proved that the computational cost of the PELT method is
 442 linear in the number of data points. For more specific information about the implementation of the PELT method,
 443 readers may refer to reference [57].

444 In this light, an automatic damage detection algorithm is implemented in MOSS based upon the PELT method.
 445 This is automatically launched every time the code finds a new data file and computes a new column of \mathbf{E} . The
 446 position of the change-points detected by the PELT method is arranged in a matrix $\mathbf{P} \in \mathbb{R}^{n \times N}$, and the number of
 447 repetitions (i.e. number of consecutive times that the PELT algorithm finds the same change-point) are collected
 448 in a vector $\mathbf{N} \in \mathbb{R}^n$. When a change-point is detected within the training period t_p , a zero value is assigned to the
 449 corresponding position in \mathbf{P} . The algorithm stops and signals an alarm when any of the elements of \mathbf{N} reaches
 450 an user-defined maximum number of repetitions cp_{max} . For clarity, the algorithm is illustrated in the following
 451 pseudo-code:

Algorithm 1 Pseudo-code for online damage detection using the PELT method.

```

1: for  $i \leftarrow 1, n$  do
2:   PELT method  $\leftarrow cp_i$ 
3:   if  $cp_i \leq t_p$  then
4:      $\mathbf{P}_{N+1,i} = 0$ 
5:   else
6:      $\mathbf{P}_{N+1,i} = cp_i$ 
7:   if  $\mathbf{P}_{N+1,i} = \mathbf{P}_{N,i}$  then
8:      $\mathbf{N}_i = \mathbf{N}_i + 1$ 
9:   else
10:     $\mathbf{N}_i = 0$ 
11: if  $\max(\mathbf{N}) = cp_{max}$  then
12:   Signal alarm
  
```

452 **4. MOVA/MOSS description and application case study**

453 The overarching purpose of MOSS is the fully autonomous management of permanent integrated SHM systems.
 454 Typically, the work-flow of an SHM system using MOSS is sketched in Fig. 8. The monitoring system
 455 consists of an integrated sensor network deployed on the structure of interest, and of an in-place DAQ system that
 456 permanently collects the monitoring data. Subsequently, computer files containing monitoring records of certain
 457 time duration are sent through the internet or another data transmission system to a server or to the cloud where the
 458 data are stored. Here MOSS automatically processes all the monitoring records and updates user-defined control
 459 charts. To do so, it distinguishes between dynamic measurements and measurement data of different nature (e.g.
 460 temperature sensors, strain gauges, or inclinometers). On one hand, MOSS performs automated OMA using the
 461 ambient vibration records according to the methodology previously introduced in Section 3.3. This process com-
 462 prises five sequential steps, namely (i) pre-processing of measurement records according to certain user-defined
 463 filtering process; (ii) automated OMA; (iii) frequency tracking; (iv) elimination of environmental effects through
 464 pattern recognition techniques; and (v) control charts and online anomaly detection. In parallel, MOSS processes
 465 the rest of measurement data and performs data fusion. Specifically, the user can freely decide to use these extra
 466 monitoring data as predictors and/or estimators. That is to say, non-dynamic monitoring data can be used to filter
 467 out the environmental effects over the resonant frequencies or, alternatively, they can be used as damage-sensitive
 468 features. In the latter case, anomalies in their time series are investigated likewise vibration data through con-
 469 trol charts. Therefore, MOSS permits the definition of multiple control charts and performs simultaneous online
 470 damage detection of diverse damage-sensitive features.

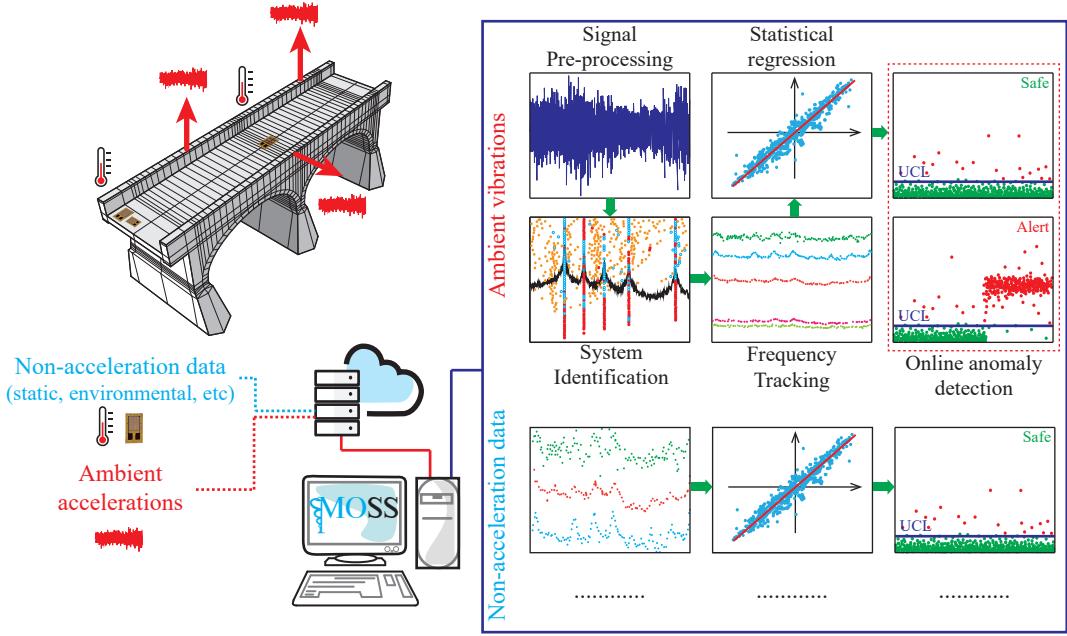


Figure 8: Schematic of a permanent SHM system using MOSS.

The main GUI of MOSS is shown in Fig. 9. The interface is organized in four consecutive steps:

- 471 The main GUI of MOSS is shown in Fig. 9. The interface is organized in four consecutive steps:
- 472 I **System Identification:** This step encompasses the main capabilities of MOVA for AVT, and has the purpose
473 of defining the geometry of the structure and the signal processing procedure used for all the measurement
474 records. This includes the following sub-sections: *GEOMETRY*, *SIGNAL PRE-PROCESSING*, *SYSTEM*
475 *IDENTIFICATION*, and *Extra monitoring variables*. The latter allows the user to introduce as many non-
476 dynamic sensors as desired by providing a reference label, the measurement unit, and the computer folder
477 that contains the record files.
- 478 II **Process of initial data set:** This step includes the sub-section named *Process initial data set* and generates
479 an initial data population of modal features to be used in the subsequent steps. The initial dataset of mea-
480 surements (preferably those corresponding to the training period) along with the results folders (including
481 the processed signals and the identification results) are introduced through the file manager located in the
482 left part of the interface.
- 483 III **Frequency tracking and elimination of environmental effects:** This comprises the sub-sections named
484 *FREQUENCY TRACKING* and *MULTIVARIATE STAT. ANAL. (MSA)*, and it is devoted to defining the
485 parameters for automated frequency tracking and the statistical models used for pattern recognition. Ad-
486 ditionally, an extra module (*SURROGATE MODEL*) for damage identification (i.e. detection, localization,
487 and quantification) by means of surrogate-based model updating is anticipated for future releases.
- 488 IV **Damage detection:** This last step constitutes the core of MOSS, and performs the online damage detection
489 of the previously defined damage-sensitive features. It includes the sub-sections indicated as *Continuous*
490 *SHM* and *Damage simulation*. The latter allows the user to explore the effects of artificial damage upon the
491 constructed control models.

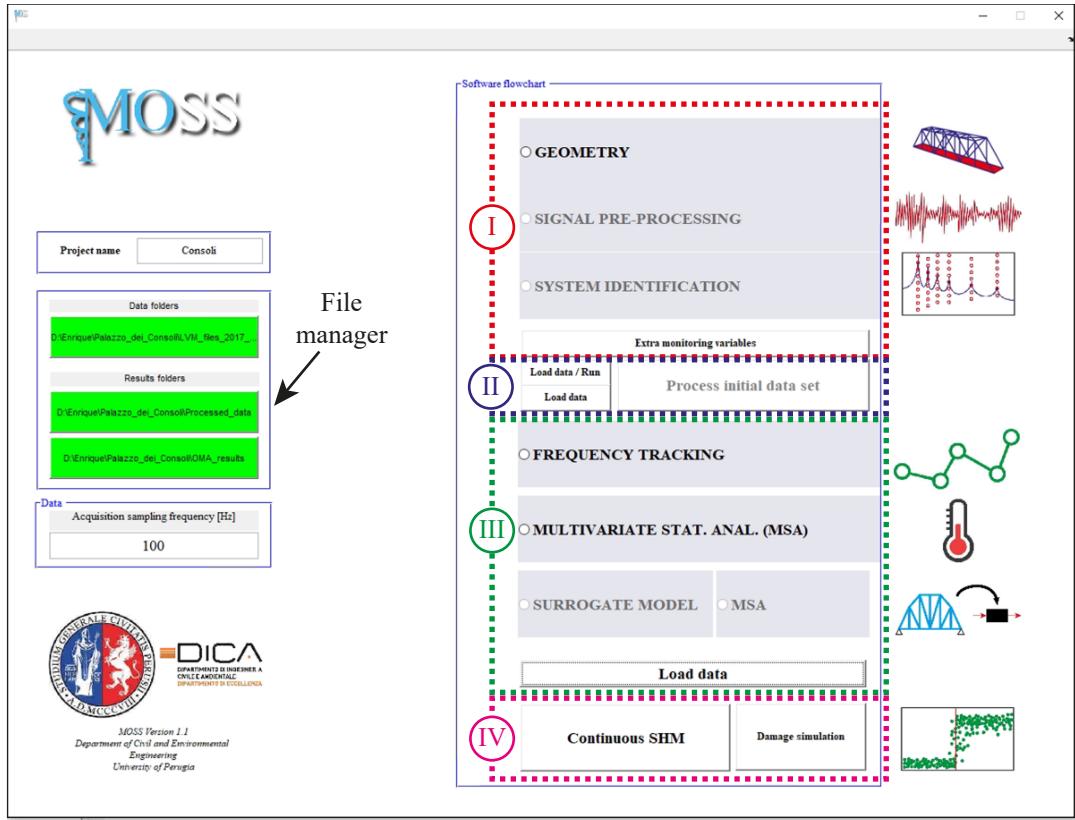


Figure 9: MOSS main GUI.

492 **Geometry module:** This interface allows the definition of a geometrical model and the accelerometer layout
 493 for the representation of the mode shapes. Three-dimensional models can be constructed using nodes, lines, and
 494 planes, as well as kinematic conditions between active and slave nodes. Every active node is defined at least
 495 by a measurement channel and the corresponding direction/orientation ($\pm x$, $\pm y$, or $\pm z$). Kinematic conditions
 496 include rigid-plane diaphragms and link conditions between slave and active nodes. Additionally, the interface
 497 incorporates a formula editor allowing for inserting general symbolic constraints between sets of nodes. The
 498 whole process can be carried out graphically using the mouse, manually by typing the information directly in
 499 the edit tables, or by loading a geometry file in ASCII format. Figure 10 (a) shows the geometrical model built
 500 for the AVT of the Consoli Palace previously described in Fig. 1. The model includes 9 acceleration channels
 501 and rigid-plane diaphragms at each floor of the building. For illustrative purposes, Fig. 10 (b) shows two sample
 502 geometries defined for a bridge structure and a tower.

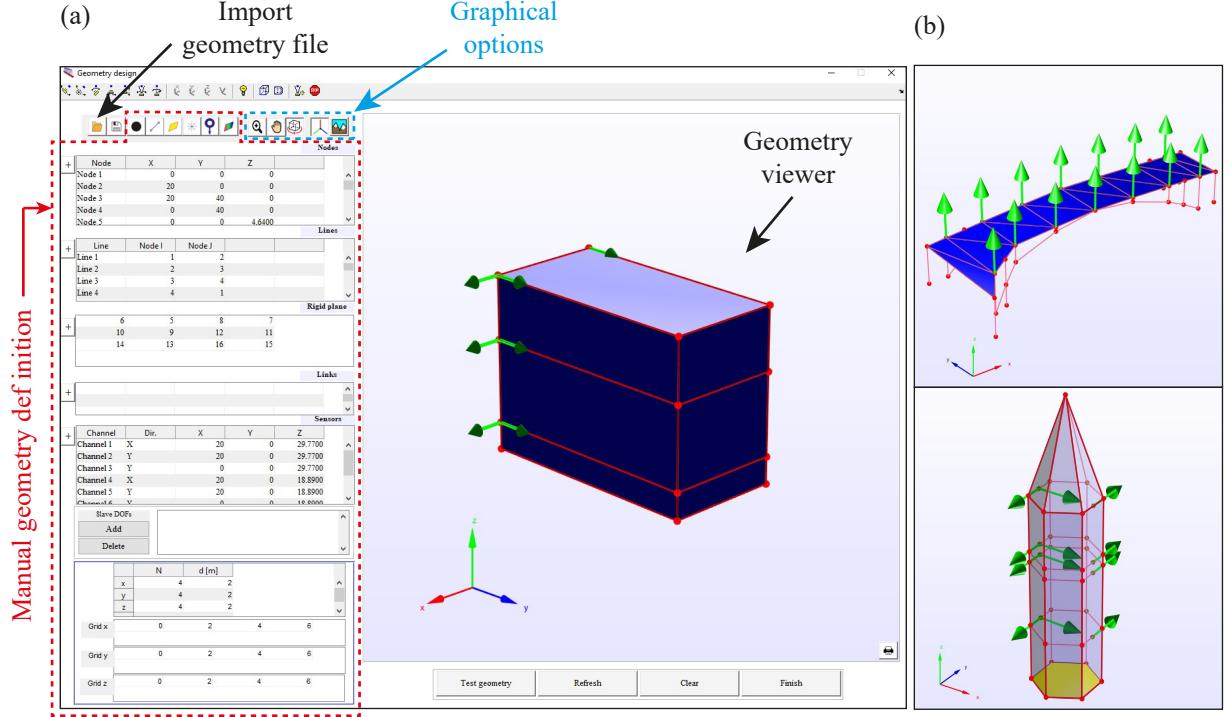


Figure 10: Screenshot of the geometry module: (a) Consoli Palace, (b) reinforced-concrete bridge and masonry tower.

503 **Signal pre-processing module:** This module, shown in Fig. 11 (a), permits the definition of signal processing
 504 sequences to minimize the effects of noise and the presence of abnormal events. Specifically, the software
 505 interface includes: signal downsampling, moving average filtering, linear detrend, band-pass filtering, Hanning
 506 window filtering of signal spikes, Hanning window filtering of non-stationary excitations produced by swing-
 507 ing bells (common in CH structures), and a robust Multichannel Singular Spectrum Analysis (MSSA) denoising
 508 approach [58]. The software accounts for the application order of the selected filtering techniques, and the graph-
 509 ical representation of the filtered signals against the raw ones enables users to check the effectiveness of the
 510 implemented signal processing sequence. The comparison can be performed in the time domain, through PSDs,
 511 time-frequency analysis, and SVs of the PSDs (see Fig. 11 (b)). Specifically, Fig. 11 presents the pre-processing of
 512 the accelerations recorded during the AVT of the Consoli Palace conducted on May 4th 2017. In this case, ambient
 513 vibration data were collected during 30 min at a sampling frequency of 1652 Hz. The raw signals evidence the
 514 strong effect of the swinging bells located in the bell-tower of the palace, which ring regularly every 15 minutes.
 515 In order to minimize these effects and improve the system identification, the selected signal processing sequence
 516 includes: downsampling to 40 Hz, linear de-trend, moving average filtering with time window length of 200 s, and
 517 Hanning window filtering to eliminate the effect of swinging bells and signal spikes. Note that the swinging of
 518 bells induces a significant violation of the white noise assumption and must be filtered out before conducting the
 519 system identification. The implemented time-domain Hanning window filter suppress those parts of the signals
 520 affected by swinging bells, in such a way that the resulting signals do comply with the white noise assumptions.

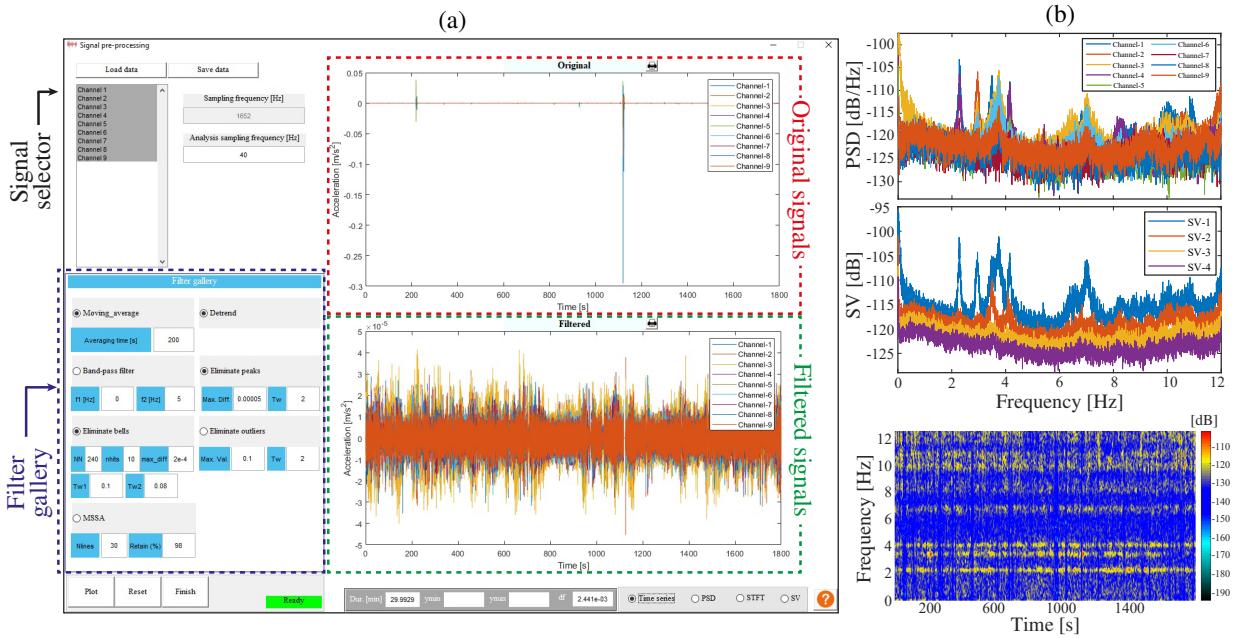


Figure 11: Screenshot of the signal pre-processing module (a), and analyses of the filtered signals (b).

521 **System identification module:** This interface manages the vibration-based identification of the structure. Here
 522 the user can select any of the identification techniques previously introduced in Section 3. The identification
 523 results are presented in the shape of tabulated data, stabilization diagrams (SSI and p-LSCF), or SVs of the PSDs
 524 (EFDD), exportable reports, and the histogram representation of the MAC matrix. Moreover, this interface counts
 525 on a specific section for mode shape representation, including the animation of complex modes, complexity plots,
 526 and display of quality factors such as the Mode Complexity Factor (MCF), Mode Phase Collinearity (MPC), and
 527 Mean Phase Deviation (MPD). As an example, Fig. 12 (a) shows a screenshot of this module with the identification
 528 results obtained with the AVT of the Consoli Palace using COV-SSI, and Fig. 12 (b) shows a screenshot of the
 529 mode shape representation interface with the analysis of the first vibration mode.

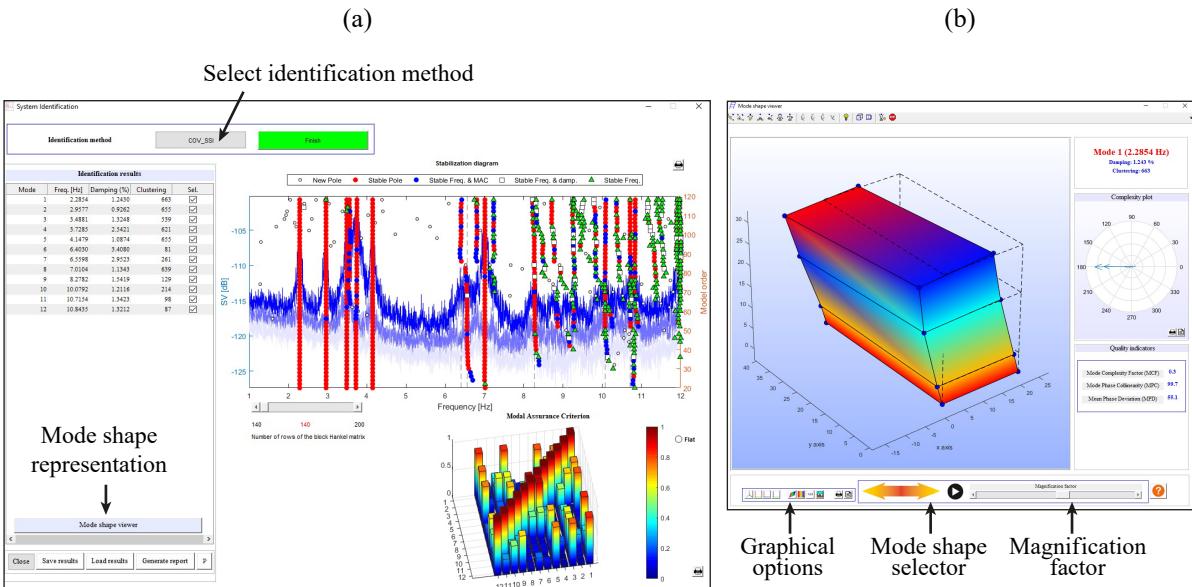


Figure 12: Screenshots of the system identification module (a) and mode shape viewer (b).

530 This module has been utilised for the system identification of the Consoli Palace using the ambient acceleration
 531 data collected during the AVT and formerly processed in the signal pre-processing module. The identification
 532 results using all the available methods in MOSS are presented in Table 1. As reported earlier, six clear modes

533 are identified in the frequency range from 0 to 12 Hz. These correspond to two global first bending modes in the
 534 x - and y -directions, denoted as Fx1 and Fy1, respectively, one global torsional mode, T1, and three local modes
 535 related to the interaction between the palace and the bell-tower, denoted as L1, L2, and L3. The global mode
 536 shapes obtained using COV-SSI in MOSS are depicted in Fig. 13. It is noted that very similar resonant frequency
 537 estimates are obtained by all the different identification methods, while large differences are found in terms of
 538 damping ratios. The quality of damping estimates is highly dependent on the level of excitation of the structure,
 539 which is often quite low in CH structures in operational conditions. This is specially critical in this case study,
 540 where ambient accelerations in the palace did not exceed $1.5E-3$ m/s 2 , so substantial uncertainties are expected to
 541 arise in the determination of damping properties.

Table 1: Vibration-based system identification results of the Consoli Palace through the AVT conducted on May 4th 2017 using the EFDD, p-LSCF, COV-SSI, and DATA-SSI methods in MOSS.

Mode	Natural frequencies [Hz]				Damping ratios [%]			
	EFDD	p-LSCF	COV-SSI	DATA-SSI	EFDD	p-LSCF	COV-SSI	DATA-SSI
Fx1	2.270	2.296	2.285	2.287	1.471	0.561	1.243	1.383
Fy1	2.953	2.970	2.958	2.961	0.361	0.166	0.926	1.017
L1	3.479	3.463	3.488	3.492	0.247	0.118	1.325	1.387
L2	3.740	3.723	3.729	3.717	0.352	1.767	2.542	2.824
T1	4.153	4.124	4.148	4.150	0.303	0.423	1.087	1.226
L3	6.986	7.016	7.010	7.008	0.138	0.549	1.134	1.121

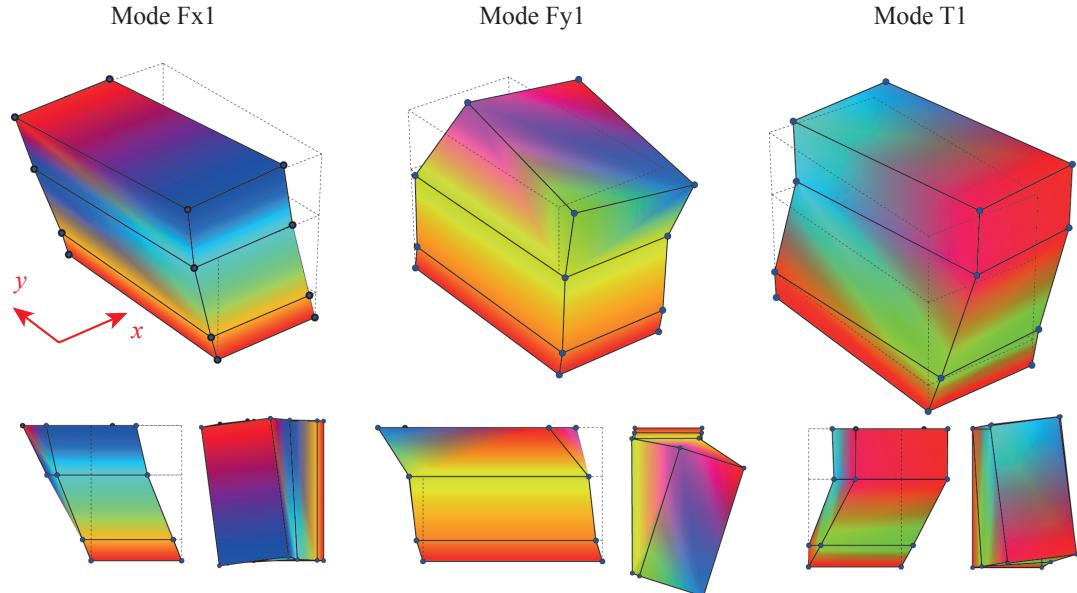


Figure 13: Global mode shapes, first bending modes Fx1 and Fy1 and torsional mode T1, obtained from the AVT of the Consoli Palace using COV-SSI.

542 **Frequency tracking module:** Once the initial data population has been processed, this module allows to
 543 extract the time series of resonant frequencies, damping ratios, and mode shapes of the structure. To do so,
 544 the user must introduce a reference set of frequencies (typically retrieved from an AVT using a relatively large
 545 set of sensors) and a set of tolerances on allowable maximum relative frequency variations and minimum MAC
 546 values. Figure 14 shows a screenshot of this interface with the results obtained from the long-term monitoring
 547 of the Consoli Palace. The vibration-based identification of the palace was conducted using COV-SSI according
 548 to the automation procedure previously presented in Section 3.3. In this case, only five modes corresponding to
 549 Fx1, Fy1, L1, T1, and L3 were tracked, while Mode L2 was disregarded because of difficulties in its separation
 550 from modes L1 and T1. This is due to the reduced number of sensors used in the monitoring (only 3), what
 551 hinders the discrimination of very closely spaced modes by means of MAC comparison. Special attention must
 552 be also devoted to the potential occurrence of freezing conditions. Typically, freezing air temperatures induce
 553 the formation of ice crystals in the micro porosity of mortar joints in masonry structures leading to an overall

stiffening effect and, as a result, the natural frequencies experience substantial increases [18, 59]. Specifically, freezing conditions are clearly visible in the time series of the resonant frequencies of the Consoli Palace in Fig. 14 during the time period from February 25th to March 1st 2017. In order to automatically detect such conditions, the frequency tracking interface counts on a specific section for that purpose. This section incorporates a gradient-based detection algorithm that allows to identify data regions of certain time length (336 h in the example of Fig. 14 and marked with black dashed lines) with sudden increases in the resonant frequencies. Once detected, the user can introduce new tolerance values for performing local frequency tracking over these regions. Afterwards, freezing conditions can be tackled in two different ways: using clustering analysis and setting different statistical regression techniques as illustrated later, or directly dismissing the identification results corresponding to the detected regions. The latter approach is acceptable when freezing conditions only occur during short periods of time.

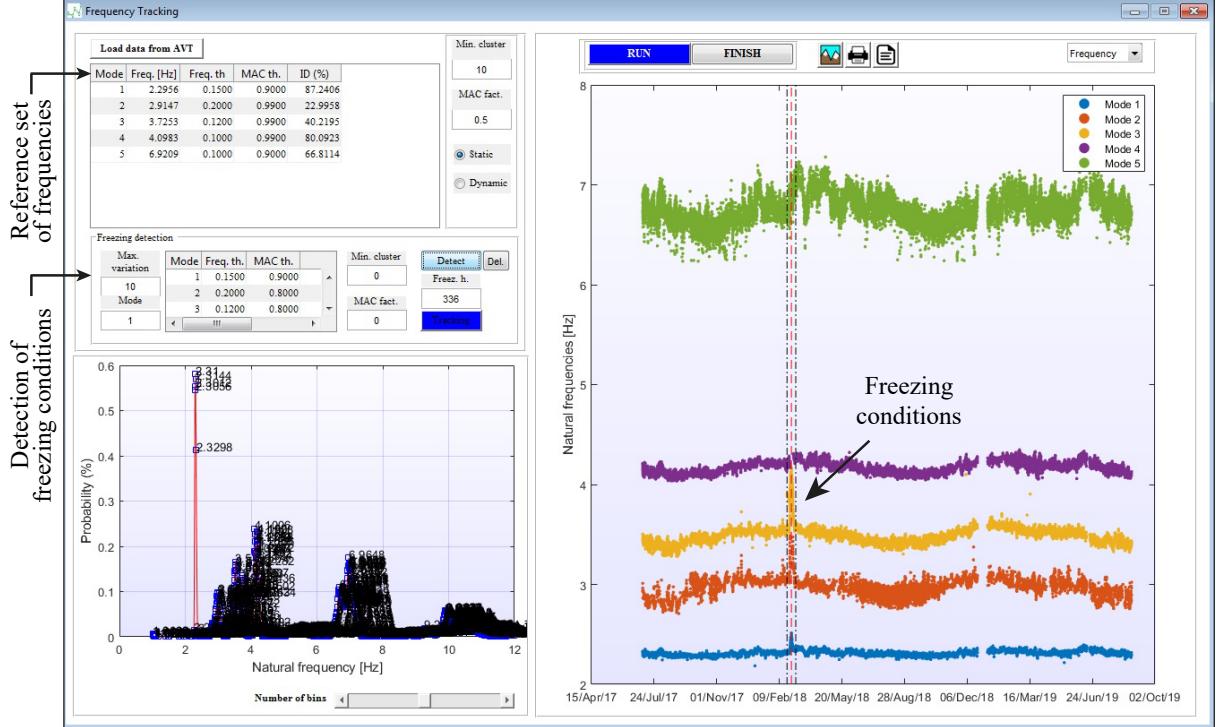


Figure 14: Screenshot of the frequency tracking module with identification results of the permanent SHM system installed in the Consoli Palace.

Multivariate statistical analysis module: This module, shown in Fig. 15, permits the definition of different statistical models accounting for distinct damage-sensitive features. Every model, identified by an user-defined label name, is assessed through statistical pattern recognition in the subsequent damage identification module. Specifically, this interface includes the following features:

- Outliers elimination:** Outliers represent anomalous data points arising as a result of identification and/or tracking errors. Their presence in the time series of damage-sensitive features may drastically reduce the effectiveness of regression models for the elimination of environmental effects, and it can grossly distort the computation of the mean and covariance matrices used later for statistical process control. With the aim of reducing the number of outliers in the training period (when the structure is assumed to be in the healthy state), this interface includes the PCA-based methodology for outliers elimination proposed by Wah *et al.* [60].
- Filling of missing data:** A very common situation in vibration-based SHM concerns the incomplete identification of the dynamic features in the frequency range of interest. This may be due to tracking errors or to low or anomalous excitation conditions precluding the identification algorithm to find some of the modes of vibration. This results into missing data in the observation matrix. To solve this issue, this module includes three different filling methods: linear interpolation, autoregressive modelling, and a PCA-based algorithm for filling data gaps.

- 582 • **Clustering analysis:** The interface incorporates a GMM for detection of freezing conditions. In particular,
 583 the algorithm classifies the damage-sensitive features into two separate groups of dissimilar variance. Then,
 584 different regression methods can be built for each data cluster and so remove the environmental effects in a
 585 more effective manner.
- 586 • **Estimators/Predictors definition:** Every statistical model is defined by a set of estimators (independent
 587 variables) and predictors (dependent variables). The user can freely select as estimators and/or predictors
 588 the resonant frequencies, damping ratios, max/min acceleration values, and acceleration root-mean-squares
 589 (RMS), as well as the mean, max/min, and standard deviation values of the non-dynamic measurements.
 590 Additionally, the interface incorporates a *variable calculator* that allows to define new estimators/predictors
 591 by typing general mathematical expressions involving different variables. This includes the possibility of
 592 adding time delays in certain parameters to build dynamic regression models, that is to say, models account-
 593 ing for past observations of certain predictors to account for thermal capacitance effects (e.g. the dynamics
 594 of heating up and cooling down processes).
- 595 • **Build of statistical models:** The user can select among six different regression models, including output-
 596 only (PCA, FA, and AANN) and input-only models (MLR, ARX, and MLR/PCA).

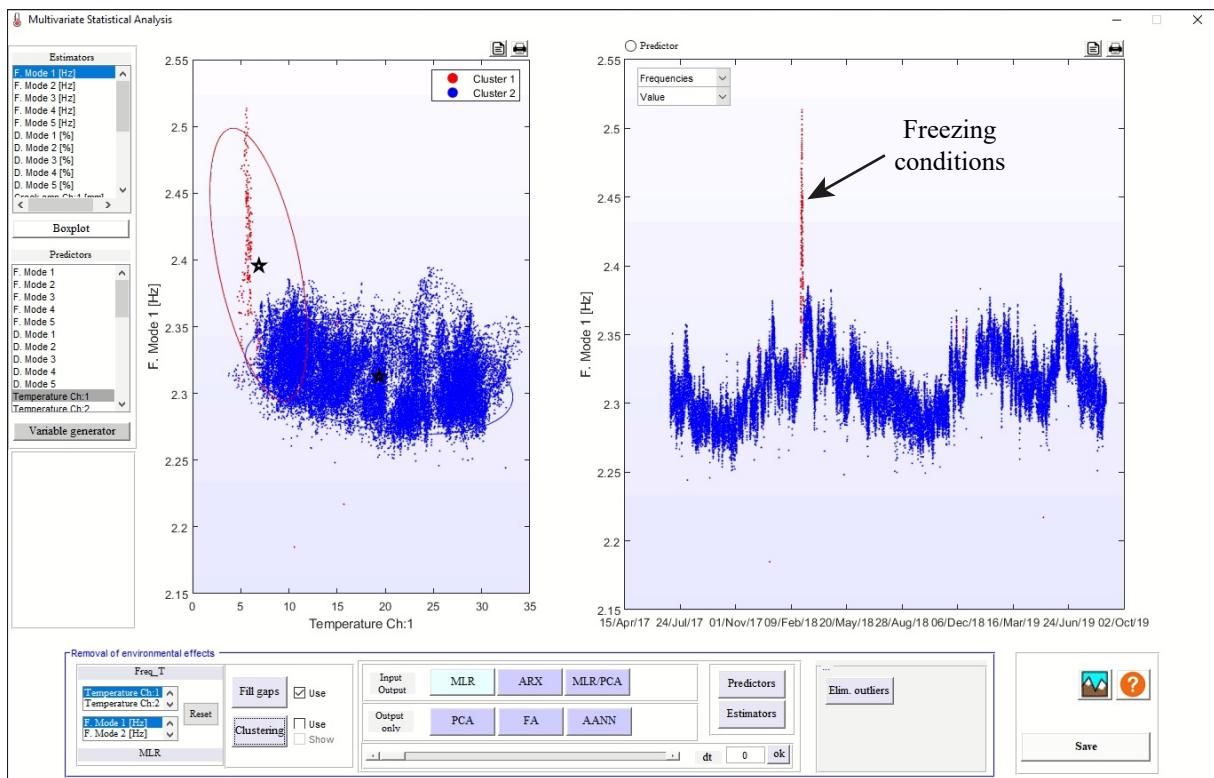


Figure 15: Screenshot of the multivariate statistical analysis module with the clustering results of the resonant frequencies of the Consoli Palace identified during the first year of monitoring.

597 The results in Fig. 15 show the application of GMM clustering for identification of freezing conditions in the
 598 case study of the Consoli Palace. It is noted that the sudden increase of natural frequencies induced by freezing
 599 conditions can be accurately detected by the model. Then, different statistical models can be applied to eliminate
 600 the environmental effects in each of the identified clusters. Nevertheless, for the sake of simplicity, and given
 601 that freezing conditions were only observed once during the whole monitoring period, the dataset corresponding
 602 to freezing conditions have been dismissed when using the *frequency tracking* module. On this basis, Fig. 16
 603 analyses the correlation between the mean temperature and crack amplitudes assessed by LVDT-1 (C1) against the
 604 resonant frequencies of global modes Fx1, Fy1, and T1 of the Consoli Palace during the one-year training period.
 605 In this figure, it is noted that the resonant frequencies exhibit a negative correlation with the mean temperature, and
 606 vice versa for the crack amplitudes. The negative frequency/temperature correlation can be conceivably ascribed
 607 to temperature-induced softening of metallic tie rods installed in the interior of the building. This agrees with
 608 previously reported results in the literature, such as the work by Gentile and co-authors [33] who identified the

609 role of metallic tie rods in the development of negative frequency/temperature correlations in the Milan Cathedral.
 610 On the other hand, the positive frequency/crack amplitude correlation is explained by the correlation between
 611 temperature and crack amplitudes. In particular, temperature increases induce the closure of cracks and vice-versa
 612 for temperature decreases. For a more exhaustive analysis of the environmental effects on the Consoli Palace,
 613 readers may refer to reference [22].

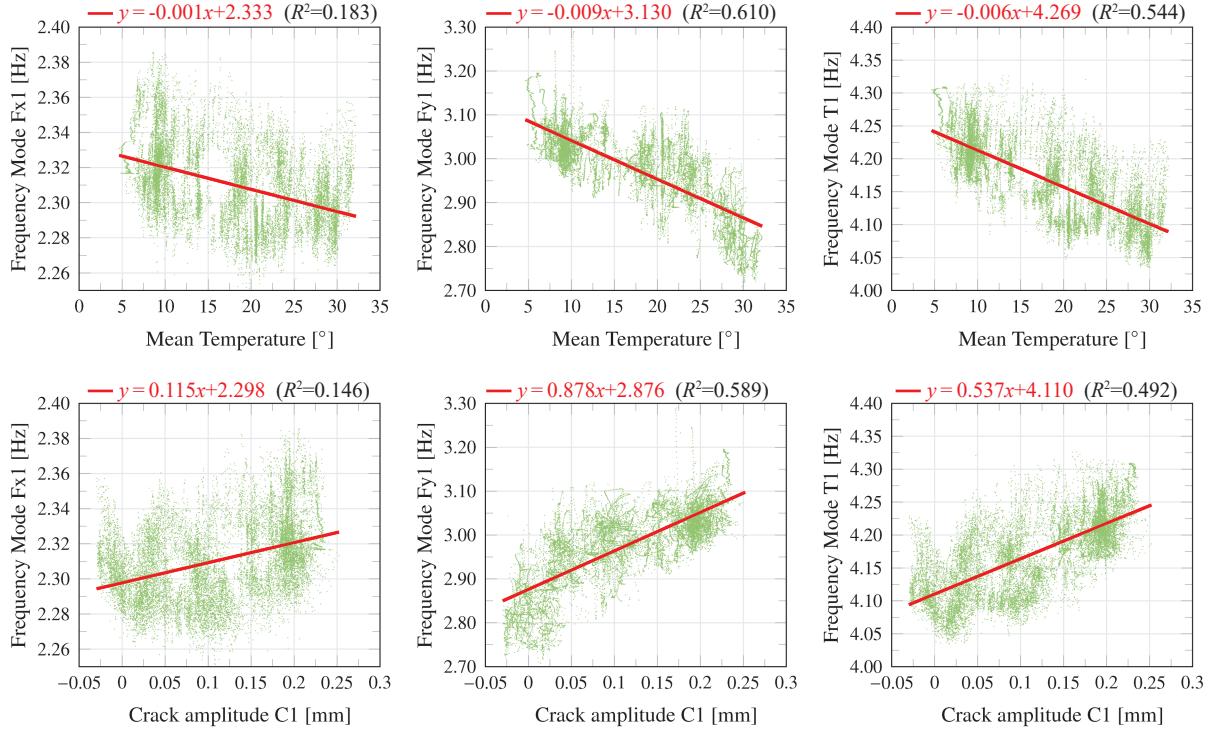


Figure 16: Correlation between mean temperature and crack amplitudes assessed by LDVT-1 and the resonant frequencies of global modes Fx1, Fy1, and T1 of the Consoli Palace during the one-year training period.

614 In light of the previous analyses, three different statistical models are defined in the *Multivariate statistical*
 615 *analysis* module, labelled as MLR-F, PCA-F and ARX-C. Models MLR-F and PCA-F define the resonant fre-
 616 quencies as estimators, while ARX-C considers for this purpose the crack amplitude C1. The aim of these models
 617 is to perform a local/global damage assessment of the Consoli Palace. On one hand, the first two models evaluate
 618 the presence of damage affecting the overall stiffness of the structure, while the second one accounts for local
 619 damage inducing behavioural variations in the amplitudes of crack C1. In the PCA-F model, only two principal
 620 components (PCs) sufficed to explain more than 90% of the variance of the estimators. The characteristics of these
 621 statistical models are as follows:

- 622 • MLR-F: Estimators → {Fx1, Fy1, L1, T1, L3}; Predictors → {T1, T2, C1, C2}; Regression model → MLR.
- 623 • PCA-F: Estimators → {Fx1, Fy1, L1, T1, L3}; Regression model → PCA (retained PCs: 2).
- 624 • ARX-C: Estimators → {C1}; Predictors → {T1, T2}; Regression model → ARX.

625 Figure 17 depicts the statistical predictions obtained for all the defined models and the corresponding Hotelling's
 626 T-square control charts. For clarity purposes, only the time series of the frequencies of mode Fx1 and crack am-
 627 plitudes C1 are plotted in the figure during the one-year training period. With regard to the statistical predictions
 628 obtained by models MLR-F and PCA-F, it is noted that better fittings of the natural frequency of Fx1 are obtained
 629 using PCA. Conversely, larger differences between experimental and statistical predictions are observed in the
 630 MLR-F model. In this case, it is noted that although the use of temperature and crack amplitude measurements
 631 allows the modelling of the daily and, to some extent, seasonal variations in the resonant frequencies, there are
 632 still some seasonal fluctuations that cannot be accurately reproduced. This may be ascribed to the specific sensor
 633 locations, which may fail at characterising the temperature distribution throughout the building. On the other
 634 hand, it is noted in the ARX-C model that the use of temperature measurements as exogenous variables can well
 635 reproduce both the seasonal and daily fluctuations in the time series of crack amplitudes C1. However, it is im-
 636 portant to remark that the statistical predictions using a MLR model instead of an autoregressive model led to

large residuals. Specifically, while seasonal fluctuations could be captured sufficiently well using only temperature measurements as predictors, daily fluctuations could not be accurately reproduced. This fact may indicate the correlation of crack amplitudes with the temperature distribution in different locations of the building (recall that the temperature sensors are located right aside the LVDTs). The graphs in the right hand side of Fig. 17 reports the time series of T^2 distances along with the UCL corresponding to a confidence level of 99%. Here, it is noted that the number of outliers after the training period is slightly larger in the MLR-F model (6.03%) compared to the PCA-F (2.85%), which confirms the better fitting of the experimental data using PCA.

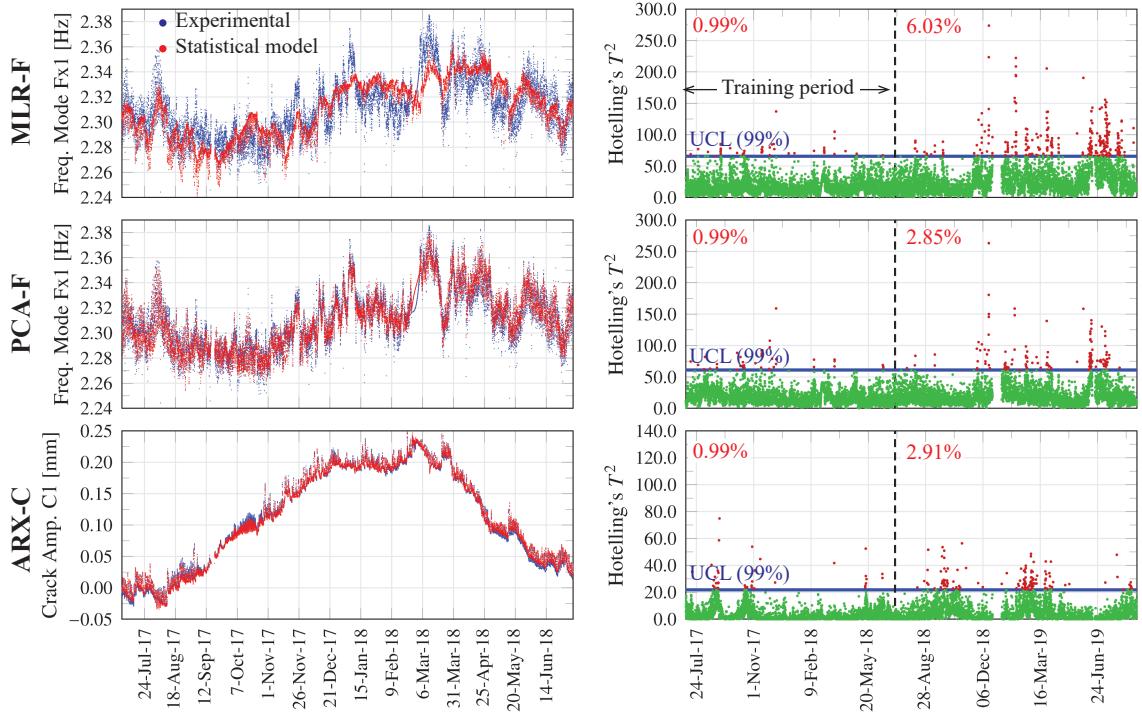


Figure 17: Plots of time histories of the natural frequency of mode Fx1 and crack amplitude C1 obtained by statistical models MLR-F, PCA-F, and ARX-C, and corresponding Hotelling's T-square control charts.

Damage detection and simulation modules: The damage detection module, shown in Fig. 18, allows to manage permanent SHM systems in real-time and in a completely autonomous way. The interface includes real-time graphs of the time series of the estimators, predictors, and measurement data, as well as the corresponding control charts. Every time a new data file is found, the interface graphs are updated and the software performs damage detection based on all the previously defined statistical models. If an anomaly is found in any of the models, the software triggers an alert and notifies the user with a sound-alert, an alert message in the console of the interface, and (if desired) an e-mail with an attached screenshot of the control chart with the detected anomaly. In this way, the user can check whether a system notification may be a false alarm or, conversely, an in-situ inspection ought to be planned. The work-flow of this interface comprises the following steps: (a) automatic detection of new data files, signal pre-processing, system identification, and frequency tracking; (b) construction of statistical models, elimination of environmental effects, and updating of control charts; and (c) automatic damage detection. The progress of each step is notified in the console of the interface. Moreover, if no files are found in a maximum period of time prescribed by the user, the software sends a warning notification of unintended system shutdown.

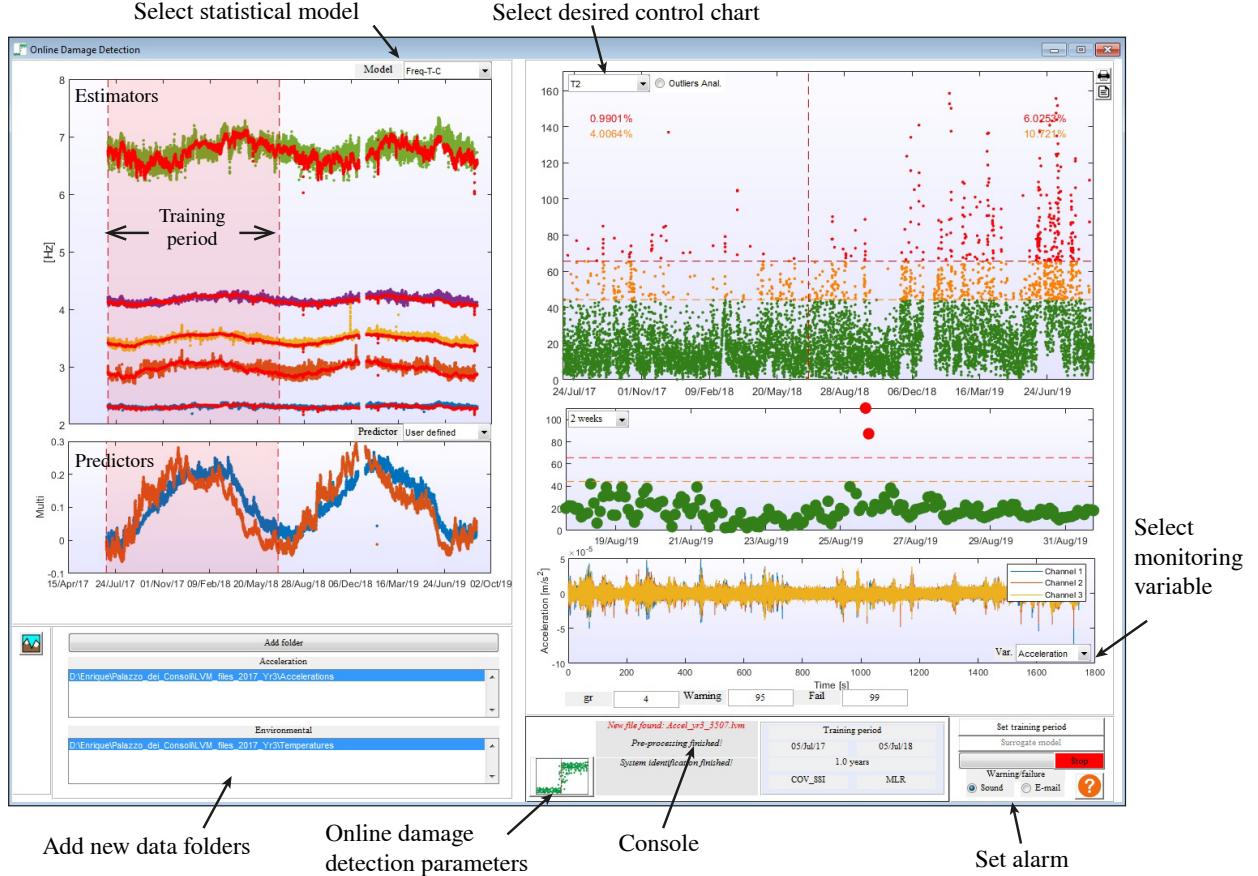


Figure 18: Screenshot of the damage identification module.

Note that a damage detection algorithm based upon the detection of outliers in the control charts would lead to a large number of false alarms. In particular, considering a subgroup size of 4 and a UPC of 99%, this would result in $(365 \cdot 24 \cdot 2/4)/100 = 43.8$ alarm notifications per year on average, even when the structure remains in healthy conditions. To minimize the rate of false alarms, MOSS includes the newly proposed damage detection method in Section 3.4.3. Moreover, in order to tune the convergence parameter cp_{max} and assess the effectiveness of a statistical model for damage detection, the software also counts on a *Damage Simulator* module available in the last section of the main GUI in Fig. 9. This allows the user to introduce artificial damage scenarios in terms of mean shifts in the estimators from a given date forward. As an example, Fig. 19 shows the control charts obtained for the previously defined statistical models (MLR-F, PCA-F, and ARX-C) when artificial damage is introduced from August 20th 2018. In particular, frequency decays of $\Delta f_1 = -3.44E-2$ Hz ($-1.5\% \bar{F}_{x1}$) and $\Delta f_1 = -2.53E-2$ Hz ($-1.0\% \bar{F}_{x1}$) are introduced in the time series of the resonant frequency of mode $Fx1$ for MLR-F and PCA-F models, respectively. It is important to remark that, given the inferior fitting performance of the MLR-F model formerly reported in Fig. 17, a larger frequency decay value was necessary in this case to successfully detect the imposed damage. In the case of the ARX-C model, a mean shift of $1.10E-2$ mm ($10\% \bar{C}_1$) is included in the time series of crack amplitudes $C1$. A convergence parameter value of $cp_{max} = 96$ is assumed, that is to say, the same anomaly must be detected in 96 consecutive steps (48 hours since every file is 30-min long) to be considered as a potential fault.

Note that in Fig. 19 the imposed damage scenarios were successfully detected by all the statistical models. Additionally, a total of 15, 17, and 14 false positives are detected for the MLR-F, PCA-F, and ARX-C models, respectively. These are indeed related to noticeable shifts in the corresponding residuals and arise even when no damage is introduced. This circumstance evidences limitations of the statistical models to reproduce certain in-control operational and/or environmental effects. It is thus concluded that the fitting efficiency of the selected statistical models within the training period determines the minimum detectable damage and the appearance rate of false alarms. In the particular case of the Consoli Palace, a denser monitoring of the temperature distribution in the building, as well as of other environmental factors such as the humidity in the masonry, may reduce the minimum detectable anomalies and the false alarm rate.

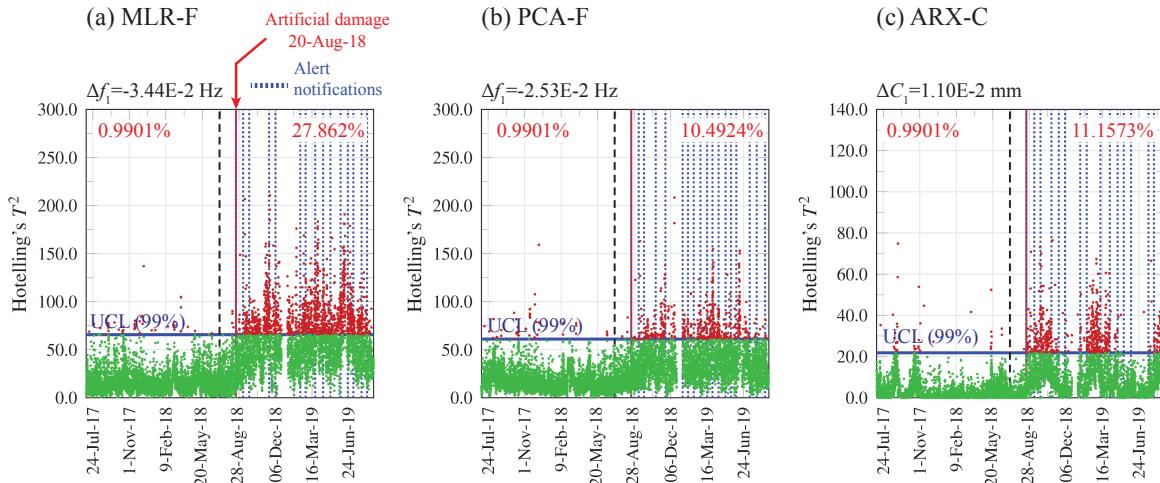


Figure 19: Automatic detection of simulated damage scenarios applied to the monitoring time series of the Consoli Palace considering different statistical models: (a) MLR-F, (b) PCA-F, and (c) ARX-C.

683 5. Concluding remarks

684 This paper has presented the development of two novel software solutions, MOVA and MOSS, for the
 685 automatic management of permanent integrated SHM systems. The developed software includes intuitive GUIs to
 686 guide users all through the process until the setting of a completely autonomous SHM system. The code com-
 687 prises a unique collection of state-of-the-art algorithms and tools for vibration-based SHM, and allows the fusion
 688 of heterogeneous monitoring data for comprehensive structural assessment. In addition, a novel anomaly detection
 689 algorithm based upon the PELT method has been implemented for performing automatic damage detection. The
 690 capabilities of MOVA/MOSS have been demonstrated through a real case study of a CH structure, the Consoli
 691 Palace in Gubbio (Italy). A mixed static/dynamic monitoring system has been installed in the building during
 692 two years, and the monitoring data have been processed online using MOSS. Three different statistical models
 693 have been defined considering the resonant frequencies of the building and the amplitudes of a major crack as
 694 estimators. The reported results have shown the potential of MOSS for simultaneously constructing different con-
 695 trol charts involving heterogeneous monitoring data. Furthermore, artificial damage scenarios have been included
 696 to demonstrate the effectiveness of the proposed automated anomaly detection algorithm for local/global damage
 697 detection.

698 Besides its scientific contribution, the ultimate goal of MOVA/MOSS is also to provide professional engineers
 699 with some of the latest state-of-the-art techniques and research breakthroughs in the field of SHM of structures.
 700 Moreover, this software is aimed at paving the way for integrated SHM systems with heterogeneous monitoring
 701 solutions for local/global damage assessment of civil infrastructure.

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 705 cultural heritage constructions through simulation and health monitoring" (protocol no. 201747Y73L).

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