

# RELATIVE INTERGENERATIONAL MOBILITY, A GLOBAL REVIEW

Student: Agustín Sanhueza\*      Guide: Javier Nuñez†

Co-Guide: Claudio Montenegro‡

May 15, 2023



Facultad de Economía y Negocios, Universidad de Chile

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## Abstract

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**Keywords:** Social Movility, Elasticity, Intergenerational Inequality

**JEL:** Código1 Código1 Código3 Código4 Código5

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\*[asanhuezac@fen.uchile.cl](mailto:asanhuezac@fen.uchile.cl)

†[jnunez@fen.uchile.cl](mailto:jnunez@fen.uchile.cl)

‡[cmontenegro@worldbank.org](mailto:cmontenegro@worldbank.org)



# 1 Motivation & Literature Review

We can summarize the reasons for estimating relative intergenerational mobility in two main types of reasons:

1) **Normative reasons:** There is broad consensus that public policy must generate the necessary conditions for the existence of a concept called '*equality of opportunities*'. This concept can be thought of as the possibility that individuals have to realize their life projects. There are economic/social differences due to factors that individuals choose, such as effort, responsibility, their choices, etc. But there are other exogenous factors that individuals do not control and that limit their opportunities to develop their life projects, such as the money needed for education or violence in the neighborhood where they live. A society in which there is equality of opportunities is one in which opportunities (public policies) mean that circumstances do not determine the results. Thus, the results would come from a "fair" process.

2) **Economic Reasons:** Under the reasonable assumption that talents are spread across different strata of society and that there is equality of opportunity, the relative position of individuals in the income/education distribution should change over generations. In reality, since there is not full equality of opportunity, much talent and ability is wasted as they are unable to realize their full potential, leading to an inefficient allocation of resources in the economy.

If people feel that there is not a strong degree of equality of opportunity, this can impact on the effort given by people in the lower tail of the distribution as they feel that their efforts will be wasted and that their children's generation will end up relatively close to where they ended up.

There are many papers that have studied this issue, in different time windows, with different methodologies and data. To date, there are only two papers, conducted by the World Bank, that have studied intergenerational mobility with countries of all income levels, and from all regions of the world.

The paper seeks to complement the two studies by Van der Weite et.al (2021), on social mobility in the world. The difference is that we have more data available and the results will be presented using the same methodology without the need to mix our own results with those of other authors. Additionally we will perform an analysis using percentile correlation coefficients, which has been shown by Chetty et.al (2014) to be a more robust estimator. We will also perform a cross section analysis using the year in which the survey was conducted, together with a cohort analysis. This can be summarized in the following table.



	Van der waide et.al		This Work	
	2021 (Education)	2018 (Education & Income)	Education	Income
Surveys	<500	<650	978	379
Methodology	IV & Coresidents	IV & Coresidents	Coresidents	Coresidents
Approach	Cohort	Cohort	Cohort + Cross Section	Cross Section
Estimations	Level	Level	Level & Range	Level & Range
Mix of results	Yes	Yes	No	No

Surveys: This would be the first study to have such a large coverage of surveys for countries around the world. We expect the results to be in line with existing literature for regional level work, or for the benchmark work we have from Van der Waide et.al. It should be noted that these surveys were chosen after applying a series of filters detailed below.

Methodology: The work of Van der Waide et al. first estimates relative intergenerational mobility using "retrospective questions" to the son to obtain information from the father. For example, it is possible to estimate mobility in education if the son reports how many years of education his father has, as this is fairly straightforward to achieve. On the other hand, income is difficult to report accurately, so if the son does not have this information from his father, it would be possible to estimate how much it would be, using instrumental variables based on the information provided by the son. In the case of not having this type of data, the authors use the coresidents methodology, which allows obtaining information from parents and children living in the same household. In our work we use only the latter methodology, which allows us to obtain more comparable results than if different ways of estimating the same thing were used.

Approach: The work of Van der Waide et al. uses a cohort approach. This allows us to know how relative mobility has evolved over different generations (using the year of birth of individuals). For the education dimension we do the same, but in addition we add a cross section approach, which allows us to see how relative mobility has evolved over different moments in time (each moment takes into account different generations). We do the same for the income dimension, which allows us to generate a richer analysis of the phenomenon under study.

Estimates: Chetty et.al the year 2014 studying relative social mobility in the United States used rank measures noting that they are a more robust way of estimating relationships between variables. In this paper we estimate relative mobility in the traditional way by level, but we also add rank estimates using spearman correlation. This would allow us to generate robustness analyses of the results found.

Mixing of results: The work of Van der Waide et.al shows results from different sources, the main one being GDMI and the "Equalchances" page. The problem is that they do



not document in detail the functional form of the regressions, or the filters of observations they used. It is possible that when presenting the results, they do so by mixing these methodologies, which is not ideal. In this paper we will estimate the results ourselves, using the same functional form and filters in each and every survey, without mixing results from other studies.

## 2 Research Question

- 1) **How has intergenerational persistence in education and income fared globally by cohort and survey years?**
- 2) **How does intergenerational persistence correlate globally, with key variables from different models that attempt to explain it?**

Variables	Model/Study	Hypothesis
Inequality (Gini Coefficient)	<a href="#">Corak (2013)</a>	Positive
Public Spent	<a href="#">Mayer &amp; Lopoo (2007)</a>	Negative
Economic Liberalization	<a href="#">Xie &amp; Chang (2022)</a>	Negative
Economic Growth	<a href="#">Yishay &amp; Moav (1999)</a>	Negative
Violence	<a href="#">Manduca &amp; Sampson (2019)</a>	Positive
Retorno de la Escolaridad	<a href="#">Solon (2004)</a>	Positive

## 3 Data

The ideal data to generate this type of work are long panel data that track parents and children in their income history and years of schooling. These types of data are extremely expensive to collect, and if they exist at all, they are typically concentrated in developed world countries.

The data we will use are household surveys that contain information on the income and years of schooling of the parents and children residing with them.

We have four data sources:

- 1) International Income Distribution Database (I2D2): In an effort to generate international evidence on different matters, the World Bank generated databases from household and labor market surveys in countries around the world. The database covers economies from developed and developing regions. There is no censoring of any kind in the survey



selection. If a survey was available and has all the needed variables, then it was included. For all the economies in this study, we have at least one point in time and in many several cases. An enormous effort was undertaken in standardizing the variable definitions across economies and time periods.

Not all of economy/year/survey points are included in our analysis because some surveys lack key variables. It should be noted that for a given economy/year, there could be more than one estimate. This is because for that economy/year, there is more than one survey available, or that the same survey is available more frequently than annually.

2) [Luxemburg Income Study](#): All surveys are nationally representative. Has more up-to-date data on income, especially for rich countries. Has recently included more developing countries. Will be used as second order data if not available in I2D2. New economies Japan, Israel, Germany, etc. These data are more public, can be requested for transparency, but access is very limited. The opening is given by entering the server and putting the code to get the results that arrive via mail.

3) [Quality of Governance](#) (Gothenburg University): In order to find correlational evidence at the international level between our estimates and macroeconomic variables of the countries, we will use this database. The observations are composed of a country-year combination.

4) [World Bank Country Classification](#): To classify countries by income level and geographic region, we use another World Bank database updated to the year 2022. The income classification has 4 categories; High income, Low income, Upper middle and Lower middle (the only country that cannot be classified was Venezuela, since the data provided is not reliable for the World Bank). The region classification has 7 categories; East Asia & Pacific, Europe & Central Asia, Latin America & Caribbean, Middle East & North Africa, North America, South Asia and Sub-Saharan Africa.



## 4 Descriptive Statistics

### 4.1 Education

Table 1: **Education Economies**

Economies	High income	Low income	Lower middle income	Upper middle income	Total
East Asia & Pacific	1	0	11	3	15
Europe & Central Asia	26	0	3	14	43
Latin America & Caribbean	5	0	5	11	21
Middle East & North Africa	2	2	7	2	13
North America	1	0	0	0	1
South Asia	0	1	6	1	8
Sub-Saharan Africa	0	22	15	5	42
Total	35	25	47	36	143

*Self Made: World Bank*

Table 2: **Median Education Estimations by Income**

Income	Beta	Correlation	Spearman	Father Scholarship	Son Scholarship
High Income	.29	.34	.33	12	12
Low Income	.45	.44	.44	4.7	7.6
Lower Middle Income	.45	.47	.5	5.9	9.4
Upper Middle Income	.42	.47	.49	8	11
Total	.4	.43	.45	8.6	11

*Self Made: World Bank*

Table 3: **Median Education Estimations by Region**

Region	Beta	Correlation	Spearman	Father Scholarship	Son Scholarship
East Asia & Pacific	.45	.47	.49	7.2	10
Europe & Central Asia	.3	.34	.34	12	12
Latin America & Caribbean	.46	.54	.54	7.1	11
Middle East & No	.3	.39	.38	8.2	12
North America	.23	.35	.4	13	13
South Asia	.5	.49	.52	4.9	8.7
Sub-Saharan Africa	.41	.44	.44	5.6	8.4
Total	.4	.44	.45	8.6	11

*Self Made: World Bank*



## 4.2 Income

Table 4: Median Income Estimations

Economy	Heckman	Elasticity	Spearman
ARG	.3	.31	.42
BOL	.22	.24	.3
BRA	.37	.38	.54
CHL	.38	.38	.49
COL	.37	.38	.43
CRI	.29	.29	.4
DOM	.33	.32	.32
ECU	.24	.26	.4
GTM	.21	.24	.32
HND	.32	.33	.5
MEX	.23	.24	.35
NIC	.23	.25	.33
PAN	.35	.35	.45
PER	.21	.21	.24
PRY	.23	.23	.38
SLV	.18	.2	.32
URY	.28	.29	.41
Total	.28	.29	.39

*Self Made: World Bank*

## 5 Empirical Approach

To measure social mobility across countries, we will use a cross-section approach (many cohorts in each survey) and a cohort approach (many surveys in each generation). The second way is the most used and allows us to see the situation of the older generations with respect to the newer ones.

To calculate the social mobility of countries, the following functional form is typically used

$$y_s = \alpha + \beta y_f + \gamma X + \epsilon_i$$

Where:

$y_s$ =ln(Children's income) or Children's Education

$y_f$ =ln(Father's income) or Father's Education



X=Control variables (following the existing literature, we used age and age squared as control variables to control for the life cycle of the children)

The closer  $\beta$  is to 0, the greater the social mobility

## 5.1 Observation and survey filters

	Education	Income
Coresidents Son's Age	23-30	23-30
Semanal Working Hours	-	$\geq 22$
Father's Age	-	$< 65$
Exclusion top 0.5% of distribution	-	Yes
Control Variables	-	Son Age
Surveys $\geq$ year 2000	Cross-Section Approach	Cross-Section Approach
N° Min Surveys per Cohort	2	2
Surveys: N° Obs Min & Max Median Error	200 y 0.2	200 y 0.2

1) Coresidents Son's Age: We believe that 23 years is a reasonable cut-off age for the coresident approach, given that around this age people finish their tertiary education cycle and start entering the labor market. On the other hand, since the surveys are conducted 3 to 5 years per country, we decided to set the upper cutoff age at 30 years in order to see the effect that exists in a cohort at different ages and to limit the possible coresidence bias. If we analyze the coresidency and labor participation rates of people in this age group, it is confirmed that this is an appropriate bracket.

2) Semanal Working Hours: In the income dimension, we seek to capture what is closest to people's permanent income, so we filter out observations that have 22 or more hours of work per week.

3) Father's Age: In the income dimension we seek to avoid a problem of selectivity of people leaving the labor market to retire. This was initially intended for men in Chile, but analyzing the retirement age for men in other countries, we consider it to be a good cut-off age.

4) Exclusion top 0.5% of distribution: For every survey, the top 0.5% of the income sample was eliminated. This is a World Bank practice to avoid possible biases due to wage outliers.

5) Control Variables: In the literature on intergenerational mobility there is the concept of "life-cycle bias". This bias occurs when calculating the intergenerational persistence of income of the father at a different age than that of the son. The solution given to solve this problem is to include as a control variable the age of the son and the age of the son squared.





Some papers additionally include the father's age. In this paper we will use this for the robustness analysis. In the educational dimension, this bias does not occur because once people obtain an educational level they do not drop out of it, so estimating the intergenerational persistence of parents and children at different ages should not present a problem.

6) Surveys  $\geq$  year 2000: We stayed with these surveys from the year 2000 for 3 reasons. Because there is a greater coverage of countries during those years. After the fall of the Berlin Wall and the Soviet Union many countries were created and destroyed, in order to give them time to organize themselves and to collect quality data, we think that the year 2000 is a good cut-off year. Finally, it is evident that the coresidency rate has been increasing over time for the relevant age range, so taking the latest years available is something that is useful in our research to reduce coresidency bias.

7) Approach: We only take into account those cohorts that have a minimum of 2 surveys as observations in order to distinguish the age effect from the cohort effect.

8) Surveys: We excluded from the survey sample those surveys with a number of observations lower than 200 for the calculation of the statistics of interest. We also excluded those with a deviation from the median of their country greater than 0.2 percentage points. A graph illustrating this can be found in the [appendix](#).

To correctly capture the importance of the father's income in the children's income, we annualize the salaries to isolate the effect that the different frequencies with which each one receives it could have.

## 5.2 Cohort and Cross-Section approach

To understand the approaches, one can rely on the sample table in the [appendix](#) section. The table contains information from Chile's Casen surveys between the years 1987 and 2017. The first column corresponds to the cohort of the person, i.e. the year of his birth. The first row corresponds to the year of the survey. The values in the matrix correspond to the age in each cohort-survey year combination.

For example, in the 2017 Casen survey, sons in the 1984 cohort were 23 years old. Since we work with the sons who are between 23 and 30 years old, we can see marked in green color the boxes that show the evolution of the relevant bracket in the different cohort-survey-year combinations.

When we obtain results of relative social mobility with the cross section approach, we are doing a column-by-column analysis. In each column we obtain how much is the average estimator for the relevant age bracket over different cohorts. When we get results with

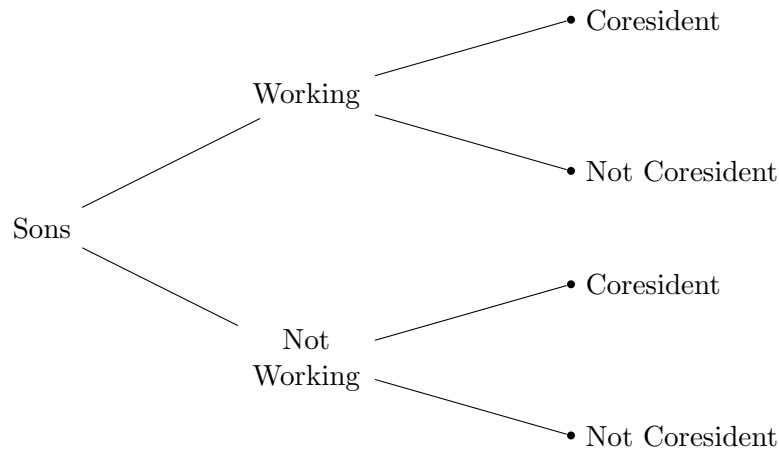


the cohort approach, we are doing a row-by-row analysis. In each row we get how much is the average estimator for the relevant age bracket across different surveys. The cohorts marked in red were eliminated for each economy, since in those cohorts we have less than two survey observations, which makes it impossible to distinguish the cohort effect from the age effect.

### 5.3 Selection Bias

There are two sources of selection bias in this work. The first is whether the person participates in the labor market, the second is whether the person coresides with his or her parents. To attenuate the first selection bias we will focus only on the father-son combination, leaving aside the mother-son, father-daughter or mother-daughter combinations since female labor participation rate is lower than that of males.

In this research we will only concentrate on those father-son combinations in which both works (have incomes). Since these father-son combinations are only observed with sons who live with their father, it is possible that there is a selection bias with respect to those sons who do not live with their fathers. This can be summarized in the following two figures.



		Son Wage	Father Wage
Working	Coresident	✓	✓
	Not Coresident	✓	×
Not Working	Coresident	×	✓
	Not Coresident	×	×

To take care of the second selection bias we will estimate by heckman maximum likelihood only for the income dimension since it has been documented that the coresident bias for



education is marginal (Emran et.al, 2016 & Emran et.al, 2018).

If we consider the latent variable  $v_s^*$  as the benefit that the son obtains by living with his father, we will observe the sample only when  $v_s^* > 0$ , so we have the following

$$v_s^* = \gamma Z_s + \epsilon_s$$

$$v_s = \begin{cases} 1 & \text{if } \gamma Z_s + \epsilon_s > 0 \\ 0 & \text{if } \gamma Z_s + \epsilon_s \leq 0 \end{cases}$$

Where  $Z_s$  corresponds to a vector of variables that influence the son's decision to live or not with his father.

The estimates of the participation equation are obtained from the following regression model:

$$Cores = \alpha + \beta_{civil} + \gamma_{urban} + \delta_1 age + \delta_2 age^2 + \rho_{crowd} + \eta_{Liability\ Ratio} + v$$

Variables	Controls	Instruments
Father's wage	✓	×
Son's age & $age^2$	✓	✓
Father's age & $age^2$	✓	×
Civil status	×	✓
Urban	×	✓
Crowd	×	✓
Liability Ratio	×	✓

Age: As people get older, the rate of coresidence decreases (see appendix), so the probability of coresidence decreases as well.

Marital status: We define this variable as a dummy that is 1 if the person is married, with a partner, divorced or widowed, and 0 otherwise. It is expected that the probability of coresidence with parents should decrease if the person is in any of these categories.

Urban: We define this variable as a dummy that is 1 if the person lives in an urban area and 0 if not. The probability of coresidence is expected to decrease if the person lives in a city.

Crowd: This is a variable that captures the number of children living in the person's household. It is expected that in a household with more children, the probability of coresidency



will decrease.

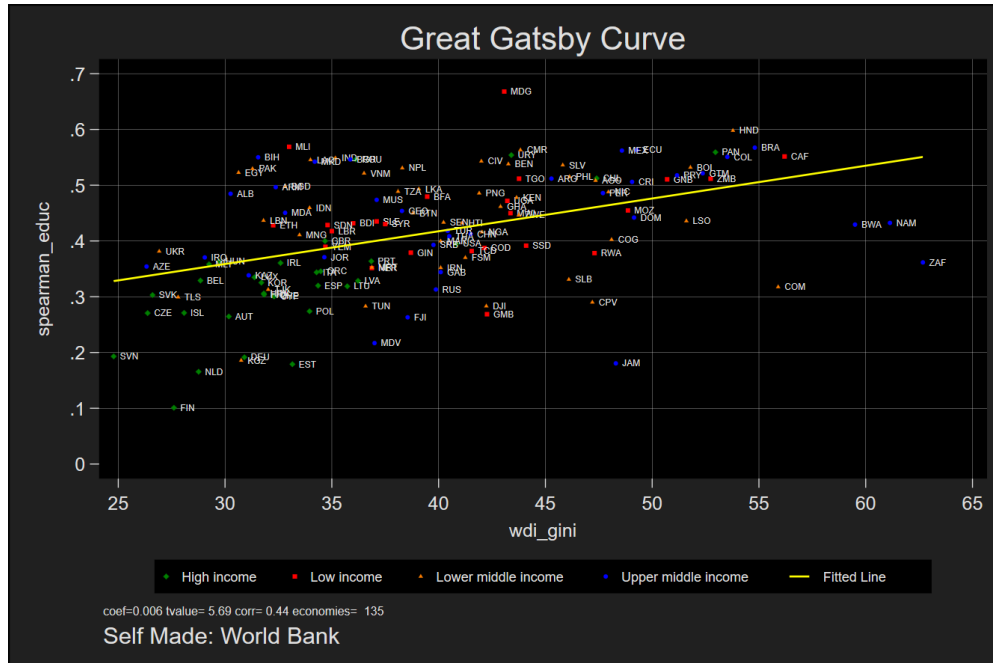
Liability Ratio: This variable divides the number of "liabilities" with the number of "assets" per household. We define "active" persons as those between the ages of 23 and 65. We define "passive" persons as those who are 75 years of age or older.

The estimates of the income dimension are obtained from the following regression models:

$$y_s = \alpha + \beta y_f + \gamma_1 age + \gamma_2 age^2 + \delta_1 father\ age + \delta_2 father\ age^2 + \epsilon_s$$

## 6 Results

### 6.1 Education Cross Section



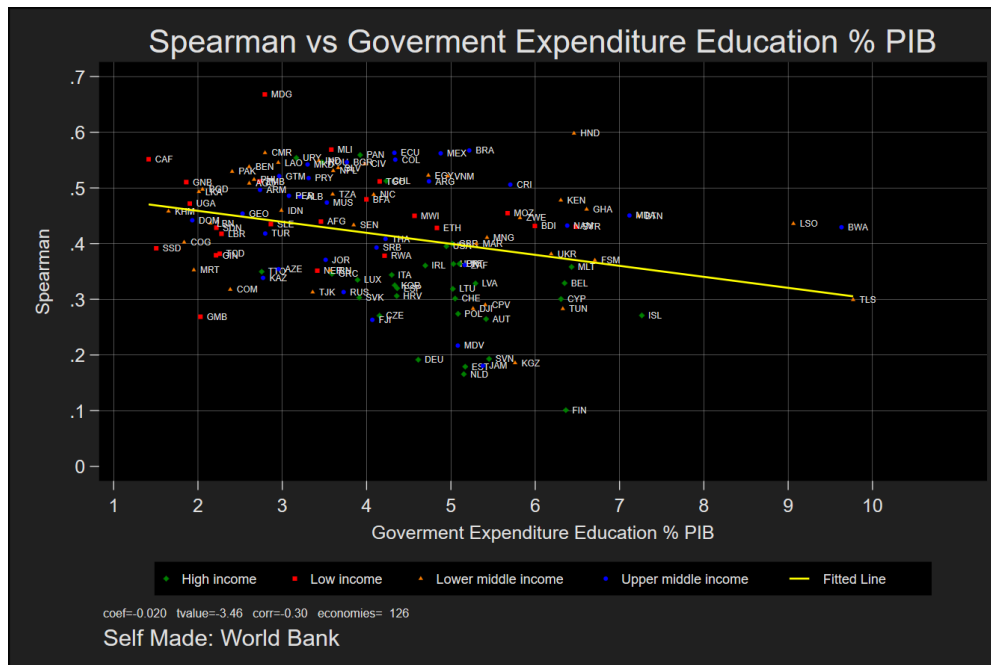




Table 5: Education Relative Mobility

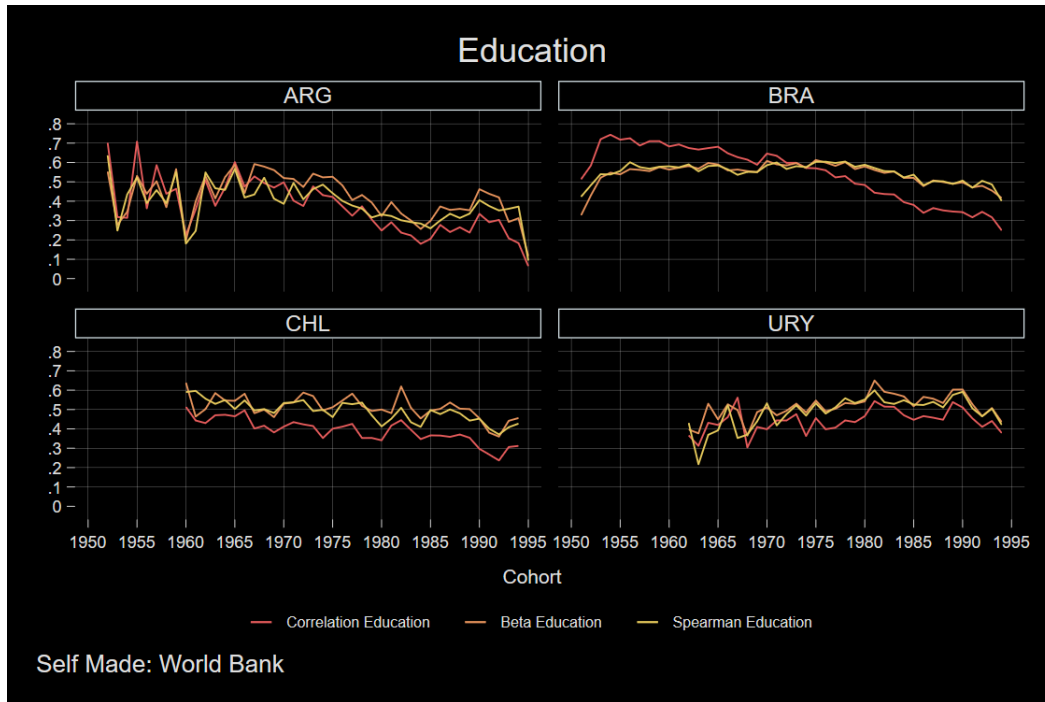
	(1) Correlation	(2) Beta Regression	(3) Spearman
ln(Per Capita PPP)	-0.0265** (-2.69)	-0.0478*** (-5.51)	-0.0146* (-2.16)
ln(Gini)	0.270*** (10.60)	0.168*** (6.26)	0.277*** (12.77)
ln(Govt Education Expenditure)	-0.0302 (-1.79)	-0.0551** (-3.22)	-0.0553*** (-4.20)
ln(Economy Liberalization)	-0.00754 (-0.22)	-0.0119 (-0.56)	-0.0799*** (-3.69)
Constant	-0.253 (-1.53)	0.354* (2.12)	-0.0470 (-0.34)
R2_adjusted	0.301	0.361	0.499
Akaike	-936.1	-940.9	-1107.4
Bayes	-913.3	-919.3	-1085.7
Observations	702	555	568

*t* statistics in parentheses

\*  $p < 0.05$ , \*\*  $p < 0.01$ , \*\*\*  $p < 0.001$



## 6.2 Education - Cohort





### 6.3 Income - Cross Section

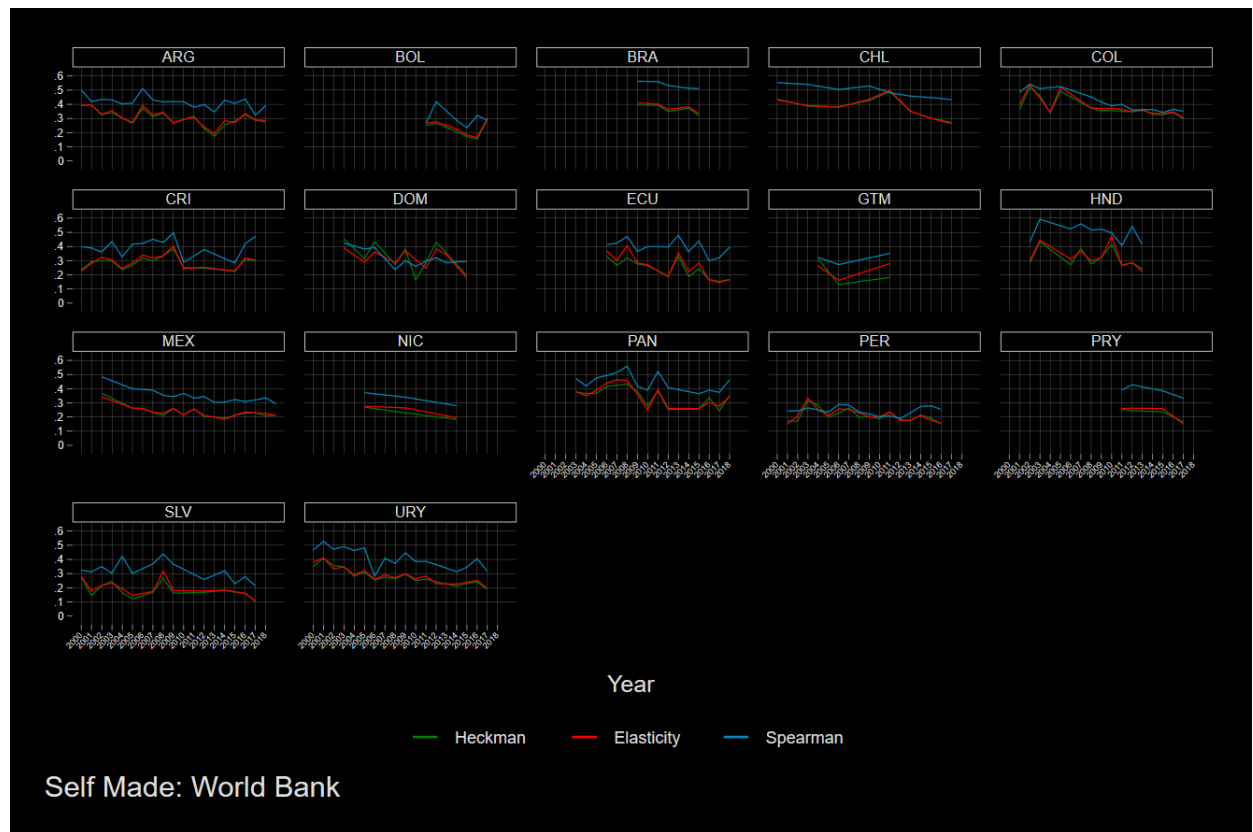






Table 6: LAC Income Relative Mobility

	(1) Heckman	(2) Elasticity	(3) Spearman
ln(Per Capita PPP)	0.134*** (8.34)	0.129*** (8.05)	0.132*** (6.50)
ln(Gini)	0.602*** (11.09)	0.592*** (11.14)	0.462*** (7.37)
ln(Govt Education Expenditure)	-0.0836*** (-3.59)	-0.0755*** (-3.43)	-0.0193 (-0.53)
ln(Economic Globalization)	-0.0477 (-1.56)	-0.0582 (-1.88)	-0.0630 (-1.91)
Constant	-3.008*** (-10.48)	-2.885*** (-9.88)	-2.379*** (-6.91)
R2_ajusted	0.504	0.494	0.377
Akaike	-331.9	-330.1	-282.6
Bayes	-318.0	-316.2	-268.6
Observations	120	120	121

*t* statistics in parentheses

\*  $p < 0.05$ , \*\*  $p < 0.01$ , \*\*\*  $p < 0.001$

## 7 Conclusions

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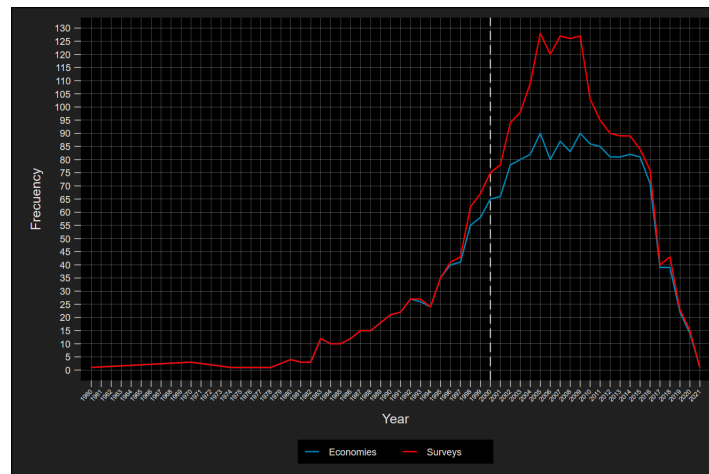
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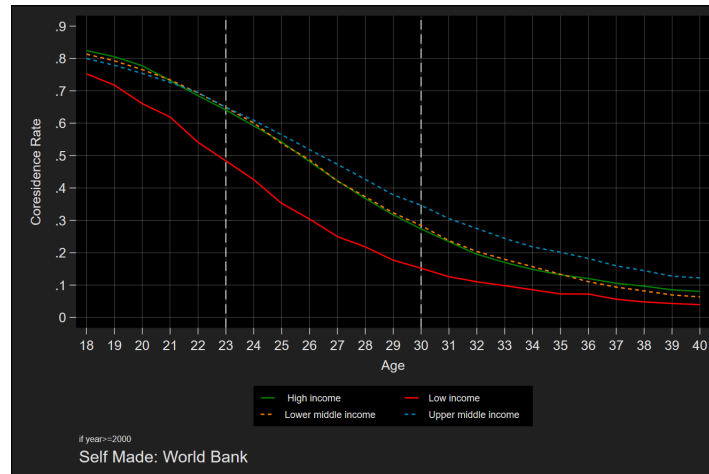
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## 9 Appendix

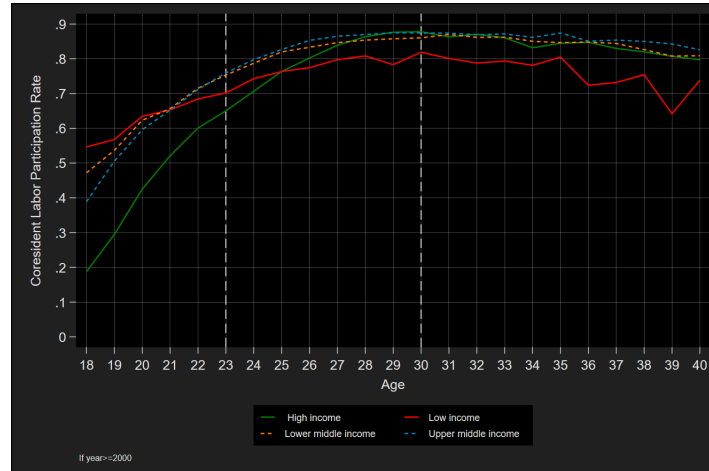




$$\text{Coresidence Rate} = \frac{\text{Son's living with their father}}{\text{Total of Son's}}$$



$$\text{Labor Force Participation Rate} = \frac{\text{Employed} + \text{Unemployed}}{\text{Working age population}}$$





	2017	2015	2013	2011	2009	2006	2003	2000	1998	1996	1994	1992	1990	1987
1998	23	21	19	17	15	12	9	6	4	2	0	-2	-4	-7
1994	24	22	20	18	16	13	10	7	5	3	1	-1	-3	-6
1992	25	23	21	19	17	14	11	8	6	4	2	0	-2	-5
1991	26	24	22	20	18	15	12	9	7	5	3	1	-1	-4
1990	27	25	23	21	19	16	13	10	8	6	4	2	0	-3
1989	28	26	24	22	20	17	14	11	9	7	5	3	1	-2
1988	29	27	25	23	21	18	15	12	10	8	6	4	2	-1
1987	30	28	26	24	22	19	16	13	11	9	7	5	3	0
1986	31	29	27	25	23	20	17	14	12	10	8	6	4	1
1985	32	30	28	26	24	21	18	15	13	11	9	7	5	2
1984	33	31	29	27	25	22	19	16	14	12	10	8	6	3
1983	34	32	30	28	26	23	20	17	15	13	11	9	7	4
1982	35	33	31	29	27	24	21	18	16	14	12	10	8	5
1981	36	34	32	30	28	25	22	19	17	15	13	11	9	6
1980	37	35	33	31	29	26	23	20	18	16	14	12	10	7
1979	38	36	34	32	30	27	24	21	19	17	15	13	11	8
1978	39	37	35	33	31	28	25	22	20	18	16	14	12	9
1977	40	38	36	34	32	29	26	23	21	19	17	15	13	10
1976	41	39	37	35	33	30	27	24	22	20	18	16	14	11
1975	42	40	38	36	34	31	28	25	23	21	19	17	15	12
1974	43	41	39	37	35	32	29	26	24	22	20	18	16	13
1973	44	42	40	38	36	33	30	27	25	23	21	19	17	14
1972	45	43	41	39	37	34	31	28	26	24	22	20	18	15
1971	46	44	42	40	38	35	32	29	27	25	23	21	19	16
1970	47	45	43	41	39	36	33	30	28	26	24	22	20	17
1969	48	46	44	42	40	37	34	31	29	27	25	23	21	18
1968	49	47	45	43	41	38	35	32	30	28	26	24	22	19
1967	50	48	46	44	42	39	36	33	31	29	27	25	23	20
1966	51	49	47	45	43	40	37	34	32	30	28	26	24	21
1965	52	50	48	46	44	41	38	35	33	31	29	27	25	22
1964	53	51	49	47	45	42	39	36	34	32	30	28	26	23
1963	54	52	50	48	46	43	40	37	35	33	31	29	27	24
1962	55	53	51	49	47	44	41	38	36	34	32	30	28	25
1961	56	54	52	50	48	45	42	39	37	35	33	31	29	26
1960	57	55	53	51	49	46	43	40	38	36	34	32	30	27
1959	58	56	54	52	50	47	44	41	39	37	35	33	31	28
1958	59	57	55	53	51	48	45	42	40	38	36	34	32	29
1957	60	58	56	54	52	49	46	43	41	39	37	35	33	30

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