Department of Electrical and Computer Engineering NYU Tandon School of Engineering Brooklyn, New York



Outline

- 1 Review
- 2 Non-linear Optimizatio
- 3 Neural Networks
- 4 Stochastic Gradient Descen
- 5 Overparameterization
- 6 La



Machine Learning Problem Pipeline

- **1** Formulate the problem: regression, classification, or others?
- 2 Gather and visualize the data
- 3 Design the model and the loss function
- 4 Train your model
 - (a) Perform feature engineering
 - (b) Construct the design matrix
 - (c) Choose regularization techniques
 - (d) Tune hyper-parameters using a validation set
 - (a) If the newformance is not estimated as healt
 - (e) If the performance is not satisfactory, go back to step (a).
- 5 Evaluate the model on a test set



Outline

- 1 Review
- 2 Non-linear Optimization
- 3 Neural Networks
- 4 Stochastic Gradient Descen
- 5 Overparameterization
- 6 La



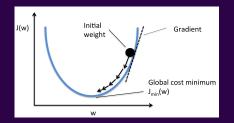
Motivation

- Cannot rely on closed form solutions
 - Computation efficiency: operations like inverting a matrix is not efficient
 - For more complex problems such as neural networks, a closed-form solution is not always available
- Need an optimization technique to find an optimal solution
 - Machine learning practitioners use **gradient**-based methods



Gradient Descent Algorithm

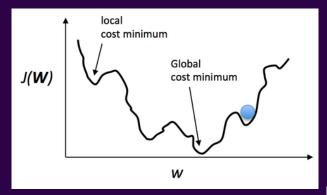
■ Update Rule $Repeat\{ egin{array}{c} \mathbf{w}_{new} = \mathbf{w} - lpha
abla J(\mathbf{w}) \ \end{pmatrix}$ lpha is the learning rate





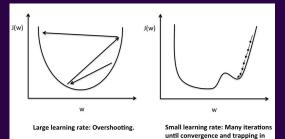
General Loss Function Contours

- Most loss function contours are not perfectly parabolic
- Our goal is to find a solution that is very close to global minimum by the right choice of hyper-parameters

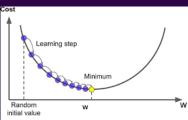




Understanding Learning Rate



local minima.



Correct learning rate



Some Animations

■ Demonstrate gradient descent animation

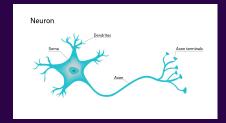


Outline

- Neural Networks



Biological Neuron



Source: David Baillot/UC San Diego

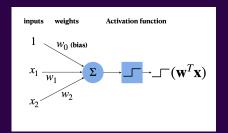


Mathematical Neuron: Perceptron

Biological Neuron:

- A neuron can receive electrochemical signals from other neurons;
- A neuron fires once its accumulated electric charge passes a certain threshold.
- Neurons that fire together wire together.

Mathematical Neuron (Perceptron)





Relation to Logistic Regression

What if we use the sigmoid function as the activation?

$$f(\mathbf{x}) = \sigma(\mathbf{w}^T \mathbf{x})$$

Decision boundary is a line: how is this supposed to revolutionize machine learning?



Multi-layer Perceptron (MLP)

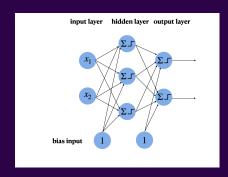
We need more neurons and we need to connect them together!

- Many ways to do that...
- Today: multi-layer perceptron/fully connected feed-forward network.



riew Opt **Neural Networks** Stochastic Gradient Descent Overparameterization

MLP Example



- What is the shape of the input and output?
- How many parameters does this model have?
- What activation function would you use for the output layer? Why?



More about MLPs

- Many choices for the activation function: Sigmoid, Tanh, ReLU, Swish, etc.
- Many choices for the number of hidden layers and the number of neurons per layer.
- MLPs can approximate any continuous function given enough data.
- MLPs can overfit, but we know many effective ways of regularization.



Exercise: TensorFlow Keras Basics

Open demo_tf_keras_basics.ipynb



Outline

- 1 Review
- 2 Non-linear Optimization
- 3 Neural Networks
- 4 Stochastic Gradient Descent
- 5 Overparameterization
- 6 Lal



Deep Learning

What does deep learning stand for?

- Deep: Neural network architectures with many hidden layers.
- Learning: Optimizing model parameters given a dataset.

In general, the deeper the model is, the more parameters we need to learn and the more data is needed.



Large-Scale Machine Learning

For deep learning systems to perform well, large datasets are required

- COCO 330K images
- ImageNet 14 million images

Challenges:

- Memory limitation: GeForce RTX 2080 Ti has 11 GB memory, while ImageNet is about 300 GB.
- Computation: Calculating gradients for the whole dataset is computationally expensive (slow), and we need to do this many times.



Stochastic Gradient Descent

Idea: Instead of calculating the gradients from the whole dataset, do it only on a subset.

- Randomly select *B* samples from the dataset
- The loss for this subset

$$\tilde{J}(\mathbf{w}) = \frac{1}{B} \sum_{i=1}^{B} \|y - \hat{y}_i\|^2$$

■ Update Rule $\begin{aligned} \textit{Repeat} \{ \\ \mathbf{w}_{\textit{new}} &= \mathbf{w} - \alpha \nabla \tilde{J}(\mathbf{w}) \\ \} \end{aligned}$



Neural Networks

This gives a noisy gradient

$$abla ilde{J}(\mathbf{w}) =
abla J(\mathbf{w}) + \epsilon$$

- **SGD**: B=1, gives very noisy gradients
- **(batch) GD**: B = N, $\epsilon = 0$, expensive to compute
- **Mini-batch GD**: Pick a small B, typical values are 32,64, rarely more than 128 for image inputs



Some Noise Helps

Even if we can, we rarely set B = N. In fact, some noise in the gradients might help to

- escape from local minima,
- escape from saddle points, and
- improve generalization.



Outline

- 1 Review
- 2 Non-linear Optimization
- 3 Neural Networks
- 4 Stochastic Gradient Descen
- 5 Overparameterization
- 6 Lal



■ Modern deep learning models are heavily overparameterized, i.e. the number of learnable parameters is much larger than the number of the training samples.



- Modern deep learning models are heavily overparameterized, i.e. the number of learnable parameters is much larger than the number of the training samples.
 - ResNet: State-of-the-art vision model, 10-60 million parameters



- Modern deep learning models are heavily overparameterized, i.e. the number of learnable parameters is much larger than the number of the training samples.
 - ResNet: State-of-the-art vision model, 10-60 million parameters
 - GPT-3: State-of-the-art language model, 175 billion parameters



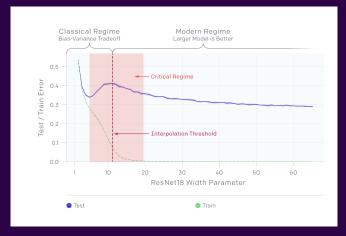
- Modern deep learning models are heavily overparameterized, i.e. the number of learnable parameters is much larger than the number of the training samples.
 - ResNet: State-of-the-art vision model, 10-60 million parameters
 - GPT-3: State-of-the-art language model, 175 billion parameters
- Conventional wisdom: Such models overfit.



- Modern deep learning models are heavily overparameterized, i.e. the number of learnable parameters is much larger than the number of the training samples.
 - ResNet: State-of-the-art vision model, 10-60 million parameters
 - GPT-3: State-of-the-art language model, 175 billion parameters
- Conventional wisdom: Such models overfit.
- It is not the case in practice!



Double Descent Curve



Source: OpenAl



Outline

- 1 Review
- 2 Non-linear Optimizatio
- 3 Neural Networks
- 4 Stochastic Gradient Descen
- 5 Overparameterization
- 6 Lab



Lab

Let's solve the mini-project with MLPs!

Open lab_mlp_fish_market_keras.ipynb

