

# **BERT4Rec: Sequential Recommendation with Bidirectional Encoder Representations from Transformer**

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## BERT4Rec: Sequential **recommendation** with bidirectional encoder representations from **transformer**

[F Sun](#), [J Liu](#), [J Wu](#), [C Pei](#), [X Lin](#), [W Ou](#)... - Proceedings of the 28th ..., 2019 - dl.acm.org

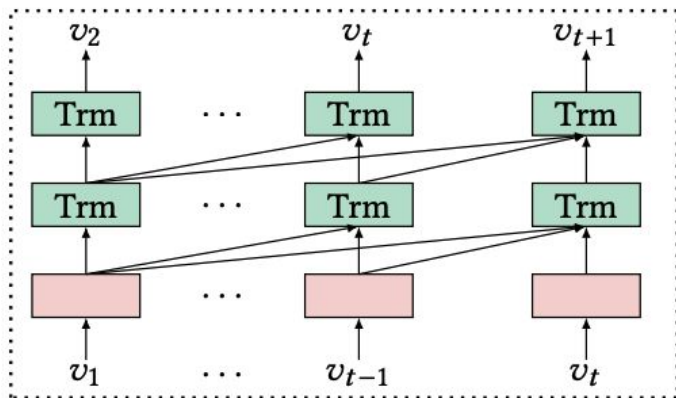
... Here, we introduce a new sequential **recommendation** model ... from **Transformers** to a new task, sequential **Recommendation**. It is built upon the popular self-attention layer, "**Transformer** ...

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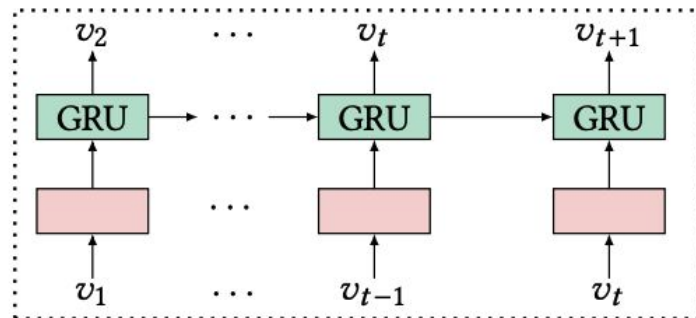
# INTRODUCTION

## Unidirectional architectures:

- a) restrict the power of hidden representation in users' behavior sequences;
- b) often assume a rigidly ordered sequence which is not always practical.



(c) SASRec model architecture.

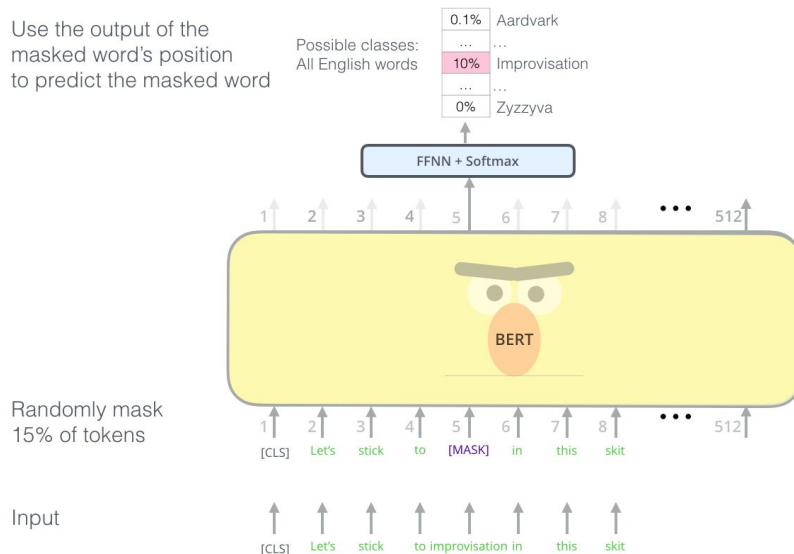


(d) RNN based sequential recommendation methods.

# INTRODUCTION

## Bidirectional architectures:

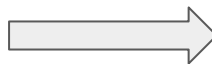
all items in the bidirectional model can leverage the contexts from both left and right side.



[The Illustrated BERT, ELMo, and co. \(How NLP Cracked Transfer Learning\)](#)

# INTRODUCTION

Jointly conditioning on both left and right context in a deep bidirectional model would cause information leakage



**Cloze task** (Masked Language Model)

Every now and then I feel [ ] a newly-qualified teacher who wants [ ] try  
everything new that he comes [ ] (honestly it doesn't happen that often any  
more [ ] when it does I take advantage [ ] it!) [ ] one [ ] these  
moments, I tried this amazing piece [ ] software [ ] create cloze texts

# RELATED WORK

## **Sequential Recommendation:**

- Markov chains (MCs)
- RNN
- Convolutional Sequence Model (Caser)

## **Attention Mechanism:**

- RNN with attention mechanism
- Self-Attentive Sequential Recommendation (SASRec)

# Problem Statement

- $\mathcal{U}=\{u_1, u_2, \dots, u_{|\mathcal{U}|}\}$ - set of users
- $\mathcal{V}=\{v_1, v_2, \dots, v_{|\mathcal{V}|}\}$ - set of items
- $\mathcal{S}_u=[v_1^{(u)}, \dots, v_t^{(u)}, \dots, v_{n_u}^{(u)}]$  - interaction sequence in chronological order for user  $u \in \mathcal{U}$

It can be formalized as modeling the probability over all possible items for user  $u$  at time step  $n_u+1$ :

$$p(v_{n_u+1}^{(u)} = v | \mathcal{S}_u)$$

# BERT4Rec Architecture

## Position-wise Feed-Forward Network:

$$\text{PFFN}(H^l) = [\text{FFN}(h_1^l)^\top; \dots; \text{FFN}(h_t^l)^\top]^\top$$

$$\text{FFN}(\mathbf{x}) = \text{GELU}(\mathbf{x}\mathbf{W}^{(1)} + \mathbf{b}^{(1)})\mathbf{W}^{(2)} + \mathbf{b}^{(2)} \quad (3)$$

$$\text{GELU}(x) = x\Phi(x)$$

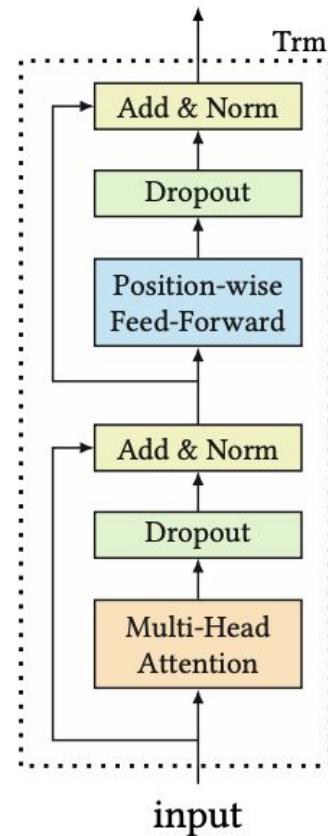
$$\text{LN}(\mathbf{x} + \text{Dropout}(\text{sublayer}(\mathbf{x})))$$

## Multi-Head Self-Attention:

$$\text{MH}(H^l) = [\text{head}_1; \text{head}_2; \dots; \text{head}_h]\mathbf{W}^O \quad (1)$$

$$\text{head}_i = \text{Attention}(H^l\mathbf{W}_i^Q, H^l\mathbf{W}_i^K, H^l\mathbf{W}_i^V)$$

$$\text{Attention}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = \text{softmax}\left(\frac{\mathbf{Q}\mathbf{K}^\top}{\sqrt{d/h}}\right)\mathbf{V} \quad (2)$$



(a) Transformer Layer.



# BERT4Rec Architecture

## Output Layer:

$$P(v) = \text{softmax}(\text{GELU}(\mathbf{h}_t^L \mathbf{W}^P + \mathbf{b}^P) \mathbf{E}^\top + \mathbf{b}^O)$$

## Stacking Transformer Layer:

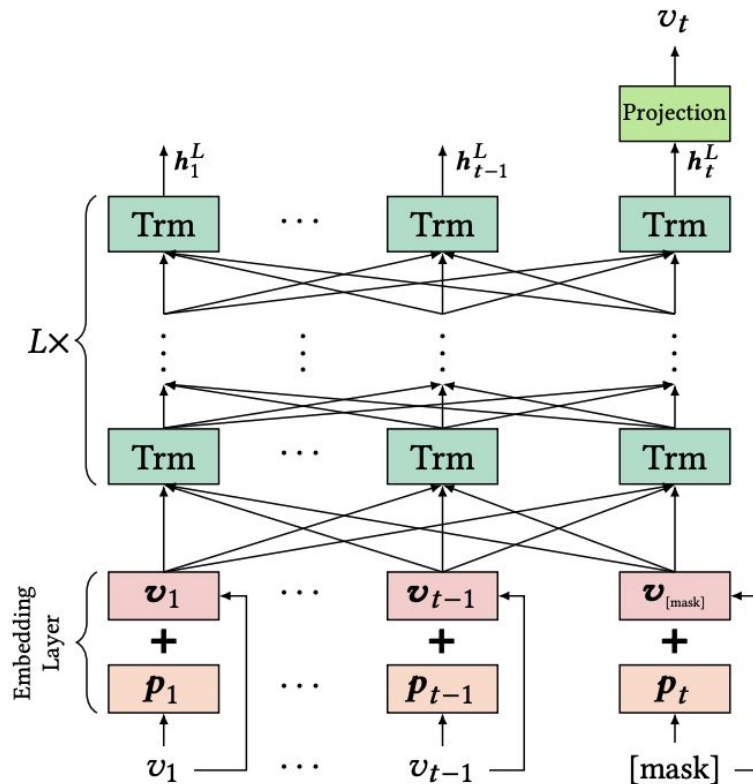
$$\mathbf{H}^l = \text{Trm}(\mathbf{H}^{l-1}), \quad \forall i \in [1, \dots, L] \quad (4)$$

$$\text{Trm}(\mathbf{H}^{l-1}) = \text{LN}(\mathbf{A}^{l-1} + \text{Dropout}(\text{PFFN}(\mathbf{A}^{l-1}))) \quad (5)$$

$$\mathbf{A}^{l-1} = \text{LN}(\mathbf{H}^{l-1} + \text{Dropout}(\text{MH}(\mathbf{H}^{l-1}))) \quad (6)$$

## Embedding Layer:

$$\mathbf{h}_i^0 = \mathbf{v}_i + \mathbf{p}_i$$



(b) BERT4Rec model architecture.

# Model Learning

## Training:

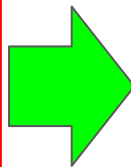
**Input:**  $[v_1, v_2, v_3, v_4, v_5]$   $\xrightarrow{\text{randomly mask}}$   $[v_1, [\text{mask}]_1, v_3, [\text{mask}]_2, v_5]$

**Labels:**  $[\text{mask}]_1 = v_2, [\text{mask}]_2 = v_4$

**Negative log-likelihood loss** 
$$\mathcal{L} = \frac{1}{|S_u^m|} \sum_{v_m \in S_u^m} -\log P(v_m = v_m^* | S'_u) \quad (8)$$

## Test:

1. Cloze objective is to predict the current masked item
2. Sequential recommendation aims to predict the future



1. Append the special token “[mask]” to the end of user’s behavior sequence
2. Produce samples that only mask the last item in the input sequences during training

# EXPERIMENT

**Table 1: Statistics of datasets.**

Datasets	#users	#items	#actions	Avg. length	Density
Beauty	40,226	54,542	0.35m	8.8	0.02%
Steam	281,428	13,044	3.5m	12.4	0.10%
ML-1m	6040	3416	1.0m	163.5	4.79%
ML-20m	138,493	26,744	20m	144.4	0.54%

# EXPERIMENT

Table 2: Performance comparison of different methods on next-item prediction. Bold scores are the best in each row, while underlined scores are the second best. Improvements over baselines are statistically significant with  $p < 0.01$ .

Datasets	Metric	POP	BPR-MF	NCF	FPMC	GRU4Rec	GRU4Rec <sup>+</sup>	Caser	SASRec	BERT4Rec	Improv.
Beauty	HR@1	0.0077	0.0415	0.0407	0.0435	0.0402	0.0551	0.0475	<u>0.0906</u>	<b>0.0953</b>	5.19%
	HR@5	0.0392	0.1209	0.1305	0.1387	0.1315	0.1781	0.1625	<u>0.1934</u>	<b>0.2207</b>	14.12%
	HR@10	0.0762	0.1992	0.2142	0.2401	0.2343	0.2654	0.2590	<u>0.2653</u>	<b>0.3025</b>	14.02%
	NDCG@5	0.0230	0.0814	0.0855	0.0902	0.0812	0.1172	0.1050	<u>0.1436</u>	<b>0.1599</b>	11.35%
	NDCG@10	0.0349	0.1064	0.1124	0.1211	0.1074	0.1453	0.1360	<u>0.1633</u>	<b>0.1862</b>	14.02%
	MRR	0.0437	0.1006	0.1043	0.1056	0.1023	0.1299	0.1205	<u>0.1536</u>	<b>0.1701</b>	10.74%
Steam	HR@1	0.0159	0.0314	0.0246	0.0358	0.0574	0.0812	0.0495	<u>0.0885</u>	<b>0.0957</b>	8.14%
	HR@5	0.0805	0.1177	0.1203	0.1517	0.2171	0.2391	0.1766	<u>0.2559</u>	<b>0.2710</b>	5.90%
	HR@10	0.1389	0.1993	0.2169	0.2551	0.3313	0.3594	0.2870	<u>0.3783</u>	<b>0.4013</b>	6.08%
	NDCG@5	0.0477	0.0744	0.0717	0.0945	0.1370	0.1613	0.1131	<u>0.1727</u>	<b>0.1842</b>	6.66%
	NDCG@10	0.0665	0.1005	0.1026	0.1283	0.1802	0.2053	0.1484	<u>0.2147</u>	<b>0.2261</b>	5.31%
	MRR	0.0669	0.0942	0.0932	0.1139	0.1420	0.1757	0.1305	<u>0.1874</u>	<b>0.1949</b>	4.00%
ML-1m	HR@1	0.0141	0.0914	0.0397	0.1386	0.1583	0.2092	0.2194	<u>0.2351</u>	<b>0.2863</b>	21.78%
	HR@5	0.0715	0.2866	0.1932	0.4297	0.4673	0.5103	0.5353	<u>0.5434</u>	<b>0.5876</b>	8.13%
	HR@10	0.1358	0.4301	0.3477	0.5946	0.6207	0.6351	<u>0.6692</u>	0.6629	<b>0.6970</b>	4.15%
	NDCG@5	0.0416	0.1903	0.1146	0.2885	0.3196	0.3705	0.3832	<u>0.3980</u>	<b>0.4454</b>	11.91%
	NDCG@10	0.0621	0.2365	0.1640	0.3439	0.3627	0.4064	0.4268	<u>0.4368</u>	<b>0.4818</b>	10.32%
	MRR	0.0627	0.2009	0.1358	0.2891	0.3041	0.3462	0.3648	<u>0.3790</u>	<b>0.4254</b>	12.24%
ML-20m	HR@1	0.0221	0.0553	0.0231	0.1079	0.1459	0.2021	0.1232	<u>0.2544</u>	<b>0.3440</b>	35.22%
	HR@5	0.0805	0.2128	0.1358	0.3601	0.4657	0.5118	0.3804	<u>0.5727</u>	<b>0.6323</b>	10.41%
	HR@10	0.1378	0.3538	0.2922	0.5201	0.5844	0.6524	0.5427	<u>0.7136</u>	<b>0.7473</b>	4.72%
	NDCG@5	0.0511	0.1332	0.0771	0.2239	0.3090	0.3630	0.2538	<u>0.4208</u>	<b>0.4967</b>	18.04%
	NDCG@10	0.0695	0.1786	0.1271	0.2895	0.3637	0.4087	0.3062	<u>0.4665</u>	<b>0.5340</b>	14.47%
	MRR	0.0709	0.1503	0.1072	0.2273	0.2967	0.3476	0.2529	<u>0.4026</u>	<b>0.4785</b>	18.85%

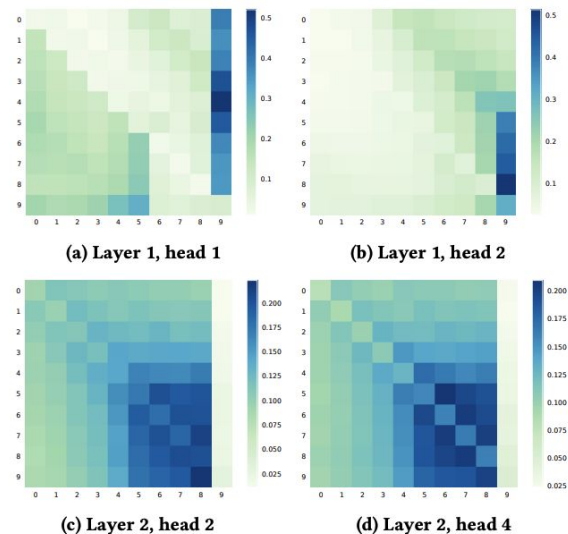
# EXPERIMENT

**Question 1:** Do the gains come from the bidirectional self-attention model or from the Cloze objective?

**Question 2:** Why and how does bidirectional model outperform unidirectional models?

**Table 3: Analysis on bidirection and Cloze with  $d = 256$ .**

Model	Beauty			ML-1m		
	HR@10	NDCG@10	MRR	HR@10	NDCG@10	MRR
SASRec	0.2653	0.1633	0.1536	0.6629	0.4368	0.3790
BERT4Rec (1 mask)	0.2940	0.1769	0.1618	0.6869	0.4696	0.4127
BERT4Rec	0.3025	0.1862	0.1701	0.6970	0.4818	0.4254



**Figure 2: Heat-maps of average attention weights on Beauty, the last position “9” denotes “[mask]” (best viewed in color).**

# EXPERIMENT

## Impact of Hidden Dimensionality $d$

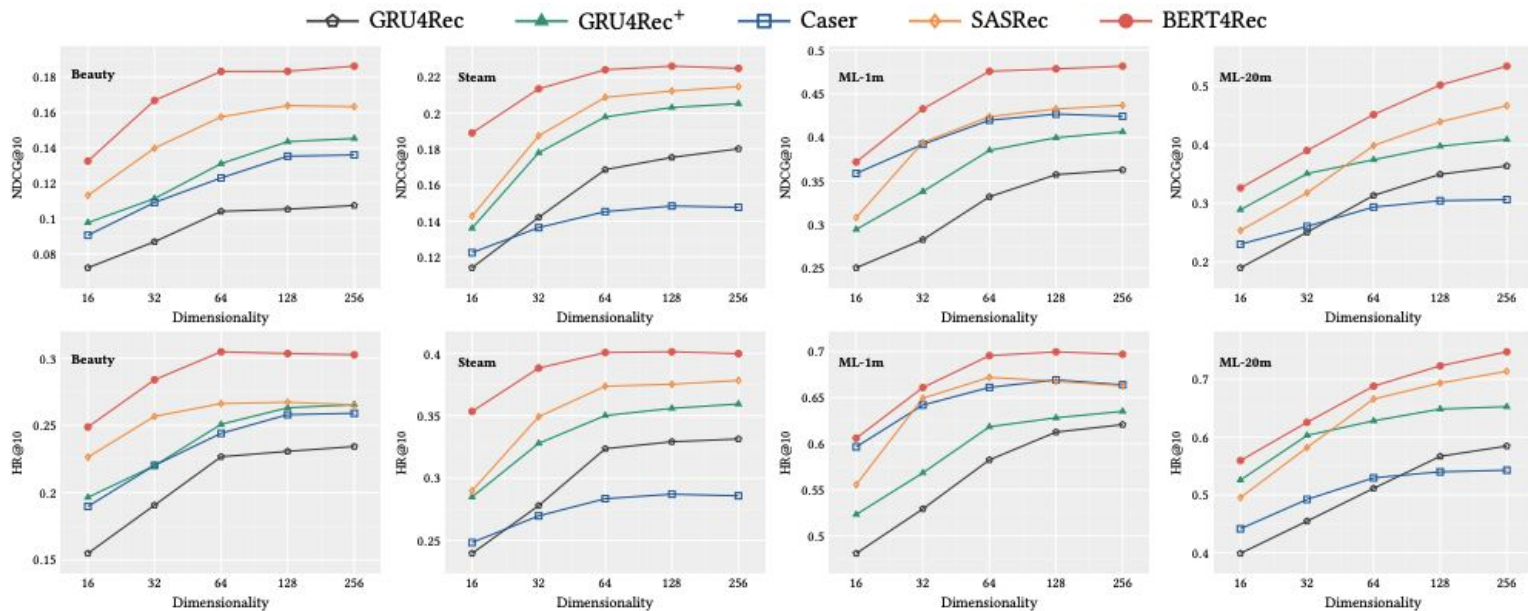
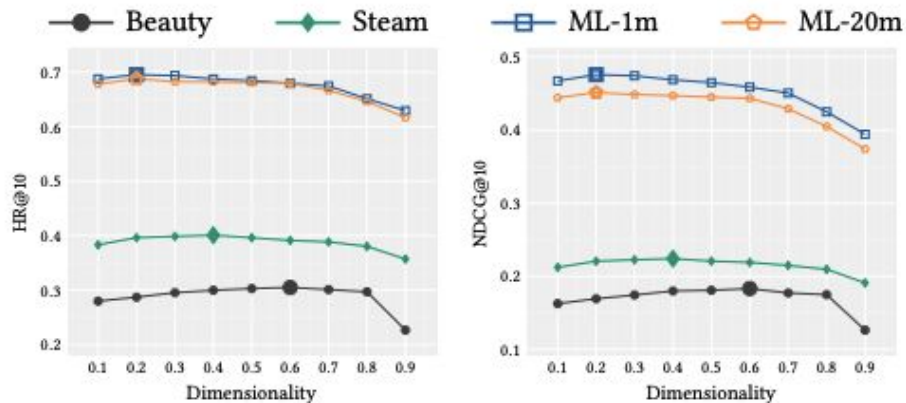


Figure 3: Effect of the hidden dimensionality  $d$  on HR@10 and NDCG@10 for neural sequential models.

# EXPERIMENT

## Impact of Mask Proportion $\rho$



**Figure 4: Performance with different mask proportion  $\rho$  on  $d = 64$ . Bold symbols denote the best scores in each line.**



# EXPERIMENT

## Impact of Maximum Sequence Length $N$

Table 4: Performance with different maximum length  $N$ .

		10	20	30	40	50
Beauty	#samples/s	5504	3256	2284	1776	1441
	HR@10	0.3006	0.3061	0.3057	0.3054	0.3047
	NDCG@10	0.1826	0.1875	0.1837	0.1833	0.1832
		10	50	100	200	400
ML-1m	#samples/s	14255	8890	5711	2918	1213
	HR@10	0.6788	0.6854	0.6947	0.6955	0.6898
	NDCG@10	0.4631	0.4743	0.4758	0.4759	0.4715

## Ablation Study

Table 5: Ablation analysis (NDCG@10) on four datasets. Bold score indicates performance better than the default version, while  $\downarrow$  indicates performance drop more than 10%.

Architecture	Dataset			
	Beauty	Steam	ML-1m	ML-20m
$L = 2, h = 2$	0.1832	0.2241	0.4759	0.4513
w/o PE	0.1741	0.2060	0.2155 $\downarrow$	0.2867 $\downarrow$
w/o PFFN	0.1803	0.2137	0.4544	0.4296
w/o LN	0.1642 $\downarrow$	0.2058	0.4334	0.4186
w/o RC	0.1619 $\downarrow$	0.2193	0.4643	0.4483
w/o Dropout	0.1658	0.2185	0.4553	0.4471
1 layer ( $L = 1$ )	0.1782	0.2122	0.4412	0.4238
3 layers ( $L = 3$ )	<b>0.1859</b>	<b>0.2262</b>	<b>0.4864</b>	<b>0.4661</b>
4 layers ( $L = 4$ )	<b>0.1834</b>	<b>0.2279</b>	<b>0.4898</b>	<b>0.4732</b>
1 head ( $h = 1$ )	<b>0.1853</b>	0.2187	0.4568	0.4402
4 heads ( $h = 4$ )	0.1830	<b>0.2245</b>	<b>0.4770</b>	<b>0.4520</b>
8 heads ( $h = 8$ )	0.1823	<b>0.2248</b>	0.4743	<b>0.4550</b>



# Links

1. [BERT4Rec: Sequential Recommendation with Bidirectional Encoder Representations from Transformer](#)
2. [Self-Attentive Sequential Recommendation](#)
3. [BERT: Pre-training of Deep Bidirectional Transformers for Language Understanding](#)
4. [The Illustrated BERT, ELMo, and co. \(How NLP Cracked Transfer Learning\)](#)
5. [Author's implementation on tensorflow](#)
6. [A Systematic Review and Replicability Study of BERT4Rec for Sequential Recommendation](#)