

Stability Analysis: Giesekus

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1 Equation Coefficients

1.1 A_{11} Equation

$$\begin{array}{l|l} A_{11} \omega = & \\ p & 0 \\ v_1 & -A_{11,x_{10}} + 2A_{11_0}ik_1 + 2A_{12_0}ik_2 \\ v_2 & -A_{11,x_{20}} \\ A_{11} & - (v_{1_0}ik_1 + v_{2_0}ik_2) + 2v_{1,x_{10}} - 1 - \alpha(2A_{11_0} - 2) \\ A_{12} & 2v_{1,x_{20}} - \alpha(2A_{12_0}) \\ A_{22} & 0 \end{array}$$

1.2 A_{12} Equation

$$\begin{array}{l|l} A_{12} \omega = & \\ p & 0 \\ v_1 & -A_{12,x_{10}} + A_{12_0}ik_1 + A_{22_0}ik_2 \\ v_2 & -A_{12,x_{20}} + A_{11_0}ik_1 + A_{12_0}ik_2 \\ A_{11} & v_{2,x_{10}} - \alpha(A_{12_0}) \\ A_{12} & - (v_{1_0}ik_1 + v_{2_0}ik_2) + v_{1,x_{10}} + v_{2,x_{20}} - 1 - \alpha(A_{11_0} + A_{22_0} - 2) \\ A_{22} & v_{1,x_{20}} - \alpha(A_{12_0}) \end{array}$$

1.3 A_{22} Equation

$$\begin{array}{l|l} A_{22} \omega = & \\ p & 0 \\ v_1 & -A_{22,x_{10}} \\ v_2 & -A_{22,x_{20}} + 2A_{12_0}ik_1 + 2A_{22_0}ik_2 \\ A_{11} & 0 \\ A_{12} & 2v_{2,x_{10}} - \alpha(2A_{12_0}) \\ A_{22} & - (v_{1_0}ik_1 + v_{2_0}ik_2) + 2v_{2,x_{20}} - 1 - \alpha(2A_{22_0} - 2) \end{array}$$

1.4 x_1 Momentum Equation

$$\begin{array}{l|l} El^{-1}v_1 \omega = & \\ p & -ik_1 \\ v_1 & -El^{-1}(v_{1,x_{10}} + v_{1_0}ik_1 + v_{2_0}ik_2) - \beta(k_1^2 + k_2^2) \\ v_2 & -El^{-1}v_{1,x_{20}} \\ A_{11} & ik_1 \\ A_{12} & ik_2 \\ A_{22} & 0 \end{array}$$

1.5 x_2 Momentum Equation

$$\begin{array}{l|l} El^{-1}v_2 \omega = & \\ p & -ik_2 \\ v_1 & -El^{-1}v_{2,x_{10}} \\ v_2 & -El^{-1}(v_{2,x_{20}} + v_{1_0}ik_1 + v_{2_0}ik_2) - \beta(k_1^2 + k_2^2) \\ A_{11} & 0 \\ A_{12} & ik_1 \\ A_{22} & ik_2 \end{array}$$

1.6 Mass Equation

0

$\omega =$

p	0
v_1	ik_1
v_2	ik_2
v_3	ik_3
A_{11}	0
A_{12}	0
A_{13}	0
A_{22}	0
A_{23}	0
A_{33}	0

2 Repeated Terms/Phrases

2.1 Most Helpful

$A_{11_0} ik_1 + A_{12_0} ik_2$

$A_{12_0} ik_1 + A_{22_0} ik_2 +$

$k_1^2 + k_2^2$

2.2 Also Helpful

$v_{1_0} ik_1 + v_{2_0} ik_2$

$v_{1,x_{20}} + v_{2,x_{10}}$