

# Stability Analysis: Giesekus

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## 1 Equation Coefficients

### 1.1 $A_{11}$ Equation

$$\begin{array}{l|l} A_{11} \omega = & \\ v_1 & -A_{11,x_{10}} + 2A_{11_0}ik_1 + 2A_{12_0}ik_2 + \frac{k_2}{k_1}A_{11,x_{20}} \\ A_{11} & - (v_{1_0}ik_1 + v_{2_0}ik_2) + 2v_{1,x_{10}} - 1 - \alpha(2A_{11_0} - 2) \\ A_{12} & 2v_{1,x_{20}} - \alpha(2A_{12_0}) \\ A_{22} & 0 \end{array}$$

### 1.2 $A_{12}$ Equation

$$\begin{array}{l|l} A_{12} \omega = & \\ v_1 & -A_{12,x_{10}} + A_{12_0}ik_1 + A_{22_0}ik_2 + \frac{k_2}{k_1}[A_{12,x_{20}} - A_{11_0}ik_1 - A_{12_0}ik_2] \\ A_{11} & v_{2,x_{10}} - \alpha(A_{12_0}) \\ A_{12} & - (v_{1_0}ik_1 + v_{2_0}ik_2) + v_{1,x_{10}} + v_{2,x_{20}} - 1 - \alpha(A_{11_0} + A_{22_0} - 2) \\ A_{22} & v_{1,x_{20}} - \alpha(A_{12_0}) \end{array}$$

### 1.3 $A_{22}$ Equation

$$\begin{array}{l|l} A_{22} \omega = & \\ v_1 & -A_{22,x_{10}} + \frac{k_2}{k_1}[A_{22,x_{20}} - 2A_{12_0}ik_1 - 2A_{22_0}ik_2] \\ A_{11} & 0 \\ A_{12} & 2v_{2,x_{10}} - \alpha(2A_{12_0}) \\ A_{22} & - (v_{1_0}ik_1 + v_{2_0}ik_2) + 2v_{2,x_{20}} - 1 - \alpha(2A_{22_0} - 2) \end{array}$$

### 1.4 Reduced Momentum Equation

$$\begin{array}{l|l} El^{-1} \left( k_2 + \frac{k_1^2}{k_2} \right) v_1 \omega = & \\ v_1 & -k_2 El^{-1}(v_{1,x_{10}} + 2(v_{1_0}ik_1 + v_{2_0}ik_2) - \frac{k_2}{k_1}v_{1,x_{20}}) + k_1 El^{-1}[v_{2,x_{10}} - \frac{k_2}{k_1}v_{2,x_{20}}] - 2k_2 \beta (k_1^2 + k_2^2) \\ A_{11} & ik_1 k_2 \\ A_{12} & ik_2^2 - ik_1^2 \\ A_{22} & -ik_1 k_2 \end{array}$$

## 2 Repeated Terms/Phrases

### 2.1 Most Helpful

$$\begin{array}{l} A_{11_0}ik_1 + A_{12_0}ik_2 \\ A_{12_0}ik_1 + A_{22_0}ik_2 \\ k_1^2 + k_2^2 \end{array}$$

### 2.2 Also Helpful

$$\begin{array}{l} v_{1_0}ik_1 + v_{2_0}ik_2 \\ v_{1,x_{20}} + v_{2,x_{10}} \end{array}$$