

Stability Analysis: Giesekus

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1 Equation Coefficients

1.1 A_{11} Equation

$$\begin{array}{l|l} A_{11} \omega = & \\ v_1 & -A_{11,x_{10}} + 2A_{11_0}ik_1 + 2A_{12_0}ik_2 + \frac{k_1}{k_2}A_{11,x_{20}} \\ A_{11} & - (v_{1_0}ik_1 + v_{2_0}ik_2) + 2v_{1,x_{10}} - 1 - \alpha(2A_{11_0} - 2) \\ A_{12} & 2v_{1,x_{20}} - \alpha(2A_{12_0}) \\ A_{22} & 0 \end{array}$$

1.2 A_{12} Equation

$$\begin{array}{l|l} A_{12} \omega = & \\ v_1 & -A_{12,x_{10}} + A_{12_0}ik_1 + A_{22_0}ik_2 + \frac{k_1}{k_2}[A_{12,x_{20}} - A_{11_0}ik_1 - A_{12_0}ik_2] \\ A_{11} & v_{2,x_{10}} - \alpha(A_{12_0}) \\ A_{12} & - (v_{1_0}ik_1 + v_{2_0}ik_2) + v_{1,x_{10}} + v_{2,x_{20}} - 1 - \alpha(A_{11_0} + A_{22_0} - 2) \\ A_{22} & v_{1,x_{20}} - \alpha(A_{12_0}) \end{array}$$

1.3 A_{22} Equation

$$\begin{array}{l|l} A_{22} \omega = & \\ v_1 & -A_{22,x_{10}} + \frac{k_1}{k_2}[A_{22,x_{20}} - 2A_{12_0}ik_1 - 2A_{22_0}ik_2] \\ A_{11} & 0 \\ A_{12} & 2v_{2,x_{10}} - \alpha(2A_{12_0}) \\ A_{22} & - (v_{1_0}ik_1 + v_{2_0}ik_2) + 2v_{2,x_{20}} - 1 - \alpha(2A_{22_0} - 2) \end{array}$$

1.4 Reduced Momentum Equation

$$\begin{array}{l|l} El^{-1}\omega(k_2 + \frac{k_1^2}{k_2})v_1 = & \\ v_1 & El^{-1}[k_1v_{1,x_{20}} - k_2(v_{1,x_{10}} + v_{1_0}ik_1 + v_{2_0}ik_2) + k_1v_{2,x_{10}} - \frac{k_1^2}{k_2}(v_{2,x_{20}} + v_{1_0}ik_1 + v_{2_0}ik_2)] - (k_2 + \frac{k_1^2}{k_2})\beta(k_1^2 + k_2^2) \\ A_{11} & ik_1k_2 \\ A_{12} & ik_2^2 - ik_1^2 \\ A_{22} & -ik_1k_2 \end{array}$$

2 Repeated Terms/Phrases

2.1 Most Helpful

$$\begin{array}{l} A_{11_0}ik_1 + A_{12_0}ik_2 \\ A_{12_0}ik_1 + A_{22_0}ik_2 \\ k_1^2 + k_2^2 \end{array}$$

2.2 Also Helpful

$$\begin{array}{l} v_{1_0}ik_1 + v_{2_0}ik_2 \\ v_{1,x_{20}} + v_{2,x_{10}} \end{array}$$