

1 Equation Coefficients

1.1 A_{11} Equation

$$A_{11i,j} \omega = \begin{array}{l|l} p_i & 0 \\ v_{1i,j} & -A_{11,x_{10}} \frac{1}{2\Delta x} \\ v_{1i+1,j} & 2A_{110} \frac{1}{2\Delta x} \\ v_{1i-1,j} & -2A_{110} \frac{1}{2\Delta x} \\ v_{1i,j+1} & 2A_{120} \frac{1}{2\Delta y} \\ v_{1i,j-1} & -2A_{120} \frac{1}{2\Delta y} \\ v_{2i,j} & -A_{11,x_{20}} \frac{1}{2\Delta y} \\ A_{11i,j} & 2v_{1,x_{10}} - 1 - \alpha(2A_{110} - 2) \\ A_{11i+1,j} & -v_{10} \frac{1}{2\Delta x} \\ A_{11i-1,j} & v_{10} \frac{1}{2\Delta x} \\ A_{11i,j+1} & -v_{20} \frac{1}{2\Delta y} \\ A_{11i,j-1} & v_{20} \frac{1}{2\Delta y} \\ A_{12i,j} & 2v_{1,x_{20}} - \alpha(2A_{120}) \\ A_{22i,j} & 0 \end{array}$$

1.2 A_{12} Equation

$$A_{12i,j} \omega = \begin{array}{l|l} p_{i,j} & 0 \\ v_{1i,j} & -A_{12,x_{10}} \frac{1}{2\Delta x} \\ v_{1i+1,j} & 2A_{120} \frac{1}{2\Delta x} \\ v_{1i-1,j} & -2A_{120} \frac{1}{2\Delta x} \\ v_{1i,j+1} & 2A_{220} \frac{1}{2\Delta y} \\ v_{1i,j-1} & -2A_{220} \frac{1}{2\Delta y} \\ v_{2i,j} & -A_{12,x_{20}} \frac{1}{2\Delta y} \\ v_{2i+1,j} & 2A_{110} \frac{1}{2\Delta x} \\ v_{2i-1,j} & -2A_{110} \frac{1}{2\Delta x} \\ v_{2i,j+1} & 2A_{120} \frac{1}{2\Delta y} \\ v_{2i,j-1} & -2A_{120} \frac{1}{2\Delta y} \\ A_{11i,j} & v_{2,x_{10}} - \alpha(A_{120}) \\ A_{12i,j} & v_{1,x_{10}} + v_{2,x_{20}} - 1 - \alpha(A_{110} + A_{220} - 2) \\ A_{12i+1,j} & -v_{10} \frac{1}{2\Delta x} \\ A_{12i-1,j} & v_{10} \frac{1}{2\Delta x} \\ A_{12i,j+1} & -v_{20} \frac{1}{2\Delta y} \\ A_{12i,j-1} & v_{20} \frac{1}{2\Delta y} \\ A_{22i,j} & v_{1,x_{20}} - \alpha(A_{120}) \end{array}$$

1.3 A_{22} Equation

$$A_{22i,j} \omega = \begin{array}{l|l} p_{i,j} & 0 \\ v_{1i,j} & -A_{22,x10} \\ v_{2i,j} & -A_{22,x20} \\ v_{2i+1,j} & 2A_{120} \frac{1}{2\Delta x} \\ v_{2i-1,j} & -2A_{120} \frac{1}{2\Delta x} \\ v_{2i,j+1} & 2A_{220} \frac{1}{2\Delta y} \\ v_{2i,j-1} & -2A_{220} \frac{1}{2\Delta y} \\ A_{11i,j} & 0 \\ A_{12i,j} & 2v_{2,x10} - \alpha(2A_{120}) \\ A_{22i,j} & 2v_{2,x20} - 1 - \alpha(2A_{220} - 2) \\ A_{22i+1,j} & -v_{10} \frac{1}{2\Delta x} \\ A_{22i-1,j} & v_{10} \frac{1}{2\Delta x} \\ A_{22i,j+1} & -v_{20} \frac{1}{2\Delta y} \\ A_{22i,j-1} & v_{20} \frac{1}{2\Delta y} \end{array}$$

1.4 x_1 Momentum Equation

$$El^{-1}v_{1i,j} \omega = \begin{array}{l|l} p_{i+1,j} & -\frac{1}{2\Delta x} \\ p_{i-1,j} & \frac{1}{2\Delta x} \\ v_{1i,j} & -El^{-1}v_{1,x10} - 2\beta \left(\frac{1}{\Delta x^2} + \frac{1}{\Delta y^2} \right) \\ v_{1i+1,j} & -El^{-1}v_{10} \frac{1}{2\Delta x} + \beta \frac{1}{\Delta x^2} \\ v_{1i-1,j} & El^{-1}v_{10} \frac{1}{2\Delta x} + \beta \frac{1}{\Delta x^2} \\ v_{1i,j+1} & -El^{-1}v_{20} \frac{1}{2\Delta y} + \beta \frac{1}{\Delta y^2} \\ v_{1i,j-1} & El^{-1}v_{20} \frac{1}{2\Delta y} + \beta \frac{1}{\Delta y^2} \\ v_{2i,j} & -El^{-1}v_{1,x20} \\ A_{11i+1,j} & \frac{1}{2\Delta x} \\ A_{11i-1,j} & -\frac{1}{2\Delta x} \\ A_{12i,j+1} & \frac{1}{2\Delta y} \\ A_{12i,j-1} & -\frac{1}{2\Delta y} \\ A_{22i,j} & 0 \end{array}$$

1.5 x_2 Momentum Equation

$$El^{-1}v_{2i,j} \quad \omega =$$

$p_{i,j+1}$	$-\frac{1}{2\Delta y}$
$p_{i,j-1}$	$\frac{1}{2\Delta y}$
$v_{1i,j}$	$-El^{-1}v_{2,x_{10}}$
$v_{2i,j}$	$-El^{-1}v_{1,x_{10}} - 2\beta \left(\frac{1}{\Delta x^2} + \frac{1}{\Delta y^2} \right)$
$v_{2i+1,j}$	$-El^{-1}v_{10} \frac{1}{2\Delta x} + \beta \frac{1}{\Delta x^2}$
$v_{2i-1,j}$	$El^{-1}v_{10} \frac{1}{2\Delta x} + \beta \frac{1}{\Delta x^2}$
$v_{2i,j+1}$	$-El^{-1}v_{20} \frac{1}{2\Delta y} + \beta \frac{1}{\Delta y^2}$
$v_{2i,j-1}$	$El^{-1}v_{20} \frac{1}{2\Delta y} + \beta \frac{1}{\Delta y^2}$
$A_{11i,j}$	0
$A_{12i+1,j}$	$\frac{1}{2\Delta x}$
$A_{12i-1,j}$	$-\frac{1}{2\Delta x}$
$A_{22i,j+1}$	$\frac{1}{2\Delta y}$
$A_{22i,j-1}$	$-\frac{1}{2\Delta y}$

1.6 Mass Equation

$$\varepsilon p_{i,j} \quad \omega =$$

$p_{i,j}$	0
$v_{1i+1,j}$	$\frac{1}{2\Delta x}$
$v_{1i-1,j}$	$-\frac{1}{2\Delta x}$
$v_{2i,j+1}$	$\frac{1}{2\Delta y}$
$v_{2i,j-1}$	$-\frac{1}{2\Delta y}$
$A_{11i,j}$	0
$A_{12i,j}$	0
$A_{22i,j}$	0