

Operations On Data

(Solutions to Solution to Review Questions and Problems)

Review Questions

- Q4-1.** Arithmetic operations interpret bit patterns as numbers. Logical operations interpret each bit as a logical value (*true* or *false*).
- Q4-3.** The bit allocation can be 1. In this case, the data type normally represents a logical value.
- Q4-5.** The decimal point of the number with the smaller exponent is shifted to the left until the exponents are equal.
- Q4-7.** The common logical binary operations are: AND, OR, and XOR.
- Q4-9.** The NOT operation inverts logical values (bits): it changes *true* to *false* and *false* to *true*.
- Q4-11.** The result of an OR operation is true when one or both of the operands are true.
- Q4-13.** An important property of the AND operator is that if one of the operands is false, the result is false.
- Q4-15.** An important property of the XOR operator is that if one of the operands is true, the result will be the inverse of the other operand.
- Q4-17.** The AND operator can be used to clear bits. Set the desired positions in the mask to 0.
- Q4-19.** The logical shift operation is applied to a pattern that does not represent a signed number. The arithmetic shift operation assumes that the bit pattern is a signed number in two's complement format.

Problems

P4-1.

a.	NOT (99)₁₆	=	NOT (10011001)₂	=	(01100110)₂	=	(99)₁₆
b.	NOT (FF)₁₆	=	NOT (11111111)₂	=	(00000000)₂	=	(00)₁₆
c.	NOT (00)₁₆	=	NOT (00000000)₂	=	(11111111)₂	=	(FF)₁₆
d.	NOT (01)₁₆	=	NOT (00000001)₂	=	(11111110)₂	=	(FE)₁₆

+ $(\overline{B}_M + 1)$. Since there is no overflow $R_M = (\overline{R}_M + 1)$ and $R_S = B_S$ The result

	No overflow				1	1	Carry
A_S		0	0	1	0	0	A_M
B_S	+	1	1	0	1	0	$\overline{(B_M + 1)}$
		1	1	1	1	0	R_M
R_S		0	0	0	0	1	$R_M = (\overline{R}_M + 1)$

$(10000100)_2 = -4$ as expected.

- c. $-19 + 23 \rightarrow A = -19 = (10010011)_2$ and $B = 23 = (00010111)_2$. Operation is addition, sign of B is not changed. $S = A_S \text{ XOR } B_S = 1$, $R_M = A_M + (\overline{B}_M + 1)$. Since there is no overflow $R_M = (\overline{R}_M + 1)$ and $R_S = B_S$

	No overflow				1	1	Carry
A_S		0	0	1	0	0	A_M
B_S	+	1	1	0	1	0	$\overline{(B_M + 1)}$
		1	1	1	1	0	R_M
R_S		0	0	0	0	1	$R_M = (\overline{R}_M + 1)$

The result is $(00000100)_2 = 4$ as expected.

- d. $-19 - 23 \rightarrow A = -19 = (10010011)_2$ and $B = 23 = (00010111)_2$. Operation is subtraction, sign of B is changed. $S = A_S \text{ XOR } B_S = 0$, $R_M = A_M + B_M$ and $R_S = A_S$

	No overflow				1	1	1	1	Carry
A_S		0	0	1	0	0	1	1	A_M
B_S	+	0	0	1	0	1	1	1	B_M
R_S		0	1	0	1	0	1	0	R_M

The result is $(10101010)_2 = -42$ as expected.

P4-19. We assume that both operands are in the presentable range.

- Overflow can occur because the magnitude of the result is greater than the magnitude of each number and could fall out of the presentable range.
- Overflow does not occur because the magnitude of the result is smaller than one of the numbers; the result is in the presentable range.
- When we subtract a positive integer from a negative integer, the magnitudes of the numbers are added. This is the negative version of case a. Overflow can occur.
- When we subtract two negative numbers, the magnitudes are subtracted from each other. This is the negative version of case b. Overflow does not occur.

- P4-21.** The result is a number with all 0's which has the value of 0. For example, if we add number $(10110101)_2$ in 8-bit allocation to its two's complement $(01001011)_2$ we obtain

								Decimal equivalent
1	1	1	1	1	1	1	1	Carry
	1	0	1	1	0	1	0	-74
+	0	1	0	0	1	0	1	+74
	0	0	0	0	0	0	0	0

We use this fact in normal mathematical calculation in the computers.