Functors and lifting

Functors are like cranes lifting a function into a context

class Functor f where $f_{map} :: (a \rightarrow b) \rightarrow f_a \rightarrow f_b$

It's like function application in the context of f:

(\$) :: $(a \rightarrow b) \rightarrow a \rightarrow b$ (\$>) :: Functor $f \Rightarrow (a \rightarrow b) \rightarrow f a \rightarrow f b$

Let's work through an example

let replace = const "a" <- function to apply
let value = [Just ["this", "that"]] <- variable to change

replace value <- apply to []
"a"

fmap replace value <- lift once - apply to Just
["a"]

(fmap . fmap) replace value <- lift twice - apply to the internal list
[Just "a"]

(fmap . fmap . fmap) replace value <- lift thrice - apply to the elements of the internal list
[Just ["a", "a"]]

(fmap . fmap . fmap . fmap) replace value <- lift one last time - apply to each letter of each string
[Just [["a", "a", "a", "a", "a"], ["a", "a", "a", "a", "a"]]]