

# Schwenker Assignment 13

Anne Schwenker

November 23, 2019

(

$$\int x 4e^{-7x} dx$$

$$u = -7x \quad du/dx = d/dx(-7x) = -7 \quad du = -7dx =$$

$$\int 4e^{-7x} dx = \int -1/7(-7)4e^{-7x} dx$$

=

$$-1/7 \int x 4e^{-7x} (-7dx) = \int -1/7(-7)4e^u du$$

$$-4/7 \int e^u du = -(4/7)e^u + c$$

replace u with -7x  $-(4/7)e^{-7x} + c$

Biologists are treating a pond contaminated with bacteria. The level of contamination is changing at a rate of  $dN/dt = 3150/t^4 - 220$  bacteria per cubic centimeter per day, where t is the number of days since treatment began. Find a function  $N(t)$  to estimate the level of contamination if the level after 1 day was 6530 bacteria per cubic centimeter.

$$N(t) = dn/dt = \int (3150t^4 - 220) dt$$

$$N(t) = 1050/t^3 - 220t + c$$

$$N(t) = 1050/t^3 - 220t + C$$

$$N(1) = 1050 - 220 + C = 6530$$

$$C = 5700$$

$$N(t) = 1050/t^3 - 220t + 5700$$

3. Find the total area of the red rectangles in the figure below, where the equation of the line is  $f(x) = 2x - 9$ .

$$Area = \int_{-1}^4 (2x - 9) dx$$

$$Area = (8.5 - 9)(8.5 + C) - (4.5 - 9)(4.5 + C) = 16$$

4. Find the area of the region bounded by the graphs of the given equations.  $y = x^2 - 2x - 2$ ,  $y = x + 2$   
 $x + 2 = x^2 - 2x - 20 = x^2 - 3x - 40 = (x - 4)(x + 1)$

$$\int_1^4 (x + 2)(x^2 - 2x - 2) dx$$

$$\int_{-1}^4 (x^2 + 3x + 4) dx$$

$$= -x^{3/3+3} \cdot 2/2 + 4x|_{-1}^4 - (-4^{3/3+3} \cdot 2/2 + 4(-1)) - (-(-1)^{3/3+3} \cdot 2/2 + 4(-1)) = 20.83333$$

5. A beauty supply store expects to sell 110 flat irons during the next year. It costs \$3.75 to store one flat iron for one year. There is a fixed cost of \$8.25 for each order. Find the lot size and the number of orders per year that will minimize inventory costs. Without knowing the sales rate, 1 order will always be the lowest cost. If it were known how long it takes to sell a flat iron once it comes in, then daily storage rates could be calculated

```
OrderYCostAll=vector()
Orders = vector()
for (i in 1:110){
  x=i
  YCostStorage = 3.75*(x*(110/x))
  YOrderCost = 8.25*(x)
  OrderYCost = YCostStorage+YOrderCost
  Orders = c(OrderYCostAll,x)
  OrderYCostAll=c(OrderYCostAll,OrderYCost)}

print(paste("number of orders",1,"costs ",min(OrderYCostAll)))

## [1] "number of orders 1 costs 420.75"
```

$$\int \ln(9x) * (x^6) dx$$

$$u=9x, du/dx = 1/x$$

$$dv/dx = x^6, v = \int x^6 dx = 1/7 x^7$$

$$\int u \frac{dv}{dx} dx = uv - \int v \frac{du}{dx} dx$$

$$\int \ln(9x) x^6 dx = \frac{1}{7} x^6 dx$$

$$\frac{7}{49} x^7 \ln(9x) - \frac{1}{49} x^7 + c$$

$$\frac{1}{49} (7 \ln(9x) - 1) + c$$

Determine whether f(x) is a probability density function on the interval

$[1, e^6]$  If not, determine the value of the definite integral.

$$f(x) = \frac{1}{6}$$

$$\int_{e^6}^1 \frac{1}{6x} dx = \frac{1}{6} \ln(x) \Big|_{e^6}^1$$

$$\frac{1}{6} \ln(e^6) - \frac{1}{6} \ln(1) = 1$$