

### Step 1

- \*Convert Grayscale
- \*Global Binary Threshold
- \*Sobel Filter
- \*Neighborhood And Operator

## Step 2

- \*Create Transformation Matrix
- \*Apply Trans. Matrix
- \*Interpolation
- \*Plot Histogram

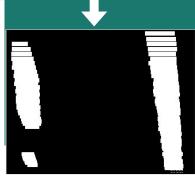
## Step 3

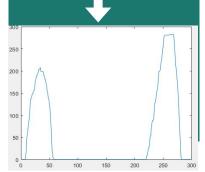
- \*Calculate Standard Deviation
- \*Calculate Mean
- \*Calculate MSE
- \*Determine Right/Left Region

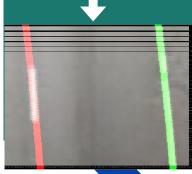
## Step 4

- \*Calculate Polynomial with LSE
- \*Draw Polynomial Line
- \*Shift Lane
- \*Result Image









## STEP 1

**Convert Grayscale** 

**Global Binary Threshold** 

Sobel Filter

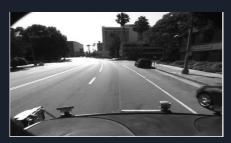
Neighborhood AND Operator

$$I_G(i,j) = 0.299 I_{RGB}(i,j,R) + 0.587 I_{RGB}(i,j,G) + 0.114 I_{RGB}(i,j,B)$$

$$I_B(i,j) = \begin{cases} 1, & \text{if } I_G(i,j) \ge th \\ 0, & \text{if } I_G(i,j)$$

Vertical Line: 
$$\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$
, Horizontal Line: 
$$\begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

$$I(i,j) = \begin{cases} 0 & \text{if } \left( \sum_{l=l-k}^{i+k} \sum_{m=j-k}^{j+k} I_{B1}(l,m) \right) \cdot \left( \sum_{l=i-k}^{i+k} \sum_{m=j-k}^{j+k} I_{B2}(l,m) \right) = 0 \\ & \text{otherwise} \end{cases}$$









## STEP 2

**Create Transformation Matrix** 

Apply Trans. Matrix

Interpolation

Plot Histogram

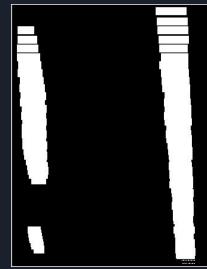
$$[C] = [B] [A]$$
  $[A] = [B-1] [C]$ 

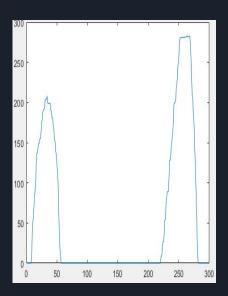
$$\begin{bmatrix} \mathbf{X_1} \\ \mathbf{Y_1} \\ \mathbf{X_2} \\ \mathbf{Y_2} \\ \mathbf{X_3} \\ \mathbf{Y_3} \\ \mathbf{X_4} \\ \mathbf{Y_4} \end{bmatrix} = \begin{bmatrix} x_1 & y_1 & 1 & 0 & 0 & 0 & -x_1\mathbf{X_1} & -y_1\mathbf{X_1} \\ 0 & 0 & 0 & x_1 & y_1 & 1 & -x_1\mathbf{Y_1} & -y_1\mathbf{Y_1} \\ x_2 & y_2 & 1 & 0 & 0 & 0 & -x_2\mathbf{X_2} & -y_2\mathbf{X_2} \\ 0 & 0 & 0 & x_2 & y_2 & 1 & -x_2\mathbf{Y_2} & -y_2\mathbf{Y_2} \\ x_3 & y_3 & 1 & 0 & 0 & 0 & -x_3\mathbf{X_3} & -y_3\mathbf{X_3} \\ 0 & 0 & 0 & x_3 & y_3 & 1 & -x_3\mathbf{Y_3} & -y_3\mathbf{Y_3} \\ x_4 & y_4 & 1 & 0 & 0 & 0 & -x_4\mathbf{X_4} & -y_4\mathbf{X_4} \\ 0 & 0 & 0 & x_4 & y_4 & 1 & -x_4\mathbf{Y_4} & -y_4\mathbf{Y_4} \end{bmatrix} \begin{bmatrix} a_{11} \\ a_{12} \\ a_{13} \\ a_{21} \\ a_{22} \\ a_{23} \\ a_{31} \\ a_{32} \end{bmatrix}$$

$$\begin{bmatrix} X_1 z \\ Y_1 z \\ z \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix}$$

$$\mathbf{X} = \frac{a_{00}\mathbf{x} + a_{01}\mathbf{y} + a_{02}}{\mathbf{z}}$$
$$\mathbf{Y} = \frac{a_{10}\mathbf{x} + a_{11}\mathbf{y} + a_{12}}{\mathbf{z}}$$









	Kaynak Noktalar	Hedef Noktalar
1.nokta	x1 = 160 , y1 = 120	X1 = 0 , Y1 = 0
2.nokta	x2 = 160 , y2 = 210	X2 = 0 , Y2 =300
3.nokta	x3 = 210 , y3 = 75	X3 = 300 , Y3 = 0
4.nokta	x4 = 210 , y4 = 255	X4 = 300 , Y4 = 300

$$\begin{bmatrix} X_1 z \\ Y_1 z \\ z \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} X_1 \\ Y_1 \\ X_2 \\ Y_2 \\ X_3 \\ X_4 \\ Y_4 \end{bmatrix} = \begin{bmatrix} x_1 & y_1 & 1 & 0 & 0 & 0 & -x_1X_1 & -y_1X_1 \\ 0 & 0 & 0 & x_1 & y_1 & 1 & -x_1Y_1 & -y_1Y_1 \\ 0 & 0 & 0 & x_2 & y_2 & 1 & -x_2Y_2 & -y_2Y_2 \\ 0 & 0 & 0 & x_2 & y_2 & 1 & -x_2Y_2 & -y_2Y_2 \\ x_3 & y_3 & 1 & 0 & 0 & 0 & -x_3X_3 & -y_3X_3 \\ 0 & 0 & 0 & x_3 & y_3 & 1 & -x_3Y_3 & -y_3Y_3 \\ 0 & 0 & 0 & x_4 & y_4 & 1 & -x_4Y_4 & -y_4Y_4 \\ 0 & 0 & 0 & x_4 & y_4 & 1 & -x_4Y_4 & -y_4Y_4 \end{bmatrix} \begin{bmatrix} a_{11} \\ a_{12} \\ a_{13} \\ a_{21} \\ a_{22} \\ a_{23} \\ a_{31} \\ a_{32} \end{bmatrix}$$

$$X = \frac{a_{00}x + a_{01}y + a_{02}}{z}$$

$$Y = \frac{a_{10}x + a_{11}y + a_{12}}{z}$$



Calculate Mean

#### Calculate MLE

Determine Right/Left Region

$$\mu_{\rm l} = \frac{2}{N} \sum_{j=1}^{N/2} \sum_{i=1}^{M} j \cdot I(i, j);$$

$$\mu_{\rm r} = \frac{2}{N} \sum_{j=N/2+1}^{N} \sum_{i=1}^{M} j I(i, j);$$

$$\sigma_l^2 = \frac{2}{N} \sum_{j=1}^{N/2} \sum_{i=1}^{M} I(i,j) \cdot (j - \mu_l)^2$$

$$\sigma_r^2 = \frac{2}{N} \sum_{j=N/2+1}^{N} \sum_{i=1}^{M} I(i,j)(j - \mu_r)^2$$

Choose left region, if  $(t P_1 - \sigma_1) \ge (t P_r - \sigma_r)$ 

Choose right region, if  $(t P_1 - \sigma_1) < (t P_r - \sigma_r)$ 

## STEP 4

**Calculate Polynomial with LSE** 

**Draw Polynomial Line** 

Shift Lane

Finish

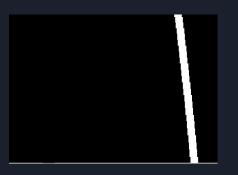
$$ai^2 + bi + c = j$$

Then, the LSE formulation determines a, b, c as

$$\bar{x} = (A^T A)^{-1} A^T \bar{j}$$

With the matrices and vectors

$$A = \begin{bmatrix} i_1^2 & i_1 & 1 \\ i_2^2 & i_2 & 1 \\ \vdots & \vdots & \vdots \\ i_N^2 & i_N & 1 \end{bmatrix}, \bar{x} = \begin{bmatrix} a \\ b \\ c \end{bmatrix}, \bar{J} = \begin{bmatrix} j_1 \\ j_2 \\ \vdots \\ j_N \end{bmatrix}$$







# Teşekkürler