$STK1100-Oblig\ 1$

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Kode og figurer ligger til slutt.

0161a)	- Han spiller et gitt antall n=20 ganger.
	- H vest spill hav for ulfall
	- Smillene er une bengral.
	- samsguligheten for sukcess en konstant.
	h = 20, $p = 18/17$, $P(X) = L(x; 20, 13,7)$, $L = 18$
	$E(x) = np = 20.\frac{18}{37} = 9,73$
	$SO(X) = \sqrt{npq'} = \sqrt{20.\frac{18}{37}.(1-\frac{19}{37})} = 2,235$
(b)	$y = \chi \left(\frac{36}{18} - 1\right) \cdot 100 - 100 \left(20 - \chi\right) = 100 \times + 100 \times - 2000$ $= 200 \times - 2000 = 200 \left[\chi - 10\right]$
	E(y) = 200 E(x) - 2000 = 200.9,73 - 2000 = -54
	$V(y) = E(y^2) - E(y)^2 = E([200x - 2000]^2) - (-54)^2$
	$= E(200^{2}X^{2} - 8e5X + 2000^{2}) - 2916$ $= 4e4 E(X^{2}) - 8e5E(X) + 4e6 - 2916$
	$=M''_{x(t)}=h(u-1)\rho^{2}+n\rho=2o(2o-1)\frac{1}{772}+2o\frac{18}{37}=99.669$
	$= 4 \cdot 4 \cdot 99,7 - 8 \cdot 5 \cdot 20' \cdot \frac{19}{37} + 4 \cdot 6 - 2916 = \frac{799200}{37}$
	$50(Y) = \sqrt{V(X)^2} \approx 450$

<i>c)</i>	$P(y) = P(x) = L(x; 20, \frac{18}{37})$
	3000 - 10
	$y = 200 \times -2000 \ge 1000 = 0 \times \ge \frac{3000}{200} = 15$
	Vinne 7000 hr eller mer; X≥15
	$Y = 200 \times -2000 \langle -1000 = P \times \langle \frac{1000}{200} = 5$
	Tape 1000 her eller men; X 5 5
python ($P(Y \ge 1000) = P(x \ge 15) = \frac{2^{\circ}}{\sum_{x=15}^{2}} L(x; 20, \frac{18}{37}) = 0.0154$
	$P(x \le -1000) = P(x \le 5) = \sum_{x=0}^{5} L(x; 20, \frac{18}{57}) = 0,0275$
d)	$P(Y) = P(X) = \lambda \left(X', 20, \frac{6}{32} \right)$
a 18.11	$Y = X(\frac{36}{6}-1) \cdot 100 - 100(20-X) = 500X + 100x - 2000$
9	= 600×-2000
	$Y = 600 \times -2000 \ge 1000 \implies X \ge \frac{3000}{600} = 5$
	Vinse 1000 hr eller men: # \$ 5
	$y = 600 \times -2000 \leq -1000 \Rightarrow \times \leq \frac{1000}{600} = \frac{5}{3} = 1.666$
	Tape 1000 hr ella men: X ≤ 1
gyllon.	$P(y \ge 1000) = P(x \ge 5) = \sum_{x=5}^{20} L(x; 20, \frac{6}{37}) = 0.214$
	$P(\gamma \leq -1000) = P(\chi \leq 1) = \sum_{\chi=0}^{6} L(\chi; 20, \frac{6}{34}) = 0.141.$
1	

e)	$P(z) = \left(\frac{36}{37}\right)^{z-1} \left(\frac{1}{37}\right)$
	First fame så vinner
	7-1 ganger in gang.
	$y = \frac{36}{1} \cdot 100 \times -100 \cdot 7$
	1 x = 1. Har me vine 1 gang for a hume time 2000 hr.
	$= 3600 - 1607 \ge 1000 \Rightarrow 7 \ge \frac{3600 - 1000}{100} = 26$
2 withon.	2 (22) = 5
	$P(y \ge 1000) = \sum_{z=1}^{26} P(z) \approx 0.51$
	P(y5-1000) = 1-P(x7-1000)
	y = 3600 - 100 ₹ > -1000 ₽ ₹ > 3600 +1000 = 46
и. ($P(Y)-1000) = \sum_{\xi=0}^{45} P(\xi) = 0.71$
Cyphon	₹ = (
-	P(ys-1000) = 1 - 0709 = 0.29
	<u> </u>

	OPPGAVE 2
a)	
	P(X) = 5 avergenlighet for X gjenstående år (fra 35)
	9 x = Samurguligheta for a do i popet an necte an
	and the same has been a second as the same
	Hvis 9x en sannsynligheber for å do innen et av i en alden
	x, er (1- 9x) samsynligheten for i onerleve det neste
	auch. Da en $(1-9,c)(1-9,c)=(1-9,c)=T(1-9,c)$
	9≤x
	Earnantigheben for à overleve de neste x avene.
	P effe Liberous P (x EX) = tr (1-4437) = 1-P(8 = x)
	Son gir
	$F(x) = P(X \le x) = 7 - \prod_{y=0}^{\infty} (1 - 4_{15+y})$
	y=0
h)	$F(x) - F(x-1) = \sum_{y \leqslant x} P(y) - \sum_{y \leqslant x-1} P(y) = P(x)$
-	9 € × 9 € × - ι

d) His X 534 blir bon under 70 ar, og fan ingen pensjon. P et er da ingen naverdi (h(X)=0). Penginen utbebalt om he år vil ha en nånesti på 100'000/1.03 E Herrom utbetalringene gan over flere år, fra 35 år for in til X år fra nå, vil den bobele vanishien bli $h(X) = \sum_{k=35}^{X} \frac{10000}{1.03^k} = 100000 \sum_{k=35}^{X} 1.03^{-k}$ $h(x) = 100000 \left[-\frac{1.03^{34} - 1.03}{1 - 7.03} \right]$ $= \frac{100000}{1.03^{25}} \left[\frac{1.03^{-34} - 1.03}{1 - 7.03} \times \frac{1.03^{25}}{1.05^{-1}} \right]$ $= \frac{100000}{1.03^{15}} \left[\frac{1.03^{24-X}}{1.03-1} - \frac{100000}{1.03^{35}} \right] \frac{1-1}{1.03-1}$ $(x) \quad \mathbb{E}\left[h(x)\right] = \sum_{x \in \mathcal{X}} h(x) P(x) = \sum_{x \in \mathcal{X}} h(x) P(x)$ $= \frac{\sum_{x=1}^{24} h(x) \rho(x) + \sum_{x=15}^{24} h(x) \rho(x)}{x^{235}}$ $= \frac{\sum_{x=35}^{71} \frac{1.0000}{1.03^{75}} \frac{1 - (1/1.03)^{x-34}}{1 - 1/4.03} \cdot P(X)$ $= \frac{100006}{1.03^{17}} \qquad P(x \ge 35) - \sum_{x=3}^{71} (1/1.05)^{x-34} P(x)$

5)
$$E[\lambda(X)] = 397000 \text{ he}$$
 (is hoole)

9) N inverties as an energy implefult on λ as an $K \cdot \frac{1}{1.01^4}$
 E Huran has between as the K horst air, when L has also in ables (70, what; 39 air, this wa = various; $M_{K}(Y,Y) = X \cdot Y_{K}(X) = X \cdot Y_{K$

 $i) \quad E[g(x)] = 21.56$ $i) \quad K = \frac{E[L(x)]}{E[g(x)]} = 17.952 \text{ hr}$

Oppgave 1c and 1d

```
from scipy import misc
import numpy as np
p = 18/37
n = 20
def binom(x, n, p):
    """ Binomial probability b(x;n,p)"""
   nCr = misc.comb(n, x)
   return nCr*p**x*(1-p)**(n-x)
def cum_binom(x_min, x_max, n, p):
    """ Cumulative distribution function F(x_min \le x \le x_max)
for a binomial function b(x;n,p) """
   P_X = 0
   for x in range(x_min, x_max+1):
      P_X += binom(x, n, p)
   return P_X
#___Exercise c__
print( cum_binom(15,20,n,p) )
print( cum_binom(0,5,n,p) )
#___Exercise d___
p = 6/37
EX = 0
for i in range(0,20):
   EX += (cum_binom(i,i,n,p))*500*i
print( cum_binom(5,20,n,p) )
print( cum_binom(0,1,n,p) )
jonas@ubuntu:~/github/other_courses/STK1100/oblig1/src$ python3 1cd.py
0.015385465001631102
0.027464357940763788
0.21400681498120722
0.14151896666419134
```

Oppgave 1e og f

```
#__Exercise 1e___
P = 0
for Z in range(1,26+1):
    P += (36/37)**(Z-1) * 1/37
print(P)

#__Exercise 1f___
P = 0
for Z in range(1,45+1):
    P += (36/37)**(Z-1) * 1/37
print(1-P)

"""
jonas@ubuntu:~/github/other_courses/STK1100/oblig1/src$ python3 1ef.py
0.5095212523720186
0.2914304665172236
"""
```

Oppgave 2c

```
import numpy as np
import matplotlib.pyplot as plt

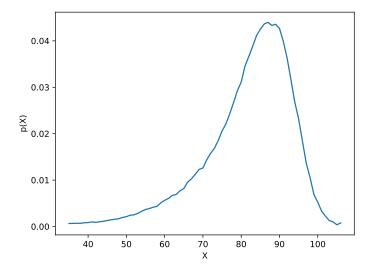
data = np.genfromtxt("dodelighet-felles.txt")[1:]
data = np.transpose(data)
```

```
ald, q_x = data

def F(x):
    value = 1
    for y in range(x+1):
        value **= (1-q_x[y+35]/1000)
    return 1 - value

p = np.zeros(72)
for x in range(72):
    p[x] = F(x) - F(x-1)

plt.plot(ald[35:], p)
plt.xlabel("X")
plt.ylabel("p(X)")
plt.savefig("../2c.pdf")
```



Oppgave 2f

```
import numpy as np
import matplotlib.pyplot as plt
def h(X):
   if X < 35:
    else:
       return 1e5/1.03**35 * (1-(1/1.03)**(X-34))/(1-1/1.03)
data = np.genfromtxt("dodelighet-felles.txt")[1:]
data = np.transpose(data)
ald, q_x = data
def F(x):
   value = 1
    for y in range(x+1):
       value *= (1-q_x[y+35]/1000)
   return 1 - value
p = np.zeros(72)
for x in range(72):
   p[x] = F(x) - F(x-1)
E_h_X = 0
for x in range(72):
   E_h_X += h(x)*p[x]
print(E_h_X)
```

```
jonas@ubuntu:~/github/other_courses/STK1100/oblig1/src$ python3 2f.py 387141.5341685992
```

Oppgave 2i

```
import numpy as np
import matplotlib.pyplot as plt
def g(X):
    if X > 34:
       X = 34
    return (1-(1/1.03)**(X+1))/(1-(1/1.03))
data = np.genfromtxt("dodelighet-felles.txt")[1:]
data = np.transpose(data)
ald, q_x = data
def F(x):
    value = 1
    for y in range(x+1):
        value *= (1-q_x[y+35]/1000)
    return 1 - value
p = np.zeros(72)
for x in range(72):
    p[x] = F(x) - F(x-1)
E_gX = 0
for x in range(72):
E_g_X += g(x)*p[x]
print(E_g_X)
jonas@ubuntu:~/github/other_courses/STK1100/oblig1/src$ python3 2i.py
21.564918895029948
```