

CSCA 67.

1 a).

p.	q.	r.	$p \leftrightarrow q$	$(p \leftrightarrow q) \rightarrow r$
T	T	T	T	F
T	T	F	T	T
T	F	T	F	F
T	F	F	F	F
F	T	T	F	F
F	T	F	F	F
F	F	T	T	F
F	F	F	T	T

b).  $(\neg p \wedge q) \vee (\neg q \wedge p) \vee r$ .

c) using the  $\rightarrow$  law, DeMorgan's law & the Biconditional law.

d)  $(p \leftrightarrow q) \rightarrow r$ .

$\hookrightarrow (p \rightarrow q) \wedge (q \rightarrow p) \rightarrow r$

$\hookrightarrow (\neg p \vee q) \wedge (\neg q \vee p) \rightarrow r$

$\hookrightarrow \neg((\neg p \vee q) \wedge (\neg q \vee p)) \vee r$

$\hookrightarrow \neg(\neg p \vee q) \vee \neg(\neg q \vee p) \vee r$

$\hookrightarrow (p \wedge \neg q) \vee (q \wedge \neg p) \vee r$

$\hookrightarrow (\neg p \wedge q) \vee (\neg q \wedge p) \vee r$

Biconditional.

$\rightarrow$  law.

$\rightarrow$  law

DeMorgan's law.

2. (a) 1 2 3 4 6

(b) 1 2 3 4 6 7 8

(c) 2, 6 4, 8

(d) 6, 2, 4, 8.

(e) 1 2 3 4 7 8 + 6.

3.  $\rightarrow$  means that only true when  $p$  is True,  $q$  is False.

$\Leftrightarrow$  means the common parts for both (both true or both false).

4. left side  ~~$\neg$~~   $\neg r \rightarrow \neg(p \vee q)$   
 $\hookrightarrow r \vee \neg(p \vee q)$   
 $\hookrightarrow \neg(p \vee q) \vee r.$

right side  $(p \rightarrow q) \rightarrow r.$   
 $\hookrightarrow \neg(p \rightarrow q) \vee r.$

as  $(p \vee q)$  is not equal to  $(p \rightarrow q)$ ,  
left side is not equal to the right side.  
The statement is disapproved.

To disapprove an equivalence without providing the entire truth table, you need to show that they're different at the same place.

