

日期: / 贾星宇 202000300125

7.30 $R(U, F) : U = \{A, B, C, D, E, G\}$

$F = \{A \rightarrow BCD, BC \rightarrow DE, B \rightarrow D, D \rightarrow A\}$

a. $B^+ = \{A, B, C, D, E\}$

b. 即证: $AG \rightarrow U$

$\because A \rightarrow BCD$

$\therefore A \rightarrow BC$ (分解律) ①

$\because BC \rightarrow DE$

$\therefore A \rightarrow DE$ (传递律) ②

$\therefore A \rightarrow BCDE$ (合并律)

$\therefore A \rightarrow ABCDE$ (增广律)

$\therefore AG \rightarrow ABCDEG$ (增广律)

$\therefore AG \rightarrow U$ 证毕

c. ① 对 $A \rightarrow BCD$, 当属性 D 去除后, 变为 $A \rightarrow BC$

$\because BC \rightarrow DE$ 由传递律, $A \rightarrow DE$; 由分解律, $A \rightarrow D$

故 D 为无关属性;

$A \rightarrow BC; BC \rightarrow DE; B \rightarrow D; D \rightarrow A$

② 对 $BC \rightarrow DE$, 去掉 C , $\because B \rightarrow D, D \rightarrow A, A \rightarrow BC, BC \rightarrow DE$

$\therefore B \rightarrow DE$ 故 C 为无关属性

$A \rightarrow BC; B \rightarrow DE; B \rightarrow D; D \rightarrow A$

③ 对 $B \rightarrow DE$: 去掉 D : $B \rightarrow D$ 依旧可得 故 D 为无关属性,

$A \rightarrow BC; B \rightarrow E; B \rightarrow D; D \rightarrow A$

④ 合并 $B \rightarrow E, B \rightarrow D$: $A \rightarrow BC; B \rightarrow DE; D \rightarrow A$

故 $F_c = \{A \rightarrow BC, B \rightarrow DE, D \rightarrow A\}$

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$$U = \{A, B, C, D, E, G\}$$

d. $F_c = \{A \rightarrow BC, B \rightarrow DE, D \rightarrow A\}$

① 找候选码: 无主属性. 不唯一:

$$AG, DG, BG$$

故由 $A \rightarrow BC$ 知此模式 $\notin 3NF$. 故分解:

② 按相同左部: $\{A, B, C\}$

$$\{B, D, E\}$$

$$\{D, A\}$$

$$\{G\}$$

③ 不存在属性因多候选码, 故:

$$P = \{R_1 \langle (A, B, C), (A \rightarrow BC) \rangle, R_2 \langle (B, D, E), (B \rightarrow DE) \rangle, \\ R_3 \langle (D, A), (D \rightarrow A) \rangle, R_4 \langle (G) \rangle, R_5 \langle (A, G) \rangle\}$$

e. $U = \{A, B, C, D, E, G\}$

$$F = \{A \rightarrow BCD, BC \rightarrow DE, B \rightarrow D, D \rightarrow A\}$$
 不符合 BCNF, 故分解:

① $A \rightarrow BCD$: $\{A, E, G\}$ $\{A, B, C, D\}$

② $A \rightarrow BCD$ $\left\{ \begin{array}{l} \text{分解} \\ A \rightarrow BC \\ \text{分解} \\ A \rightarrow DE \\ \text{分解} \\ A \rightarrow E \end{array} \right\} \left\{ \begin{array}{l} \{A, G\} \\ \{A, E\} \end{array} \right.$

$B \rightarrow D$: $\{A, B, C\}$ $\{B, D\}$

$A \rightarrow BC$ $\left\{ \begin{array}{l} \text{分解} \\ A \rightarrow B \end{array} \right\} \left\{ \begin{array}{l} \{A, C\}, \{A, B\}, \{B, D\} \end{array} \right.$

综上, 为 $\{A, B\}, \{A, C\}, \{B, D\}, \{A, E\}, \{A, G\}$.