# Day 4 Hands on: Forces and phonons

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#### Today's theme:

- 1) Relaxations: adsorption of oxygen on graphene and automatic lattice constant optimization
- 2) Phonons: compute phonon in  $\Gamma$  and along the BZ, for Si and AlAs

# Exercise 1: Learning Goals: optimize atomic position and lattice constants

#### **Exercise 1**

#### Topics of the exercise:

- 1. How to perform relaxation of atomic structure (graphane and oxygen adsorption)
- 2. Understanding forces.
- 3. Optimizing the lattice constant of Silicon and comparing with total energy approaches
- 4. Understanding stresses.

## Exercise 1.1: graphane and O adsorption

#### Input file scf calculation

```
&CONTROL
calculation = 'scf'.
prefix = 'Graphane',
outdir = '/tmp',
pseudo dir = '../../pseudo',
&SYSTEM
&ELECTRONS
conv thr = 1.0d-8
ATOMIC SPECIES
C 12.0107 C.pbe-rrkjus.UPF
H 1.00007 H.pbe-rrkjus.UPF
ATOMIC POSITIONS alat
K POINTS automatic
991 000
```

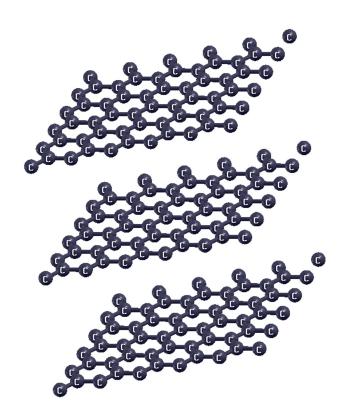
#### Input file for relaxation

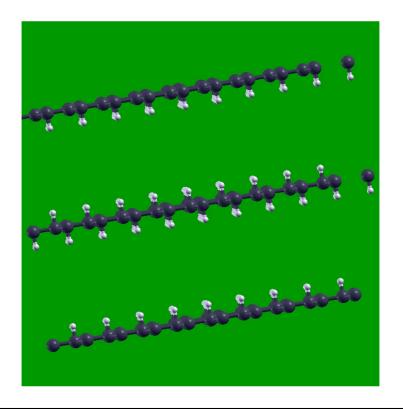
```
&CONTROL
                                  This relaxes only the atomic
calculation = 'relax'.
                                  positions
prefix = 'Graphane'.
outdir = '/tmp',
pseudo dir = '../../pseudo',
&SYSTEM
&ELECTRONS
conv thr = 1.0d-8
                         lons is jargon for atoms, this cell
&IONS
                         must appear!
ATOMIC SPECIES
C 12.0107 C.pbe-rrkjus.UPF
H 1.00007 H.pbe-rrkjus.UPF
ATOMIC POSITIONS alat
K POINTS automatic
991 000
```

## Exercise 1.1: graphane

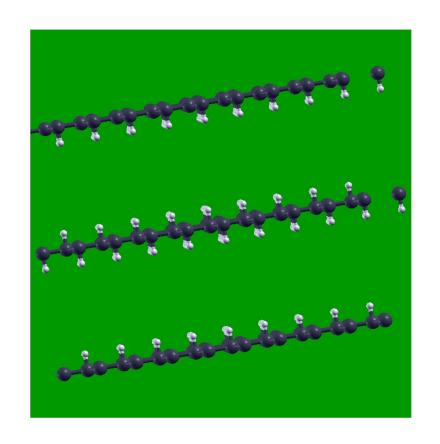
Graphane is hydrogenated graphene:

- → H saturates double-bonds and destroys the pi-delocalized cloud
- → remove tendency to be planar (why?)

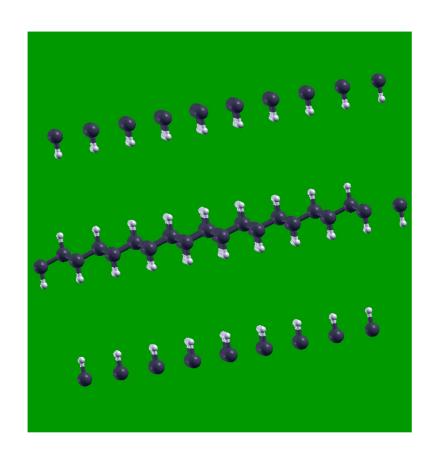




## Exercise 1.1: graphane buckling



Relax →



## **Exercise 1.1: finding forces**

#### Output relaxation file

#### Iteration #1

Forces acting on atoms (cartesian axes, Ry/au):

```
atom 1 type 2 force = -0.00000000 -0.00000000 0.29668613
atom 2 type 1 force = 0.00000000 0.00000000 0.24378433
atom 3 type 1 force = 0.00000000 0.00000000 -0.24378433
atom 4 type 2 force = 0.00000000 0.00000000 -0.29668613
Total force = 0.543053 Total SCF correction = 0.000031
```

#### What is the condition on forces for the material to be in equilibrium?

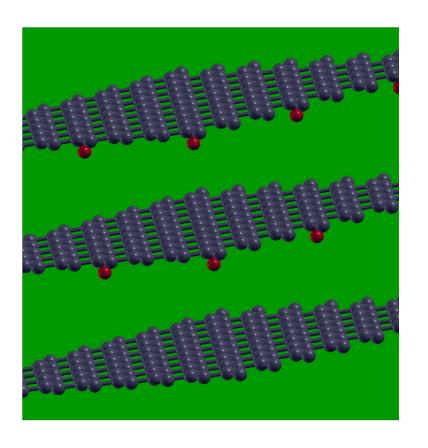
#### Iteration #6

Forces acting on atoms (cartesian axes, Ry/au):

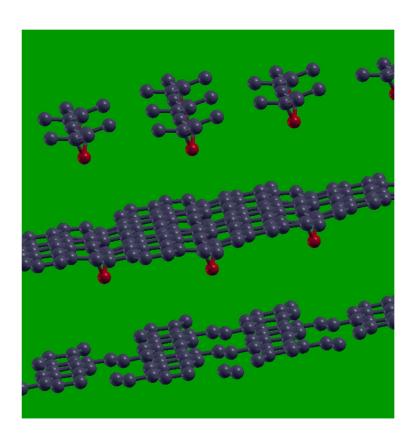
```
atom 1 type 2 force = 0.00000000 0.00000000 0.00017761
     2 type 1 force =
                       0.00000000
                                   0.00000000 -0.00064644
atom
     3 type 1 force = 0.00000000 0.00000000 0.00064644
atom
atom 4 type 2 force =
                       0.00000000 -0.00000000 -0.00017761
Total force =
             0.000948 Total SCF correction =
                                             0.000003
Energy error
                    2.7E-05 Ry
Gradient error
                     6.5E-04 Ry/Bohr
```

## Exercise 1.1: O adsorption on graphene

Oxygen is strongly electronegative → electron acceptor







## Exercise 1.1: optimizing silicon

#### Input file for cell relaxation

```
&CONTROL
                                     This relaxes both cell and atomic
  calculation='vc-relax',
                                     positions
  prefix='silicon',
  pseudo dir='../../pseudo/',
  outdir='./tmp'
&SYSTEM
  ibrav = 2,
  celldm(1) = 10.6,
  nat = 2.
  ntyp = 1,
  nbnd=10,
  ecutwfc = 36,
&ELECTRONS
                         We need also a CELL section
&IONS
&CELL
ATOMIC SPECIES
 Si 28.086 Si.pz-vbc.UPF
ATOMIC POSITIONS
 Si 0.00 0.00 0.00
 Si 0.25 0.25 0.25
K POINTS automatic
 666 111
```

## **Exercise 1.1: finding stresses**

#### Output relaxation file

#### Iteration #1

Forces acting on atoms (cartesian axes, Ry/au):

```
atom 1 type 1 force = 0.00000000 0.00000000 0.00000000 atom 2 type 1 force = 0.00000000 0.00000000 0.00000000
```

Total force = 0.000000 Total SCF correction = 0.000000

Computing stress (Cartesian axis) and pressure

```
total stress (Ry/bohr**3) (kbar) P= -85.01

-0.00057789 -0.00000000 0.00000000 -85.01 -0.00 0.00

-0.00000000 -0.00057789 0.00000000 -0.00 -85.01 0.00

0.00000000 0.00000000 -0.00057789 0.00 0.00 -85.01
```

#### Iteration #6

Forces acting on atoms (cartesian axes, Ry/au):

```
atom 1 type 1 force = -0.00000000 -0.00000000 -0.00000000 atom 2 type 1 force = 0.00000000 0.00000000 -0.00000000
```

Total force = 0.000000 Total SCF correction = 0.000000

#### Computing stress (Cartesian axis) and pressure

total stress (Ry/bohr**3)			(kbar) P=	0.29	
0.00000194	0.00000000	-0.00000000	0.29	0.00	-0.00
0.00000000	0.00000194	-0.00000000	0.00	0.29	-0.00
-0.00000000	-0.00000000	0.00000194	-0.00	-0.00	0.29

## **End of exercise 1**

# Questions?

## Topics of the following session: Phonons

- Exercise 2: Phonons at Gamma in non-polar materials
- Exercise 3: Phonons dispersion in non-polar materials
- Exercise 4: Phonon at Gamma in polar materials

#### Optional:

Exercise 5: Phonon dispersion in polar materials

#### **Introduction: Phonons**

Normal mode frequencies, , and eigenvectors, are determined by the secular equation:

$$\sum_{s',\beta} \widetilde{D}_{s\alpha,s'\beta} (\boldsymbol{q}) \widetilde{\boldsymbol{u}}_{s'\beta} (\boldsymbol{q}) = \omega_{\boldsymbol{q}}^2 \widetilde{\boldsymbol{u}}_{s\alpha} (\boldsymbol{q})$$

where

$$\widetilde{D}_{s\alpha,s'\beta}(\boldsymbol{q}) = \frac{1}{\sqrt{M_s M_{s'}}} \sum_{\boldsymbol{R},\boldsymbol{R'}} \frac{\partial^2 E_{\text{tot}}}{\partial u_{s\alpha}(\boldsymbol{R}) \partial u_{s'\beta}(\boldsymbol{R'})} e^{i\boldsymbol{q}(\boldsymbol{R}-\boldsymbol{R'})}$$

is the dynamical matrix.

Interatomic Force Constant (IFC)

This Matrix can be calculated from linear response and diagonalized to get phonon modes at  $\mathbf{q}$ .

Go to the directory with the input files:

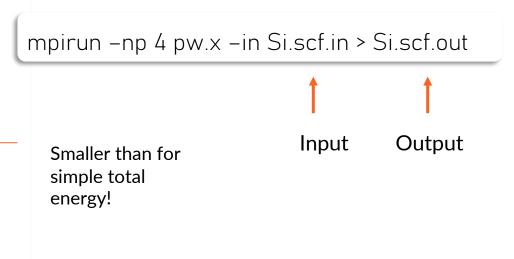
cd ~/ASESMA2025/Day4/example2.phonon.Gamma.Si/

In this directory you will find:

- README.md File describing how to do the exercise
- Si.scf.in Input file for the SCF ground-state calculation
- Si.ph.in Input file for the phonon calculation at Γ
- Si.dynmat.in Input file to impose the acoustic sum rule
- reference Directory with the reference results

```
&CONTROL
calculation = 'scf'.
prefix = 'si'.
pseudo_dir = '../pseudo/'.
outdir = '../tmp'
&SYSTEM
ibrav = 2.
celldm(1) = 10.2
nat = 2.
ntvp = 1.
ecutwfc = 60
ecutrho = 720
&FLECTRONS
mixing_beta=0.7,
conv thr=1d-10.
ATOMIC_SPECIES
Si 28.086 Si.pz-vbc.UPF
ATOMIC POSITIONS
Si
            0 0 0 0 00
                          0.00
            0.25, 0.25
                          0.25
K POINTS automatic
444 111
```

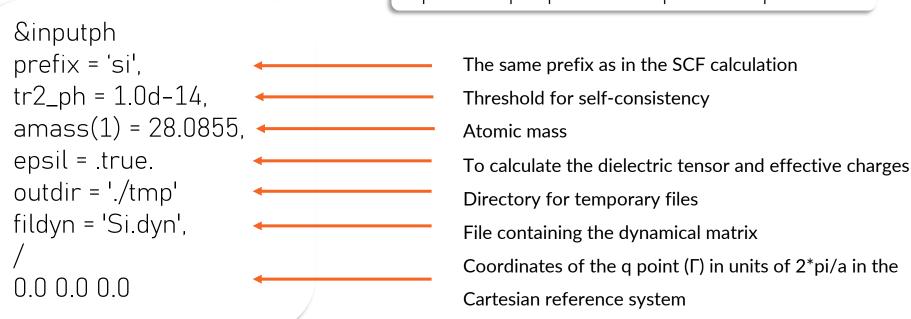
**Step 1:** Perform a Self-Consistent Field ground-state calculation for silicon at the equilibrium structure using the pw.x program.



Input file for phonon at Gamma

**Step 2:** Perform a phonon calculation at Γ using the ph.x program.

mpirun –np 4 ph.x –in Si.ph.in > Si.ph.out



Dynamical matrix file: Si.dyn

#### Dielectric Tensor:

13.581468280806	-0.00000000000	-0.00000000000
0.000000000000	13.581468280806	0.00000000000
-0.000000000000	0.00000000000	13.581468280806

```
Effective Charges E-U: Z_{alpha}{s,beta}
```

```
atom #
    -0.069382139635
                            -0.000000000000
                                                     -0.000000000000
    -0.000000000000
                            -0.069382139635
                                                     -0.000000000000
    -0.000000000000
                            -0.000000000000
                                                     -0.069382139635
atom #
    -0.069382139635
                             0.000000000000
                                                      0.000000000000
     0.000000000000
                            -0.069382139635
                                                     -0.000000000000
     0.000000000000
                            -0.000000000000
                                                     -0.069382139635
```

Dielectric constant and Born effective charges (BECs)

$$Z_{s,\alpha\beta}^* = \frac{V}{e} \frac{\partial P_{\alpha}}{\partial u_{s,\beta}(\boldsymbol{q}=0)} = \frac{1}{e} \frac{\partial F_{s\beta}}{\partial \mathcal{E}_{\alpha}(\boldsymbol{q}=0)}$$

#### Dynamical matrix file: Si.dyn

```
Diagonalizing the dynamical matrix
q = ( 0.000000000 0.000000000 0.000000000 )
```

```
1) =
                                                12.315990 [cm-1]
   frea (
                         0.369224 [THz] =
 -0.502437
             0.000000
                       0.469222
                                  0.000000
                                            0.165492
                                                      0.000000
 -0.502437
            0.000000
                       0.469222
                                  0.000000
                                            0.165492
                                                      0.000000
   freq (
              2) =
                         0.369224 [THz] =
                                                12.315990 [cm-1]
 -0.186720
            0.000000
                       0.040185
                                 0.000000 - 0.680824
                                                      0.000000
( -0.186720
            0.000000
                                 0.000000 - 0.680824
                       0.040185
                                                      0.000000
   frea (
              3) =
                         0.369224 [THz] =
                                                12.315990 [cm-1]
  0.461186
            0.000000
                       0.527462
                                 0.000000 - 0.095350
                                                      0.000000
  0.461186
            0.000000
                       0.527462
                                  0.000000 - 0.095350
                                                      0.000000
              4) =
                        15.306901 [THz] =
                                               510.583264 [cm-1]
   frea (
  0.700260 - 0.000000 - 0.059885
                                  0.000000 - 0.077779
                                                      0.000000
 -0.700260
            0.000000
                       0.059885 -0.000000
                                            0.077779
                                                      0.000000
   freq (
              5) =
                        15.306901
                                   [THz] =
                                               510.583264 [cm-1]
  0.067676
            0.000000
                       0.700365
                                 0.000000
                                            0.070066
                                                      0.000000
 -0.067676
            0.000000 - 0.700365
                                 0.000000 -0.070066
                                                      0.000000
                        15.306901 [THz] =
                                               510.583264 [cm-1]
   frea (
              6) =
 -0.071103
             0.000000
                       0.076832
                                  0.000000
                                           -0.699315
                                                      0.000000
            0.000000 - 0.076832
                                 0.000000
                                            0.699315
  0.071103
                                                      0.000000
```

Acoustic modes (in-phase)



Optical modes (out-of-phase)



#### Acoustic sum rule at Γ

Problems with the frequency of the acoustic phonon mode at  $\Gamma$  and with effective charges.

Because of the numerical inaccuracies the interatomic force constants (IFC) and effective charges ( $Z^*$ ) do not strictly satisfy the acoustic sum rule (ASR).

ASR comes directly from the continuous translational invariance of the crystal: if we translate the whole solid by a uniform displacement, the forces acting on the atoms must be zero

 $\implies$  for each cartesian direction  $\alpha$ ,  $\beta$  and s,s'-th atom:

$$\sum_{\mathbf{R}j} C_{s\alpha,s'\beta} (\mathbf{R}) = 0, \qquad \sum_{j} Z_{s\alpha\beta}^* = 0$$

As a consequence, the frequencies of the acoustic modes at Gamma must be zero.

#### Acoustic sum rule at $\Gamma$

Reason for numerical inaccuracy:

- Insufficiently accurate SCF thresholds (in pw.x and/or ph.x)
- XC energy is computed in real space. More problematic for GGA than in LDA, for US pseudopotentials it could require large ecutrho.
- K-points sampling not accurate enough (especially, BECs and dielectric constant required denser k-point sampling).

#### Acoustic sum rule at Γ

The acoustic sum rule (ASR) can however be imposed after the phonon calculations. To do this we use the dynmat.x program that imposes the ASR on the elements of the dynamical matrix and diagonalize it.

**Step 3:** Run a dynmat.x calculation to impose the ASR

mpirun –np 4 dynmat.x –in Si.dynmat.in > Si.dynmat.out

#### The input file is Si.dynmat.in:

```
&input
fildyn = 'Si.dyn',
asr = 'simple',
/

A way to impose the acoustic sum rule (simple, crystal, one-dim, zero-dim, all)
```

The program dynmat.x produces the file **dynmat.out** which contains the new acoustic frequencies, which are exactly equal to zero

```
0.0000
                     0.0000
                                 0.0000
            1) =
                        0.000000 [THz] =
                                                0.000000 [cm-1]
  freq (
            0.000000
                          0.707107
                                                               0.000000
 0.000000
                                      0.000000
                                                   0.000000
 0.000000
            0.000000
                          0.707107
                                      0.000000
                                                   0.000000
                                                               0.000000
                        0.000000 [THz] =
                                                0.000000 [cm-1]
            2) =
  freq (
-0.707107
            0.000000
                          0.000000
                                      0.000000
                                                   0.000000
                                                               0.000000
-0.707107
            0.000000
                          0.000000
                                      0.000000
                                                   0.000000
                                                               0.000000
            3) =
                        0.000000 [THz] =
                                                0.000000 [cm-1]
  frea (
            0.000000
 0.000000
                          0.000000
                                      0.000000
                                                   0.707107
                                                               0.000000
 0.000000
            0.000000
                          0.000000
                                      0.000000
                                                   0.707107
                                                               0.000000
            4) =
                       15.302447 [THz] =
                                              510.434704 [cm-1]
  frea (
            0.000000
 0.000000
                          0.707107
                                      0.000000
                                                   0.000000
                                                               0.000000
            0.000000
 0.000000
                         -0.707107
                                      0.000000
                                                   0.000000
                                                               0.000000
  frea (
            5) =
                       15.302447 [THz] =
                                              510.434704 [cm-1]
 0.000000
            0.000000
                          0.000000
                                      0.000000
                                                  -0.707107
                                                               0.000000
 0.000000
            0.000000
                          0.000000
                                      0.000000
                                                   0.707107
                                                               0.000000
            6) =
                       15.302447 [THz] =
                                              510.434704 [cm-1]
  freq (
-0.707107
            0.000000
                          0.000000
                                     0.000000
                                                   0.000000
                                                               0.000000
 0.707107
            0.000000
                          0.000000
                                      0.000000
                                                   0.000000
                                                               0.000000
```

Go to the directory with the input files:

cd ~/ASESMA2025/Day4/example3.phonon.dispersion.Si/

In this directory you will find:

- README.md File describing how to do the exercise
- Si.scf.in Input file for the SCF ground-state calculation
- Si.ph.in Input file for the phonon calculation at Γ
- Si.q2r.in Input file for calculation of Interatomic Force Constants
- Si.matdyn.in Input file for Fourier Interpolation for various q points
- Si.plotband.in Input file for plotting a phonon dispersion
- **reference** Directory with the reference results

**Step 1:** Perform a Self-Consistent Field ground-state calculation for silicon at the equilibrium structure using the pw.x program.

mpirun –np 4 pw.x –in Si.scf.in > Si.scf.out

**Step 2:** Perform a phonon calculation on a uniform grid of q points the ph.x program.

mpirun –np 4 ph.x –in Si.ph.in > Si.ph.out

Flags for the calculation on a grid Uniform grid of q points:

$$q_{ijk} = \frac{i-1}{nq_1} G_2 + \frac{j-1}{nq_2} G_1 + \frac{k-1}{nq_3} G_1$$

```
&inputph
prefix = 'si',
tr2_ph = 1.0d-14,
amass(1) = 28.0855
ldisp = .true.,
nq1 = 4,
nq2 = 4,
nq3 = 4,
outdir = './tmp'
fildyn = 'Si.dyn',
```

4x4x4 = 64 **q**-points => **Use of symmetry** => 8 non-equivalent **q** points The file Si.dyn0 contains a list of the non-equivalent **q** points (8, in this case).

```
0.00000000000000E+00
                         0.000000000000000E+00
                                                 0.000000000000000E+00
-0.250000000000000E+00
                         0.250000000000000E+00
                                                -0.250000000000000E+00
 0.500000000000000E+00
                        -0.500000000000000E+00
                                                 0.500000000000000E+00
 0.00000000000000E+00
                         0.500000000000000E+00
                                                 0.00000000000000E+00
 0.750000000000000E+00
                        -0.250000000000000E+00
                                                 0.750000000000000E+00
 0.50000000000000E+00
                         0.00000000000000E+00
                                                 0.50000000000000E+00
 0.00000000000000E+00
                        -0.100000000000000E+01
                                                 0.000000000000000E+00
-0.500000000000000E+00
                        -0.100000000000000E+01
                                                 0.00000000000000E+00
```

The phonon code ph.x generates a file for every non-equivalent q point (Si.dyn1, Si.dyn2, ..., Si.dyn8), which contain information about dynamical matrices, phonon frequencies and atomic displacements

**Step 3:** Calculation of the Interatomic Force Constants (IFC) using the q2r.x program

IFCs in reciprocal space (Fourier transform of IFCs):

$$\tilde{C}_{s\alpha,s'\beta}(\boldsymbol{q}) = \frac{\partial^2 E_{\text{tot}}}{\partial \widetilde{\boldsymbol{u}}_{s\alpha}(\boldsymbol{q}) \partial \widetilde{\boldsymbol{u}}_{\beta}(\boldsymbol{q})}$$

where  $\alpha$ ,  $\beta$  are the cartesina direction and s,s' the atomic index

$$C_{s\alpha,s'\beta}(R) = \sum_{q_n} \tilde{C}_{s\alpha,s'\beta}(q) e^{iq_n(R-R')}$$

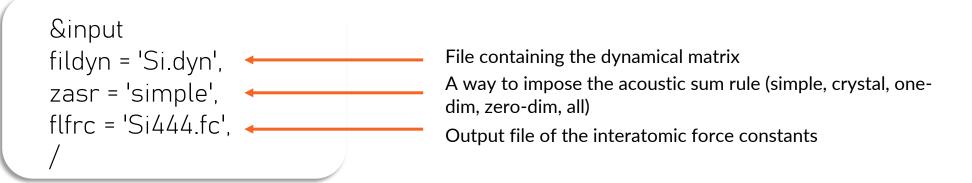
$$\tilde{C}_{s\alpha,s'\beta}(q) \longrightarrow C_{s\alpha,s'\beta}(R)$$

Fourier transforms of IFCs on a grid of  $\mathbf{q}$  points nq1 x nq2 x nq3 in reciprocal space

IFCs in a supercell nq1 x nq2 x nq3 in real space

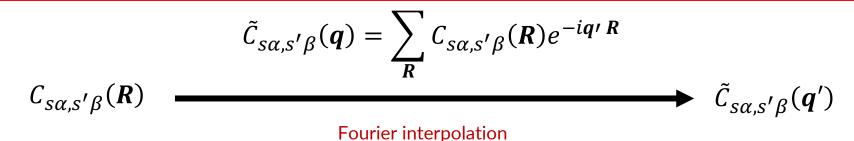
**Step 3:** Calculation of the Interatomic Force Constants (IFC) using the q2r.x program

mpirun –np 4 q2r.x –in Si.q2r.in > Si.q2r.out



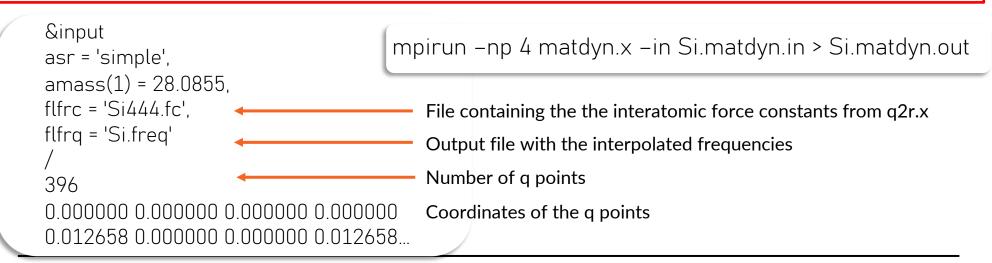
Note: The denser the grid of q points, the larger the vectors R for which the IFCs are calculated.

**Step 4:** Calculate phonons at generic **q**' points using IFC using the matdyn.x code

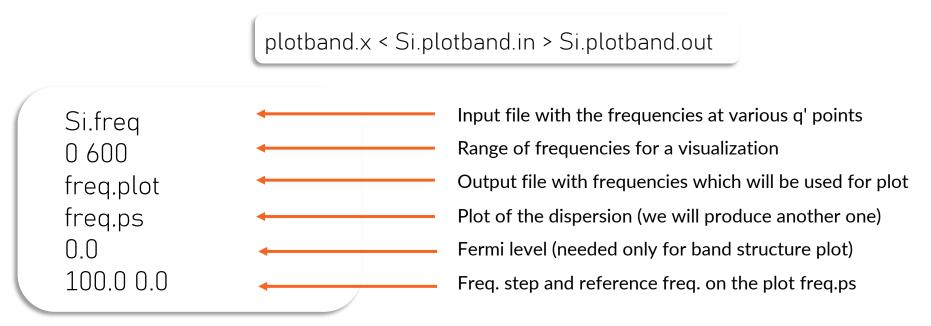


IFC's on a grid in real space

Fourier transforms of IFC's at generic q' points in reciprocal space

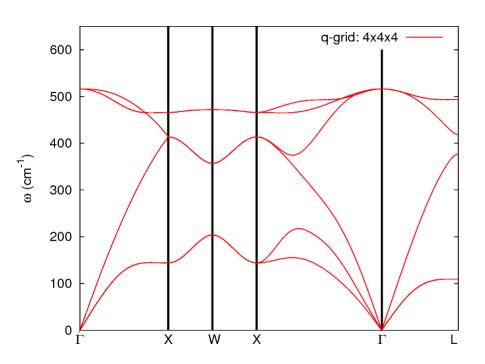


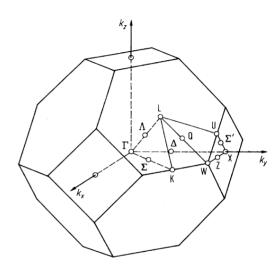
**Step 5:** Plot the phonon dispersion using the plotband.x program and gnuplot.



Use gnuplot and the file **plot\_dispersion.gp** in order to plot the phonon dispersion of silicon (look at the file experimental\_data.dat for the experimental reference). You will get a postscript file phonon dispersion.eps which you can visualize.

Phonon dispersion of silicon along some high-symmetry directions in the Brillouin zone (file phonon\_dispersion.eps).





How to determine whether the quality of the Fourier interpolation is satisfactory? Compare with the direct calculation (no interpolation)!

**Homework-1**: Perform a direct phonon calculation (no interpolation) at several **q**' points and make a comparison with the phonon frequencies obtained from the interpolation. (Use exercise2 as an example).

Some **q**' points along the Gamma-X high symmetry line are listed in the file reference/q\_points\_direct\_calc.txt

**Homework-2**: Perform a phonon dispersion calculation for several q-points grids (eg. 2x2x2, 4x4x4, and 6x6x6) and compare the dispersions. Do they converge?

The phonon modes are not always easy to visualize, especially if we are not at  $\Gamma$ . An online phonon visualizer is very helpful in this regard.

https://interactivephonon.materialscloud.io

Let's click on the link and look at your phonons.

## Phonons in polar materials

Polar materials in the q = 0 limit: a macroscopic electric field appears as a consequence of the long-range character of the Coulomb interaction (incompatible with Periodic Boundary Conditions). A non-analytic term must be added to Interatomic Force Constants at  $\mathbf{q} = 0$ :

$$\tilde{C}_{s\alpha,s'\beta}(q) = \tilde{C}_{s\alpha,s'\beta}^{analytic} + \frac{4\pi}{V} \frac{(q \cdot Z_s^*)_{\alpha} (q \cdot Z_s^*)_{\beta}}{q \cdot \varepsilon_{\infty} \cdot q}$$

Effective charges  $Z_s^*$  are related to polarization P induced by a lattice

$$Z_{s,\alpha\beta}^* = V \frac{\partial P_{\alpha}}{\partial u_s^{\beta}}$$

Dielectric tensor  $\varepsilon_{\infty}^{\alpha\beta}$  is related to polarization P induced by an electric field E:

$$\varepsilon_{\infty}^{\alpha\beta} = \delta_{\alpha\beta} + 4\pi \frac{\partial P_{\alpha}}{\partial E_{\beta}} \bigg|_{u_{s}(\boldsymbol{q}=0)=0}$$

All of the above can be calculated from (mixed) second order derivatives of the total energy.

Go to the directory with the input files:

cd ~/ASESMA2025/Day4/example4.phonon.Gamma.AlAs/

In this directory you will find:

- README.md File describing how to do the exercise
- AlAs.scf.in Input file for the SCF ground-state calculation
- AlAs.ph.in Input file for the phonon calculation at Γ
- AlAs.dynmat.in Input file for Fourier Interpolation for various q points
- reference Directory with the reference results

**Step 1:** Perform a Self-Consistent Field ground-state calculation for AsAl at the equilibrium structure using the pw.x program.

mpirun –np 4 pw.x –in AlAs.scf.in > AlAs.scf.out

**Step 2:** Perform a phonon calculation in Gamma using ph.x.

mpirun –np 4 ph.x –in AlAs.ph.in > AlAs.ph.out

Phonons at Gamma & Sinputph prefix = 'AlAs', tr2\_ph = 1.0d-14, amass(1) = 26.98, amass(2) = 74.92, epsil = .true. outdir = './tmp' fildyn = 'AlAs.dyn', / 0.0 0.0 0.0

In the file **ph.AlAs.out** you will find information about the dielectric tensor and effective charges (BECs)

```
Effective charges (d Force / dE) in cartesian axis with asr applied:
                   1 Al Mean Z*:
                                         4.43445
         atom
    E*x (
                 4.43445
                               0.00000
                                             -0.00000)
    E*v (
            0.00000 4.43445
                                             -0.00000)
                                                               Z_{s,\alpha\beta}^* = \frac{V}{e} \frac{\partial P_{\alpha}}{\partial u_{s,\beta}(\boldsymbol{q}=0)} = \frac{1}{e} \frac{\partial F_{s\beta}}{\partial \mathcal{E}_{\alpha}(\boldsymbol{q}=0)}
                         -0.00000
    E*z (
           -0.00000
                                       4.43445 )
                   2 As Mean Z*:
                                    -4.43445
         atom
            -4.43445
                              -0.00000
                                              0.00000 )
    F*x (
    E*y ( -0.00000 -4.43445 0.00000 )
    E*z ( 0.00000
                         0.00000
                                             -4.43445)
   Diagonalizing the dynamical matrix
   q = (
            0.000000000
                         0.000000000
                                       0.000000000 )
frea (
             1) =
                      -0.062455 [THz] =
                                             -2.083289 [cm-1]
   freg (
                      -0.062455 [THz] = -2.083289 [cm-1]
             3) =
                      -0.062455 [THz] = -2.083289 [cm-1]
   freq (
           4) =
                      11.807415 [THz] = 393.852972 [cm-1]
   freq (
                                                                           — No LO-TO splitting
             5) =
                      11.807415 [THz] = 393.852972 [cm-1]
   freq (
                      11.807415 [THz] =
                                            393.852972 [cm-1]
   freq (
```

**Step 3:** Impose Acoustic Sum Rule and add the non analytic LO-TO splitting using the dynmat.x program

mpirun –np 4 dynmat.x –in AlAs.dynmat.in > AlAs.dynmat.out

```
&input
fildyn = 'AlAs.dyn',
asr='simple',
amass(1)=26.98,
amass(2)=74.92
q(1) = 1.0,
q(2) = 0.0,
q(3) = 0.0
```

IR activities are in (D/A)^2/amu units

[cm-1]	[THz]	IR
-0.00	-0.0000	0.0000
0.00	0.0000	0.0000
0.00	0.0000	0.0000
393.86	11.8075	22.8709
393.86	11.8075	22.8709
430.19	12.8969	22.8709
	-0.00 0.00 0.00 393.86 393.86	-0.00

LO-TO splitting

Direction in the Brillouin zone along which we want to compute the LO-TO splitting

**Step 3:** Impose Acoustic Sum Rule and add the non analytic LO-TO splitting using the dynmat.x program

mpirun –np 4 dynmat.x –in AlAs.dynmat.in > AlAs.dynmat.out

```
&input
fildyn = 'AlAs.dyn',
asr='simple',
amass(1)=26.98,
amass(2)=74.92
q(1) = 1.0,
q(2) = 0.0,
q(3) = 0.0
```

IR activities are in (D/A)^2/amu units

IR intensities 
$$I_{IR}(\nu) = \sum_{\alpha} \left| \sum_{S\beta} Z_{S}^{*\alpha\beta} u_{S}^{\beta}(\nu) \right|^{2}$$

can be calculated directly from effective charges and phonon displacement patterns

# Exercise 5 (Optional): Phonons dispersion in polar materials

### Exercise 5: Phonons dispersion in polar materials

Go to the directory with the input files:

cd ~/ASESMA2025/Day4/example5.phonon.dispersion.AlAs/

In this directory you will find:

- README.md File describing how to do the exercise
- AlAs.scf.in Input file for the SCF ground-state calculation
- AlAs.ph.in Input file for the phonon calculation at Γ
- AlAs.q2r.in Input file for calculation of Interatomic Force Constants
- AlAs.matdyn.in Input file for Fourier Interpolation for various q points
- AlAs.plotband.in Input file for plotting a phonon dispersion
- reference Directory with the reference results

### Exercise 5: Phonons dispersion in polar materials

**Step 1:** Perform a Self-Consistent Field ground-state calculation at the equilibrium structure using the pw.x program.

**Step 2:** Perform a phonon calculation on a uniform grid of q points the ph.x program.

mpirun –np 4 ph.x –in Al
$$A$$
s.ph.in > Al $A$ s.ph.out

**Step 3:** Calculation of the Interatomic Force Constants (IFC) using the q2r.x program

**Step 4:** Calculate phonons at generic **q**' points using IFC using the matdyn.x code

**Step 5:** Plot the phonon dispersion using the plotband.x program and gnuplot.

plotband.x < AlAs.plotband.in > AlAs.plotband.out

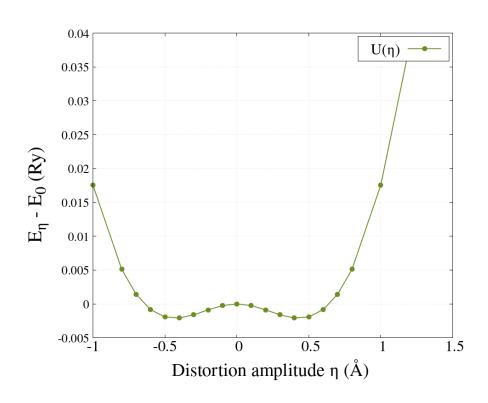
(Note: some parts of the input files are left empty for you to fill!

# Exercise 6 (Optional): Phonons dispersion of unstable materials

### Negative phonon frequencies

Phonons are the solution of the secular equation:

$$\sum_{s',\beta} \widetilde{D}_{s\alpha,s'\beta} (\mathbf{q}) \widetilde{\mathbf{u}}_{s'\beta} (\mathbf{q}) = \omega_{\mathbf{q}}^2 \widetilde{\mathbf{u}}_{s\alpha} (\mathbf{q})$$



$$\widetilde{D}_{s\alpha,s'\beta}(\boldsymbol{q}) =$$

$$\frac{1}{\sqrt{M_{S}M_{S'}}}\sum_{\boldsymbol{R},\boldsymbol{R'}}\frac{\partial^{2}E_{\text{tot}}}{\partial u_{s\alpha}(\boldsymbol{R})\partial u_{s'\beta}(\boldsymbol{R'})}e^{i\boldsymbol{q}(\boldsymbol{R}-\boldsymbol{R'})}$$

If you are not in the minimum of the PES, you will get negative phonons frequencies (imaginary values of  $\omega_{\bf q}$ )

(where  $\eta$  is :  $\eta \boldsymbol{u}_k = \eta \boldsymbol{\epsilon}_k e^{i\boldsymbol{q}\boldsymbol{R}_l}$ )

### **Exercise 6: Negative phonons**

Go to the directory with the input files:

cd ~/ASESMA2025/Day4/example6.negative.phonon/

In this directory you will find:

- README.md File describing how to do the exercise
- Si.scf.in Input file for the SCF ground-state calculation
- Si.ph.in Input file for the phonon calculation at Γ
- Si.q2r.in Input file for calculation of Interatomic Force Constants
- Si.matdyn.in Input file for Fourier Interpolation for various q points
- Si.plotband.in Input file for plotting a phonon dispersion
- reference Directory with the reference results

### **Exercise 6: Negative phonons**

**Step 1:** Perform a Self-Consistent Field ground-state calculation at the equilibrium structure using the pw.x program.

**Step 2:** Perform a phonon calculation on a uniform grid of q points the ph.x program (here we use 2x2x2).

**Step 3:** Calculation of the Interatomic Force Constants (IFC) using the q2r.x program

**Step 4:** Calculate phonons at generic **q**' points using IFC using the matdyn.x code

**Step 5:** Plot the phonon dispersion using the plotband.x program and gnuplot.

### **Exercise 6: Negative phonons**

 Look at the results of the phonon dispersion: can you explain what you see? What is the difference with the band dispersion in exercise3?

## Thank you!

## Questions?