

# Modelos matemáticos de rehabilitación y reparto en condiciones de inseguridad para logística humanitaria

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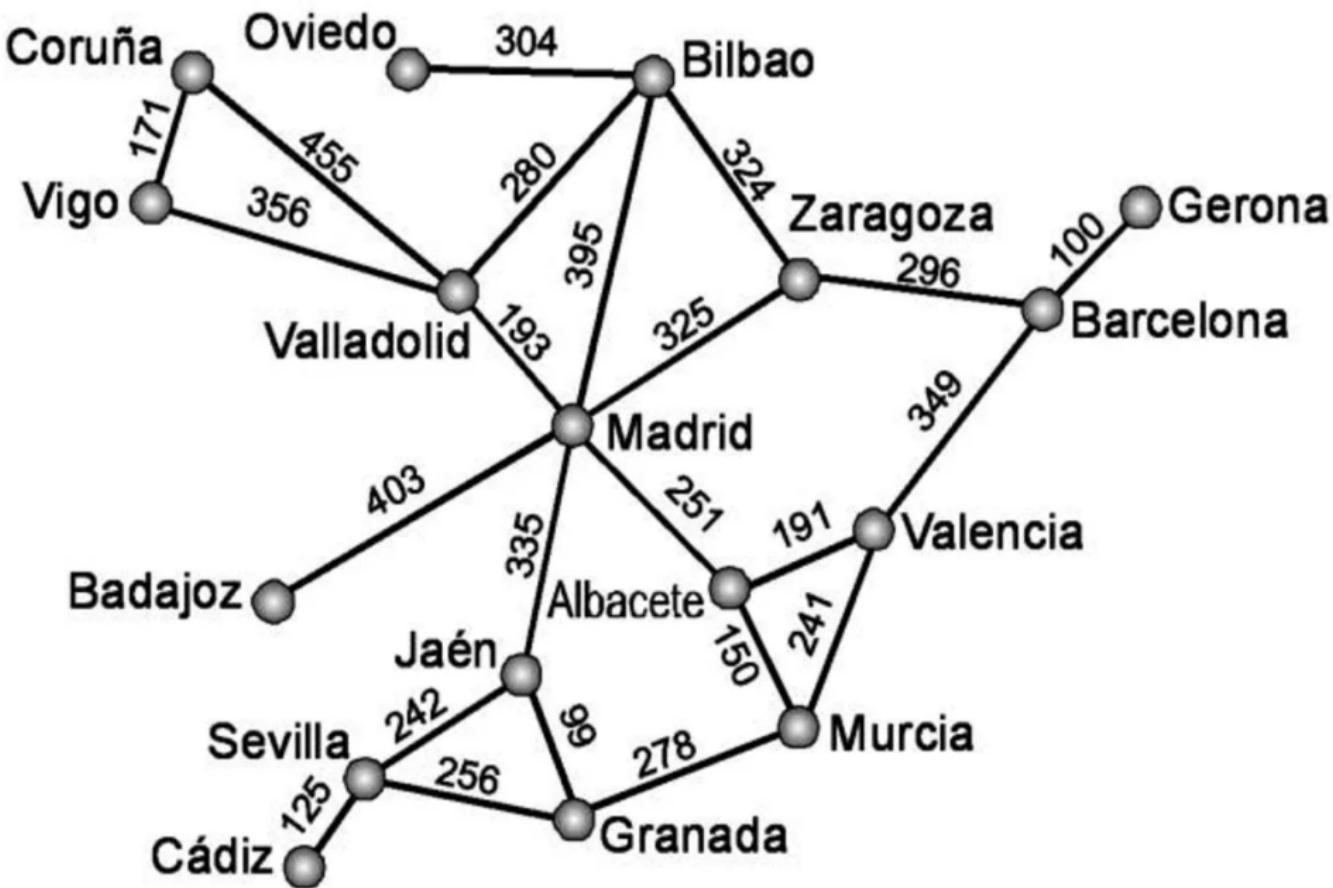
Dpto. de estadística e investigación operativa

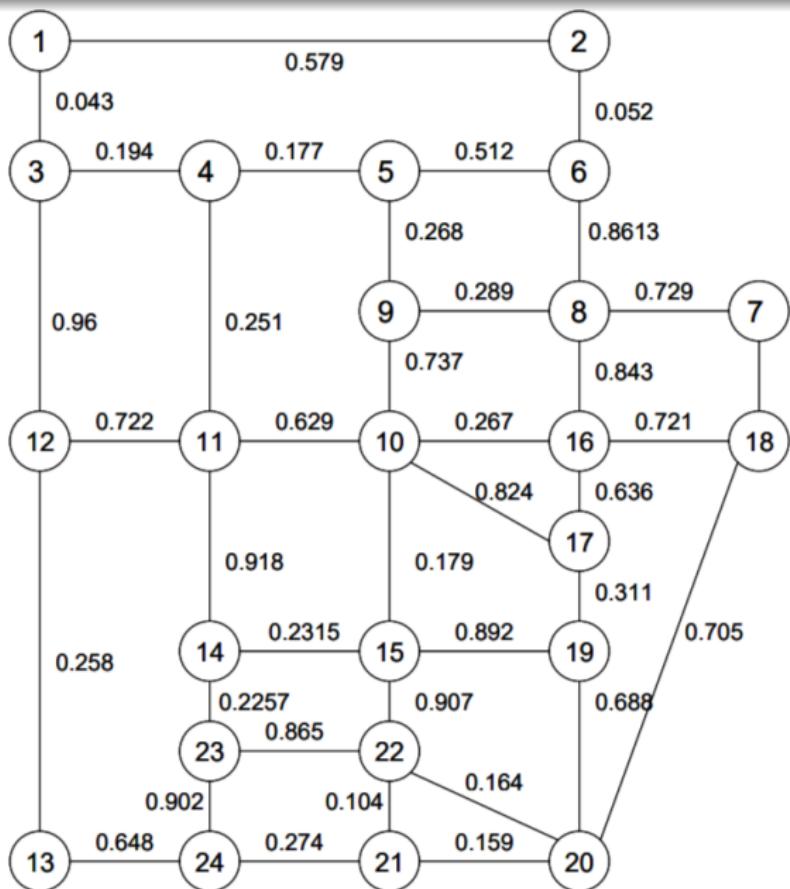


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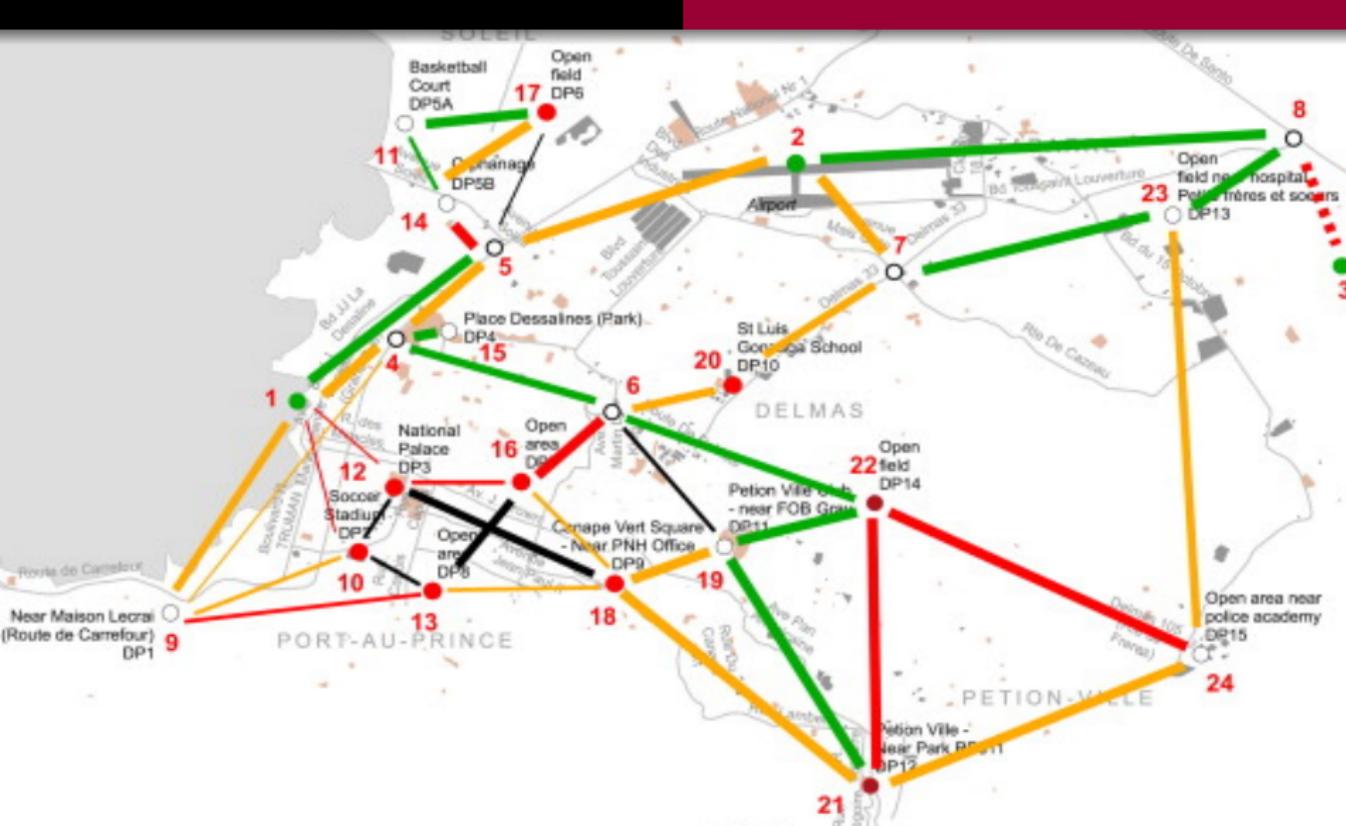








**FIGURE 5 Test Network 2: Modified Sioux Falls network**



# Índices

Índice	Descripción
$j, i$	Nodos.
$v$	Tipos de convoy.
$w$	Cada convoy de tipo $v$ .

# Variables principales

Nombre	Índices	Descripción
X	$i, j, v, w$	Variable binaria que determina si el convoy de tipo $v$ $w$ -ésimo recorre el arco de $i$ a $j$ .
Y	$i, j, v, w$	Variable binaria que determina si el convoy $w$ -ésimo recorre el arco de $i$ a $j$ volviendo.
Z	$i, v, w$	Variable binaria que determina si el convoy de tipo $v$ $w$ -ésimo reparte a $i$ .
H	$i, j$	Variable binaria que determina si se habilita el arco de $i$ a $j$ .

## Restricciones ida

- (1)  $\sum_i X_{i,j,v,w} \geq \sum_i X_{j,i,v,w}$   $\forall j, v, w \mid j > 1$
- (2)  $Z_{j,v,w} \leq \sum_i X_{i,j,v,w}$   $\forall j, v, w$
- (3)  $Z_{j,v,w} \leq 1 - \sum_i X_{j,i,v,w}$   $\forall j, v, w$
- (4)  $\sum_j X_{i,j,v,w} \leq 1$   $\forall i, v, w$
- (5)  $Salio_{v,w} = \sum_j Z_{j,v,w}$   $\forall v, w$
- (6)  $\sum_j X_{0,j,v,w} = Salio_{v,w}$   $\forall v, w$

## Restricciones vuelta

$$(9) \text{ Ayuda}_j \leq \text{dem}_j \quad \forall j$$

$$(10) \sum_i \text{Y}_{i,j,v,w} + \text{Z}_{j,v,w} \geq \sum_i \text{Y}_{j,i,v,w} \quad \forall j, v, w$$

$$(11) \sum_j \text{Y}_{i,j,v,w} \leq 1 \quad \forall i, v, w$$

$$(14) \text{Z}_{i,v,w} \leq \sum_j \text{Y}_{i,j,v,w} \quad \forall i, v, w$$

$$(15) \text{Y}_{0,j,v,w} = 0 \quad \forall j, v, w$$

$$(16) \text{Salio}_{v,w} = \sum_i \text{Y}_{i,0,v,w} \quad \forall v, w$$

## Restricciones existencia y usabilidad

- (7)  $X_{i,j,v,w} \leq E_{i,j}$   $\forall i, j, v, w$
- (8)  $X_{i,j,v,w} \leq U_{i,j} + H_{i,j}$   $\forall i, j, v, w \mid E_{i,j} > 0$
- (12)  $Y_{i,j,v,w} \leq E_{i,j}$   $\forall i, j, v, w \mid E_{i,j} > 0$
- (13)  $Y_{i,j,v,w} \leq U_{i,j} + H_{i,j}$   $\forall i, j, v, w \mid E_{i,j} > 0$

## Definición criterios

$$(17) \text{ Ayuda}_j = \sum_v \left( \sum_w (Z_{j,v,w} \cdot \text{capacidad}_v) \right) \quad \forall j$$

$$(18) \text{ Insatis} = \sum_j \text{Insatisaux}_j$$

$$(19) \text{ Eq} \geq \text{Prop\_insatis}_j \quad \forall j$$

$$(20) \text{ Prop\_insatis}_j \cdot \text{dem}_j = \text{Insatisaux}_j \quad \forall j$$

$$(21) \text{ Insatisaux}_j = \text{dem}_j - \text{Ayuda}_j \quad \forall j$$

$$(22) \text{ Coste\_rehab} = \sum_i \left( \sum_j (H_{i,j} \cdot \text{coste\_rehabilitacion}_{i,j}) \right)$$

$$(23) \text{ Coste\_rehab} \leq \text{max\_coste\_rehab}$$

$$(24) \text{ Coste} = \sum_i \left( \sum_j \left( \sum_v \left( \sum_w ((X_{i,j,v,w} + Y_{i,j,v,w}) \cdot \text{coste\_variable}_v \cdot \text{dist}_{i,j})) \right) \right) \right) + \\ \sum_v \left( \sum_w (\text{Salio}_{v,w} \cdot \text{coste\_fijo}_v) \right)$$

$$(25) \text{ Coste} \leq \text{max\_coste}$$

## Restricciones fiabilidad y seguridad

$$(27) \quad M \cdot \text{Usado}_{i,j} \geq \sum_v \left( \sum_w (\mathsf{X}_{i,j,v,w} + \mathsf{Y}_{i,j,v,w}) \right) \quad \forall i, j \mid E_{i,j} > 0$$

$$(28) \quad \text{Seguridad} = \sum_i \left( \sum_j (\text{Usado}_{i,j} \cdot \text{PS}_{i,j}) \right)$$

$$(29) \quad \text{Seguridad} \geq \text{PS\_total}$$

$$(30) \quad \text{Fiabilidad} = \sum_i \left( \sum_j (\text{Usado}_{i,j} \cdot P_{i,j}) \right)$$

$$(31) \quad \text{Fiabilidad} \geq P\_total$$

## Restricciones temporales

$$(32) \quad t_{v,w} = \sum_i \left( \sum_j ((\mathsf{X}_{i,j,v,w} + \mathsf{Y}_{i,j,v,w}) \cdot \text{dist}_{i,j}) \right) \quad \forall v, w$$

$$(33) \quad t_{v,w} \leq TZ \quad \forall v, w$$

$$(34) \quad TZ \leq T\_max$$

## Índices

Índice	Descripción
j, i	Nodos.
v	Tipos de convoy.

## Variables principales

Nombre	Índices	Descripción
Xmas	i, j, v	Flujo positivo de convoyes de tipo $v$ en el arco de $i$ a $j$ .
Xmenos	i, j, v	Flujo negativo de convoyes de tipo $v$ en el arco de $i$ a $j$ .
Y	j, v	Cantidad de convoyes de tipo $v$ que reparten su mercancía en $j$ .
Z	i	Ayuda total en toneladas repartida a $i$ .
H	i, j	Variable binaria que determina si se habilita el arco de $i$ a $j$ .

## Restricciones de flujo

- (1)  $Y_{j,v} \geq 0 \quad \forall j, v \mid j > 1$
- (2)  $Y_{j,v} = \sum_i (X_{mas,i,j,v} - X_{menos,i,j,v}) - \sum_i (X_{mas,j,i,v} - X_{menos,j,i,v}) \quad \forall j, v$
- (3)  $X_{mas,j,i,v} = 0 \quad \forall i, j, v \mid i \leq j \wedge E_{i,j} > 0$
- (4)  $X_{menos,j,i,v} = 0 \quad \forall i, j, v \mid i \leq j \wedge E_{i,j} > 0$
- (5)  $X_{mas,i,j,v} - X_{menos,i,j,v} \leq M \cdot E_{i,j} \quad \forall i, j, v$
- (6)  $X_{mas,i,j,v} - X_{menos,i,j,v} \geq -(M \cdot E_{i,j}) \quad \forall i, j, v$
- (7)  $X_{mas,i,j,v} - X_{menos,i,j,v} \leq M \cdot (U_{i,j} + H_{i,j}) \quad \forall i, j, v \mid E_{i,j} > 0$
- (8)  $X_{mas,i,j,v} - X_{menos,i,j,v} \geq -(M \cdot (U_{i,j} + H_{i,j})) \quad \forall i, j, v \mid E_{i,j} > 0$
- (9)  $Z_j \leq dem_j \quad \forall j$
- (10)  $Z_j = \sum_v (Y_{j,v} \cdot capacidad_v) \quad \forall j$

## Definición criterios

$$(11) \text{Insatis} = \sum_j \text{Insatisaux}_j$$

$$(12) \text{Eq} \geq \text{Prop\_insatis}_j \quad \forall j$$

$$(13) \text{Prop\_insatis}_j \cdot \text{dem}_j = \text{Insatisaux}_j \quad \forall j$$

$$(14) \text{Insatisaux}_j \geq \text{dem}_j - Z_j \quad \forall j \mid j > 1$$

$$(15) \text{Coste\_rehab} = \sum_i \left( \sum_j (\text{coste\_rehabilitacion}_{i,j} \cdot H_{i,j}) \right)$$

$$(16) \text{Coste\_rehab} \leq \text{max\_coste\_rehab}$$

$$(17) \text{Coste} = - \sum_v (Y_{0,v} \cdot \text{coste\_fijo}_v) + \sum_v \left( \sum_i \left( \sum_j ((X_{mas,i,j,v} + X_{menos,i,j,v}) \cdot \text{dist}_{i,j} \cdot \text{coste\_variable}_v) \right) \right)$$

$$(18) \text{Coste} \leq \text{max\_coste}$$

$$(19) - \sum_v (Y_{0,v} \cdot \text{capacidad}_v) \leq \text{max\_ayuda}$$

## Restricciones fiabilidad y seguridad

$$(20) \quad M \cdot \text{Usado}_{i,j} \geq \sum_v (\text{Xmas}_{i,j,v} + \text{Xmenos}_{j,i,v}) \quad \forall i, j$$

$$(21) \quad \text{Seguridad} = \sum_i (\sum_j (\text{Usado}_{i,j} \cdot \text{PS}_{i,j}))$$

$$(22) \quad \text{Seguridad} \geq \text{PS\_total}$$

$$(23) \quad \text{Fiabilidad} = \sum_i (\sum_j (\text{Usado}_{i,j} \cdot \text{P}_{i,j}))$$

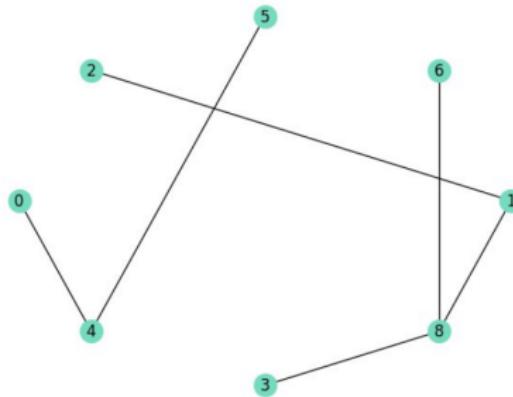
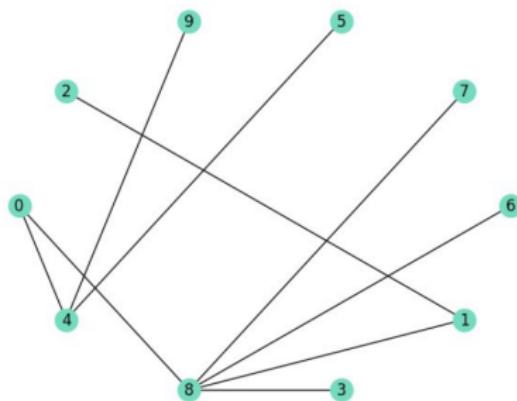
$$(24) \quad \text{Fiabilidad} \geq \text{P\_total}$$

## Restricciones temporales

$$(25) \quad \text{TM}_j \geq \text{TM}_i + \text{dist}_{i,j} \cdot \text{velocidad\_convoy} - M \cdot (1 - \text{Usado}_{i,j}) \quad \forall i, j \mid E_{i,j} > 0$$

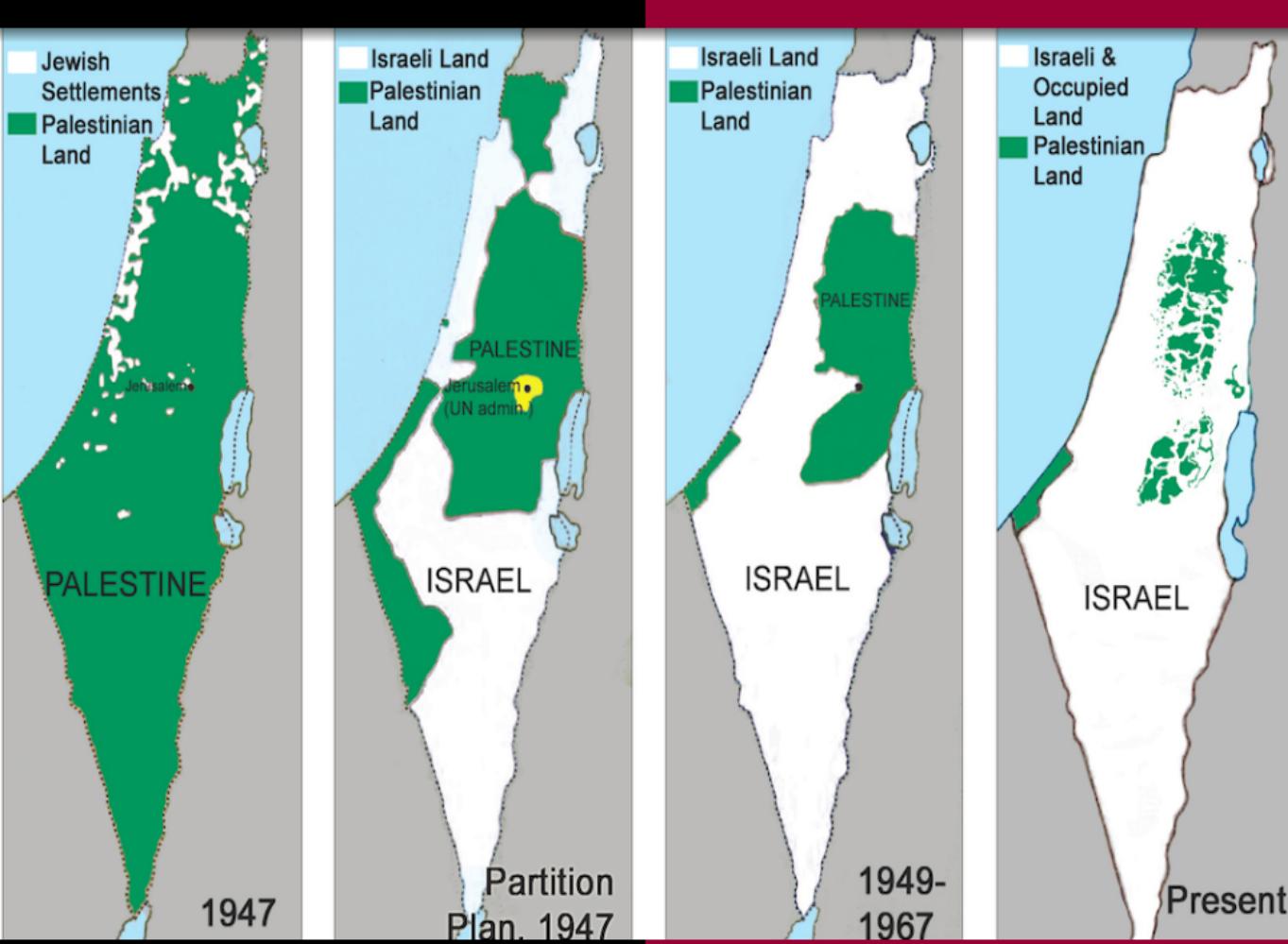
$$(26) \quad \text{TZ} \geq \text{TM}_j \quad \forall j$$

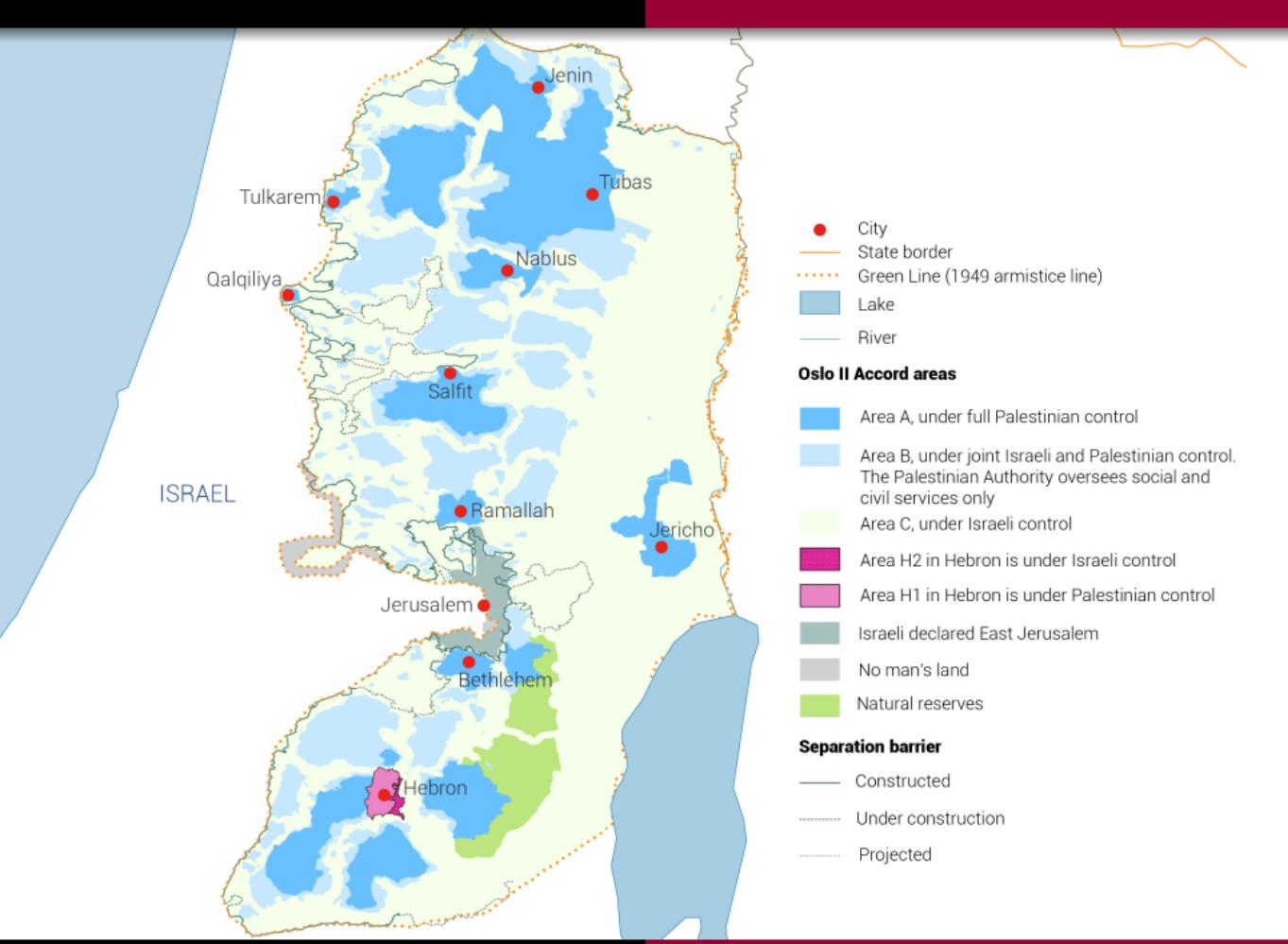
$$(27) \quad \text{TZ} \leq \text{T\_max} \quad \forall j$$

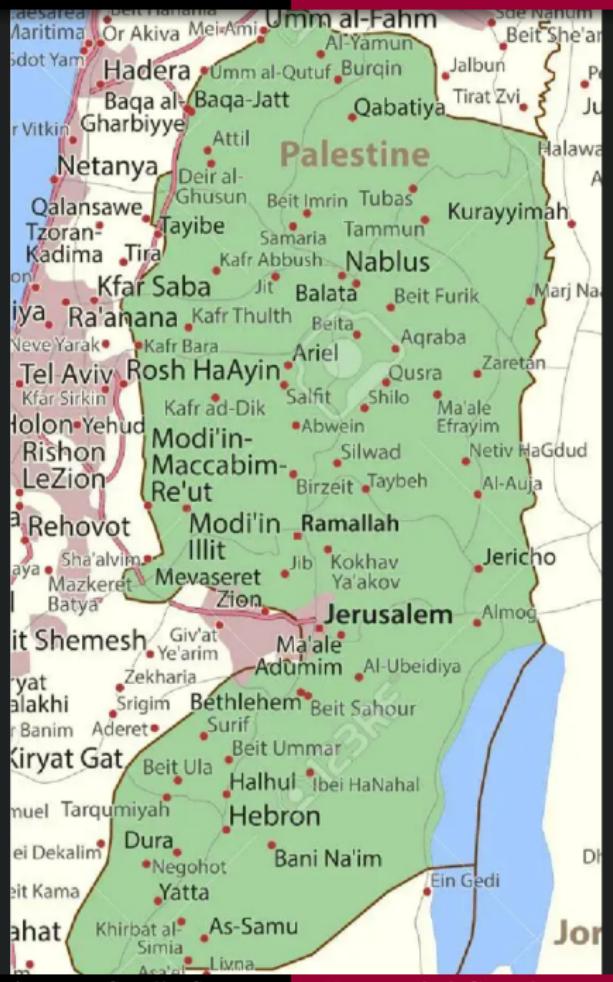


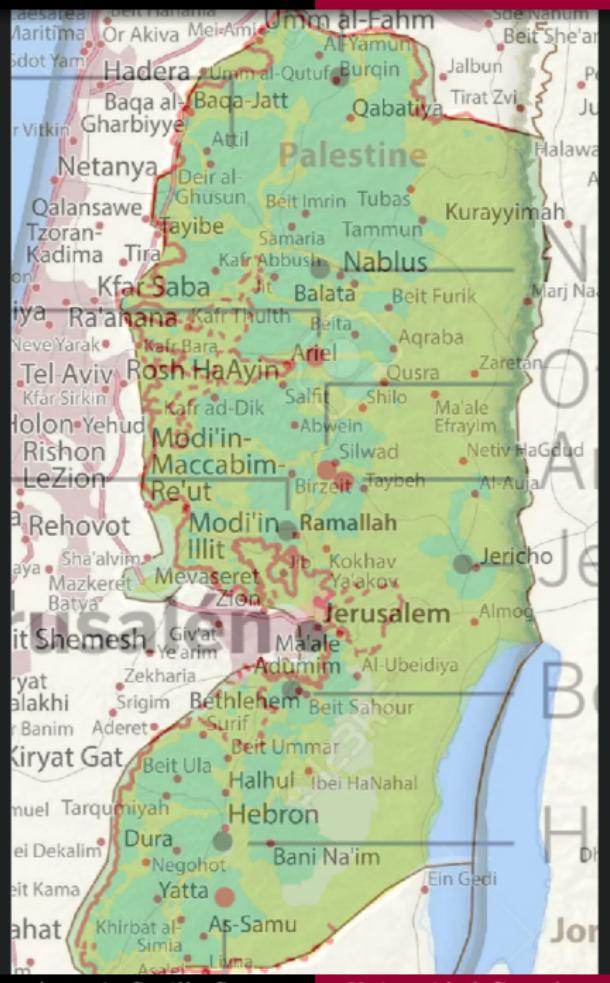
## Experiencia computacional

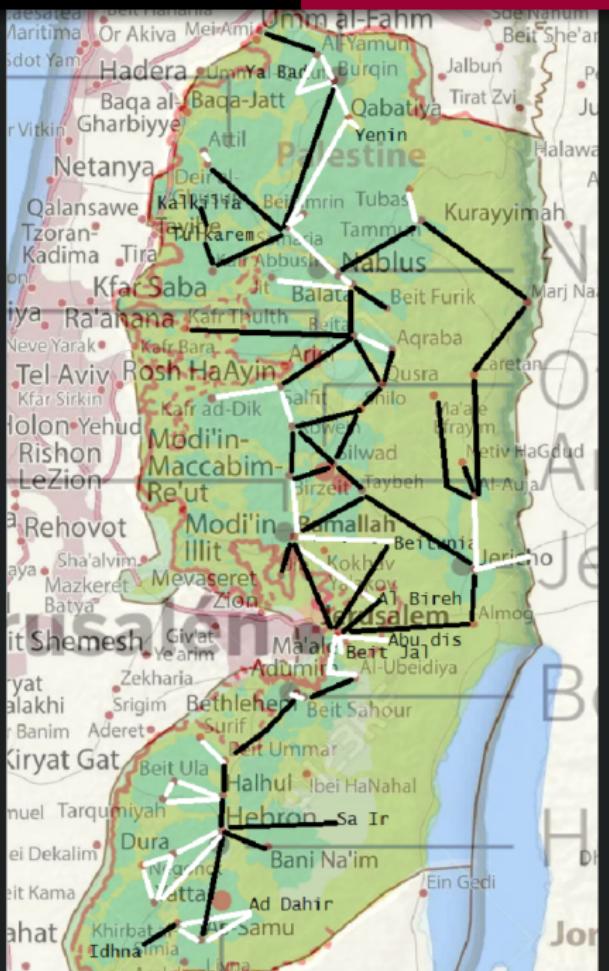
	Primer modelo	Segundo modelo
80 arcos	10 " 6200 iters 191200 cols	2 " 200 iters 80000 cols
200 arcos	300 " 251000 iters 191500 cols	7 " 750 iters 80000 cols
300 arcos	500 " 415000 iters 193100 cols	10 " 950 iters 80000 cols







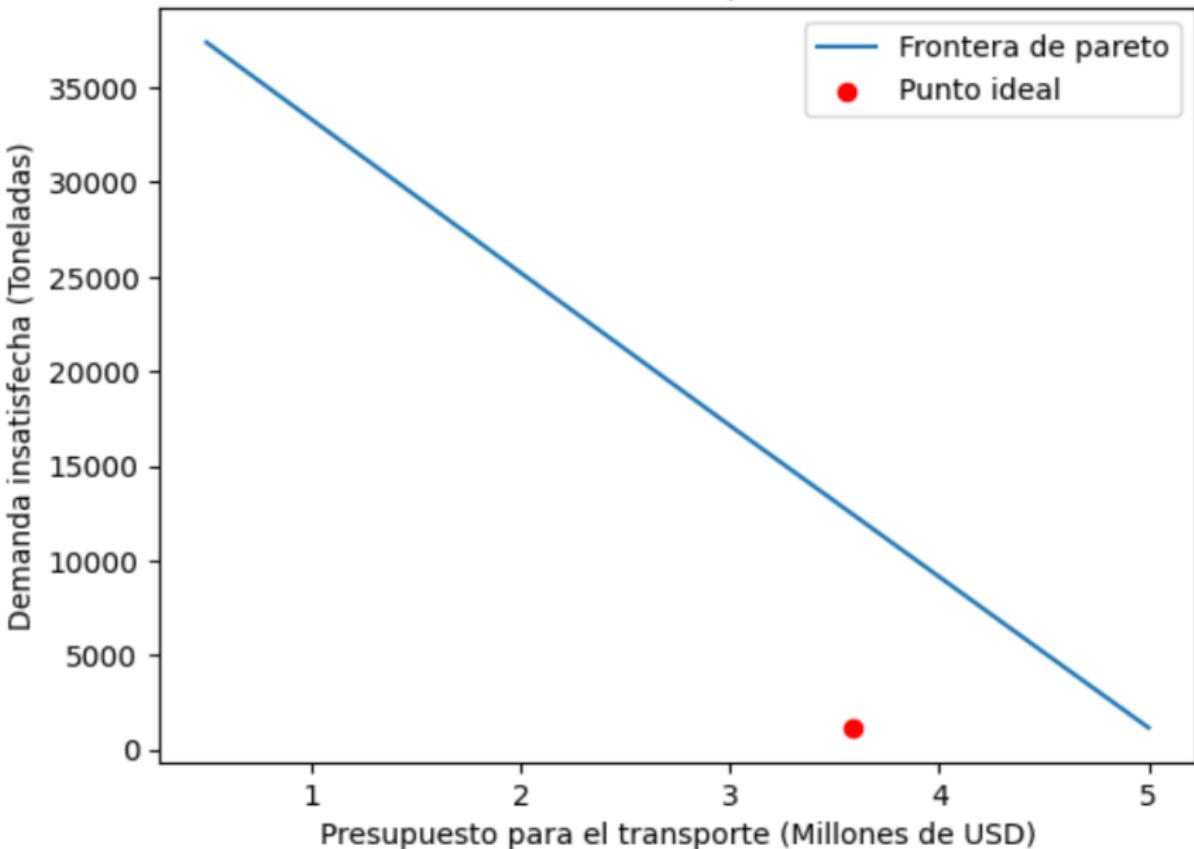




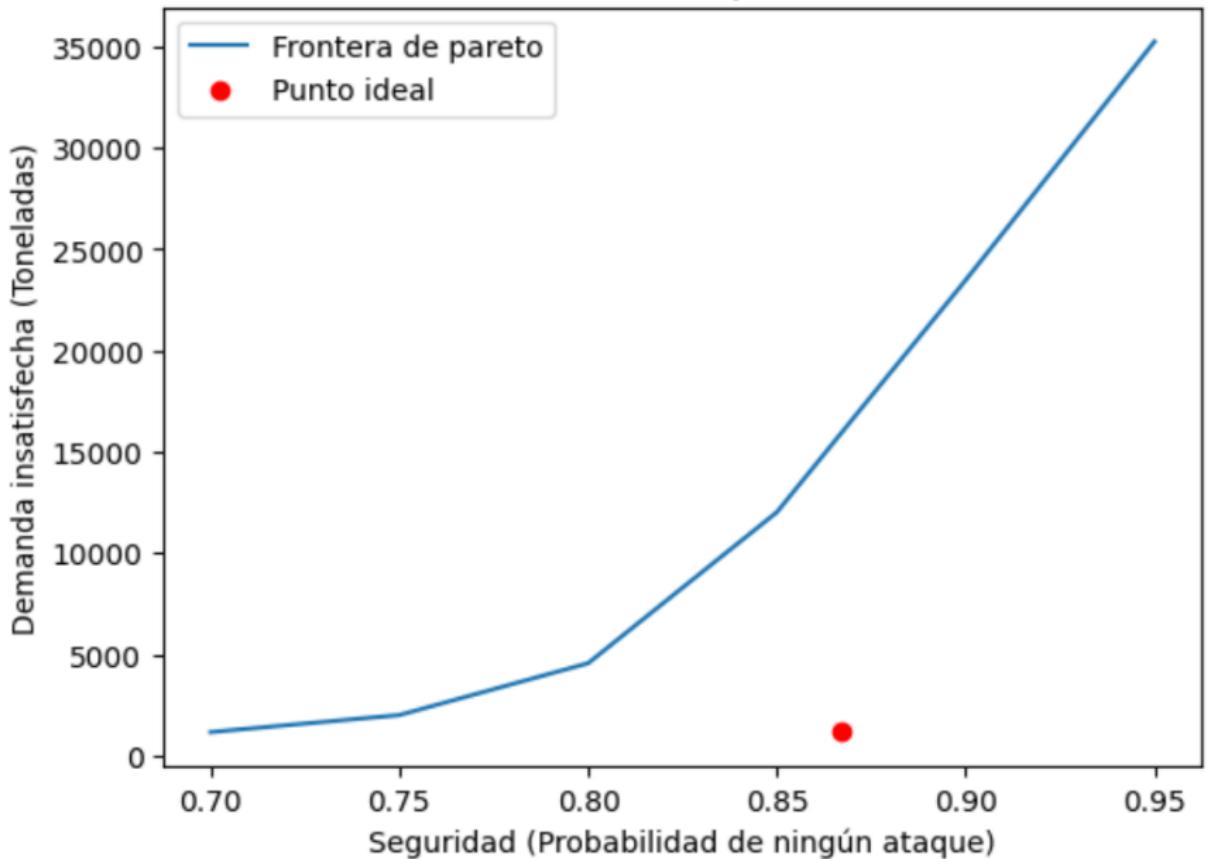
## Matriz de pagos

$$\begin{pmatrix} 1156 & 0,1078 & 4\,623\,070 & 0,795 & 0,827 \\ 1156 & 0,1078 & 4\,623\,070 & 0,795 & 0,827 \\ 12436 & 1 & 3\,586\,475 & 0,660 & 0,713 \\ 12449 & 1 & 3\,617\,682 & 0,867 & 0,851 \\ 12449 & 1 & 3\,607\,212 & 0,799 & 0,882 \end{pmatrix}$$

## Frontera de pareto

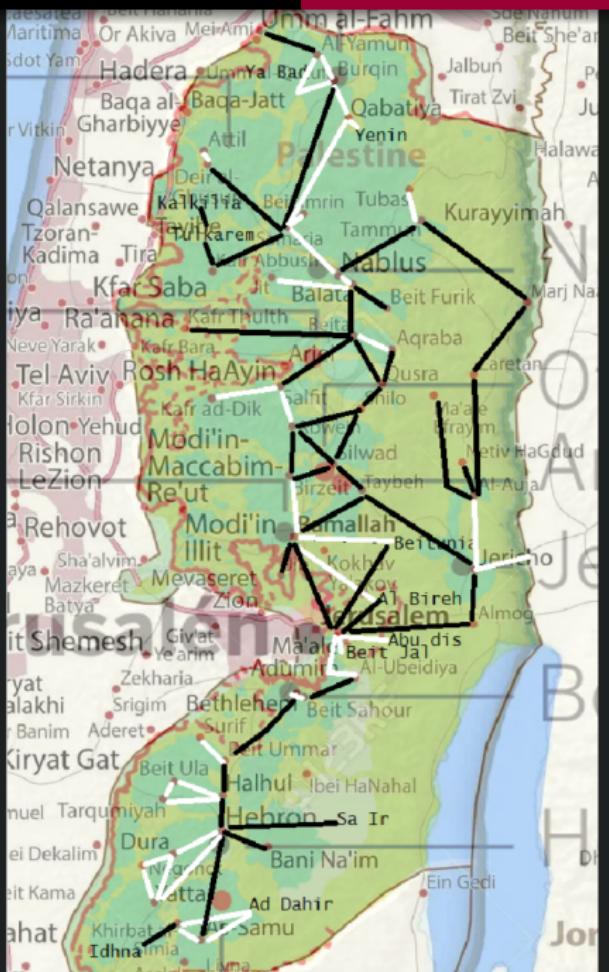


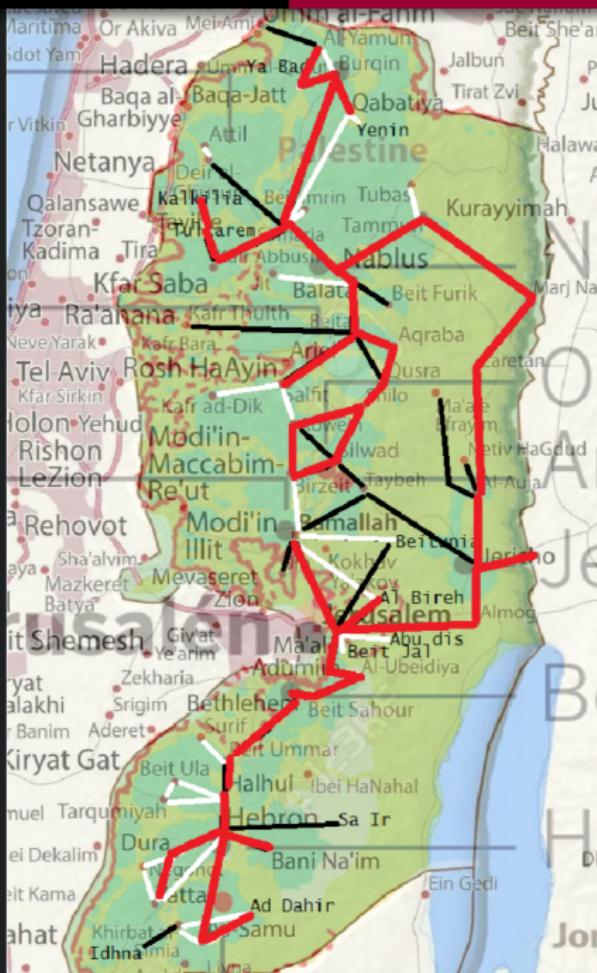
## Frontera de pareto



## Solución compromiso

Demanda insatisfecha	Equidad	Coste	Seguridad	Fiabilidad
12016 T	1	3 681 000 USD	0.850	0.851





## Solución por metas ponderadas 1

Demanda insatisfecha	Equidad	Coste	Seguridad	Fiabilidad
8416 T	1	4 112 400 USD	0.814	0.851

## Solución por metas ponderadas 1

Demanda insatisfecha	Equidad	Coste	Seguridad	Fiabilidad
8416 T	1	4 112 400 USD	0.814	0.851

## Solución por metas ponderadas 2

Demanda insatisfecha	Equidad	Coste	Seguridad	Fiabilidad
8296 T	0.787	4 142 600 USD	0.663	0.660

## Solución por metas ponderadas 1

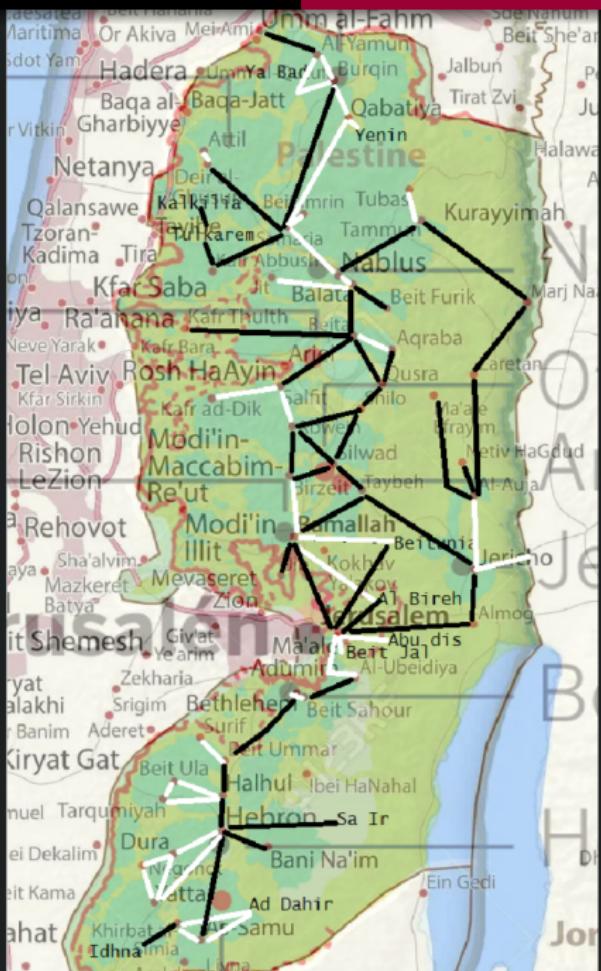
Demanda insatisfecha	Equidad	Coste	Seguridad	Fiabilidad
8416 T	1	4 112 400 USD	0.814	0.851

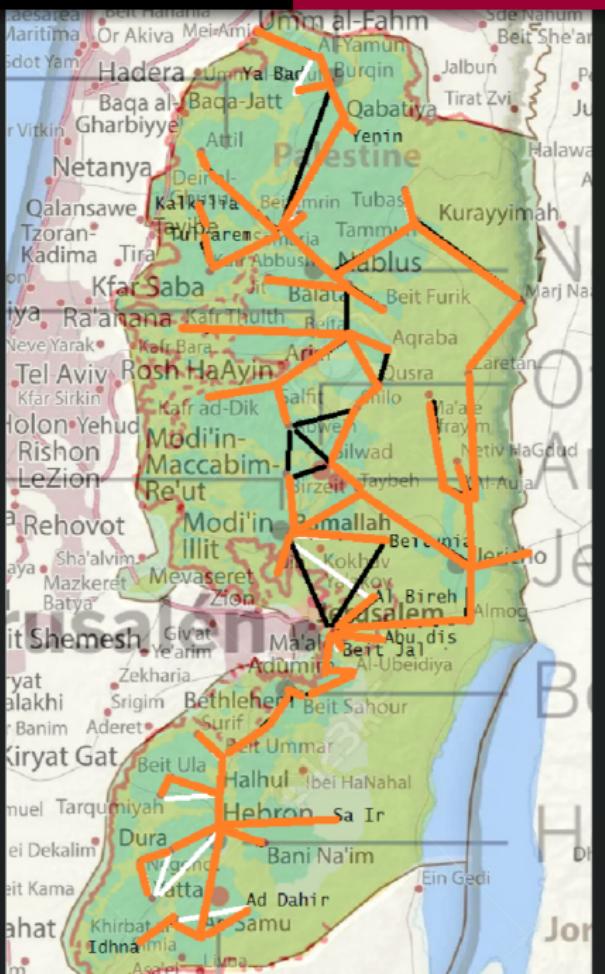
## Solución por metas ponderadas 2

Demanda insatisfecha	Equidad	Coste	Seguridad	Fiabilidad
8296 T	0.787	4 142 600 USD	0.663	0.660

## Solución por metas indexadas

Demanda insatisfecha	Equidad	Coste	Seguridad	Fiabilidad
4200 T	0.120	4 671 100 USD	0.644	0.687







Gracias por su atención

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