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### Problem 1:

General Problem with constraints and objective:

$$\begin{aligned} r_i &= |ax_i + b - y_i| \\ \min a, b \quad &\sum_{i=1}^n r_i \\ r_i &\geq ax_i + b - y_i \\ -r_i &\leq ax_i + b - y_i \end{aligned}$$

```
from pulp import *

points = [(1, 3), (2, 5), (3, 7), (5, 11), (7, 14), (8, 15), (10,
19)]

prob = LpProblem("problem", LpMinimize)

a = LpVariable("slope")
b = LpVariable("intercept")
r = LpVariable("absolute deviation")

prob += r

for point in points:
    (x, y) = point
    prob += r >= a*x + b - y
    prob += r >= -(a*x + b - y)

status = prob.solve()

print "The slope of the line is", value(a)
print "The intercept of the line is", value(b)
print "The maximum absolute deviation from the line is", value(r)

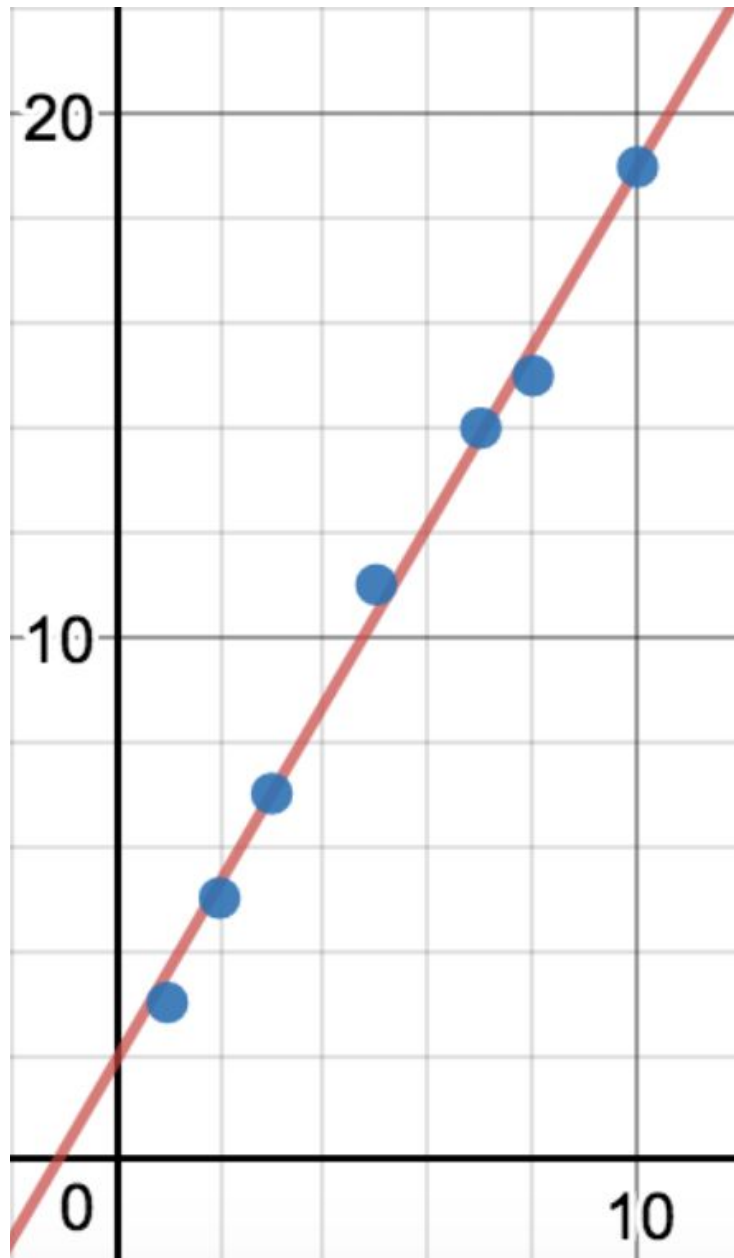
print "The solution is " + LpStatus[status]
```

### Solution:

The slope (a) of the line is 1.7142857

The intercept (b) of the line is 1.8571429

The maximum absolute deviation from the line (r) is 0.57142857  
The solution is Optimal



## Problem 2 (Warming Up):

```
import math
from pulp import *

f = iter(open("Corvallis.csv"))

temps = []

f.next()

for entry in f:
    entry = entry.split(";")
    temps.append((int(entry[-1]), float(entry[-2])))

prob = LpProblem("problem", LpMinimize)

x0 = LpVariable("x0")
x1 = LpVariable("x1")
x2 = LpVariable("x2")
x3 = LpVariable("x3")
x4 = LpVariable("x4")
x5 = LpVariable("x5")
r = LpVariable("absolute deviation")

prob += r

for i in xrange(len(temps)):
    (d, t) = temps[i]
    T = x0 + x1*d + x2*math.cos(2*math.pi*d/365.25) +
    x3*math.sin(2*math.pi*d/365.25) +
    x4*math.cos(2*math.pi*d/(365.25*10.7)) +
    x5*math.sin(2*math.pi*d/(365.25*10.7))

    prob += r >= T - t
    prob += r >= -(T - t)
```

```

status = prob.solve()

print "x0:", value(x0)
print "x1:", value(x1)
print "x2:", value(x2)
print "x3:", value(x3)
print "x4:", value(x4)
print "x5:", value(x5)

print "The maximum absolute deviation from the line is",
value(r)

print "The solution is " + LpStatus[status]

```

#### Description:

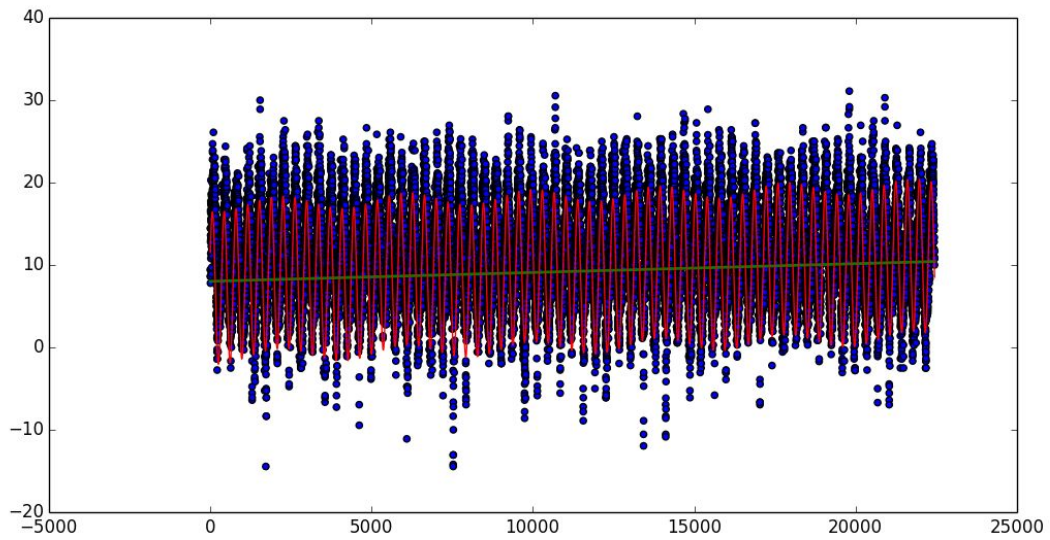
$$T = x_0 + x_1 \cdot d[i] + x_2 \cdot \cos(2\pi \cdot d[i] / 365.25) + x_3 \cdot \sin(2\pi \cdot d[i] / 365.25) + x_4 \cdot \cos(2\pi \cdot d[i] / (365.25 \cdot 10.7)) + x_5 \cdot \sin(2\pi \cdot d[i] / (365.25 \cdot 10.7))$$

```

Minimize R;
R >= T - temperature[i]
R >= -(T - temperature[i])

```

#### Graph:



Optimal Solutions:

$R = 14.23554$   
 $X_0 = 8.0214197$   
 $X_1 = 0.00010694836$   
 $X_2 = 4.2808907$   
 $X_3 = 8.1868578$   
 $X_4 = -0.79063079$   
 $X_5 = -0.29536021$

Change per century:

Based on the value of  $x_1$ , which is the daily change in temperature in Corvallis, the amount of degrees Corvallis is getting warmer per century is  $3.906288849^\circ$  Celsius, This is a warming trend, as the amount is positive.