



ML Math-percentage-percentile



Percentage and Percentile



What is a Percentage?

A percentage is just a number out of 100.

If you scored 90% on a test, it means

- you got 90 out of 100 marks or
- 9 out of 10 or
- 18 out of 20
- 180 out of 200 and so on.

What is percentile ?

A percentile is a value below which a certain percentage of data falls. It shows the **relative standing of a value within a dataset**.

If you are in the 90th percentile of a test, it means

- you scored better than 90% of the people who took it or
- you can say that 90% of students are below your score.



Example1: Let's say 10 students took a test and got the following scores out of 200.

[90, 60, 180, 170, 120, 140, 150, 160, 100, 30].

Calculate the percentage and percentile of student who scored 120.

ANSWER:

Percentage: The test is out of 200, and the student scored 120

So, his percentage would be $\frac{120}{200} * 100 = 60\%$

Percentile:

Step1) First arrange in ascending order.

[30, 60, 90, 100, 120, 140, 150, 160, 170, 180]

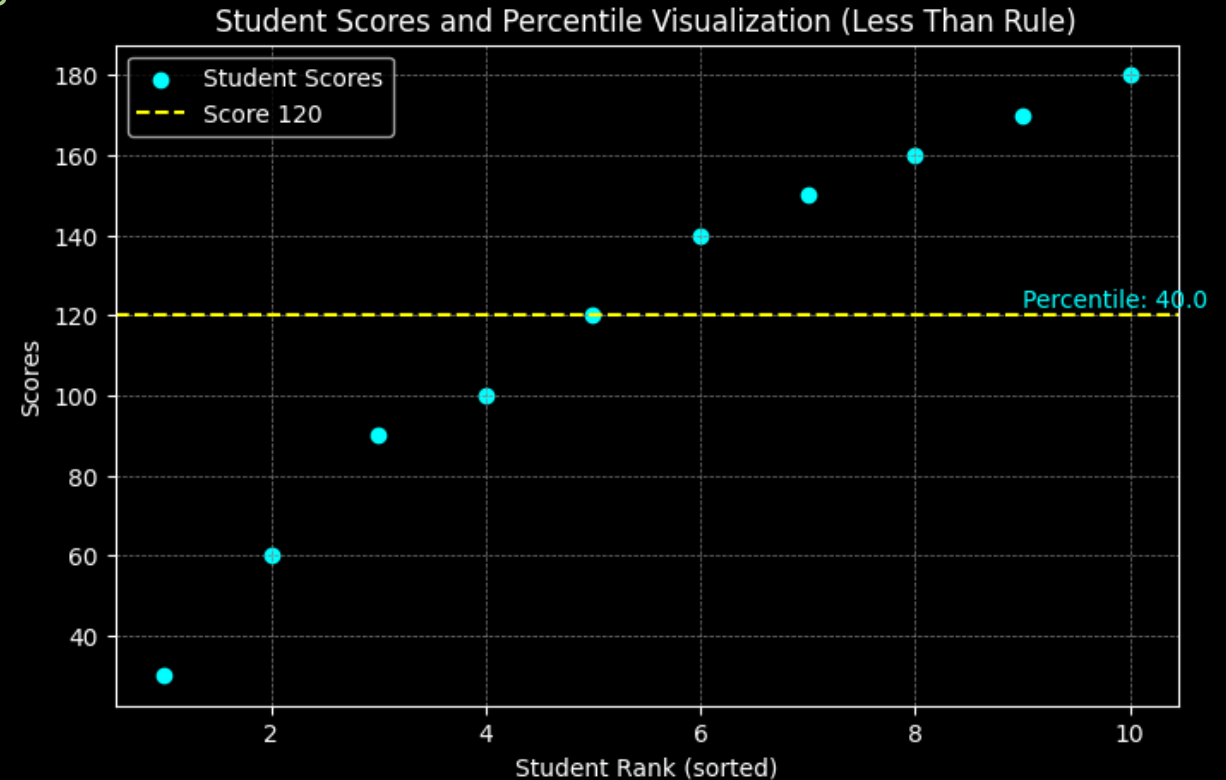
Step2) Count how many scores are less than 120 and convert that into percentage.

Scores below 120 = [30, 60, 90, 100] → 4 students

Percentage of students who scored below 120

$$= \frac{4}{10} * 100 = 40$$

So, his percentile is 40th percentile. **Even if the student's percentage is 60%, his percentile (i.e. 40) depends on how others performed** — in this case, better-performing students pushed the percentile down.



Example2: Let's say 10 students took a test and got the following scores out of 200:

[30, 60, 180, 170, 120, 140, 150, 160, 100, 90].

Calculate the 30th percentile

ANSWER:

1) First arrange in ascending order:

[30, 60, 90, 100, 120, 140, 150, 160, 170, 180]

2) Calculate the rank (position):

The formula for the position (rank) is:

$$R = \frac{P}{100} \times (n + 1)$$

where

- P = desired percentile (30 here)
- n = number of data points

$$R = \frac{30}{100} \times (10 + 1) = 0.3 \times 11 = 3.3$$

So, the 30th percentile lies at the 3.3rd position in the ordered list.



3) Interpolate if necessary:

The rank is **3.3**, which means the 30th percentile lies between the **3rd** and **4th** values in the sorted list:

3rd value = 90

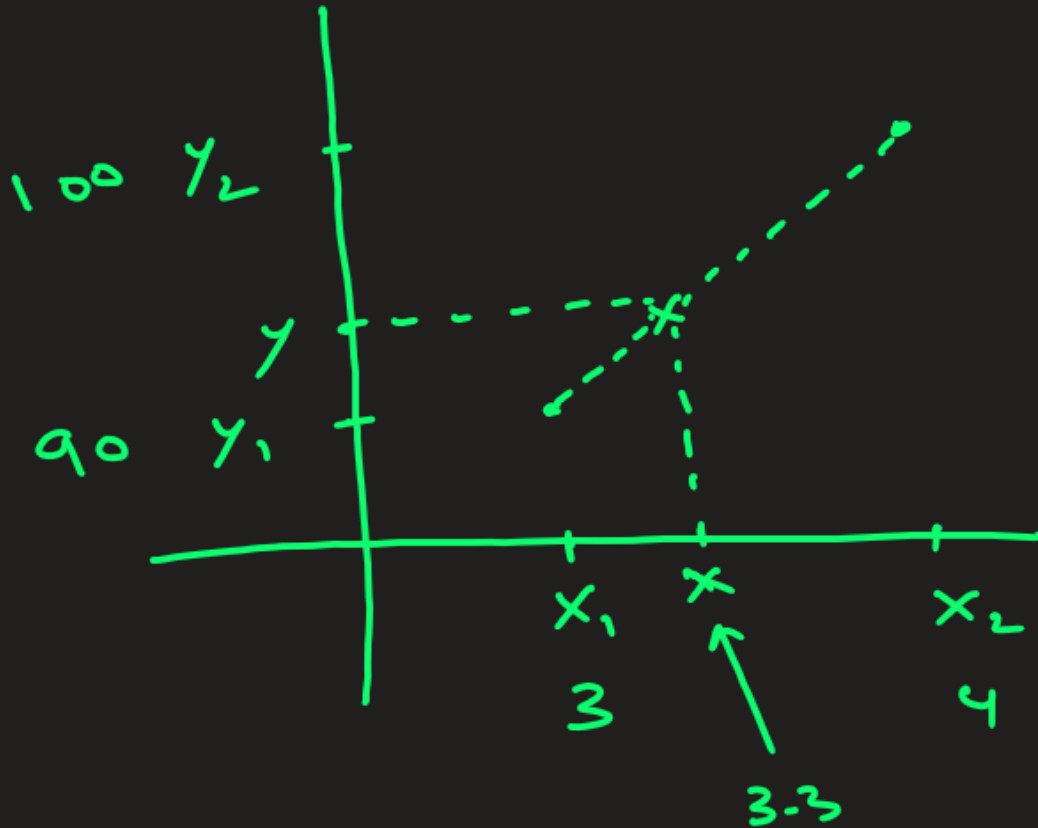
4th value = 100

Now interpolate between these two (explained on next page):

$$\begin{aligned} 30\text{th percentile} &= 90 + 0.3 \times (100 - 90) \\ &= 90 + 3 \\ &= \mathbf{93} \end{aligned}$$

Interpretation: 30% of students scored below 93.

Linear Interpolation Explained



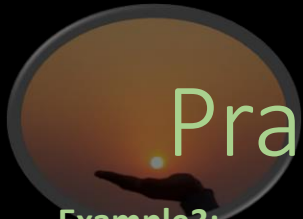
$$\begin{aligned} m &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{100 - 90}{4 - 3} \\ &= 10 \end{aligned}$$

$$\begin{aligned} y &= y_1 + (x - x_1) \cdot m \\ &= 90 + .3(10) \\ &= 93 \end{aligned}$$



STOP





Practice: Percentile (p2)



Example3:

Let's say 10 students took a test and got the following scores out of 200:

[45, 50, 65, 70, 75, 185, 80, 55, 60, 190].

a) Compute percentage and percentile of student who scored 80.

ANSWER: a) Arrange the numbers in ascending:

[45, 50, 55, 60, 65, 70, 75, 80, 185, 190].

Percentage of students who scored 80 = $(80/200) * 100 = 40\%$

Percentile of this student who scored 80 = There are 7 students out of 10 whose scores are below 80:

So percentile of this student is $(7/10) * 100 \rightarrow 70\text{th percentile}$





ML Math-PERCENTAGE-percentile



What is Statistics?



Fndksfndsklf

Fnkjsdfkls'/

Nfkslj/dfjls

nfkldsfs



Hfdslfds

fkdsdjfsD[]

fkdsifa