



## Ensemble Learning

*Training multiple models and combining their predictions.*

Model 1

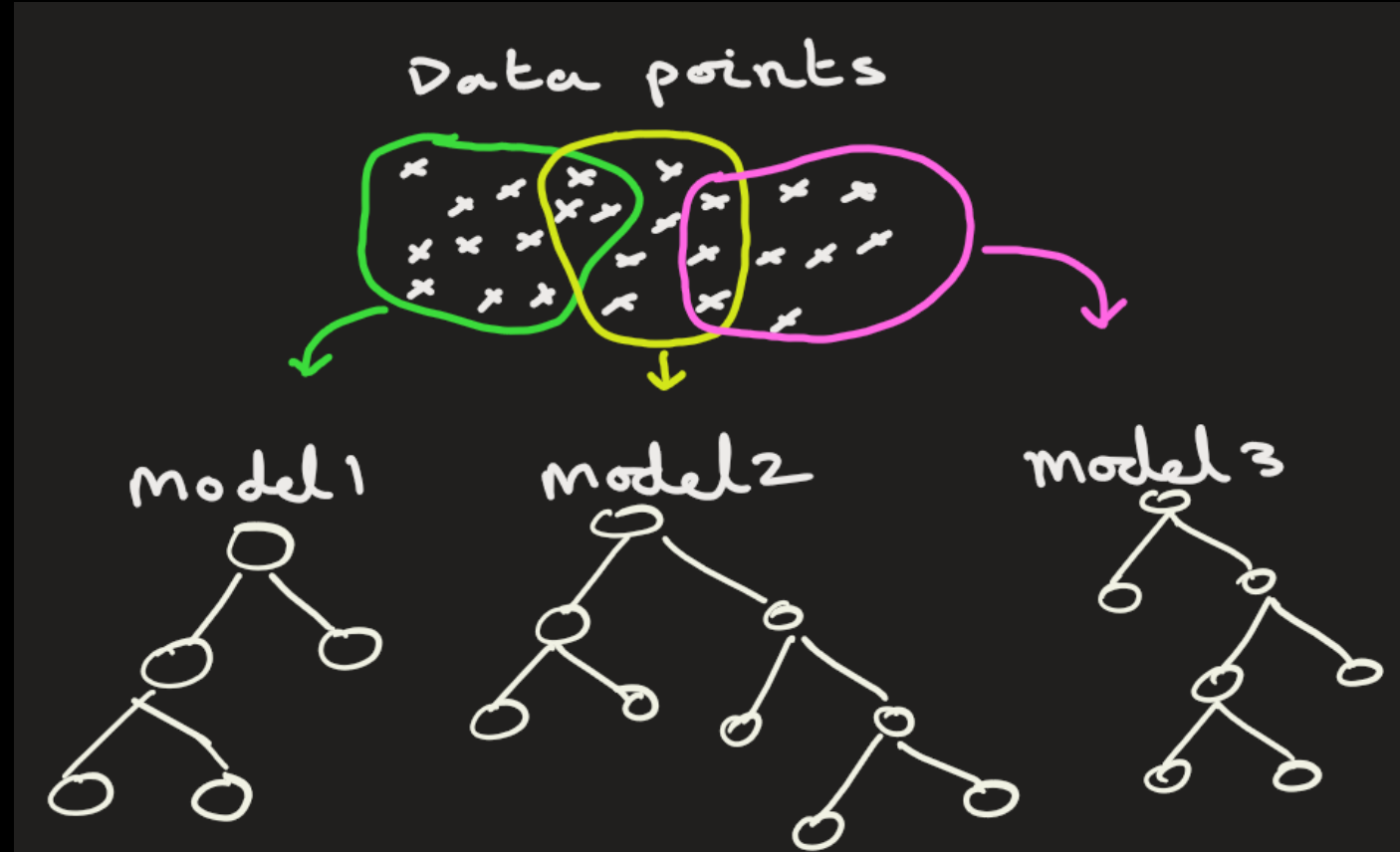
Model 2

...

Model n

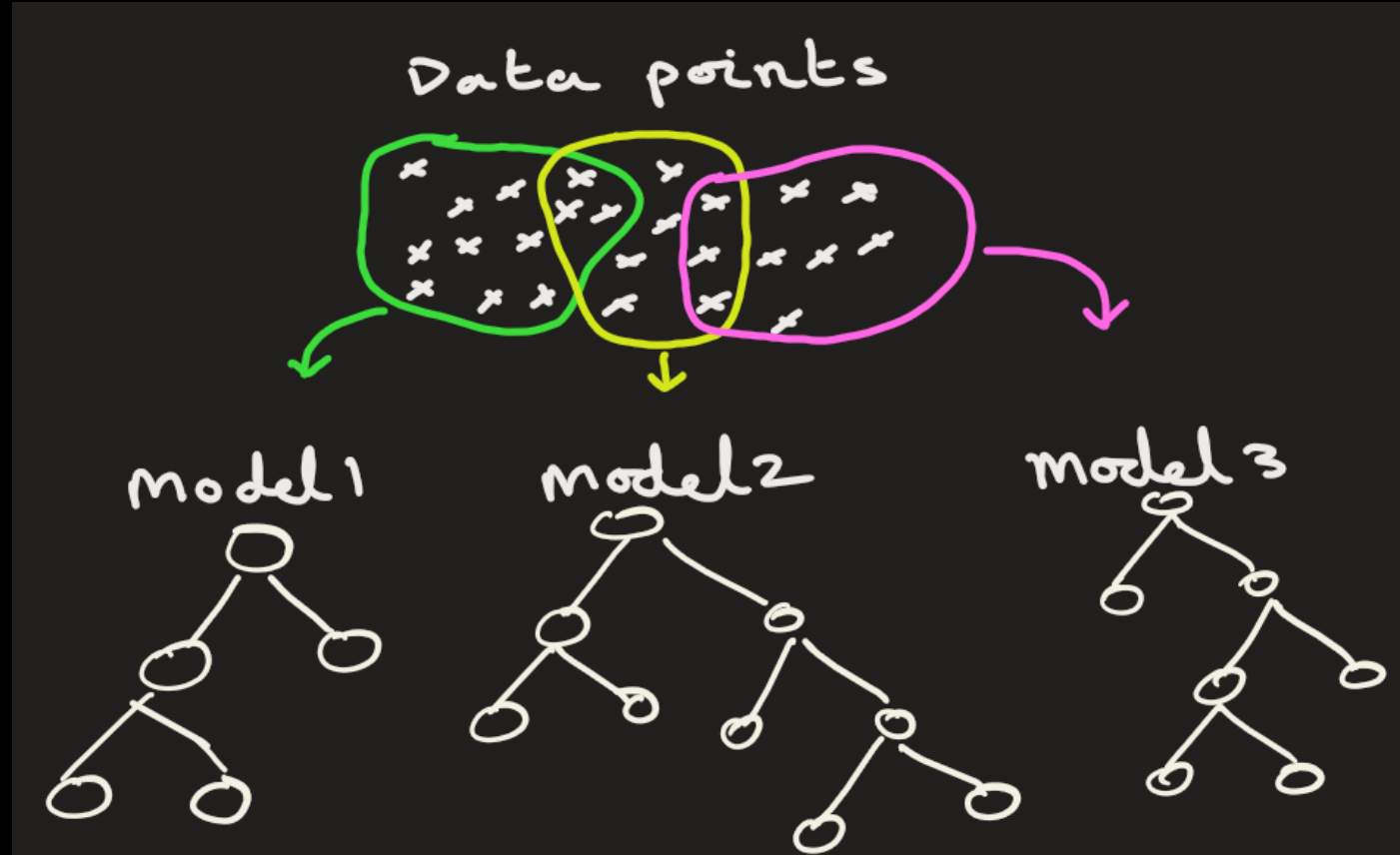
## Bagging (Bootstrap Aggregating):

Train **many models independently** on **different random samples** of the data and **average** their predictions.



## How it Works

1. Create multiple datasets using **bootstrapping** (sampling with replacement)
2. Train a **separate model** on each dataset
3. Combine predictions:  
Classification → **majority vote**  
Regression → **average**





# Example: Random Forest



## Step 1: Create Random Samples of Data and Features

From a dataset with  $k$  total records, we repeatedly select:

- **$n$  random data points** (with replacement)  $\rightarrow$  bootstrap sample
- **$m$  random features** out of all available features

Each sample + feature subset will be used to build one decision tree.

This randomness ensures that every tree is slightly different.

$k=6$

id	$x_1$	$x_2$	$x_3$	$x_4$	$y$
1	-	-	-	-	0
2	-	-	-	-	0
3	-	-	-	-	1
4	-	-	-	-	0
5	-	-	-	-	1
6	-	-	-	-	1

Example: Below we show 3 random samples from  $k=6$  data points with 4 features.

Each sample has  $n=4$  data points and  $m=3$  features.

$n=4, m=3$

id	$x_2$	$x_3$	$x_4$	$y$
2	-	-	-	0
4	-	-	-	0
6	-	-	-	1
2	-	-	-	0

$n=4, m=3$

id	$x_1$	$x_3$	$x_4$	$y$
1	-	-	-	0
5	-	-	-	1
3	-	-	-	1
5	-	-	-	1

$n=4, m=3$

id	$x_1$	$x_2$	$x_3$	$y$
2	-	-	-	0
1	-	-	-	0
4	-	-	-	0
3	-	-	-	1

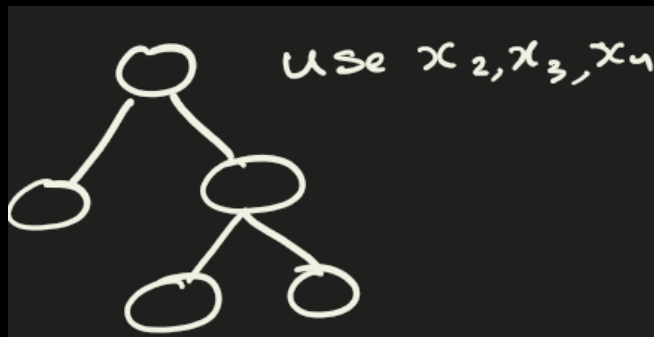


## Step 2: Build a Decision Tree for Each Sample

For each bootstrap sample grow a decision tree.  
Each decision tree is a model.

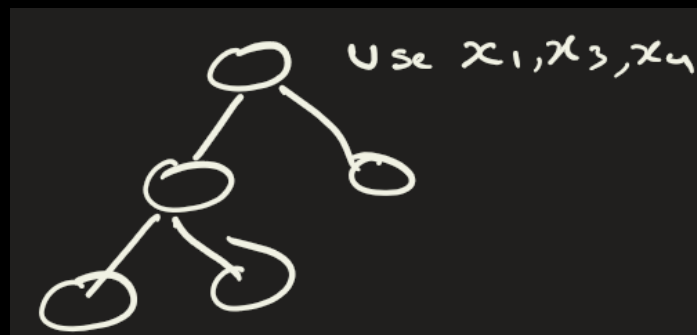
$n=4, m=3$

id	$x_2$	$x_3$	$x_4$	$y$
2	—	—	—	0
4	—	—	—	0
6	—	—	—	1
2	—	—	—	0



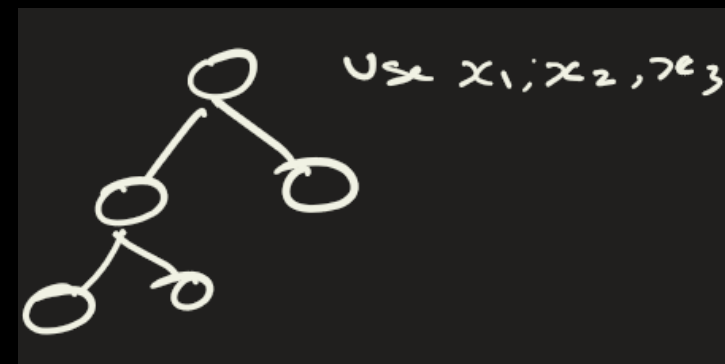
$n=4, m=3$

id	$x_1$	$x_3$	$x_4$	$y$
1	—	—	—	0
5	—	—	—	1
3	—	—	—	1
5	—	—	—	1



$n=4, m=3$

id	$x_1$	$x_2$	$x_3$	$y$
2	—	—	—	0
1	—	—	—	0
4	—	—	—	0
3	—	—	—	1





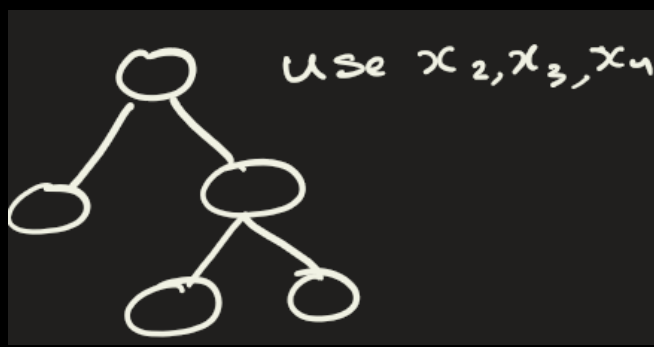
## Step 3: Generate Predictions from All Trees

Each decision tree makes its own prediction:

- A class label (for classification)
- A numerical value (for regression)

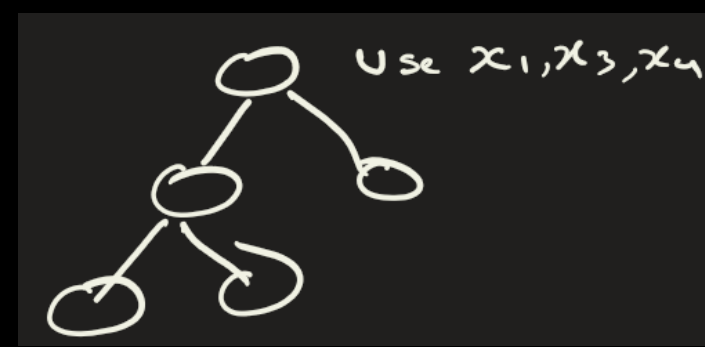
$n=4, m=3$

id	$x_2$	$x_3$	$x_4$	$y$
2	—	—	—	0
4	—	—	—	0
6	—	—	—	1
2	—	—	—	0



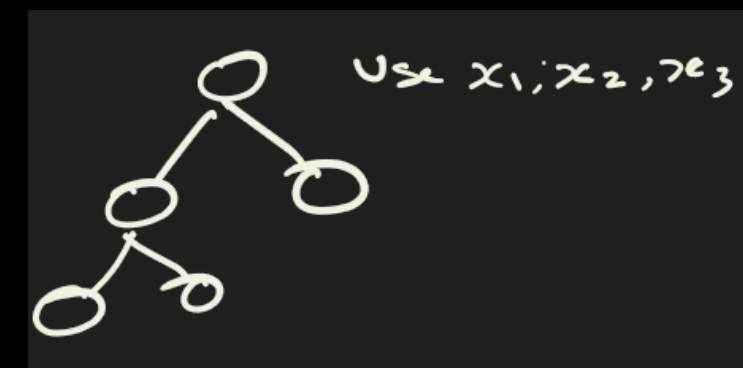
$n=4, m=3$

id	$x_1$	$x_3$	$x_4$	$y$
1	—	—	—	0
5	—	—	—	1
3	—	—	—	1
5	—	—	—	1



$n=4, m=3$

id	$x_1$	$x_2$	$x_3$	$y$
2	—	—	—	0
1	—	—	—	0
4	—	—	—	0
3	—	—	—	1



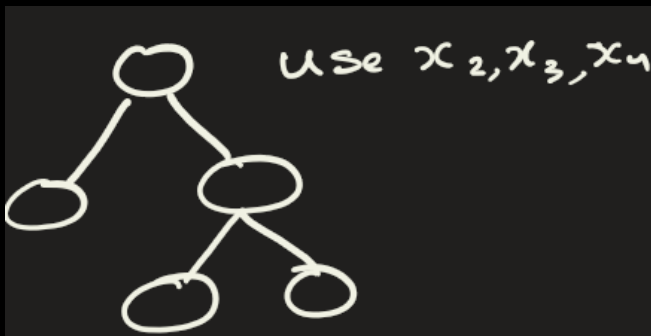
## Step 4: Combine All Predictions to Form the Final Output

- **Classification:** Use **majority voting** → the class predicted by most trees becomes the final prediction.
- **Regression:** Use **averaging** → take the mean of all tree predictions.

Note: Bootstrapping in step1 and Aggregation in step4 is called **Bagging**.

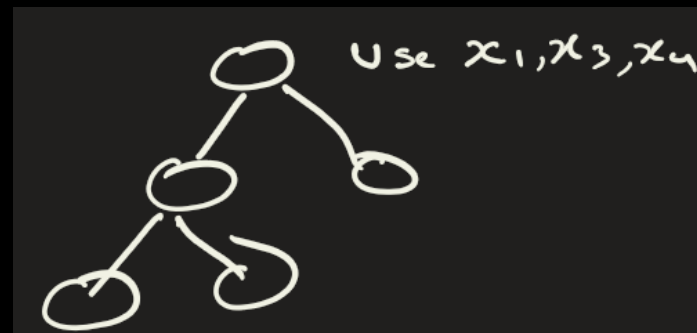
$n=4, m=3$

id	$x_2$	$x_3$	$x_4$	$y$
2	—	—	—	0
4	—	—	—	0
6	—	—	—	1
2	—	—	—	0



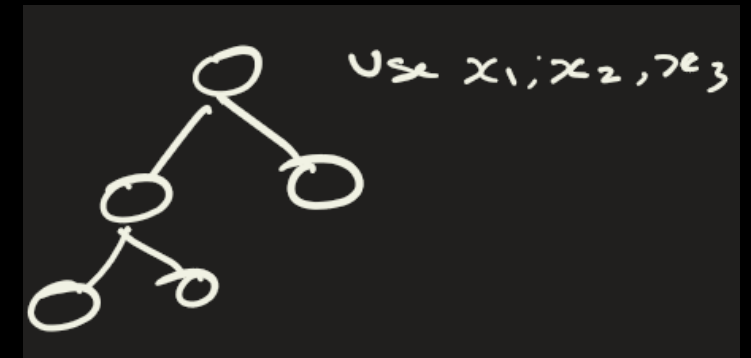
$n=4, m=3$

id	$x_1$	$x_3$	$x_4$	$y$
1	—	—	—	0
5	—	—	—	1
3	—	—	—	1
5	—	—	—	1



$n=4, m=3$

id	$x_1$	$x_2$	$x_3$	$y$
2	—	—	—	0
1	—	—	—	0
4	—	—	—	0
3	—	—	—	1



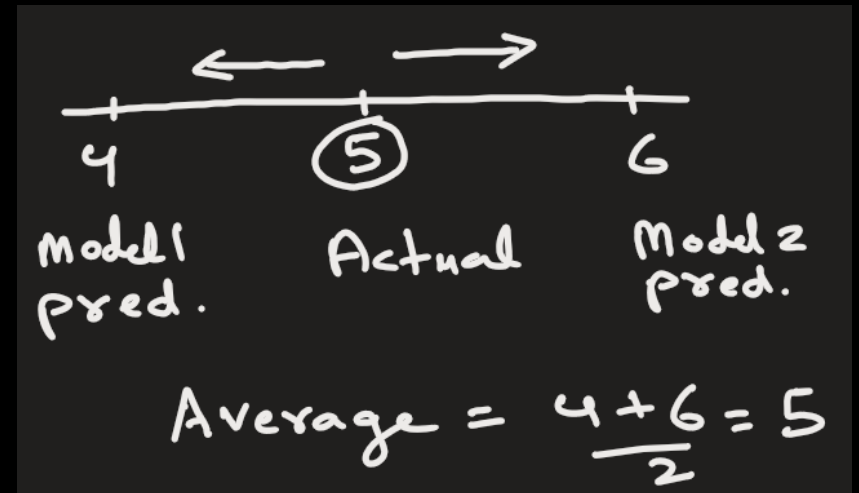
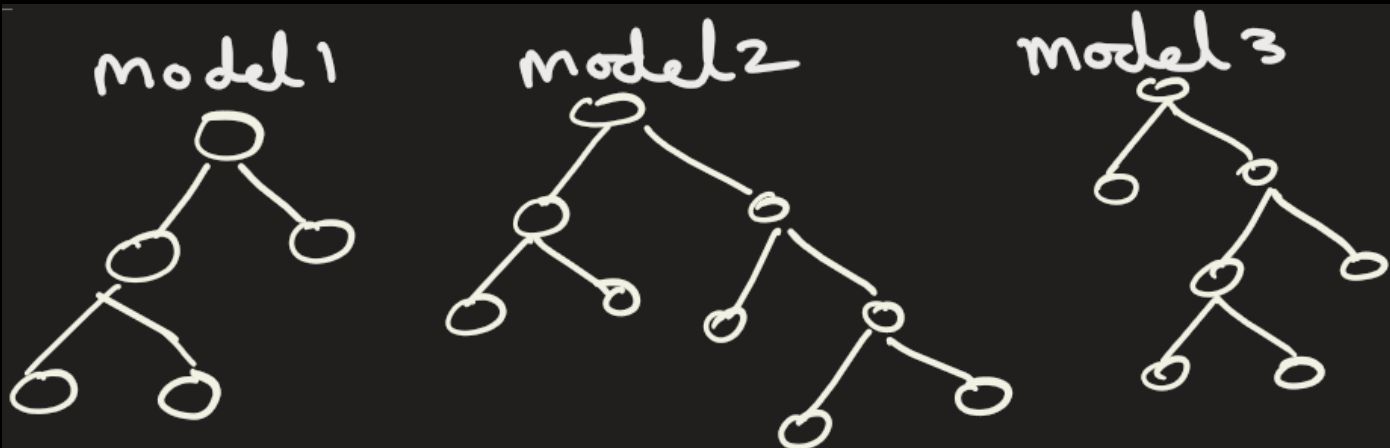


## Bagging (Bootstrap Aggregating):

### Key Characteristics

- Models are trained **in parallel** because each model is **independent**
- Reduces overfitting

Key idea: Reduce variance by averaging noisy models







Fhdsklf  
Fjdsklf  
Fjsklfd

# Heading Goes Here

