



Ensemble Learning

Training multiple models and combining their predictions.

Model 1

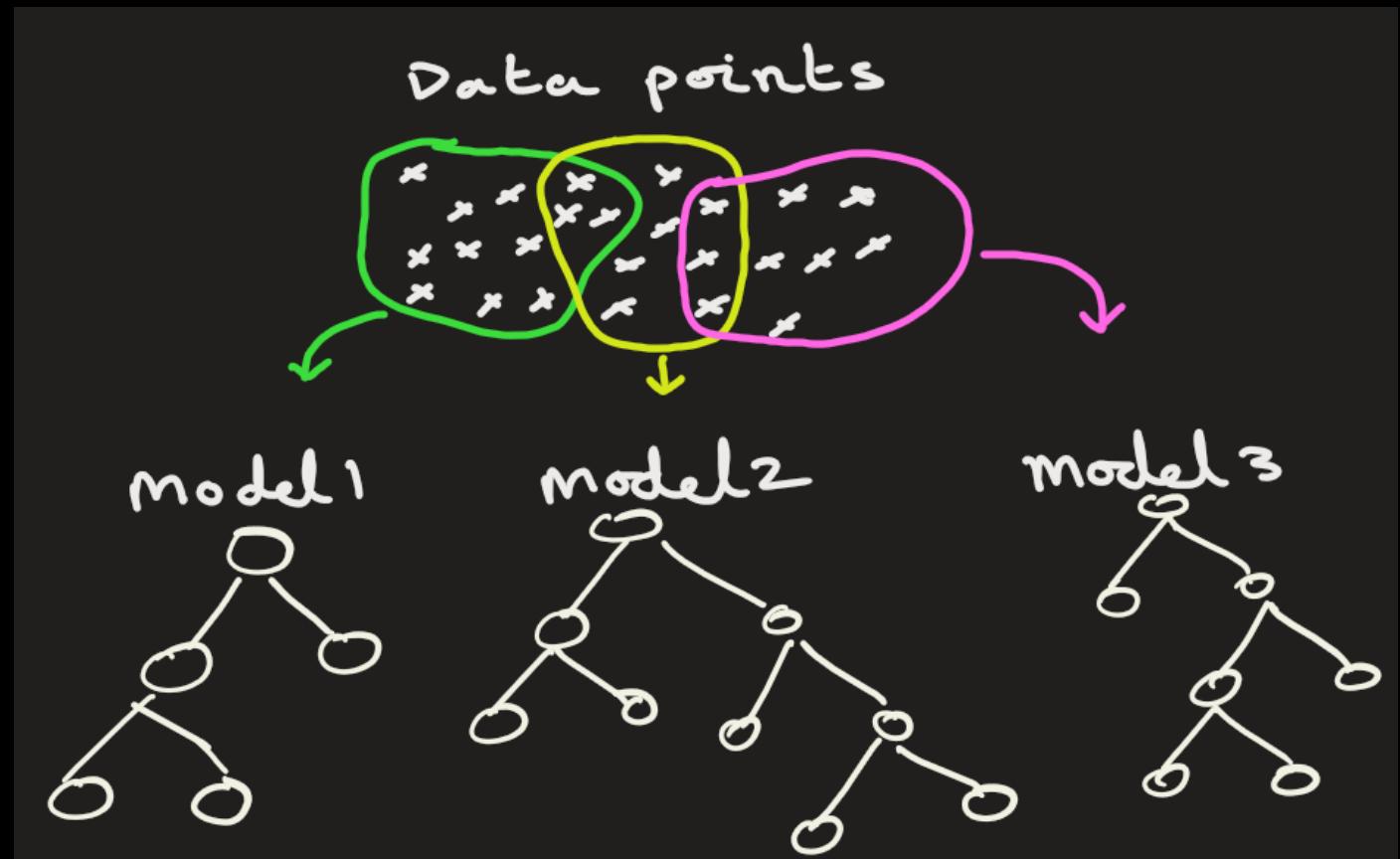
Model 2

...

Model n

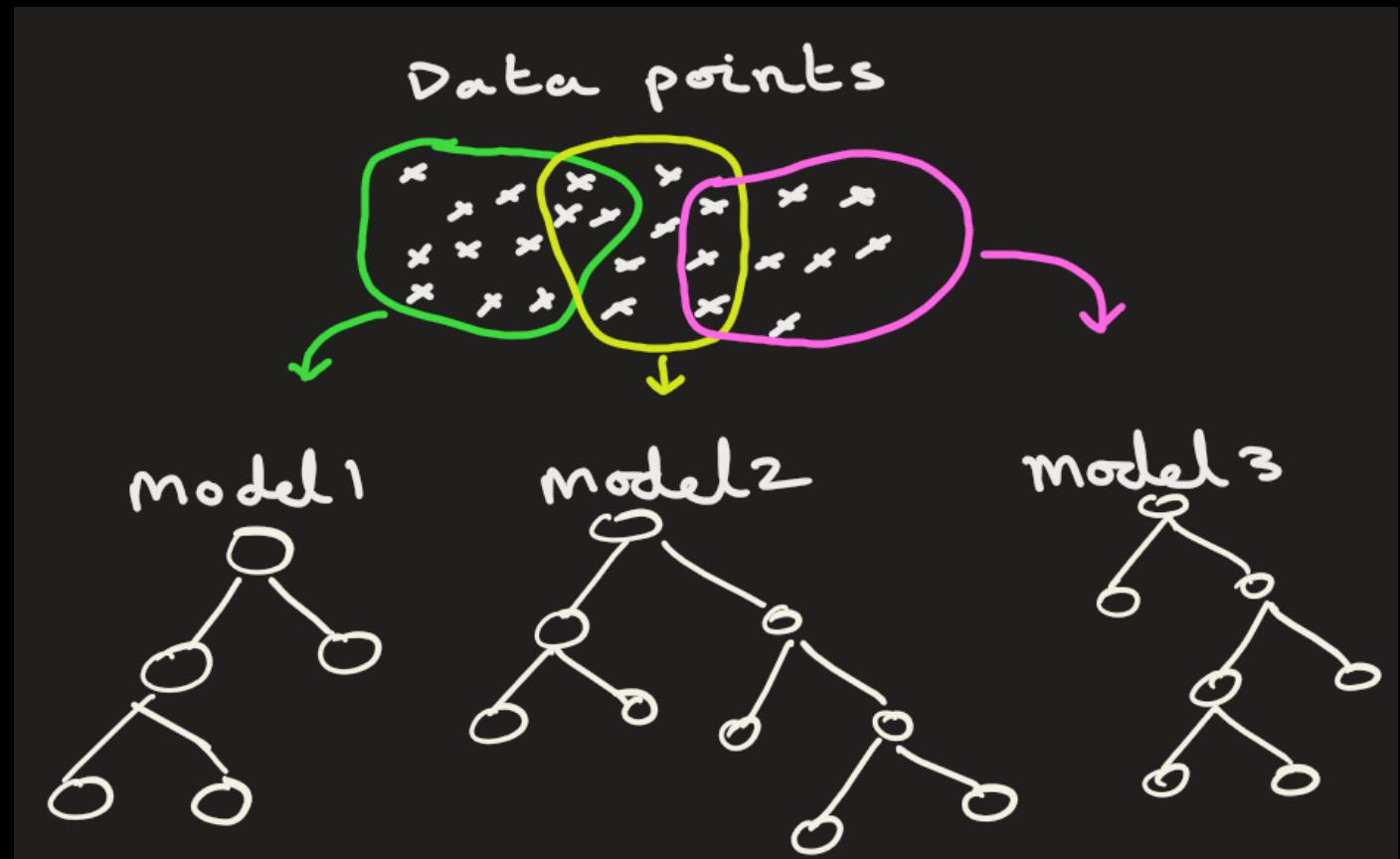
Bagging (Bootstrap Aggregating):

Train **many models independently** on **different random samples** of the data and **average their predictions**.



How it Works

1. Create multiple datasets using **bootstrapping** (sampling with replacement)
2. Train a **separate model** on each dataset
3. Combine predictions:
Classification → **majority vote**
Regression → **average**



Example: Random Forest

Step 1: Create Random Samples of Data and Features

From a dataset with k total records, we repeatedly select:

- **n random data points** (with replacement) → bootstrap sample
- **m random features** out of all available features

Each sample + feature subset will be used to build one decision tree.

This randomness ensures that every tree is slightly different.

$k=6$

<u>id</u>	<u>x_1</u>	<u>x_2</u>	<u>x_3</u>	<u>x_4</u>	<u>y</u>
1	-	-	-	-	0
2	-	-	-	-	0
3	-	-	-	-	1
4	-	-	-	-	0
5	-	-	-	-	1
6	-	-	-	-	1

Example: Below we show 3 random samples from $k=6$ data points with 4 features.

Each sample has $n=4$ data points and $m=3$ features.

$n=4, m=3$

<u>id</u>	<u>x_1</u>	<u>x_2</u>	<u>x_3</u>	<u>x_4</u>	<u>y</u>
2	-	-	-	-	0
4	-	-	-	-	0
6	-	-	-	-	1
2	-	-	-	-	0

$n=4, m=3$

<u>id</u>	<u>x_1</u>	<u>x_2</u>	<u>x_3</u>	<u>x_4</u>	<u>y</u>
1	-	-	-	-	0
5	-	-	-	-	1
3	-	-	-	-	1
5	-	-	-	-	1

$n=4, m=3$

<u>id</u>	<u>x_1</u>	<u>x_2</u>	<u>x_3</u>	<u>x_4</u>	<u>y</u>
2	-	-	-	-	0
1	-	-	-	-	0
4	-	-	-	-	0
3	-	-	-	-	1



Step 2: Build a Decision Tree for Each Sample

For each bootstrap sample grow a decision tree.
Each decision tree is a model.

$n=4, m=3$

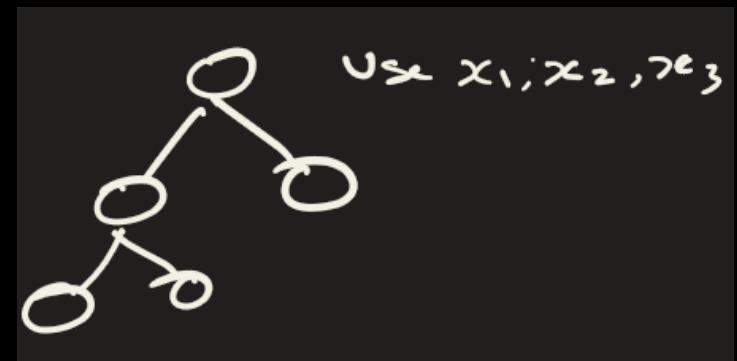
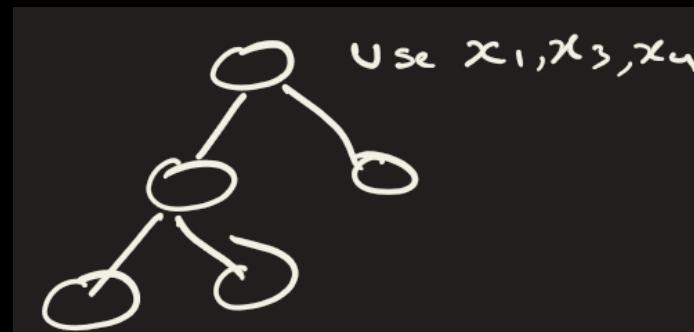
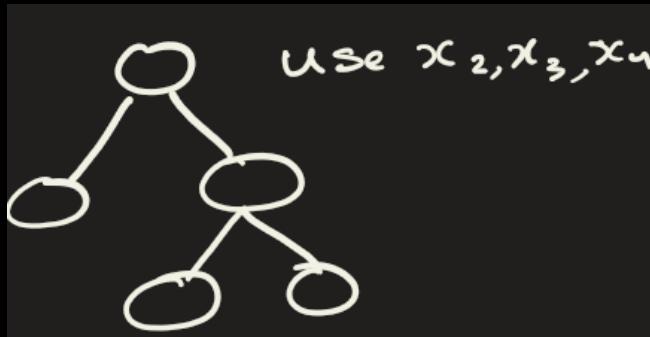
id	x_2	x_3	x_4	y
2	-	-	-	0
4	-	-	-	0
6	-	-	-	1
2	-	-	-	0

$n=4, m=3$

id	x_1	x_3	x_4	y
1	-	-	-	0
5	-	-	-	1
3	-	-	-	1
5	-	-	-	1

$n=4, m=3$

id	x_1	x_2	x_3	y
2	-	-	-	0
1	-	-	-	0
4	-	-	-	0
3	-	-	-	1





Step 3: Generate Predictions from All Trees

Each decision tree makes its own prediction:

- A class label (for classification)
- A numerical value (for regression)

$n=4, m=3$

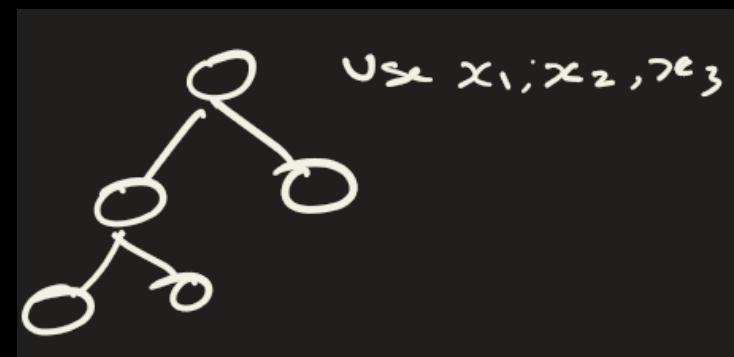
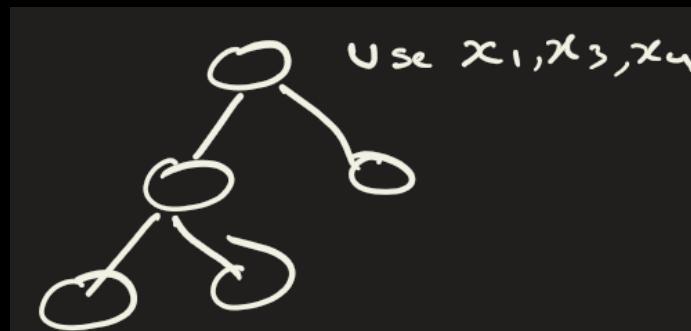
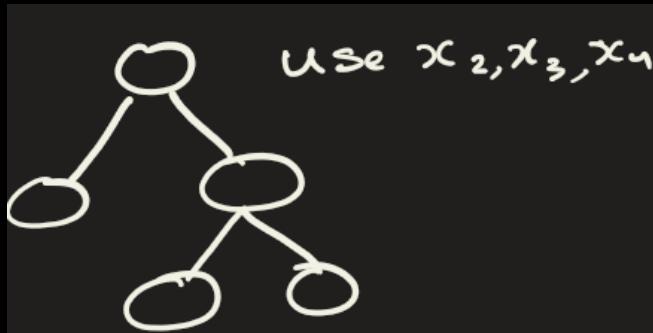
id	x_2	x_3	x_4	y
2	-	-	-	0
4	-	-	-	0
6	-	-	-	1
2	-	-	-	0

$n=4, m=3$

id	x_1	x_3	x_4	y
1	-	-	-	0
5	-	-	-	1
3	-	-	-	1
5	-	-	-	1

$n=4, m=3$

id	x_1	x_2	x_3	y
2	-	-	-	0
1	-	-	-	0
4	-	-	-	0
3	-	-	-	1



Step 4: Combine All Predictions to Form the Final Output



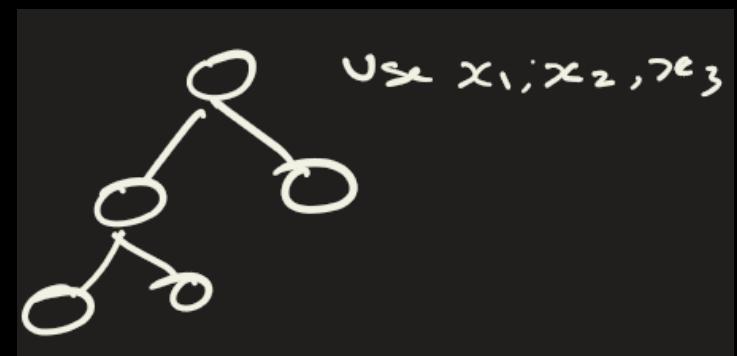
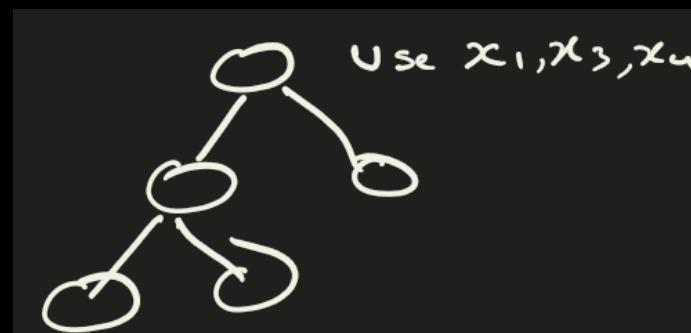
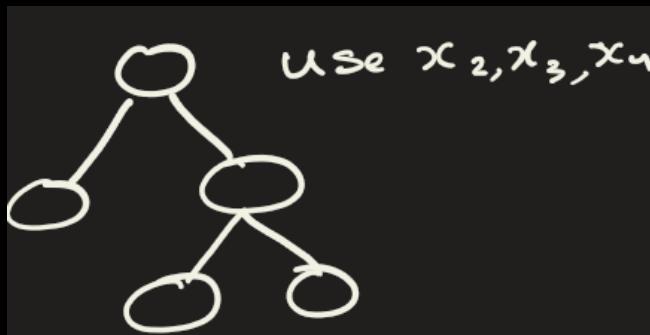
- **Classification:** Use **majority voting** → the class predicted by most trees becomes the final prediction.
- **Regression:** Use **averaging** → take the mean of all tree predictions.

Note: Bootstrapping in step1 and Aggregation in step4 is called **Bagging**.

$n=4, m=3$				
id	x_2	x_3	x_4	y
2	-	-	-	0
4	-	-	-	0
6	-	-	-	1
2	-	-	-	0

$n=4, m=3$				
id	x_1	x_3	x_4	y
1	-	-	-	0
5	-	-	-	1
3	-	-	-	1
5	-	-	-	1

$n=4, m=3$				
id	x_1	x_2	x_3	y
2	-	-	-	0
1	-	-	-	0
4	-	-	-	0
3	-	-	-	1



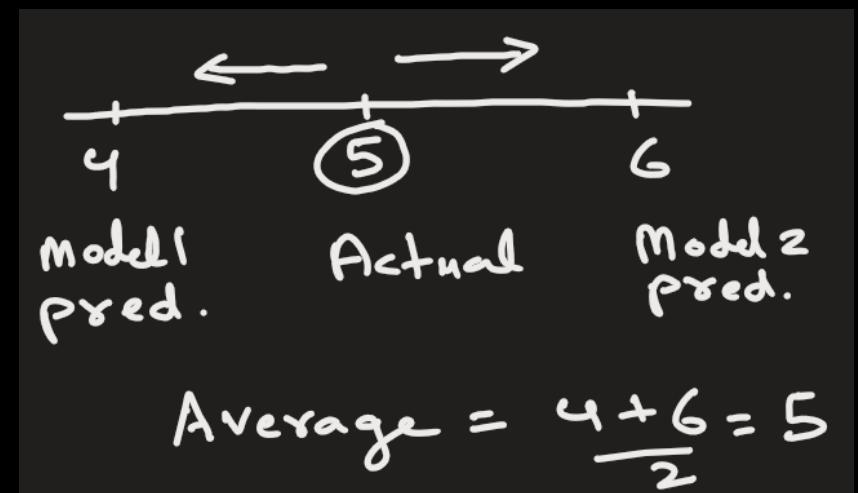
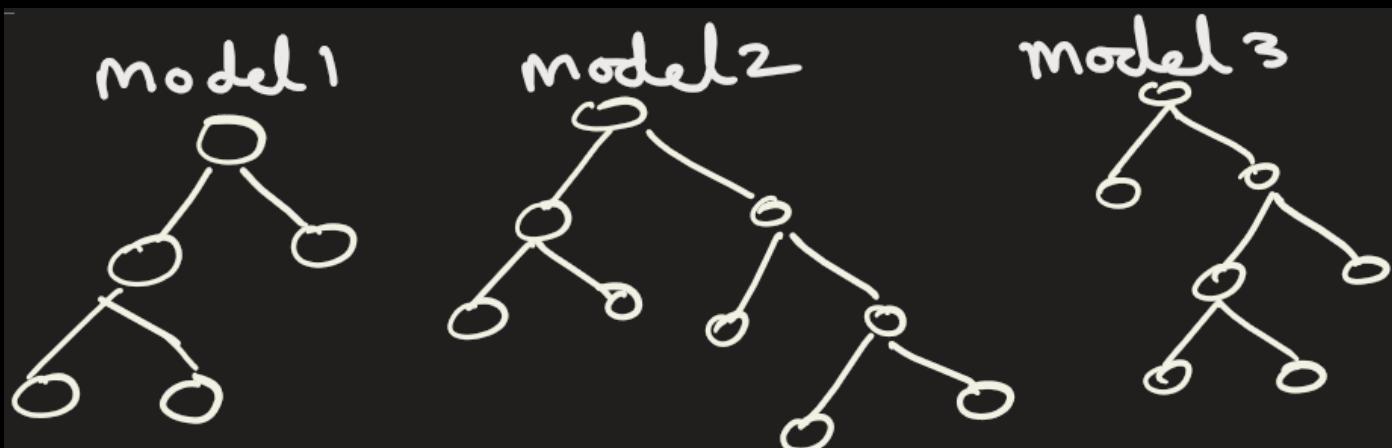


Bagging (Bootstrap Aggregating):

Key Characteristics

- Models are trained **in parallel** because each model is **independent**
- Reduces overfitting

Key idea: Reduce variance by averaging noisy models



Heading Goes Here



Fhdsklf
Fjdsklf
Fjskldf

