

$$a) \quad 0 = v|_v - v|_{v+\Delta v} - v_{leak}$$

$$0 = v|_z - v|_{z+\Delta z} - v_{leak}$$

$$\lim_{\Delta z \rightarrow 0} \frac{v_{leak}}{\Delta z} = \frac{v|_z - v|_{z+\Delta z}}{\Delta z}$$

$$\frac{v_{leak}}{\Delta z} = \frac{dv}{dz} = v_0 \left(-\frac{1}{2L}\right)$$

$$dv = v_0 \left(-\frac{1}{2L}\right) dz \quad \frac{v_{leak}}{\Delta z} = -\frac{v_0}{2L}$$

$$v = v_0 \left(1 - \frac{z}{2L}\right)$$

$$b) \quad \frac{dN_A}{dt} = F_A|_v - F_A|_{v+\Delta v} - k_C A \Delta v - C_A v_{leak}$$

$$\frac{dF_A}{dV} = -k_C A - C_A \frac{v_{leak}}{\Delta v}$$

$$\frac{dF_A}{dV} = -k_C A - \frac{C_A v_0}{A_c} \left(-\frac{1}{2L}\right)$$

$$\frac{dF_A}{dz} = -k_C A_c + \frac{C_A v_0}{2L}$$

c)

$$\frac{dF_A}{dz} = -k \frac{F_A A_c}{v_0 \left(1 - \frac{z}{2L}\right)} + \frac{F_A v_0}{2L v_0 \left(1 - \frac{z}{2L}\right)}$$

$$\frac{dF_A}{dz} = -k \frac{F_A A_c}{v_0 \left(1 - \frac{z}{2L}\right)} + \frac{F_A}{2L \left(1 - \frac{z}{2L}\right)}$$

$$\frac{dF_A}{dz} = -k \frac{F_A A_c}{v_0 \left(1 - \frac{z}{2L}\right)} + \frac{F_A v_0}{v_0 \left(1 - \frac{z}{2L}\right) 2L}$$

$$\frac{dF_A}{dz} = -k \frac{F_A A_c}{v_0 \left(1 - \frac{z}{2L}\right)} + \frac{F_A}{2L \left(1 - \frac{z}{2L}\right)}$$