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# Domain-sum Feature Transformation Applied to Sign Language Feature Extraction

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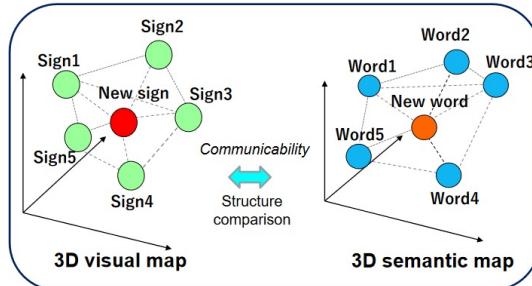
# Agenda

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- Introduction
- Background
- Proposed Research
- Results-so-far
- Next-up

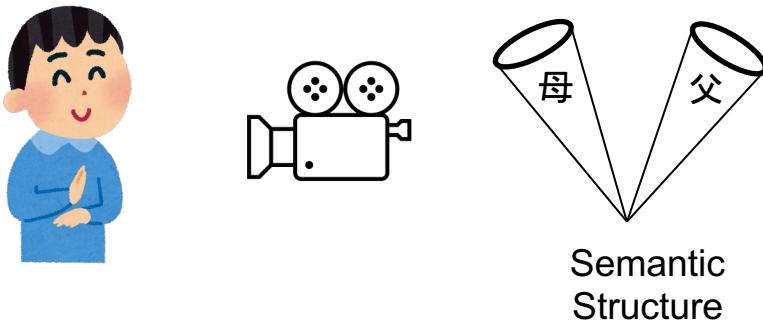
# Introduction

- Sign languages are **visual-based languages**
- On our first work, we proposed a metric to measure similarity between semantic and visual modes



# Introduction

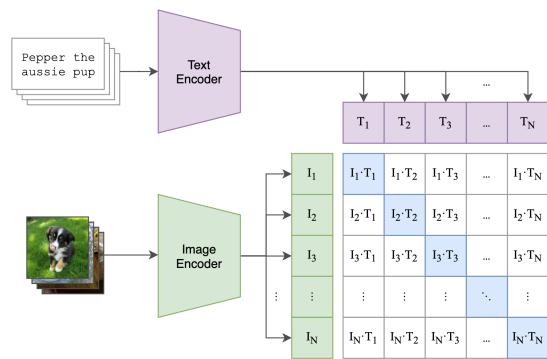
- This time we are tackling feature-generation process.



- How to generate features that better incorporate semantic meaning?

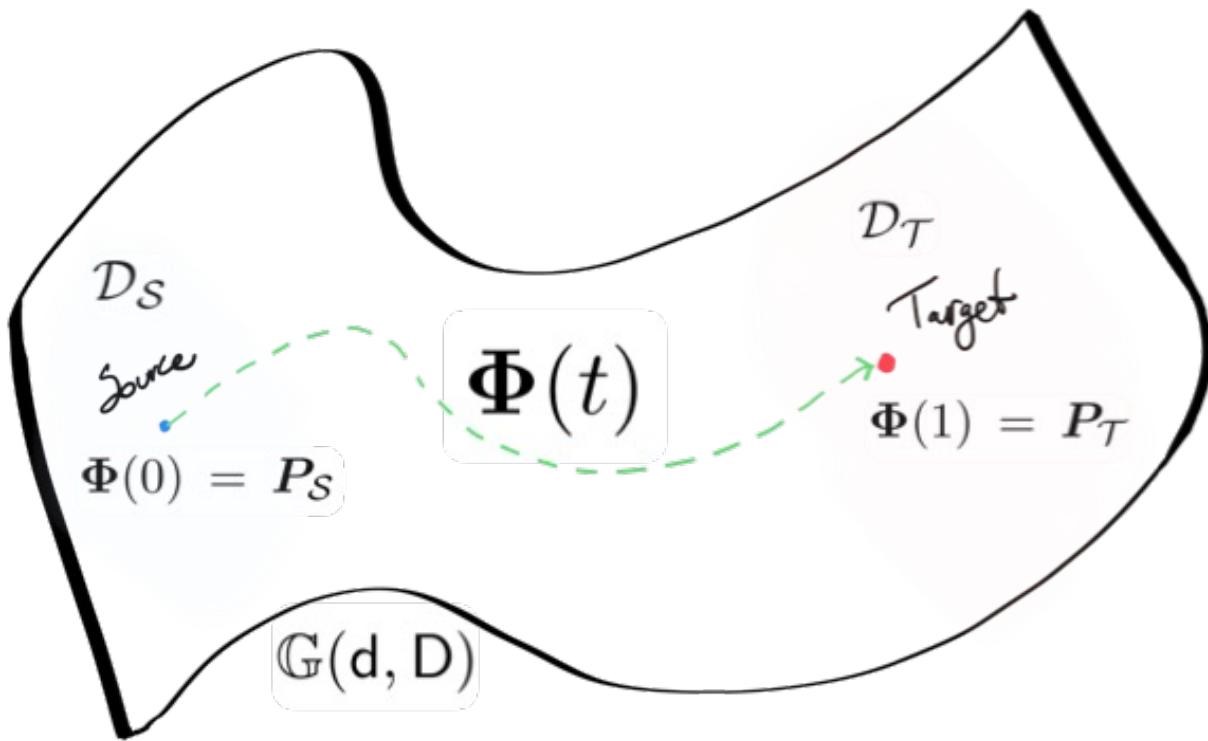
# Introduction

- Learning Transferable Visual Models From Natural Language Supervision (2021)



- Many models tackle this problem: WiFi-CLIP, InternVideo, etc...
- We are interested in investigating an approach called **Domain-sum Feature Transformation**

## Background: Geodesic flow kernel for unsupervised domain adaptation



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- Constructs the **geodesic flow**, which parametrizes how source domain smoothly transitions to target domain

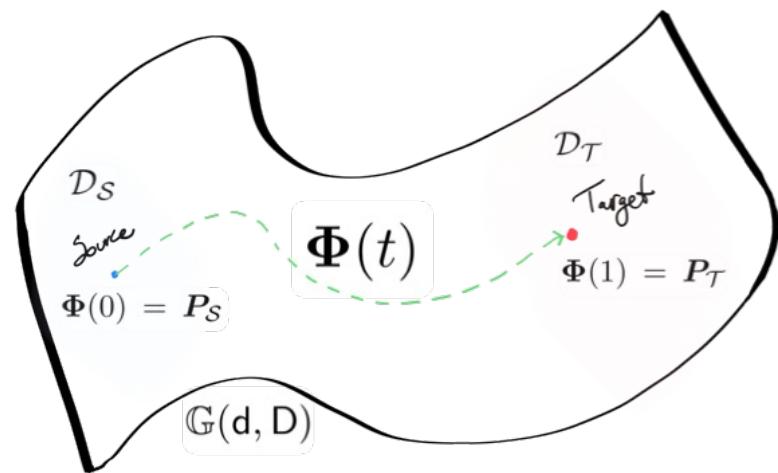
$$\Phi(t) = P_S U_1 \Gamma(t) - R_S U_2 \Sigma(t),$$

$$P_S^T P_T = U_1 \Gamma V^T, \quad R_S^T P_T = -U_2 \Sigma V^T.$$

- By projecting features vectors  $x_i$  into  $\phi(t)$  for *all* continuous values of  $t \in [0, 1]$ , we get an infinite-size feature vector  $z_i^\infty = \phi(t)^T x_i$ .

- The inner-product  $\langle z_i^\infty, z_j^\infty \rangle$  of two feature vectors  $x_i, x_j$  is the **geodesic flow kernel (GFK)**

$$\langle z_i^\infty, z_j^\infty \rangle = \int_0^1 (\Phi(t)^T x_i)^T (\Phi(t)^T x_j) dt = x_i^T G x_j$$



## Background: Domain-Sum Feature Transformation For Multi-Target Domain Adaptation

- **GFK** is harder to incorporate in end-to-end learning.
- Kobayashi et al. [2] proposes that GFK integral can be approximate by the sum of the geodesic flow's extremes.

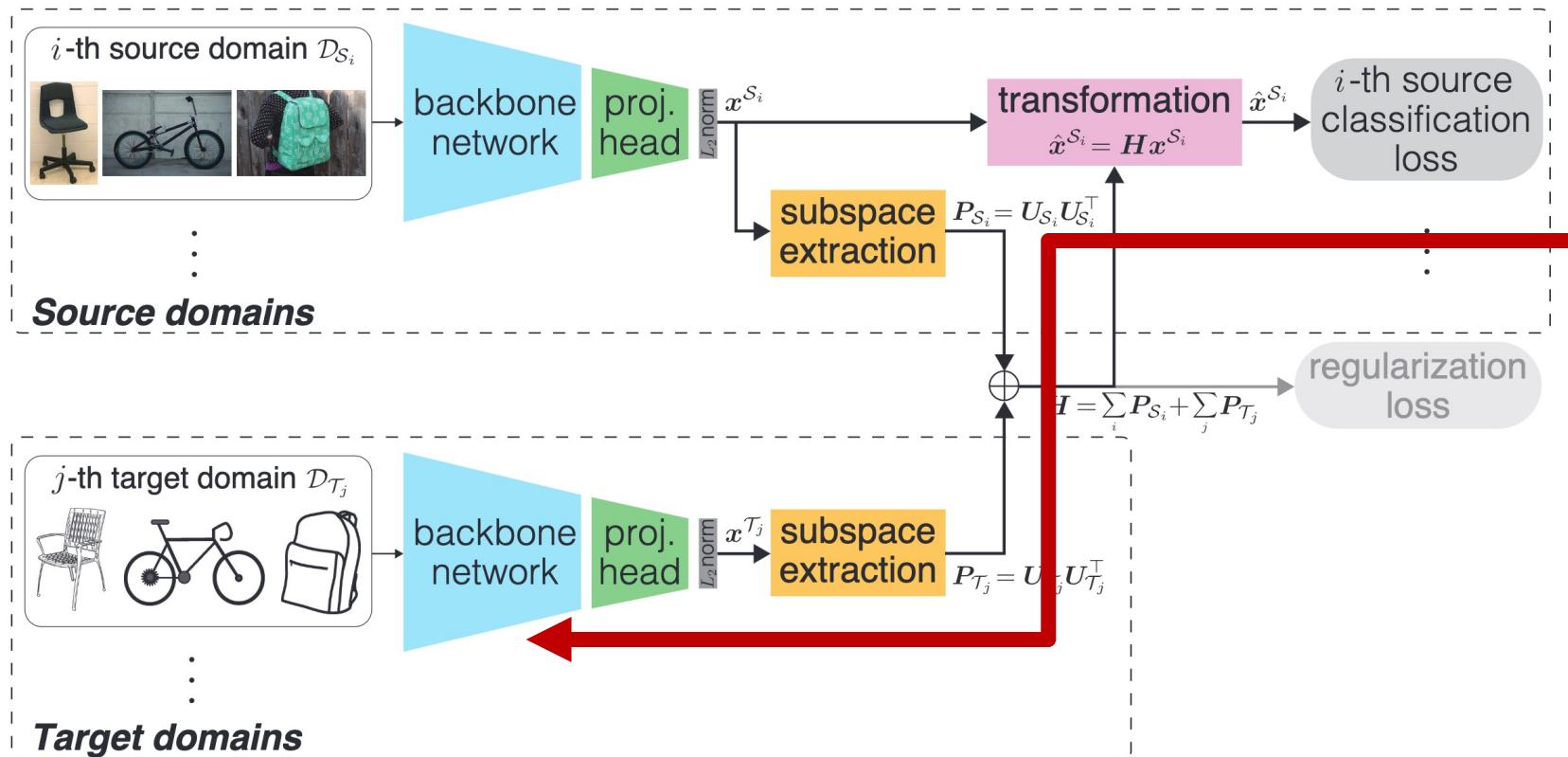
$$G = \int_0^1 \phi(t)\phi(t)^T dt \quad \rightarrow \quad H = \sum_{t \in \{0,1\}} \phi(t)\phi(t)^T$$

- They propose a feature transformation using  $\widehat{H} = H^2$  for the domain adaptation, as

$$x_i^T \widehat{H} x_j = (Hx_i)^T H x_j \rightarrow \widehat{x} = Hx$$

- This is the so-called **domain-sum feature transformation**.

## Background: Domain-Sum Feature Transformation For Multi-Target Domain Adaptation



## Background: Domain-Sum Feature Transformation For Multi-Target Domain Adaptation

- Problem: differentiability of SVD operator

SVD backward isn't correctly defined when multiple 0 eigenvalues #49886

 Clos [feature request] A rank-revealing SVD for better stability in backward. #69532  
 Open (svd|pca)\_lowrank: backward is unstable when for a matrix A, the parameter q is set to a value q > rank(A). #69531  
 Open nikit

Consistent treatment of non-differentiability in linear algebra operations #57272

 Open lezcano opened this issue on Apr 29, 2021 · 2 comments

 Lincon 10h15  
 Oi Mateus, eu to de volta ao trabalho hoje.  
 Sobre o stable/robust SVD: Parece q vc resolveu sua duvida ne.  
 Mas assim, vou explicar qual eh a questao do SVD, pq ele precisa ser "robusto".  
 O fato eh que o SVD nao tem uma derivada definida em todo o espectro.  
 O PDF em anexo demonstra a derivada do SVD, eh bem complicado mas mando pra referencia.  
 Existe uma parte onde eh necessario o calculo do reciproco da diferenca entre dois autovalores.  
 (a equacao entre 11 e 12, no texto, que comeca com F\_ij). Se os dois autovalores s\_i e s\_j forem iguais, a diferenca eh zero e o reciproco eh indefinido, inviabilizando toda a cadeia de calculo.  
 Faz sentido? Espero que isso ajude a entender porque o SVD eh instavel na regiao de autovalores proximos.  
 E isso nao eh uma fronteira nitida, eh uma funcao continua que cresce exponencialmente, entao ate mesmo valores diferentes, mas proximos eh suficiente para explodir o gradiente bastam para inviabilizar o SVD no forward de uma rede neural. Na minha experiencia isso se manifesta como erros de convergencia na funcao torch.svd e/ou torch.eig.

- The differential of SVD operator depends on a matrix  $\tilde{K}$  inversely proportional to the difference of eigenvalues.

$$\tilde{\mathcal{K}}_{ij} = \begin{cases} 1/(\lambda_i - \lambda_j), & i \neq j \\ 0, & i = j \end{cases}$$

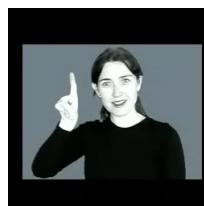
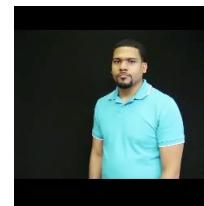
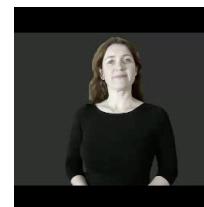
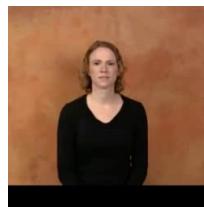
- To solve this, some methods have been proposed using Taylor approximation [3] and Padé approximations [4]. Kobayashi et al. used Taylor approximations.

## Background: Word-level Deep Sign Language Recognition from Video: A New Large-scale Dataset and Methods Comparison

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- A new dataset: WLASL2000

- 2000 Glosses (labels)
- 21.083 Videos



- Classified this dataset using 4 different architectures

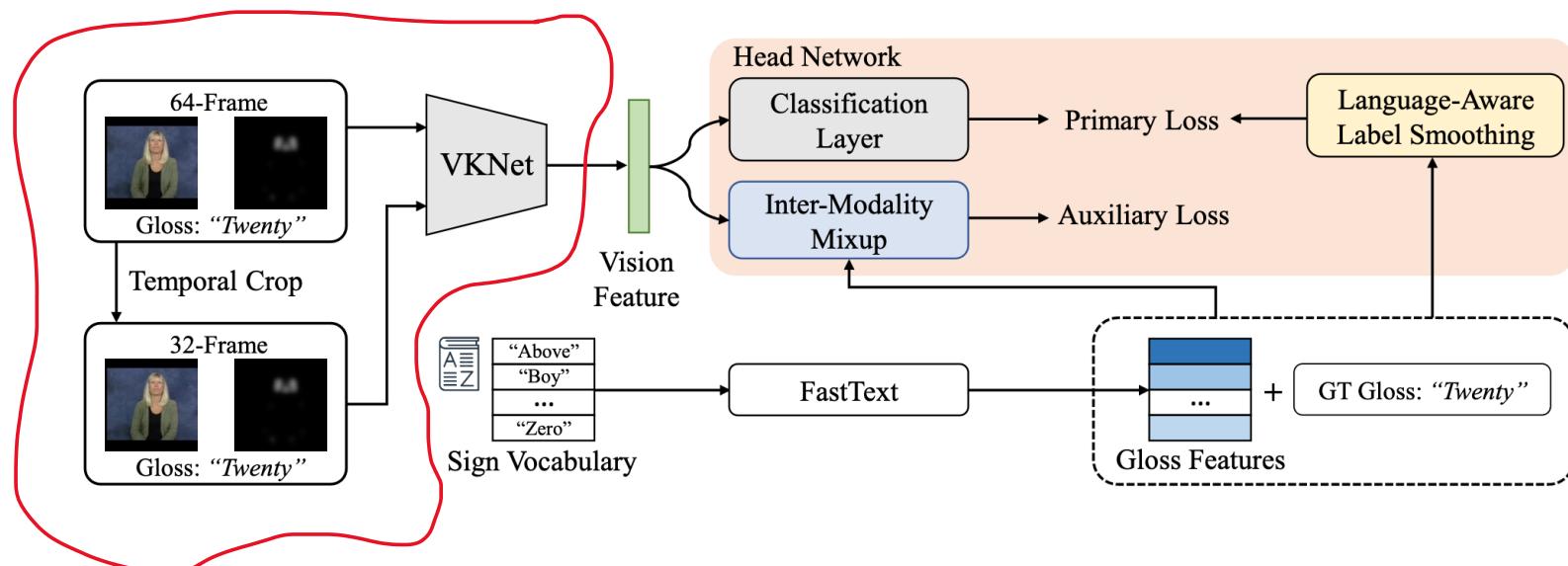
Method	WLASL2000		
	top-1	top-5	top-10
Pose-GRU	22.54	49.81	61.38
Pose-TGCN	23.65	51.75	62.24
VGG-GRU	8.44	23.58	32.58
I3D	<b>32.48</b>	<b>57.31</b>	<b>66.31</b>

## Background: Natural Language-Assisted Sign Language Recognition

- NLA-SLR: (current) state-of-the-art model on WLASL2000

Method	WLASL2000			
	Per-instance		Per-class	
	Top-1	Top-5	Top-1	Top-5
NLA-SLR (Ours)	61.05	91.45	58.05	90.70
NLA-SLR (Ours, 3-crop)	<b>61.26</b>	<b>91.77</b>	<b>58.31</b>	90.91

- Classification head incorporates language knowledge using label-smoothing and mix-up.

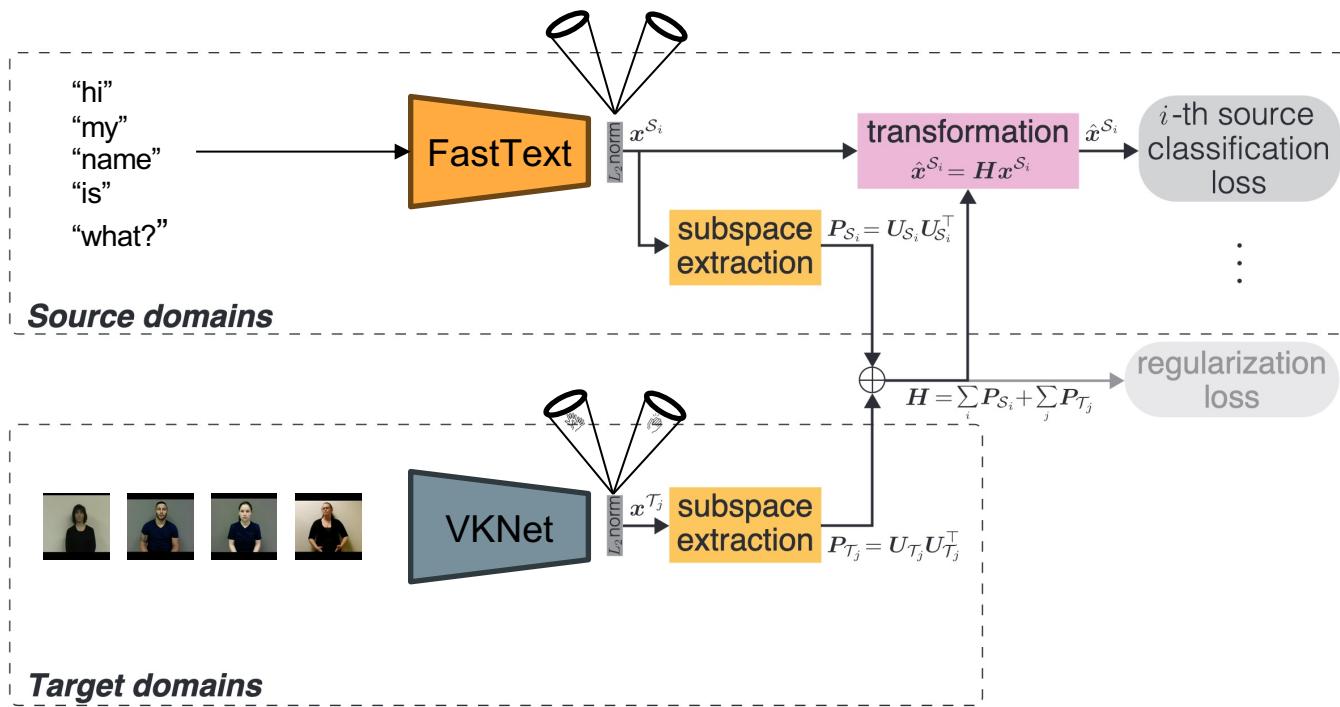


## Proposed Research

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- Domain-sum Feature Transformation has been shown to be effective in bridging the gap between same-modal datasets:
  - Ex: **photos** of cars and **drawings** of cars
- Could it be effective for datasets in different modes?
  - Ex: **Visual**-language and **Textual**-language.
- Can we generate a richer semantic feature-space from the videos by bridging the gap between visual and textual representation?

# Proposed Research



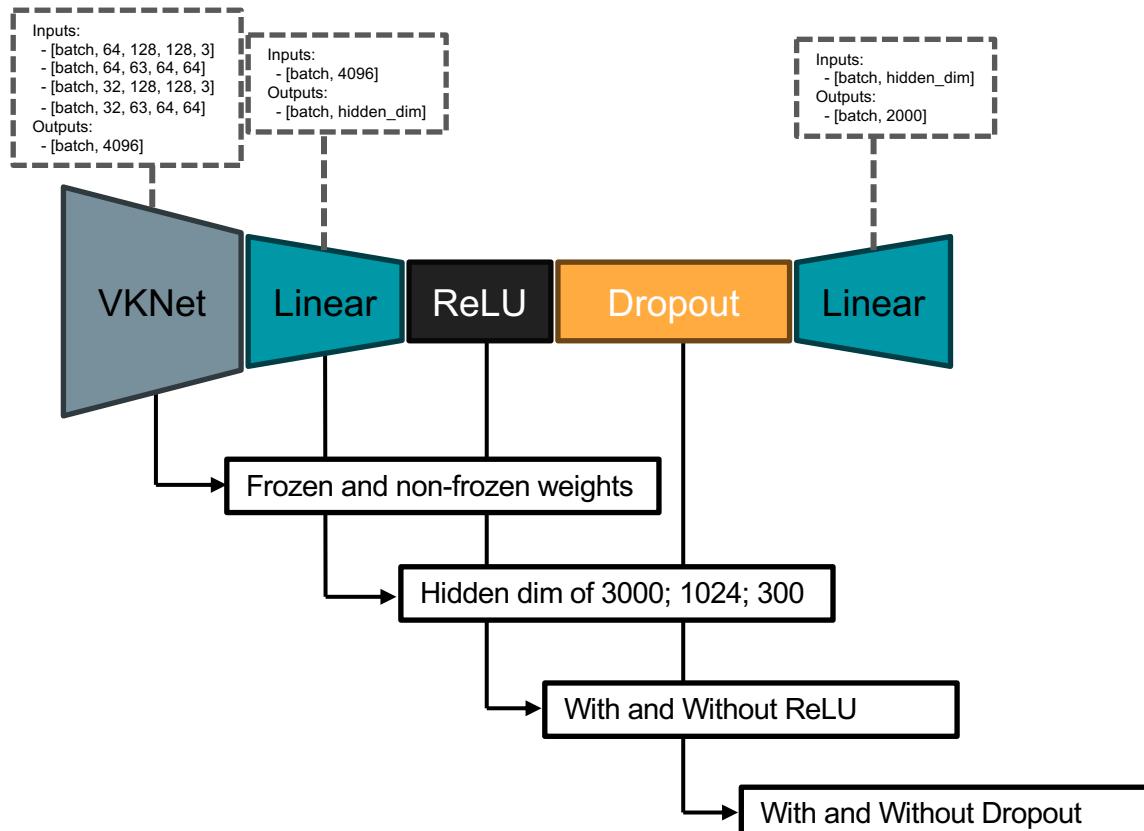
## Proposed Research

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- Does the method converge?
- Does it improve classification accuracy?
- Does it improves the communicability between visual-semantic modes?

## Results-so-far

- Trained VKNet on WLASL2000 from pre-trained weights, removing language head.



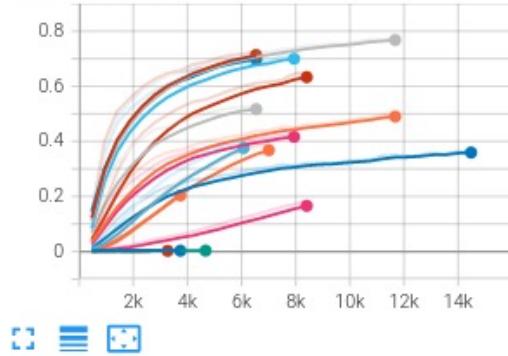
```

batch_size: 10
min_number_of_frames: 25
criterion:
  cross_entropy_loss:
    reduction: mean
optimizer:
  adam:
    lr: 0.001
    weight_decay: 0.001
    betas:
      - 0.9
      - 0.998
lr_scheduler:
  cosine_annealing_lr:
    eta_min: 0
    T_max: 100
  
```

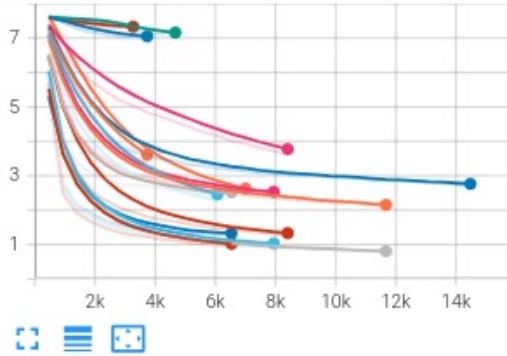
## Results-so-far

- VKNet training stats

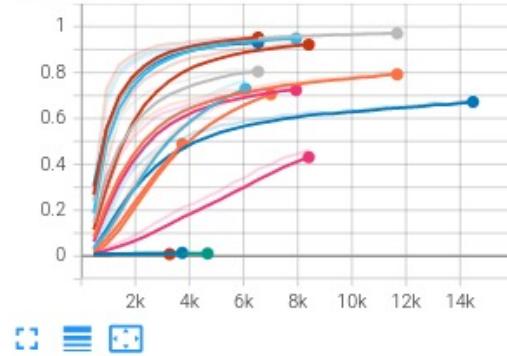
Train/Accuracy  
tag: Train/Accuracy



Train/Loss  
tag: Train/Loss

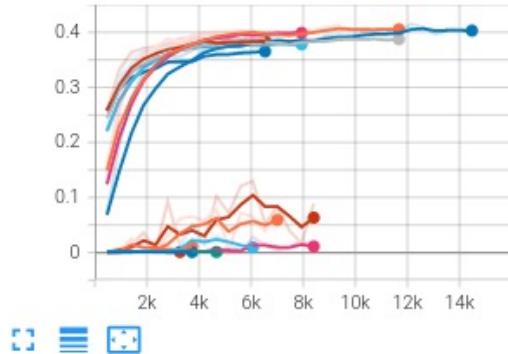


Train/Top-5 Accuracy  
tag: Train/Top-5 Accuracy

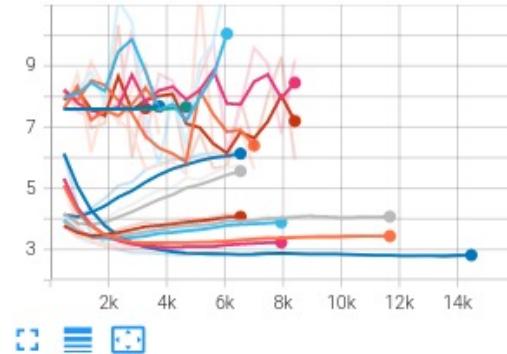


### Validation

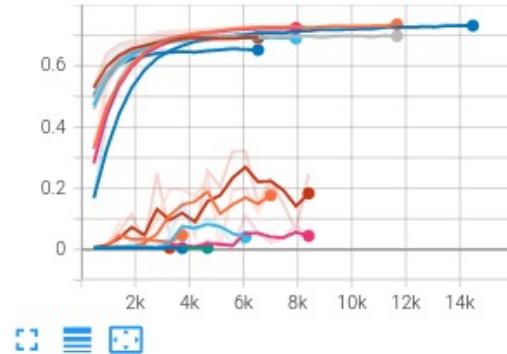
Validation/Accuracy  
tag: Validation/Accuracy



Validation/Loss  
tag: Validation/Loss



Validation/Top-5 Accuracy  
tag: Validation/Top-5 Accuracy



## Next-up

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- Test training using video augmentation.
- Calculate communicability from current model (torchmetrics).
- Implement domain-sum architecture. Especially, implement SVD backwards pass (torch.autograd).
- Vizualize and compare metrics.

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# Thank you

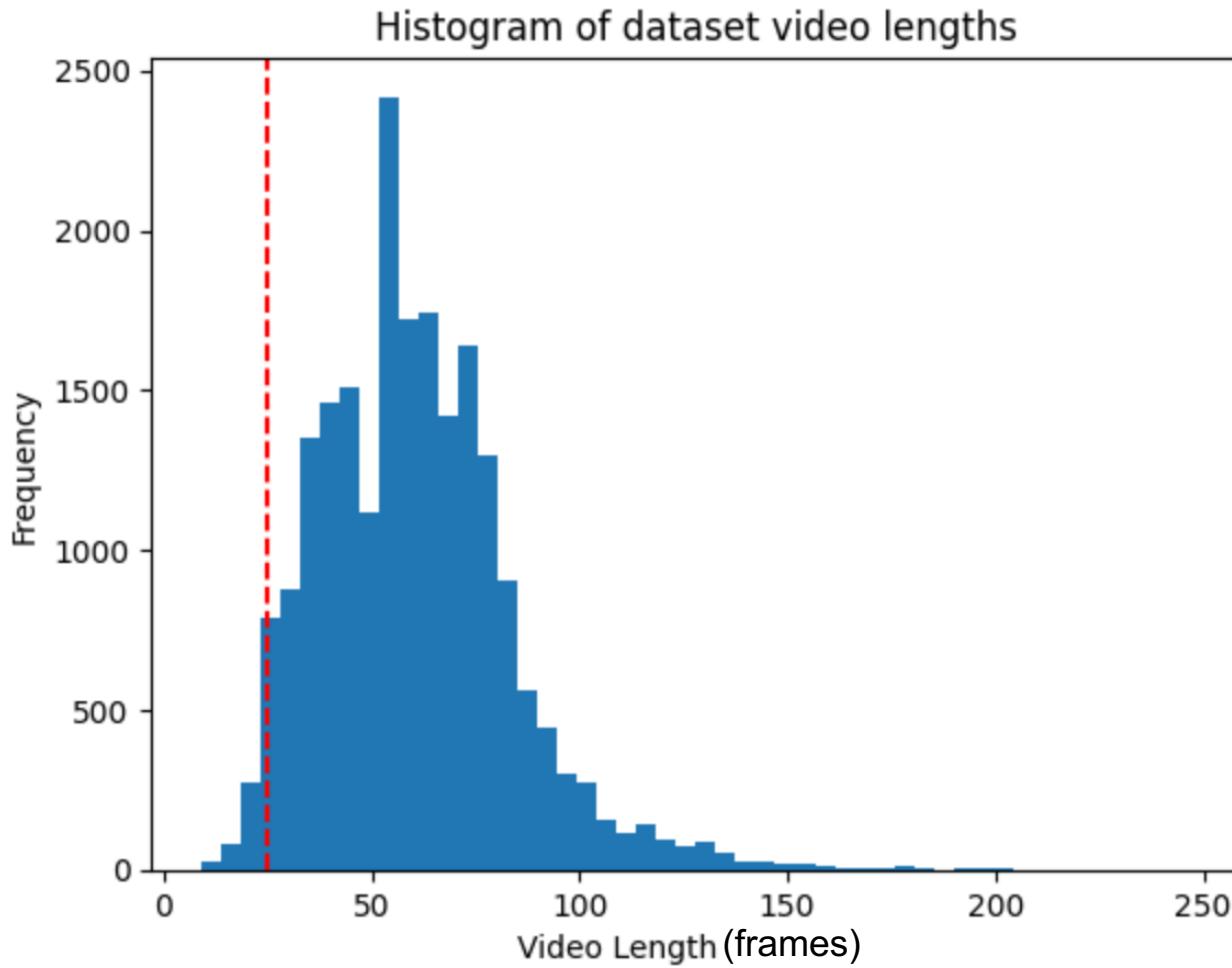
## References

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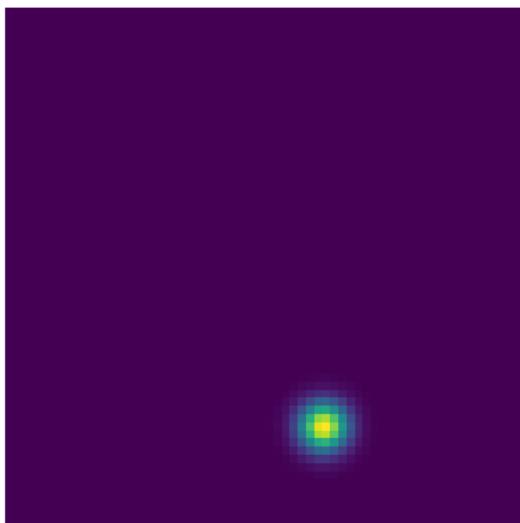
1. [Geodesic flow kernel for unsupervised domain adaptation](#)
2. [Domain-Sum Feature Transformation For Multi-Target Domain Adaptation](#)
3. [Robust Differentiable SVD](#)
4. [Why Approximate Matrix Square Root Outperforms Accurate SVD in Global Covariance Pooling](#)
5. [WLASL: A large-scale dataset for Word-Level American Sign Language](#)
6. [Natural Language-Assisted Sign Language Recognition](#)
7. [Differentiating the Singular Value Decomposition](#)

## Extras

Proportion of numbers greater than n=25: 0.9778494521652517 467 count=20616



## Extras

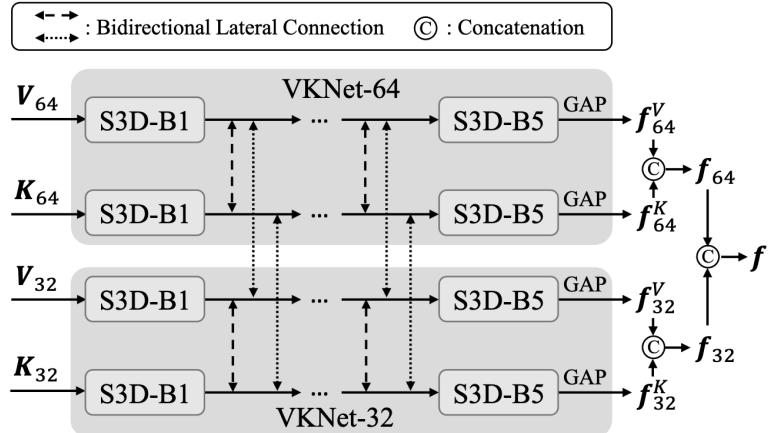


Example of keypoint heatmap

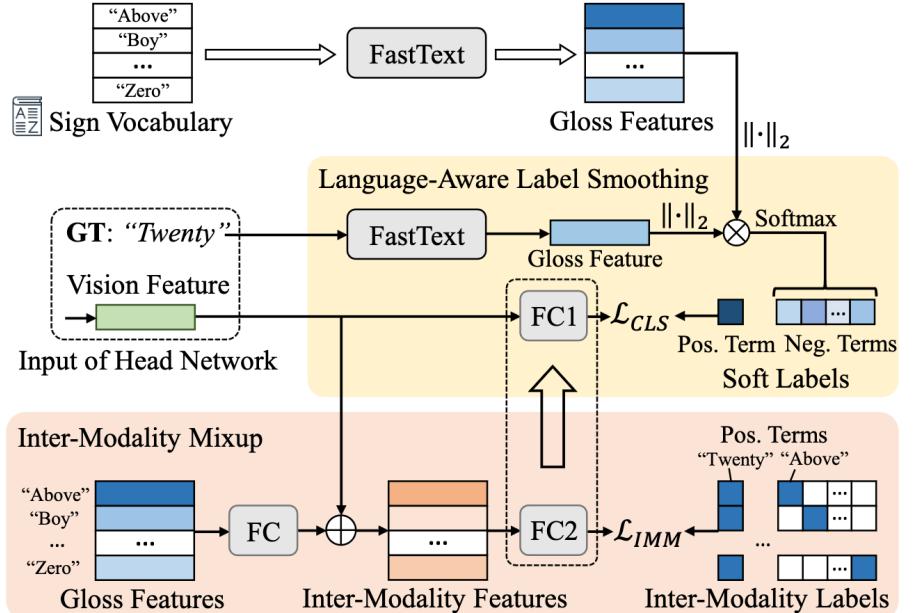


Mean heatmaps overlayed on video

## Extras



$$\mathbf{y}[i] = \begin{cases} 1 - \epsilon & \text{if } i = b, \\ \epsilon \cdot \frac{\exp(\mathbf{s}[i]/\tau)}{\sum_{i=1, i \neq b}^N \exp(\mathbf{s}[i]/\tau)} & \text{otherwise,} \end{cases}$$



## Extras

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**Algorithm 1** Subspace extraction module

**Input:**  $\mathbf{X} \in \mathbb{R}^{d \times B}$ : features on a mini-batch of size  $B$ ,

$r$ : subspace rank,

$\mathbf{M} \in \mathbb{R}^{d \times Q}$ : memory bank to store samples,

**Output:**  $\mathbf{P} \in \mathbb{R}^{d \times d}$ : subspace projection matrix

1:  $[\mathbf{X}, \mathbf{M}] = \mathbf{U} \Lambda \mathbf{V}^\top$  : SVD [8]

2:  $\mathbf{P} = \mathbf{U}_{:,r} \mathbf{U}_{:,r}^\top$  : extract the first  $r$ -rank basis vectors

3: Enqueue  $\mathbf{X}$  to  $\mathbf{M}$  and dequeue old samples from  $\mathbf{M}$

4: **return**  $\mathbf{P}$

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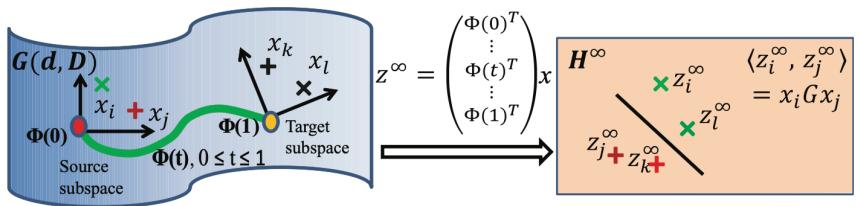


Figure 1. Main idea of our geodesic flow kernel-based approach for domain adaptation (Best viewed in color). We embed source and target datasets in a Grassmann manifold. We then construct a geodesic flow between the two points and integrate an infinite number of subspaces along the flow  $\Phi(t)$ . Concretely, raw features are projected into these subspaces to form an infinite-dimensional feature vector  $z^\infty \in \mathcal{H}^\infty$ . Inner products between these feature vectors define a kernel function that can be computed over the original feature space in closed-form. The kernel encapsulates incremental changes between subspaces that underly the difference and commonness between the two domains. The learning algorithms thus use this kernel to derive low-dimensional representations that are invariant to the domains.