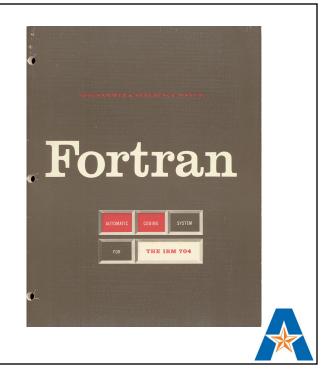
Compilers

CSE 4305 / CSE 5317 M02 Syntactic Analysis Fall 2020



M02 Syntactic Analysis



Phases of Compilation Character stream Scanner (lexical analysis) Token stream Front Parser (syntax analysis) end Parse tree Semantic analysis and Symbol table intermediate code generation Abstract syntax tree or other intermediate form Machine-independent code improvement (optional) Modified intermediate form Target code generation Target language Back (e.g., assembler) end Machine-specific Modified code improvement (optional) target language

Program Analysis

- A compiler's *Front End* is concerned with the *Analysis* of the source program.
 - Determining the *Meaning* of the source program.
- Generally thought of as breaking apart into three *phases*:
 - Lexical Analysis: Convert a text source program into tokens.
 - *Syntactic Analysis*: Convert a token stream into a *parse tree*.
 - *Semantic Analysis*: Enforce semantic rules and convert a parse tree into an *intermediate form*.
 - Two activities, but often happen in an interleaved fashion.



Syntactic Analysis

- Take a stream of *tokens* and convert it into a *parse tree*.
- Capture the *hierarchical* structure of the program.
 - o Declarations, definitions, blocks, statements, expressions, ...
- Provide representation for subsequent *semantic* analysis.
- Detect *syntactic* errors.
 - Mostly, improper structure, including misspelled keywords, bad statement and expression construction.
 - But *not*, e.g., undeclared identifiers, mismatched function calls.
 - (Why not?)



Syntactic Analysis

- So how to do this analysis?
- In the *Lexical Analysis* phase, we used a formal specification of the token formats.
 - Regular expressions (with action routines).
- Can we use Regular Expressions as the notation for the formal specification of program structure?
- No!



Why Not Regular Expressions?

- We have shown that Regular Expressions can be directly converted to an NFA, which can then be converted to a DFA.
- And that DFA can then be used to accept or reject an input string as belonging or not belonging to the RE's language.
- The important letter here is *F*, for *finite*.
- That means that the DFA cannot be used to recognize, e.g., *nesting* that is "too deep".
 - There just won't be enough states in the DFA.



Context-Free Grammar (CFG)

- Regular Expressions are limited in expressiveness.
 - Cannot define strings that are required to have ...
 - Well-formed and/or nested parentheses, brackets, etc. e.g., ([[{(){}[][]}]{[]}])
 - Matching pairs e.g., $a^nb^n \rightarrow ab$, aabb, aaabbb, ...
- Next step up in expressiveness is a *Context-Free Grammar*.
 - Definitions can refer to themselves, i.e., can *recurse*.



Context-Free Grammar

1. A set of *Terminal Symbols*.

The *tokens* generated by the lexical analyzer.

2. A set of *Non-terminal Symbols*.

Representing syntactic categories. Distinguished from the *Terminal Symbols*.



Relating the syntactic categories to their structure. The LHS of each must be a single *Non-Terminal Symbol*. The RHS of each can be arbitrarily complex.

4. A Start Symbol.

One of the Non-terminal Symbols.



Noam Chomsky





CFG Example

$$expr \rightarrow id \mid number \mid -expr \mid (expr) \mid expr \ op \ expr \ id \rightarrow (_ \mid a \mid b \mid ... \mid z)(_ \mid a \mid b \mid ... \mid z \mid 0 \mid 1 \mid ... \mid 9)^* \ op \rightarrow + \mid - \mid * \mid /$$

- Notice that *expr* refers to itself. This definition is *recursive*.
 - It's *not* left or right recursive exclusively.
- Q: What set of strings does *id* define?



- To derive (or generate) a string from a CFG, begin with the start symbol and replace non-terminals according to the rules until only terminals remain.
 - A *sentential form* is the start symbol or any form derived from it.
 - A sentence is a sentential form which has only terminal symbols.
- Example, generate
 slope * x + intercept
 using the expr CFG.

```
expr op expr
expr op id
expr + id
expr op expr + id
expr op id + id
expr * id + id
id * id + id
slope * x + intercept
```

expr



CFG Example

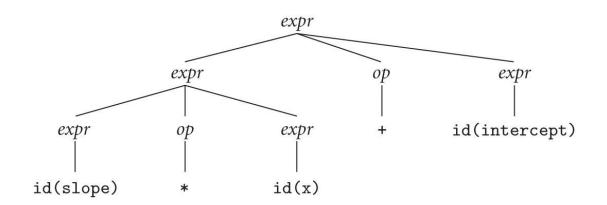
- That derivation was Right-Most.
 - We replaced the *right-most* non-terminal each time we took a step in the derivation.
 - *Except* for the final replacement of the *id* non-terminals with their actual words. (This was to make the derivation a little shorter and easier to fit on the slide.)
- A *Left-Most* derivation replaces the *left-most* non-terminal each time a step is taken in the derivation. (Duh.)



- The steps we took in the derivation correspond to the construction of a *parse tree*.
- The *root* of the parse tree is the *start symbol*.
- Every time we use a production rule, it's the same as adding a new (set of) node(s) to the tree.
- All internal nodes of the parse tree are *non-terminals*.
- The leaves of the final parse tree are terminals.
 - These terminals are the *tokens* of the original string.



CFG Example Parse Tree (from the Right)





There's another way to do the generation of

slope * x + intercept using the expr CFG.

• This derivation goes from the *left* instead of the *right*.

expr op expr
id op expr
id * expr
id * expr op expr
id * id op expr
id * id + expr

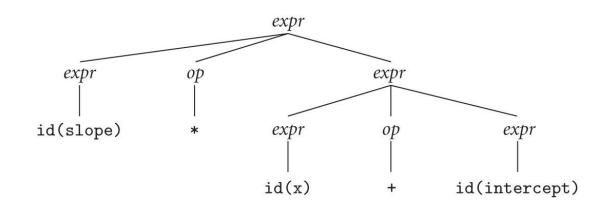
<u>expr</u>

 $\underline{id} * \underline{id} + \underline{id}$

-- -- -slope * x + intercept



CFG Example Parse Tree (from the Left)





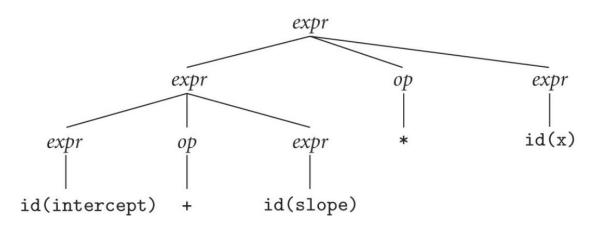
- The CFG allows two parse trees for the same string because its definition is *ambiguous*.
 - Also, it allows incorrect parsing of operator precedence.
- So is the answer to always derive from the right?
 - $\circ\quad$ After all, that got the correct derivation.
- No!
 - Consider the right-most derivation of intercept + slope * x

expr
expr op expr
expr op id
expr * id
expr op expr * id
expr op expr * id
expr op id * id
expr + id * id
id + id * id

intercept + slope * x



CFG Example 2 Parse Tree (from the Right)





Improved CFG Example

- We need a CFG that is not ambiguous *and* honors our concept of operator precedence.
- A better (though more complex) CFG would be
 expr → term | expr add_op term
 term → factor | term mul_op factor
 factor → id | number | factor | (expr)

 $add_op \longrightarrow + \mid -$

 $mul_op \rightarrow * | /$

```
expr add_op <u>term</u>
```

expr add op id

expr

expr add_op <u>factor</u>

expr + id

 $\underline{term} + id$

term mul_op <u>factor</u> + id

 $term \underline{mul op} id + id$

term * id + id

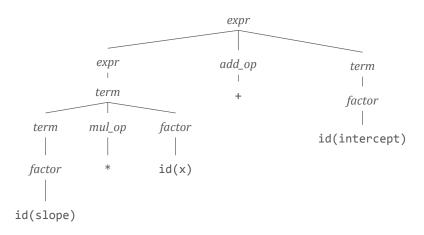
 $\underline{factor} * id + id$

 $\underline{id} * \underline{id} + \underline{id}$

slope * x + intercept



Improved CFG Parse Tree (from the Right)





Improved CFG Example

- What about doing the derivation from the left?
- We still get the correct derivation!
 - The grammar is unambiguous and it honors our intuitive understanding of operator precedence.
 - Multiply and divide are "tighter" than addition and subtraction.
- But what about associativity?
 - How are "like" operations grouped?

expr

expr add_op term

term add_op term

 $\underline{term}\ mul_op\ factor\ add_op\ term$

<u>factor</u> mul_op factor add_op term

id <u>mul op</u> factor add_op term

id * factor add_op term

id * id <u>add op</u> term

id * id + <u>term</u>

id * id + <u>factor</u>

 $\underline{id} * \underline{id} + \underline{id}$

expr

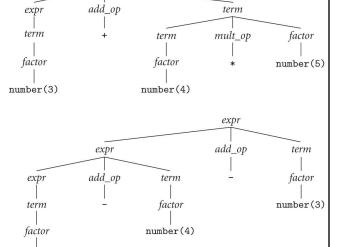
number(10)

slope * x + intercept



Improved CFG Example

- This CFG handles *precedence* and *associativity* according to our intuitive expectations.
 - o 3+4*5 means
 - 3+(4*5)=23
 - not (3+4)*5 = 35.
 - 10-4-3 means
 - (10-4)-3=3
 - not 10-(4-3) = 9.





Improved CFG Example

- OK, so it works. But why does it work?
- Operator *precedence* is enforced by having nested rules that permit the repetition of only certain operators at each precedence level.
 - *expr* is "looser" than *term* as it occurs higher in the CFG definition.
 - Therefore the *add_op* operators are "looser" than the *mul_op* operators.
- Operator associativity is enforced by having the expr and term rules recurse on their left side rather than the right.
 - Therefore operations group from the left instead of the right.

```
expr \rightarrow term \mid expr \ add\_op \ term
term \rightarrow factor \mid term \ mul\_op \ factor
factor \rightarrow id \mid number \mid -factor \mid (expr)
add\_op \rightarrow + \mid -
mul\_op \rightarrow * \mid /
```



Improved CFG Example Comments ...

- We "fixed" the grammar's ambiguity by introducing additional productions to keep the operators separate.
- Suppose we want to add *another* operator at yet *another* level of precedence?
 - ... and *another* and *another* and ...?
- How far might this have to go? How many levels?



Precedence

- Lots and lots of operators.
- Table goes from highest precedence down to lowest.
- Languages try to organize precedence to ease expression writing.

Fortran	Pascal	С	Ada			
		++, (post-inc., dec.)				
**	not	++, (pre-inc., dec.), abs (absol +, - (unary), not, ** &, * (address, contents of), !, - (logical, bit-wise not)				
*, /	*,/, div, mod, and	* (binary), /, % (modulo division)				
+, - (unary and binary)	+, - (unary and binary), or	+, - (binary)	+, - (unary)			
		<<, >> (left and right bit shift)	+, - (binary), & (concatenation)			
.eq., .ne., .lt., .le., .gt., .ge. (comparisons)	<, <=, >, >=, =, <>, IN	<, <=, >, >= =, $/=, <, <=, >,$ (inequality tests)				
.not.		==, != (equality tests)				
		& (bit-wise and)				
		^ (bit-wise exclusive or)				
		(bit-wise inclusive or)				
.and.		&& (logical and)	and, or, xor (logical operators)			
.or.		(logical or)				
.eqv., .neqv. (logical comparisons)		?: (ifthenelse)				
		=, +=, -=, *=, /=, ½=, >>=, <<=, &=, ^=, = (assignment)				
		, (sequencing)				

Precedence

- C's **15** levels of operator precedence are tricky to remember.
 - But once one knows and uses them effectively, one hardly ever needs to use parentheses for grouping.
 - Watch out! The shift operators (<<, >>) are lower precedence than the add and subtract (+, -) operators! 1 << 3 + 1 << 5 is (1 << (3+1)) << 5.
- Ada has only **6** levels, but the **and** and **or** operators are at the same level of precedence.
 - Hard to believe, but A or B and C means (A or B) and C.
- Pascal's **4** levels have **and** at a higher precedence than the comparisons.
 - A < B and C < D means A < (B and C) < D, a static error.



WTF?

- Wow.
- Imagine having to make up 15 levels of production rules just to get C's operator precedence to work correctly.
 - And then start worrying about associativity.
- There has *got* to be a better way to do this!
- Also, how do we get from those *Production Rules* to an actual program?
 - That is, how do we get from a *grammar* to a *parser*?



[C's Precedence Levels in the Grammar]

```
unary_operator
: '&' | '*' | '+' | '-' | '~' | '!' ;
                                                                                                                                                                                                                                                               : and_expression | exclusive_or_expression '^' and_expression ;
       I_CONSTANT | F_CONSTANT | ENUMERATION_CONSTANT
STRING_LITERAL | FUNC_NAME
                                                                                                                                      cast_expression
                                                                                                                                                                                                                                                           inclusive or expression
         '(' expression
                                                                                                                                               unary expression
                                                                                                                                         | '(' type_name ')' cast_expression;
                                                                                                                                                                                                                                                              : exclusive_or_expression | inclusive_or_expression ;
      generic_selection ;
generic_selection
                                                                                                                                      multiplicative expression
                                                                                                                                                                                                                                                           logical_and_expression
: inclusive_or_expression
| logical_and_expression AND_OP inclusive_or_expression ;
                                                                                                                                           Testive_expression '*' cast_expression | multiplicative_expression '/' cast_expression | multiplicative_expression '/' cast_expression | multiplicative_expression '%' cast_expression ;
       GENERIC '(' assignment_expression ',' generic_assoc_list ')';
   : generic_association
| generic_assoc_list ',' generic_association ;
                                                                                                                                                                                                                                                           logical_or_expression
  : logical_and_expression
  | logical_or_expression OR_OP logical_and_expression ;
                                                                                                                                         unitive_expression
| additive_expression '+' multiplicative_expression
| additive_expression '-' multiplicative_expression ;
generic association
                                 assignment_expression
   : type_name ':' assignment_expression
| DEFAULT ':' assignment_expression;
                                                                                                                                                                                                                                                           conditional expression
                                                                                                                                                                                                                                                               : logical_or_expression | logical_or_expression '?' expression ':' conditional_expression ;
postfix expression
       tfix_expression
postfix_expression '[' expression ']'
postfix_expression '(' ')'
postfix_expression '(' ')'
postfix_expression '(' argument_expression_list ')'
postfix_expression 'N_DENTIFIER
postfix_expression PR_OP_IDENTIFIER
postfix_expression_INE_OP_IDENTIFIER
                                                                                                                                          int_expression
| shift_expression
| shift_expression LEFT_OP additive_expression
| shift_expression RIGHT_OP additive_expression ;
                                                                                                                                                                                                                                                           assignment_expression
  : conditional_expression
  | unary_expression assignment_operator assignment_expression;
                                                                                                                                     relational_expression
: shift_expression
: shift_expression
| relational_expression '<' shift_expression
| relational_expression '>' shift_expression
| relational_expression | E.OP shift_expression
| relational_expression | Shift_expression ;
                                                                                                                                                                                                                                                           assignment_operator
: '=' | MUL_ASSIGN | DIV_ASSIGN | MOD_ASSIGN | ADD_ASSIGN | SUB_ASSIGN | LEFT_ASSIGN | RIGHT_ASSIGN | AND_ASSIGN | XOR_ASSIGN | OR_ASSIGN ;
         postfix_expression DEC_OF
      '(' type_name ')' '{' initializer_list '}'
'(' type_name ')' '{' initializer_list ',' '}' ;
                                                                                                                                                                                                                                                               : assignment_expression
| expression ',' assignment_expression ;
argument expression list
                                                                                                                                      equality expression
                                                                                                                                         quality_expression
| equality_expression EQ_OP relational_expression
| equality_expression NE_OP relational_expression;
   : assignment_expression | argument_expression_list ',' assignment_expression;
 unary_expression
: postfix_expression
| INC_OP unary_expression
| DEC_OP unary_expression
                                                                                                                                      and_expression
  : equality_expression
  | and_expression '&' equality_expression ;
      unary_operator cast_expression
SIZEOF unary_expression
SIZEOF '(' type_name ')'
ALIGNOF '(' type_name ')';
```



Excerpted from http://www.quut.com/c/ANSI-C-grammar-y.html

Some Context-Free Grammar Theory

- As CFGs are a *formal notation* (as are the *regular expressions*), what can we do with them *mechanically*?
 - That is, *automatically* and *without human intelligence*.
- This is important as it helps us understand for which operations we can construct *tools* that will process a CFG in a useful way.
 - Like getting a *parser* from a *grammar*.



Some Context-Free Grammar Theory

- Unfortunately, many useful properties of CFGs are *undecidable*.
 - X Does a CFG generate *all* possible strings of its *terminals*?
 - X Do two CFGs generate the *same* language?
 - Does a CFG generate *all* strings another CFG generates?
 - X Does a CFG generate *any* string another CFG generates?
 - X Is the *language* a CFG generates *regular*?
 - X Is a CFG ambiguous?
- [Take a *theory* class to understand the *why* of these.]



Context-Free Grammar Theory

- On the other hand, some incredibly useful properties are decidable.
 - ✓ Is the language a CFG generates *empty*?
 - ✓ Is the language a CFG generates finite?
 - ✓ Is a *CFG* regular? (Either *left* or *right*.)
 - *Not* "Is the CFG's *language* regular?" as that's *undecidable*.
 - ✓ Does a CFG *generate* a given string?
 - That is, can we *parse* a given string using a given CFG?
 - ✓ Is a non-terminal of a CFG reachable, productive, or nullable?
 - ✓ Is a CFG LL(1)?



Predictive Parsing

- So what's that last item, LL(1), mean?
- Essentially, can we *automatically* construct a parser from the CFG that will *efficiently* create an *unambiguous* parse tree from *any* given string?
 - Or tell us the string is *unparseable*.
- LL(1) \equiv *Left-to-right* scan of the input, producing a *Leftmost* derivation, using only 1 token of lookahead.
- This sort of parser never has to *backtrack*.
 - It can parse in time *linear* in the size of the input string.



- Let's go back to our improved CFG for expressions.
- It's unambiguous already.
- [id and number will be token categories returned by the scanner.]

```
expr \rightarrow term \mid expr \ add\_op \ term
term \rightarrow factor \mid term \ mul\_op \ factor
factor \rightarrow id \mid number \mid -factor \mid (expr)
add\_op \rightarrow + \mid -
mul\_op \rightarrow * \mid /
```



- Eliminate explicit alternation to make the production rules more obvious.
- Just make a rule for each case of alternation.

```
expr \rightarrow expr \ add\_op \ term
expr \rightarrow term
term \rightarrow term \ mul\_op \ factor
term \rightarrow factor
factor \rightarrow id
factor \rightarrow number
factor \rightarrow -factor
factor \rightarrow (expr)
add\_op \rightarrow +
add\_op \rightarrow -
mul\_op \rightarrow *
mul\_op \rightarrow /
```



- The *expr* and *term* productions exhibit *left recursion*.
- While the grammar is not ambiguous, it's non-deterministic without arbitrary lookahead.
 - o (1+2+3) vs. (1+2+3)+4
 - o $expr \rightarrow term$ in the first case but $expr \rightarrow expr \ add_op \ term$ in the second.

```
expr \rightarrow expr \ add\_op \ term
expr \rightarrow term

term \rightarrow term \ mul\_op \ factor

term \rightarrow factor

factor \rightarrow id

factor \rightarrow number

factor \rightarrow - factor

factor \rightarrow (expr)

add\_op \rightarrow +

add\_op \rightarrow +

add\_op \rightarrow +

mul\_op \rightarrow /
```



Predictive Parsing Example

- Predictive Parsing requires that we can predict from the next token[†] which production rule to use.
- We will have to eliminate the left recursion.
 - This can be done mechanically.

 $mul_op \rightarrow *$ $mul_op \rightarrow /$

 † Actually, it doesn't have to be the *next* token. It could be the *next* k tokens. However, k has to be a constant, so ambiguous cases can always be constructed.



 $expr \rightarrow expr \ add_op \ term$ $expr \rightarrow term$ $term \rightarrow term \ mul_op \ factor$ $term \rightarrow factor$ $factor \rightarrow id$ $factor \rightarrow number$ $factor \rightarrow - factor$ $factor \rightarrow (\ expr \)$ $add_op \rightarrow +$ $add_op \rightarrow -$

[Eliminating Left Recursion]

- Rule sets of the form
 - \circ *X* → *X*α (where α does not start with *X*)
 - \circ $X \longrightarrow \beta$

generate strings of the form $\beta\alpha^*$.

- This can be replaced by
 - \circ $X \longrightarrow \beta X'$
 - \circ $X' \longrightarrow \alpha X'$
 - \circ $X' \rightarrow \varepsilon$

This method isn't restricted to a single production. For example,

moving the recursion from the left side to the right side.



Predictive Parsing Example

- Eliminate left recursion by rewriting the *expr* and *term* production rules.
- We introduce non-terminals
 expr1 and term1 to handle the
 right recursion.

```
expr \rightarrow term \ expr1

expr1 \rightarrow add\_op \ term \ expr1

expr1 \rightarrow \epsilon
```

 $term \rightarrow factor\ term1$ $term1 \rightarrow mul_op\ factor\ term1$ $term1 \rightarrow \epsilon$

```
factor \rightarrow id

factor \rightarrow number

factor \rightarrow - factor

factor \rightarrow (expr)

add\_op \rightarrow +

add\_op \rightarrow -

mul\_op \rightarrow *

mul\_op \rightarrow /
```



- Let's number the final set of production rules to make them easier to refer to as we continue the processing.
- 1. $expr \rightarrow term \ expr1$
- 2. $expr1 \rightarrow add_op term expr1$
- 3. $expr1 \rightarrow \varepsilon$
- 4. $term \rightarrow factor term 1$
- 5. $term1 \rightarrow mul_op\ factor\ term1$
- 6. $term1 \rightarrow \epsilon$
- 7. $factor \rightarrow id$
- 8. $factor \rightarrow number$
- 9. $factor \rightarrow factor$
- 10. $factor \rightarrow (expr)$
- 11. $add op \rightarrow +$
- 12. $add_op \rightarrow -$
- 12. uuu_op → -
- 13. $mul_op \rightarrow *$
- 14. $mul_{op} \rightarrow /$



- To predict which production rule to use, we have to know three items for each non-terminal *X*.
- NULLABLE(*X*): Does *X* ever derive ε?
- FIRST(*X*): Which terminals can appear *first* in a string derived from *X*?
- FOLLOW(*X*): Which terminals can appear *immediately after X*?

- 1. $expr \rightarrow term \ expr1$
- 2. $expr1 \rightarrow add_op term expr1$
- 3. $expr1 \rightarrow \varepsilon$
- 4. $term \rightarrow factor term 1$
- 5. $term1 \rightarrow mul_op factor term1$
- 6. $term1 \rightarrow \varepsilon$
- 7. $factor \rightarrow id$
- 8. $factor \rightarrow number$
- 9. $factor \rightarrow factor$
- 10. $factor \rightarrow (expr)$
- 11. $add_op \rightarrow +$
- 12. $add_op \rightarrow -$
- 13. $mul_op \rightarrow *$
- 14. $mul_op \rightarrow /$



[NULLABLE]

- Computing NULLABLE(X) is a tedious straightforward though iterative process.
- For our grammar, the only NULLABLE items are expr1 and term1.
 - They derive ε directly.
 - No other non-terminal derives either of these non-terminals without also including something else.

```
for each terminal and non-terminal X  \begin{array}{l} \text{NULLABLE}[\textbf{X}] \leftarrow \text{False} \\ \\ \text{repeat} \\ \text{for each rule X} \rightarrow \text{Y1 Y2 ... Yk} \\ \text{if k = 0} \\ \text{NULLABLE}[\textbf{X}] \leftarrow \text{True} \\ \\ \text{else if Y1 Y2 ... Yk are all NULLABLE} \\ \text{NULLABLE}[\textbf{X}] \leftarrow \text{True} \\ \\ \text{until NULLABLE didn't change.} \\ \end{array}
```



[FIRST]

- As with NULLABLE, computing FIRST(X) is an incredibly tedious straightforward though iterative process.
- After iterating, for a while, we find these FIRST sets.

```
FIRST(add_op) = { '+', '-' }

FIRST(mul_op) = { '*', '/' }

FIRST(factor) = { id, number, '-', '(' }

FIRST(term1) = { '*', '/' }

FIRST(expr1) = { id, number, '-', '(' }

FIRST(expr1) = { '+', '-' }

FIRST(expr) = { id, number, '-', '(' }
```

```
for each terminal X
   FIRST[X] ← { X }

for each non-terminal X
   FIRST[X] ← {}

repeat
   for each rule X → Y1 Y2 ... Yk
    for i ← 1 .. k
        if i = 1
            FIRST[X] ← FIRST[X] ∪ FIRST[Yi]

        elif Y1 Y2 ... Yi-1 are all NULLABLE
        FIRST[X] ← FIRST[X] ∪ FIRST[Yi]

until FIRST didn't change.
```



[*FOLLOW*]

- Yes, computing FOLLOW(X) is an incredibly, mind-bogglingly tedious straightforward though iterative process.
- After iterating for a while, we find these FOLLOW sets.

```
FOLLOW( add_op ) = { id, number, '-', '(' }
FOLLOW( mul_op ) = { id, number, '-', '(' }
FOLLOW( factor ) = { '*', '/', '+', '-', ')', EOF }
FOLLOW( term1 ) = { '+', '-', ')', EOF }
FOLLOW( term ) = { '+', '-', ')', EOF }
FOLLOW( expr1 ) = { ')', EOF }
FOLLOW( expr ) = { ')', EOF }
```

```
for each terminal and non-terminal X FOLLOW[X] \leftarrow {} repeat for each rule X \rightarrow Y1 Y2 ... Yk for i \leftarrow 1 .. k if i = k FOLLOW[Yi] \leftarrow FOLLOW[Yi] \cup FOLLOW[X] elif Yi+1 ... Yk are all NULLABLE FOLLOW[Yi] \leftarrow FOLLOW[Yi] \cup FOLLOW[X] for j \leftarrow i+1 .. k if i+1 = j FOLLOW[Yi] \leftarrow FOLLOW[Yi] \cup FIRST[Yj] elif Yi+1 ... Yj-1 are all NULLABLE FOLLOW[Yi] \leftarrow FOLLOW[Yi] \cup FIRST[Yj] until FOLLOW didn't change.
```



- Given the NULLABLE and FIRST and FOLLOW sets, we can now construct a parse table for our CFG.
- This table tells us which rule to use when we are trying to parse a given non-terminal and are seeing a given terminal.
- We have one row for each *non-terminal* and one column for each *terminal*.

```
for each terminal X for each non-terminal Y TABLE[X,Y] \leftarrow {} for each rule X \rightarrow \delta for each T \in FIRST[\delta] TABLE[X,T] \leftarrow TABLE[X,T] \cup {X\rightarrow\delta} if NULLABLE[\delta] for each T \in FOLLOW[X] TABLE[X,T] \leftarrow TABLE[X,T] \cup {X\rightarrow\delta}
```



• For our CFG, we get this parse table.

	+	-	*	/	id	number	()	EOF
add_op	11	12							
mul_op			13	14					
factor		9			7	8	10		
term1	6	6	5	5				6	6
term		4			4	4	4		
expr1	2	2						3	3
expr		1			1	1	1		



- For example, if we are trying to parse an *expr* and we are seeing the (token, we use production rule 1.
- Any box that does not have a rule number indicates an error condition for that non-terminal / terminal combination.
 - E.g., trying to parse a *mul_op* and seeing the token is an error.
- Since no box has more than one rule, we are confirmed in our thinking that the grammar is *unambiguous*.



- Great, we have the parse table.How do we get a parser?
- It's not difficult. We just write a routine for each non-terminal.
- The parse table tells us what to do in each case.
 - At right are two of the seven required routines.

```
def EXPR() :
 token = peekToken()
 if token in FIRST EXPR :
   value = TERM() + EXPR1()
   print( 'Error! EXPR saw %s when expecting %s.'
     % ( token, FIRST_EXPR ) )
   raise ValueError
 return value
def EXPR1() :
 token = peekToken()
 if token in [ PLUS, MINUS ] :
   value = ADD_OP() + TERM() + EXPR1()
 elif token in [ RPAREN, EOF ] :
   print( 'Error! EXPR1 saw %s when expecting %s.'
    % ( token, FIRST_EXPR1 ) )
   raise ValueError
 return value
```



- For each non-terminal, we peek at the next token and then take the action recorded in the parse table.
- E.g., if EXPR() sees -, id, number, or (, it knows it's supposed to use rule 1, expr → term expr1.
- It therefore calls TERM() and then
 EXPR1().
- Anything else is an error.

```
def EXPR() :
 token = peekToken()
 if token in FIRST EXPR :
   value = TERM() + EXPR1()
   print( 'Error! EXPR saw %s when expecting %s.'
     % ( token, FIRST_EXPR ) )
   raise ValueError
 return value
def EXPR1() :
 token = peekToken()
 if token in [ PLUS, MINUS ] :
   value = ADD_OP() + TERM() + EXPR1()
 elif token in [ RPAREN, EOF ] :
    value = '\epsilon'
   print( 'Error! EXPR1 saw %s when expecting %s.'
     % ( token, FIRST_EXPR1 ) )
   raise ValueError
 return value
```

- Eventually we get to routines that have to *consume* tokens after peeking at them.
- advanceToken() moves to the next token.
- eat() ensures that the token matches its argument, then moves across it.

```
def FACTOR( indent ) :
  token = peekToken()
  if token in [ ID, NUMBER ] :
    advanceToken()
    value = token
  elif token == MINUS :
    advanceToken()
    value = MINUS + FACTOR()
  elif token == LPAREN :
    advanceToken()
    value = LPAREN + EXPR() + RPAREN
    eat( RPAREN )
    print( 'Error! FACTOR saw %s when expecting %s.'
     % ( token, FIRST_FACTOR ) )
    raise ValueError
  return value
```



- This is known as a recursive descent parser.
- Writing this kind of parser by hand is very common ...
 - When the grammar is simple!
- ... which is the main reason we spend the time exploring the method.

```
def FACTOR( indent ) :
 token = peekToken()
  if token in [ ID, NUMBER ] :
   advanceToken()
   value = token
  elif token == MINUS :
   advanceToken()
    value = MINUS + FACTOR()
  elif token == LPAREN :
   advanceToken()
   value = LPAREN + EXPR() + RPAREN
   eat( RPAREN )
   print( 'Error! FACTOR saw %s when expecting %s.'
     % ( token, FIRST_FACTOR ) )
   raise ValueError
  return value
```



[Table-Driven Predictive Parsing]

- By the way, we do not have to hand-code the parser.
- A general method exists that parses *directly* from the table.
- Simpler than using hand-coded routines, but can be inefficient.
- (If we're going to use a generator, why not a more powerful one?)

```
push( startSymbol )
token ← readNextToken()
repeat
 X \leftarrow pop()
  if terminal(X) or X = EOF
    if X = token
      token ← readNextToken()
      // Needed a token and current one didn't match.
  elif TABLE[X, token] is empty
    // No rule for this non-terminal / token pair.
    error()
   // Have a rule to use. Push its RHS onto
    // the stack in reverse order.
    for Y in reverse(RHS(TABLE[X, token]))
      push(Y)
until X = EOF
```



Predictive Parsing Example

• And, the parser really, really works!

```
Trying ['number', '/', 'number', '-', 'number', 'EOF'] ...
Trying ['number', '-', 'number', 'EOF'] ...
FACTOR:
             number
TERM1 :
                                                                                                    number
TERM :
           numberε
                                                                                       MUL OP:
ADD OP:
                                                                                       FACTOR:
                                                                                                      number
                                       Trying ['number', '+', 'number',
                                                                                       TERM1 :
FACTOR:
               number
                                                 *', 'number', 'EOF'] ...
TERM1 :
                                                                                       TERM1 :
                                                                                                    /numberε
               3
                                                    number
TERM :
             numberε
                                                                                       TERM :
                                                                                                  number/number&
                                       TERM1 :
EXPR1:
                                                                                       ADD_OP:
                                       TERM :
                                                  numberε
EXPR1:
                                                                                       FACTOR:
                                                                                                      number
          -numberεε
                                       ADD OP:
EXPR : numberε-numberεε
                                                                                       TERM1:
                                                                                                      3
                                       FACTOR:
                                                       number
                                                                                                    numberε
                                       MUL OP:
                                                                                       EXPR1:
Success!
                                                                                                    3
                                       FACTOR:
                                                         number
  numberε-numberεε
                                                                                       EXPR1:
                                                                                                  -numberεε
                                       TERM1 :
                                                                                       EXPR : number/numberε-numberεε
                                       TERM1 :
                                                       *number&
                                       TERM :
                                                    number*numberε
                                                                                       Success!
                                       EXPR1:
                                                                                         number/numberε-numberεε
                                       EXPR1:
                                                  +number*numberεε
                                       EXPR : number \( \psi + \text{number} \( \psi \) number \( \psi \)
                                         number&+number*number&&
```



Even with errors and complex cases!

```
#-----
Trying [')', 'EOF'] ...
Error! EXPR saw ) when expecting ['-', 'id', 'number', '('].
Parse error!

#-----
Trying ['-', '*', 'EOF'] ...
Error! FACTOR saw * when expecting ['-', 'id', 'number', '('].
Parse error!

#-----
Trying ['number', '-', '+', 'EOF'] ...
FACTOR: number
TERM1 : &
TERM : number
ADD_OP: -
Error! TERM saw + when expecting ['-', 'id', 'number', '('].
Parse error!
```

```
Trying ['(', 'number', '+', 'number', ')', '*', 'number', 'EOF'] ...
FACTOR:
                   number
TERM :
                 numbers
ADD_OP:
FACTOR:
                    number
TERM1 :
                     3
TERM :
                   numberε
EXPR1:
                   3
EXPR1:
                +numberεε
EXPR :
               number&+number&&
FACTOR:
             (numberε+numberεε)
MUL_OP:
FACTOR:
               number
TERM1 :
TERM1 :
             *numberε
TERM :
          (numberε+numberεε)*numberε
EXPR1:
EXPR : (numberε+numberεε)*numberεε
  (numberε+numberεε)*numberεε
```



- So what are those ε characters?
- That's where expr1 or term1 derived the empty string (ε).
 - Rules 3 and 6.
- Remember, we got rid of *left* recursion by converting it to *right* recursion.

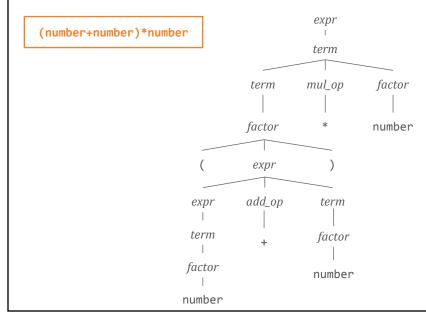
- 1. $expr \rightarrow term \ expr1$
- 2. $expr1 \rightarrow add_op term expr1$
- 3. $expr1 \rightarrow \varepsilon$
- 4. $term \rightarrow factor term 1$
- 5. $term1 \rightarrow mul_op\ factor\ term1$
- 6. $term1 \rightarrow \varepsilon$
- 7. $factor \rightarrow id$
- 8. $factor \rightarrow number$
- 9. $factor \rightarrow factor$
- 10. $factor \rightarrow (expr)$
- 11. $add_op \rightarrow +$
- 12. $add_op \rightarrow -$
- 13. $mul_op \rightarrow *$
- 14. $mul_op \rightarrow /$



- Well, that was painful.
- Also, the eventual parsing we got from the LL(1) method is not exactly what we might have expected.
 - We had to change our grammar to eliminate left recursion.
- Did you notice the weird way the productions came out?



Expected Parse Tree for (number+number)*number





Actual Parse Tree expr (number+number)*number term expr1 factor term1 3 expr mul_op factor term1 number 3 term expr1 factor add_op term expr1 number factor number

- Pretty awful, huh?
- Well, no matter, we can always fix it up in the action routines.
- But ... do we want to?
- *Again*, there has *got* to be a better way!



- There is a better way.
- It's called LR(k) parsing.
- LR(k) = Left-to-right scan of the input, producing a Rightmost derivation, using k tokens of lookahead.



LL(1) vs LR(k) Parsing

- The LL(1) Predictive Parsing that we did was *top-down*.
 - We used the production rules from *left* to *right*.
- LR(k) parsing is bottom-up.
 - We use the production rules from *right* to *left*.
- As with the table-driven predictive parsing, we use a stack with LR(k) parsing.
 - But we use the stack in a more sophisticated way.



- We use a *stack* and the *input stream* to decide what to do.
- The first *k* tokens in the input stream form the *lookahead*.
- Depending on the stack and the lookahead, the parser takes one of two possible actions:
 - > *Shift* : Push the first input token onto the stack.
 - > *Reduce* : Select some grammar rule, e.g., $X \rightarrow ABC$; pop *C*, *B*, *A* off the stack; and push *X* onto the stack.



LR(k) Parsing

- Initially the *stack* is empty and the *lookahead* is the first *k* tokens from the *input stream*.
- If the parser makes it to the point where it can *shift* the *EOF* marker onto the stack, it has *accepted* the input as valid.



- The decision to *reduce* is made based on the top few items on the stack, which need to match the RHS of a production rule. Three cases can occur.
- ① The top few items do not match the RHS of *any* rule of the grammar.
 - This is *easy* to resolve.
 - Just *shift* another token from the input stream onto the stack and look again.



LR(k) Parsing

- ② The top few items match the RHS of *one* rule of the grammar.
 - This is *easy* to resolve as well.
 - Just *reduce* by popping off the stack items corresponding to the RHS of the rule.
 - The popped items are known as a *handle*.
 - Then push the LHS of the rule (a non-terminal) onto the stack.



- ③ The top few items match the RHS of *multiple* rules of the grammar.
 - This is *not* so easy to resolve.
 - The grammar is *ambiguous* so we don't know which reduction to make.
 - This is known as a *reduce/reduce* ambiguity.



LR(k) Parsing

- So how do we find such issues in the grammar?
 - And are there other kinds of problems?
- We have to produce the ACTION and GOTO tables and see what problems show up along the way.
- Producing these tables is similar to what we did with *Predictive Parsing*.
- Aside from *reduce/reduce* conflicts, there are *shift/reduce* conflicts, which occur when it's not clear whether to shift a token onto the stack or to reduce what's already there.



- We analyze the grammar by building *item sets* based on the rules and how far we've gotten into a parse.
- For example, the *item*
 - E -> E . + T

indicates we using the rule $E \rightarrow E + T$, we have seen an E, and that we are expecting a '+' token next.

• An *item set* is a collection of *items* that are all in the same state.



Analyzing an Example Grammar

- We'll start with a simplified version of the classic expression grammar.
 - Only one add op, +.
 - Only one mul op, *.
- It's unambiguous, so it shouldn't have any analysis problems.

 $S \rightarrow E$

 $E \rightarrow E + T$

 $\mathsf{E} \, \to \, \mathsf{T}$

 $T \rightarrow T * F$

 $T \rightarrow F$

 $\mathsf{F}\,\to\,\mathsf{id}$

 $F \rightarrow (E)$



Analyzing an Example Grammar

Rule 0 S' -> S
Rule 1 S -> E
Rule 2 E -> E + T
Rule 3 E -> T
Rule 4 T -> T * F
Rule 5 T -> F
Rule 6 F -> id
Rule 7 F -> (E)

Grammar

Terminals, with rules where they appear

(: 7 * : 4 + : 2) : 7 error : id : 6

Nonterminals, with rules where they appear

E : 1 2 7 F : 4 5 S : 0 T : 2 3 4



Analyzing an Example Grammar

```
state 0
     (0) S' \rightarrow . S
     (1) S \rightarrow . E
     (2) E \rightarrow . E + T
     (3) E \rightarrow . T
     (4) T \rightarrow T * F
     (5) T \rightarrow . F
     (6) F \rightarrow . id
     (7) F \rightarrow . (E)
                         shift and go to state 5
                         shift and go to state 6
     (
     S
                                            shift and go to state 1
     Ε
                                            shift and go to state 2
     Т
                                            shift and go to state 3
     F
                                            shift and go to state 4
```



Analyzing an Example Grammar



Analyzing an Example Grammar

```
state 3
    (3) E \rightarrow T.
    (4) T -> T . * F
             reduce using rule 3 (E -> T .)
    $end
             reduce using rule 3 (E -> T .)
             reduce using rule 3 (E -> T .)
    )
             shift and go to state 8
state 4
    (5) T \rightarrow F.
             reduce using rule 5 (T -> F .)
             reduce using rule 5 (T -> F .)
    $end
             reduce using rule 5 (T -> F .)
             reduce using rule 5 (T -> F .)
```



```
state 5

(6) F -> id .

*         reduce using rule 6 (F -> id .)
+         reduce using rule 6 (F -> id .)
$end         reduce using rule 6 (F -> id .)
)         reduce using rule 6 (F -> id .)
```



```
state 6
     (7) F -> ( . E )
     (2) E \rightarrow E + T
     (3) E \rightarrow . T
     (4) T \rightarrow . T * F
     (5) T \rightarrow . F
     (6) F \rightarrow .id
     (7) F \rightarrow . (E)
     id
                  shift and go to state 5
                  shift and go to state 6
     (
                                           shift and go to state 9
     Т
                                           shift and go to state 3
                                           shift and go to state 4
```







```
state 10
    (2) E \rightarrow E + T.
    (4) T \rightarrow T . * F
                     reduce using rule 2 (E -> E + T .)
    $end
                     reduce using rule 2 (E -> E + T .)
                     reduce using rule 2 (E -> E + T .)
    )
                     shift and go to state 8
state 11
    (4) T \rightarrow T * F.
                     reduce using rule 4 (T -> T * F .)
    +
                     reduce using rule 4 (T -> T * F .)
                     reduce using rule 4 (T -> T * F \cdot)
    $end
                     reduce using rule 4 (T -> T * F .)
```





Action Table

n Table Goto Table

```
0: {'id': 5, '(': 6},
                                                   0: {'S': 1, 'E': 2, 'T': 3, 'F': 4},
 1: {'$': 0},
                                                  6: {'E': 9, 'T': 3, 'F': 4},
 2: {'$': -1, '+': 7},
                                                  7: {'T': 10, 'F': 4},
 3: {'$': -3, '+': -3, ')': -3, '*': 8},
                                                  8: {'F': 11}
 4: {'$': -5, '+': -5, ')': -5, '*': -5},
 5: {'$': -6, '+': -6, ')': -6, '*': -6},
 6: {'id': 5, '(': 6},
7: {'id': 5, '(': 6},
8: {'id': 5, '(': 6},
9: {'+': 7, ')': 12},
10: {'$': -2, '+': -2, ')': -2, '*': 8},
11: {'$': -4, '+': -4, ')': -4, '*': -4},
12: {'$': -7, '+': -7, ')': -7, '*': -7},
```



- This example grammar is straightforward.
 - There are no ambiguities.
 - No shift/reduce conflicts.
 - No reduce/reduce conflicts.
- How boring.
- Let's try another grammar, this time with a problem.



- Our grammar is simple, merely demonstrating how one might represent an if statement.
- We have two kinds of if statement, one with an else clause and one without.
- The ambiguity is obvious.
 Let's see what the analysis reports.

Grammar

```
S \rightarrow if E then S else S S \rightarrow if E then S S \rightarrow E E \rightarrow ID
```



Grammar with a Shift/Reduce Conflict

Rule 0 S'-> S ELSE : 1

Rule 1 S -> IF E THEN S ELSE S ID : 4 Rule 2 S -> IF E THEN S IF : 1 2 Rule 3 S -> E THEN : 1 2 Rule 4 E -> ID error :

Nonterminals, with rules where they appear

Terminals, with rules where they appear

E : 1 2 3 S : 1 1 2 0



state 0



Grammar with a Shift/Reduce Conflict





Grammar with a Shift/Reduce Conflict

```
(1) S \rightarrow IF E . THEN S ELSE S
    (2) S \rightarrow IF E . THEN S
    THEN
                       shift and go to state 6
state 6
    (1) S -> IF E THEN . S ELSE S
    (2) S \rightarrow IF E THEN . S
    (1) S \rightarrow IF E THEN S ELSE S
    (2) S \rightarrow . IF E THEN S
    (3) S \rightarrow . E
    (4) E \rightarrow . ID
    ΙF
                        shift and go to state 2
    ID
                       shift and go to state 4
    Ε
                                          shift and go to state 3
    S
                                          shift and go to state 7
```





Grammar with a Shift/Reduce Conflict

```
state 8

(1) S -> IF E THEN S ELSE . S
(1) S -> . IF E THEN S ELSE S
(2) S -> . IF E THEN S
(3) S -> . E
(4) E -> . ID

IF shift and go to state 2
ID shift and go to state 4

E shift and go to state 3
S shift and go to state 9
```





Grammar with a Shift/Reduce Conflict

Action Table

Goto Table

```
0: { 'IF': 2, 'ID': 4 }
1: { '$end': 0 }
2: { 'E': 5 }
2: { 'ID': 4 }
3: { '$end': -3, 'ELSE': -3 }
4: { '$end': -4, 'ELSE': -4, 'THEN': -4 }
5: { 'THEN': 6 }
6: { 'IF': 2, 'ID': 4 }
7: { '$end': -2, 'ELSE': 8 }
8: { 'IF': 2, 'ID': 4 }
9: { '$end': -1, 'ELSE': -1 }
```



- OK, so there was a shift/reduce conflict.
- What do we do about?
- First, we have to decide what the correct, expected parse is supposed to be.
 - Normally, this would be to have the else clause bind with the closest available if that doesn't already have an else clause.
- Guess what? That's exactly what happens if we just resolve the shift/reduce conflict by *always* shifting!
 - That's the *default* behavior of the parser generator anyway.



Grammar with a Shift/Reduce Conflict

- So that wasn't very exciting after all.
- We could have rewritten the grammar so that this shift/reduce conflict doesn't occur, but why?
 - Or, we could have introduced a terminating marker for the if statement (as, e.g., Ada has, end if).
- OK, let's try another grammar, this one with *lots* of shift/reduce conflicts.



 Another expression grammar, this time with multiple binary operators and no indication of precedence or associativity.

 $E \rightarrow INTEGER$ $E \rightarrow E + E$ $E \rightarrow E - E$ $E \rightarrow E * E$ $E \rightarrow E / E$ $E \rightarrow (E)$

The ambiguity is obvious.
 Let's see what the analysis reports.

Grammar



Another Grammar with Shift/Reduce Conflicts

Rule 0 S' -> E DIVIDE : 1 Rule 1 E -> INTEGER INTEGER Rule 2 E -> E PLUS E LPAREN Rule 3 E -> E MINUS E MINUS : 3 Rule 4 : 4 E -> E MULTIPLY E MULTIPLY Rule 5 E -> E DIVIDE E PLUS : 2 Rule 6 E -> LPAREN E RPAREN RPAREN error

Nonterminals, with rules where they appear

Terminals, with rules where they appear

E : 2 2 3 3 4 4 5 5 6 0



state 0

state 1





```
state 2

(1) E -> INTEGER .

PLUS         reduce using rule 1 (E -> INTEGER .)
MINUS         reduce using rule 1 (E -> INTEGER .)
MULTIPLY         reduce using rule 1 (E -> INTEGER .)
DIVIDE         reduce using rule 1 (E -> INTEGER .)
$end               reduce using rule 1 (E -> INTEGER .)
RPAREN         reduce using rule 1 (E -> INTEGER .)
```



```
(6) E -> LPAREN . E RPAREN
(1) E -> . INTEGER
(2) E -> . E PLUS E
(3) E -> . E MINUS E
(4) E -> . E MULTIPLY E
(5) E -> . E DIVIDE E
(6) E -> . LPAREN E RPAREN

INTEGER shift and go to state 2
LPAREN shift and go to state 3

E shift and go to state 8
```



```
(2) E -> E PLUS . E
(1) E -> . INTEGER
(2) E -> . E PLUS E
(3) E -> . E MINUS E
(4) E -> . E MULTIPLY E
(5) E -> . E DIVIDE E
(6) E -> . LPAREN E RPAREN

INTEGER shift and go to state 2
LPAREN shift and go to state 3

E shift and go to state 9
```

state 4

state 5



```
(3) E -> E MINUS . E
(1) E -> . INTEGER
(2) E -> . E PLUS E
(3) E -> . E MINUS E
(4) E -> . E MULTIPLY E
(5) E -> . E DIVIDE E
(6) E -> . LPAREN E RPAREN

INTEGER shift and go to state 2
LPAREN shift and go to state 3

E shift and go to state 10
```



```
state 6

(4) E -> E MULTIPLY . E
(1) E -> . INTEGER
(2) E -> . E PLUS E
(3) E -> . E MINUS E
(4) E -> . E MULTIPLY E
(5) E -> . E DIVIDE E
(6) E -> . LPAREN E RPAREN

INTEGER shift and go to state 2
LPAREN shift and go to state 3

E shift and go to state 11
```



Another Grammar with Shift/Reduce Conflicts

```
(5) E -> E DIVIDE . E
(1) E -> . INTEGER
(2) E -> . E PLUS E
(3) E -> . E MINUS E
(4) E -> . E MULTIPLY E
(5) E -> . E DIVIDE E
(6) E -> . LPAREN E RPAREN

INTEGER shift and go to state 2
LPAREN shift and go to state 3

E shift and go to state 12
```



state 8



```
state 9
    (2) E \rightarrow E PLUS E.
    (2) E -> E . PLUS E
    (3) E \rightarrow E . MINUS E
    (4) E -> E . MULTIPLY E
    (5) E -> E . DIVIDE E
  ! shift/reduce conflict for PLUS resolved as shift
 ! shift/reduce conflict for MINUS resolved as shift
  ! shift/reduce conflict for MULTIPLY resolved as shift
  ! shift/reduce conflict for DIVIDE resolved as shift
   $end
                    reduce using rule 2 (E -> E PLUS E .)
   RPAREN
                    reduce using rule 2 (E -> E PLUS E .)
   PLUS
                    shift and go to state 4
   MTNUS
                    shift and go to state 5
   MULTIPLY
                    shift and go to state 6
   DIVIDE
                    shift and go to state 7
  ! PLUS
                    [ reduce using rule 2 (E -> E PLUS E .) ]
  ! MINUS
                    [ reduce using rule 2 (E -> E PLUS E .) ]
  ! MULTIPLY
                    [ reduce using rule 2 (E -> E PLUS E .) ]
  ! DIVIDE
                    [ reduce using rule 2 (E -> E PLUS E .) ]
```



```
state 10
    (3) E \rightarrow E MINUS E.
    (2) E -> E . PLUS E
    (3) E \rightarrow E . MINUS E
    (4) E -> E . MULTIPLY E
    (5) E -> E . DIVIDE E
 ! shift/reduce conflict for PLUS resolved as shift
  ! shift/reduce conflict for MINUS resolved as shift
  ! shift/reduce conflict for MULTIPLY resolved as shift
  ! shift/reduce conflict for DIVIDE resolved as shift
                    reduce using rule 3 (E -> E MINUS E .)
   RPAREN
                    reduce using rule 3 (E -> E MINUS E .)
   PLUS
                    shift and go to state 4
   MINUS
                    shift and go to state 5
   MULTIPLY
                    shift and go to state 6
   DIVIDE
                    shift and go to state 7
  ! PLUS
                    [ reduce using rule 3 (E -> E MINUS E .) ]
                    [ reduce using rule 3 (E -> E MINUS E .) ]
  ! MINUS
                    [ reduce using rule 3 (E -> E MINUS E .) ]
  ! MULTIPLY
  ! DIVIDE
                    [ reduce using rule 3 (E -> E MINUS E .) ]
```



```
state 11
    (4) E -> E MULTIPLY E .
    (2) E -> E . PLUS E
    (3) E \rightarrow E . MINUS E
    (4) E -> E . MULTIPLY E
    (5) E -> E . DIVIDE E
  ! shift/reduce conflict for PLUS resolved as shift
  ! shift/reduce conflict for MINUS resolved as shift
  ! shift/reduce conflict for MULTIPLY resolved as shift
  ! shift/reduce conflict for DIVIDE resolved as shift
   $end
                    reduce using rule 4 (E -> E MULTIPLY E .)
                    reduce using rule 4 (E -> E MULTIPLY E .)
   RPAREN
   PLUS
                    shift and go to state 4
   MTNUS
                    shift and go to state 5
   MULTIPLY
                    shift and go to state 6
   DIVIDE
                    shift and go to state 7
                    [ reduce using rule 4 (E -> E MULTIPLY E .) ]
  ! PLUS
                    [ reduce using rule 4 (E -> E MULTIPLY E .) ]
  ! MINUS
  ! MULTIPLY
                    [ reduce using rule 4 (E -> E MULTIPLY E .) ]
  ! DIVIDE
                    [ reduce using rule 4 (E -> E MULTIPLY E .) ]
```



```
(5) E -> E DIVIDE E .
  (2) E \rightarrow E . PLUS E
  (3) E \rightarrow E . MINUS E
  (4) E -> E . MULTIPLY E
  (5) E -> E . DIVIDE E
! shift/reduce conflict for PLUS resolved as shift
! shift/reduce conflict for MINUS resolved as shift
! shift/reduce conflict for MULTIPLY resolved as shift
! shift/reduce conflict for DIVIDE resolved as shift
                  reduce using rule 5 (E -> E DIVIDE E .)
 RPAREN
                  reduce using rule 5 (E -> E DIVIDE E .)
 PLUS
                  shift and go to state 4
 MINUS
                  shift and go to state 5
 MULTIPLY
                  shift and go to state 6
 DIVIDE
                  shift and go to state 7
! PLUS
                  [ reduce using rule 5 (E -> E DIVIDE E .) ]
! MINUS
                  [ reduce using rule 5 (E -> E DIVIDE E .) ]
                  [ reduce using rule 5 (E -> E DIVIDE E .) ]
! MULTIPLY
! DIVIDE
                  [ reduce using rule 5 (E -> E DIVIDE E .) ]
```

state 12



```
(6) E -> LPAREN E RPAREN .

PLUS reduce using rule 6 (E -> LPAREN E RPAREN .)

MINUS reduce using rule 6 (E -> LPAREN E RPAREN .)

MULTIPLY reduce using rule 6 (E -> LPAREN E RPAREN .)

DIVIDE reduce using rule 6 (E -> LPAREN E RPAREN .)

$end reduce using rule 6 (E -> LPAREN E RPAREN .)

RPAREN reduce using rule 6 (E -> LPAREN E RPAREN .)
```



```
WARNING:
WARNING: Conflicts:
WARNING:
WARNING: shift/reduce conflict for PLUS in state 9 resolved as shift
WARNING: shift/reduce conflict for MINUS in state 9 resolved as shift
WARNING: shift/reduce conflict for MULTIPLY in state 9 resolved as shift
WARNING: shift/reduce conflict for DIVIDE in state 9 resolved as shift
WARNING: shift/reduce conflict for PLUS in state 10 resolved as shift
WARNING: shift/reduce conflict for MINUS in state 10 resolved as shift
WARNING: shift/reduce conflict for MULTIPLY in state 10 resolved as shift
WARNING: shift/reduce conflict for DIVIDE in state 10 resolved as shift
WARNING: shift/reduce conflict for PLUS in state 11 resolved as shift
WARNING: shift/reduce conflict for MINUS in state 11 resolved as shift
WARNING: shift/reduce conflict for MULTIPLY in state 11 resolved as shift
WARNING: shift/reduce conflict for DIVIDE in state 11 resolved as shift
WARNING: shift/reduce conflict for PLUS in state 12 resolved as shift
WARNING: shift/reduce conflict for MINUS in state 12 resolved as shift
WARNING: shift/reduce conflict for MULTIPLY in state 12 resolved as shift
WARNING: shift/reduce conflict for DIVIDE in state 12 resolved as shift
```



- This grammar has 16 shift/reduce conflicts (4×4 because of the operators) and we can't just always shift.
 - This would cause precedence problems in some cases.
 - E.g., + might happen before *.
- The key word here is *precedence*. We could rewrite the grammar to separate precedence levels (as in that C excerpt), but why?
- Most compiler-compilers however allow the specification of operator precedence (and associativity).



Specifying Precedence and Associativity in bison

- Use the **%left** directive.
- Here we state that TOKEN_PLUS and TOKEN_MINUS are lower precedence than TOKEN_SLAHS and TOKEN_STAR.

%left TOKEN_MINUS TOKEN_PLUS
%left TOKEN_SLASH TOKEN_STAR

- They are all **left** associative.
- (There're also %right and %nonassoc options for those kinds of operators.)



Another Grammar ...

- Inserting the directives and rerunning bison results in *no* shift/reduce conflicts at all.
- We still have the same number / structure of states, but now we know when to shift and when to reduce so that precedence and associativity are honored.



Grammar

S' -> E Rule 0 DIVIDE : 5 Rule 1 E -> INTEGER INTEGER : 1 Rule 2 E -> E PLUS E LPAREN : 6 Rule 3 E -> E MINUS E Rule 4 E -> E MULTIPLY E MINUS : 3 MULTIPLY : 4 Rule 5 E -> E DIVIDE E PLUS : 2 Rule 6 E -> LPAREN E RPAREN RPAREN : 6 error

Nonterminals, with rules where they appear

Terminals, with rules where they appear

E : 2 2 3 3 4 4 5 5 6 0



Another Grammar ...

```
state 0
```

```
(0) S' -> . E
(1) E -> . INTEGER
(2) E -> . E PLUS E
(3) E -> . E MINUS E
(4) E -> . E MULTIPLY E
(5) E -> . E DIVIDE E
(6) E -> . LPAREN E RPAREN
```

INTEGER shift and go to state 2 LPAREN shift and go to state 3

E shift and go to state 1



```
state 1

(0) S' -> E .
(2) E -> E . PLUS E
(3) E -> E . MINUS E
(4) E -> E . MULTIPLY E
(5) E -> E . DIVIDE E

PLUS shift and go to state 4
MINUS shift and go to state 5
MULTIPLY shift and go to state 6
DIVIDE shift and go to state 7
```



Another Grammar ...

```
(1) E -> INTEGER .

PLUS reduce using rule 1 (E -> INTEGER .)
MINUS reduce using rule 1 (E -> INTEGER .)
MULTIPLY reduce using rule 1 (E -> INTEGER .)
DIVIDE reduce using rule 1 (E -> INTEGER .)
$end reduce using rule 1 (E -> INTEGER .)
RPAREN reduce using rule 1 (E -> INTEGER .)
```



```
state 3

(6) E -> LPAREN . E RPAREN
(1) E -> . INTEGER
(2) E -> . E PLUS E
(3) E -> . E MINUS E
(4) E -> . E MULTIPLY E
(5) E -> . E DIVIDE E
(6) E -> . LPAREN E RPAREN

INTEGER shift and go to state 2
LPAREN shift and go to state 3

E shift and go to state 8
```



Another Grammar ...



state 5

```
(3) E -> E MINUS . E
(1) E -> . INTEGER
(2) E -> . E PLUS E
(3) E -> . E MINUS E
(4) E -> . E MULTIPLY E
(5) E -> . E DIVIDE E
(6) E -> . LPAREN E RPAREN

INTEGER shift and go to state 2
LPAREN shift and go to state 3

E shift and go to state 10
```



Another Grammar ...





Another Grammar ...

```
(6) E -> LPAREN E . RPAREN
(2) E -> E . PLUS E
(3) E -> E . MINUS E
(4) E -> E . MULTIPLY E
(5) E -> E . DIVIDE E

RPAREN

RPAREN

Shift and go to state 13
PLUS

Shift and go to state 4
MINUS

Shift and go to state 5
MULTIPLY

Shift and go to state 6
DIVIDE

Shift and go to state 7
```



```
state 9
    (2) E \rightarrow E PLUS E.
    (2) E \rightarrow E . PLUS E
    (3) E \rightarrow E . MINUS E
    (4) E -> E . MULTIPLY E
    (5) E \rightarrow E . DIVIDE E
    PLUS
                     reduce using rule 2 (E -> E PLUS E .)
                     reduce using rule 2 (E -> E PLUS E .)
    MINUS
                     reduce using rule 2 (E -> E PLUS E .)
    $end
    RPAREN
                     reduce using rule 2 (E -> E PLUS E .)
                     shift and go to state 6
    MULTIPLY
    DIVIDE
                     shift and go to state 7
  ! MULTIPLY
                     [ reduce using rule 2 (E -> E PLUS E .) ]
  ! DIVIDE
                     [ reduce using rule 2 (E -> E PLUS E .) ]
  ! PLUS
                     [ shift and go to state 4 ]
  ! MINUS
                     [ shift and go to state 5 ]
```



Another Grammar ...

```
state 10
    (3) E \rightarrow E MINUS E.
    (2) E \rightarrow E . PLUS E
    (3) E \rightarrow E . MINUS E
    (4) E -> E . MULTIPLY E
    (5) E \rightarrow E . DIVIDE E
    PLUS
                     reduce using rule 3 (E -> E MINUS E .)
    MINUS
                     reduce using rule 3 (E -> E MINUS E .)
                     reduce using rule 3 (E -> E MINUS E .)
    $end
                     reduce using rule 3 (E -> E MINUS E .)
    RPAREN
    MULTIPLY
                     shift and go to state 6
    DIVIDE
                     shift and go to state 7
  ! MULTIPLY
                     [ reduce using rule 3 (E -> E MINUS E .) ]
                     [ reduce using rule 3 (E -> E MINUS E .) ]
  ! DIVIDE
  ! PLUS
                     [ shift and go to state 4 ]
  ! MINUS
                     [ shift and go to state 5 ]
```



state 11

```
(4) E -> E MULTIPLY E .
  (2) E \rightarrow E . PLUS E
  (3) E \rightarrow E . MINUS E
  (4) E -> E . MULTIPLY E
  (5) E \rightarrow E . DIVIDE E
  PLUS
                   reduce using rule 4 (E -> E MULTIPLY E .)
  MINUS
                   reduce using rule 4 (E -> E MULTIPLY E .)
                   reduce using rule 4 (E -> E MULTIPLY E .)
  MULTIPLY
                   reduce using rule 4 (E -> E MULTIPLY E .)
  DIVIDE
                   reduce using rule 4 (E -> E MULTIPLY E .)
 $end
  RPAREN
                   reduce using rule 4 (E -> E MULTIPLY E .)
! PLUS
                   [ shift and go to state 4 ]
! MINUS
                   [ shift and go to state 5 ]
! MULTIPLY
                   [ shift and go to state 6 ]
! DIVIDE
                   [ shift and go to state 7 ]
```



Another Grammar ...

state 12

! DIVIDE

```
(5) E -> E DIVIDE E .
  (2) E \rightarrow E . PLUS E
  (3) E \rightarrow E . MINUS E
  (4) E -> E . MULTIPLY E
  (5) E \rightarrow E . DIVIDE E
  PLUS
                   reduce using rule 5 (E -> E DIVIDE E .)
                   reduce using rule 5 (E -> E DIVIDE E .)
  MINUS
                   reduce using rule 5 (E -> E DIVIDE E .)
  MULTIPLY
                   reduce using rule 5 (E -> E DIVIDE E .)
  DIVIDE
                   reduce using rule 5 (E -> E DIVIDE E .)
  $end
  RPAREN
                   reduce using rule 5 (E -> E DIVIDE E .)
                   [ shift and go to state 4 ]
! PLUS
! MINUS
                   [ shift and go to state 5 ]
! MULTIPLY
                   [ shift and go to state 6 ]
```

[shift and go to state 7]



```
(6) E -> LPAREN E RPAREN .

PLUS reduce using rule 6 (E -> LPAREN E RPAREN .)

MINUS reduce using rule 6 (E -> LPAREN E RPAREN .)

MULTIPLY reduce using rule 6 (E -> LPAREN E RPAREN .)

DIVIDE reduce using rule 6 (E -> LPAREN E RPAREN .)

$end reduce using rule 6 (E -> LPAREN E RPAREN .)

RPAREN reduce using rule 6 (E -> LPAREN E RPAREN .)
```



Another Grammar ...

Action Table

Goto Table

```
0: {'INTEGER': 2, 'LPAREN': 3}
                                                            0: {'E': 1}
1: {'$end': 0, 'PLUS': 4, 'MINUS': 5,
     'MULTIPLY': 6, 'DIVIDE': 7}
                                                             3: {'E': 8}
2: {'$end': -1, 'PLUS': -1, 'MINUS': -1,
                                                            4: {'E': 9}
     'MULTIPLY': -1, 'DIVIDE': -1, 'RPAREN': -1}
3: {'INTEGER': 2, 'LPAREN': 3}
4: {'INTEGER': 2, 'LPAREN': 3}
                                                             5: {'E': 10}
5: {'INTEGER': 2, 'LPAREN': 3}
                                                             6: {'E': 11}
6: {'INTEGER': 2, 'LPAREN': 3}
                                                            7: {'E': 12}
7: {'INTEGER': 2, 'LPAREN': 3}
8: {'PLUS': 4, 'MINUS': 5, 'MULTIPLY': 6,
'DIVIDE': 7, 'RPAREN': 13}
9: {'$end': -2, 'PLUS': -2, 'MINUS': -2, 'MULTIPLY': 6, 'DIVIDE': 7, 'RPAREN': -2}
10: {'$end': -3, 'PLUS': -3, 'MINUS': -3,
      'MULTIPLY': 6, 'DIVIDE': 7, 'RPAREN': -3}
11: {'$end': -4, 'PLUS': -4, 'MINUS': -4,
      'MULTIPLY': -4, 'DIVIDE': -4, 'RPAREN': -4}
12: {'$end': -5, 'PLUS': -5, 'MINUS': -5,
      'MULTIPLY': -5, 'DIVIDE': -5, 'RPAREN': -5}
13: {'$end': -6, 'PLUS': -6, 'MINUS': -6,
      'MULTIPLY': -6, 'DIVIDE': -6, 'RPAREN': -6}
```



- Now there are no conflicts, precedence and associativity are properly honored, and the parse tree will be as expected.
- However, shift/reduce is not the only kind of conflict that can occur.
- There's also reduce/reduce.



Grammar with a Reduce/Reduce Conflict

 A contrived example grammar, but this is the kind of rule structure that leads to reduce/reduce conflicts.

$$A \rightarrow B c d$$

$$A \rightarrow E c f$$

$$B \, \to \, x \ y$$

$$E \rightarrow x y$$

The ambiguity is obvious.
 Let's see what the analysis reports.



У

Grammar

Rule 0 S' -> A Rule 1 A -> B c d

Rule 2 A -> E c f Rule 3 B -> x y Rule 4 E -> x y Terminals, with rules where they appear

c : 1 2 d : 1 error : f : 2 x : 3 4

Nonterminals, with rules where they appear

: 3 4

A : 0 B : 1 E : 2



Grammar with a Reduce/Reduce Conflict

```
state 0
```

```
(0) S' -> . A
(1) A -> . B c d
(2) A -> . E c f
(3) B -> . x y
```

 $(4) E \rightarrow . x y$

x shift and go to state 4

A shift and go to state 1
B shift and go to state 2
E shift and go to state 3



```
state 1
    (0) S' -> A .

state 2
    (1) A -> B . c d
    c     shift and go to state 5

state 3
    (2) A -> E . c f
    c     shift and go to state 6
```



Grammar with a Reduce/Reduce Conflict





Grammar with a Reduce/Reduce Conflict



WARNING:

WARNING: Conflicts:

WARNING:

WARNING: reduce/reduce conflict in state 7 resolved using rule (B -> x y)

WARNING: rejected rule (E -> x y) in state 7 WARNING: Rule (E -> x y) is never reduced



Grammar with a Reduce/Reduce Conflict

- To resolve the reduce/reduce conflict, the parser generator *arbitrarily* picked one of the rules and reduced by it.
- While letting a shift/reduce conflict be resolved by picking shift over reduce *might* be the proper resolution, letting the parser generator *arbitrarily* pick a rule to reduce by is *not* the proper way to resolve this sort of conflict.
- Reduce/reduce conflicts *must always* be investigated and resolved by refactoring / restating that part of the grammar.



- Fixing the contrived example is kind of pointless.
 - It's contrived.
- We'll look at reduce/reduce conflicts some more as we develop the grammar for our language.

```
A \rightarrow B \ c \ d
A \rightarrow E \ c \ f
B \rightarrow x \ y
E \rightarrow x \ y
```



Table-Driven Shift-Reduce Parsing

- The generalized *Shift-Reduce* parser is similar to the one for *Predictive Parsing*.
- We again stay in a loop looking at tokens and taking actions until we succeed or fail.
- Here, there are three kinds of entries in the ACTION table: shift, reduce, and accept.
- There's also a GOTO table for resetting the state after a reduce.



LR(k) Parsing

- The parser decides between *shifting* and *reducing* via a DFA.
 - This DFA is not *parsing* the input as a DFA is too weak to parse a CFG.
 - The DFA is applied to the contents of the *stack*.
- The possible DFA actions are:
 - Shift(n): Advance one token; push n onto the stack.
 - *Reduce*(*m*): Pop as many items as the number of symbols on the RHS of CFG production rule *m*. For the state now on the top of the stack, look up the LHS of rule *m* to get the next state *n*. Push *n* onto the stack.
 - *Accept*: Stop parsing and report success.
 - *Error*: Stop parsing and report failure.



A Simple CFG ...

```
\begin{array}{ll}
1 & S \to S; S \\
2 & S \to \text{id} := E \\
3 & S \to \text{print } (L)
\end{array}
```

4
$$E \rightarrow id$$

5 $E \rightarrow num$
6 $E \rightarrow E + E$
7 $E \rightarrow (S, E)$

8
$$L \to E$$

9 $L \to L$. E



A Simple CFG's LR Parsing Table

	id	num	print	;	,	+	:=	()	\$	S	E	L
1	s4		s7								g2		
2				s3						a			
2 3 4 5	s4		s7								g5		
4							s6						
5				r1	r1					r1			
6 7	s20	s10						s8				g11	
7								s9					
8	s4		s7								g12		
9	s20	s10						s8				g15	g14
10				r5	r5	r5			r5	r5			
11				r2	r2	s16				r2			
12				s3	s18								
13				r3	r3					r3			
14					s19				s13				
15					r8				r8				
16	s20	s10						s8				g17	
17				r6	r6	s16			r6	r6			
18	s20	s10						s8				g21 g23	
19	s20	s10						s8				g23	
20				r4	r4	r4			r4	r4			
21									s22				
22				r7	r7	r7			r7	r7			
23					r9	s16			r9				
					5,890	100-100			546				

sn Shift into state n.

gn Go to state n.

r*m* Reduce by rule *m*.

a Accept

Blanks indicate error.



LR Parsing Example

```
a := 7;
b := c + (d := 5 + 6, d)
```

```
Action
                             a := 7 ; b := c + (d := 5 + 6 , d) $
                                                                                                              shift
                                := 7 ; b := c + ( d := 5 + 6 , d ) $
                                                                                                              shift
_1 id_4 :=_6
                                                                                                              shift
                                          ; b := c + ( d := 5 + 6 , d )
_{1} id_{4} :=_{6} num_{10}
                                                                                                             reduce E \rightarrow num
_{1} id_{4} :=_{6} E_{11}
                                                                                                              reduce S \rightarrow id := E
                                         ; b := c + ( d := 5 + 6
                                                                                                              shift
_1 S_2
                                             b := c + (d := 5 + 6)
_{1} S_{2};_{3}
                                                                                                              shift
                                                 := c + (d := 5 + 6, d)
                                                                                                              shift
1 S2;3 id4
_{1} S_{2};_{3} id_{4} :=_{6}
                                                                                                              shift
                                                                                                              reduce E \rightarrow id
_{1} S_{2};_{3} id_{4} :=_{6} id_{20}
                                                            + (d := 5 + 6, d)
_{1} S_{2};_{3} id_{4} :=_{6} E_{11}
                                                                                                             shift
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16}
                                                                                                              shift
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8}
                                                                                                              shift
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} id_{4})
                                                                                                              shift
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} id_{4} :=_{6}
                                                                                                              shift
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} id_{4} :=_{6} num_{10})
                                                                                                              reduce E \rightarrow num
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} id_{4} :=_{6} E_{11}
                                                                                  +6,d)$
                                                                                                             shift
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} id_{4} :=_{6} E_{11} +_{16}
                                                                                     6 , d )
                                                                                                              shift
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} id_{4} :=_{6} E_{11} +_{16} num_{10})
                                                                                                             reduce E \rightarrow num
                                                                                         , d) $
_{1} S_{2} ;_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} id_{4} :=_{6} E_{11} +_{16} E_{17}
                                                                                                             reduce E \rightarrow E + E
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} id_{4} :=_{6} E_{11}
                                                                                                             reduce S \rightarrow id := E
                                                                                         , d) $
                                                                                                             shift
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} S_{12})
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} S_{12},_{18})
                                                                                                             shift
                                                                                                             reduce E \rightarrow id
_{1} S_{2} ;_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} S_{12} ,_{18} id_{20})
                                                                                                 ) $
_{1} S_{2};_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} S_{12},_{18} E_{21})
                                                                                                              shift
_{1} S_{2} ;_{3} id_{4} :=_{6} E_{11} +_{16} (_{8} S_{12} ,_{18} E_{21} )_{22}
                                                                                                             reduce E \rightarrow (S, E)
                                                                                                             reduce \ E \rightarrow E + E
_{1} S_{2} ;_{3} id_{4} :=_{6} E_{11} +_{16} E_{17}
                                                                                                             reduce S \rightarrow id := E
_{1} S_{2};_{3} id_{4} :=_{6} E_{11}
                                                                                                             reduce S \rightarrow S; S
_{1} S_{2};_{3} S_{5}
_1 S_2
                                                                                                             accept
```

LR(k) Parsing

- OK, enough theory.
- No, I am not going to drag you through how to process the CFG to get the DFA for parsing.
 - That's the job of a compiler-compiler tool such as ply, yacc, bison, etc.
 - FYI, at last check, Wikipedia's list of *Deterministic Context-Free Language Parser Generators* list had **99** entries.

2020 Feb 11, https://en.wikipedia.org/wiki/Comparison_of_parser_generators



The bison Parser Generator

- The point is that someone else has already done all of the work for you.
- Just use the bison parser generator so we can concentrate on the *language* instead of the tool that got us there.



bison calc Example

- A barebones "desk calculator".
- Add +, Subtract -, Multiply *, and Divide / operators.
- Includes named variables to hold results.

```
calc > a+3
calc > b = a*4
calc > a+b
calc > c = a+b
calc > d = e = f = 1
Syntax error at '='
           https://github.com/dabeaz/ply
```



Parse Tree

- The output of the *Syntactic Analyzer* phase is a *Parse Tree*.
 - This tree represents the *structure* of the particular input token stream as determined by the language's grammar rules.
 - *Unique* for a given stream of tokens.
 - If not, the grammar is ambiguous and needs to be fixed.
- It's normally called a *Raw* (or *Concrete*) tree in that its leaves are the tokens and its internal nodes correspond to the applied production rules.



Parse Tree

- Correspondence is not always exact.
 - Not all tokens may be represented.
 - Alterations / Simplifications may have been made.
- There can be a *blurring* of the line between the *Parse Tree* and the *Abstract Syntax Tree* (*AST*).
 - ASTs will be considered in *Semantic Analysis*.

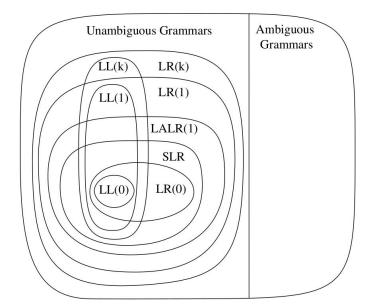


Syntactic Error Recovery

- What to do when a syntax error is detected?
 - Complain and die? Most obvious answer but very unfriendly. Probably would like to see *other* errors.
 - However, have to avoid an avalanche of cascading errors.
- Exactly what's possible depends on how the parser was generated.
 - Different compiler compilers have (very) different error detection, control, and recovery mechanisms.
 - Hand-written parsers have the best flexibility!



Another Hierarchy of Grammar Classes



LR — (ply)

LALR — "LookAhead LR" merges some rules to get better memory usage. (yacc / Bison)

SLR — "Simple LR" merges still more rules.

Merging rules can cause Reduce / Reduce conflicts in some grammars.



