HonestDiD: Vignette

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April 28, 2024

Description

The HonestDiD package implements the methods developed in Rambachan and Roth [2021] for performing inference in difference-in-differences and event-study designs that is robust to violations of the parallel trends assumption. See Rambachan and Roth [2021] for methodological details.

We illustrate how the package can be used by replicating Figure 4 in Rambachan and Roth [2021], which applies these methods to Benzarti and Carloni [2019]'s results on the effects of a decrease in the value-added tax in France on restaurant profits, and replicating Figure 6 in Rambachan and Roth [2021], which applies these methods to Lovenheim and Willen [2019]'s results on the effect of public sector bargaining laws on long-run female labor market outcomes.

The estimated event study coefficients and variance-covariance matrix for the baseline estimates on profits in Benzarti and Carloni [2019] are included in the package as BCdata_EventStudy (see Section 6.1 of Rambachan and Roth [2021] for details on the underlying event study specification). The estimated event study coefficients and variance-covariance matrix for the baseline female estimates on employment of Lovenheim and Willen [2019] are included in the package as LWdata_EventStudy (see Section 6.2 of Rambachan and Roth [2021] for details on the underlying event study specification). The underlying raw data for the estimated event study of Lovenheim and Willen [2019] are also included in the package.

Installation

To install the package, use the function install_github() from the remotes package:

```
install.packages("remotes") # if remotes package not installed
# Turn off warning-error-conversion, because the tiniest
# warning stops installation
Sys.setenv(R_REMOTES_NO_ERRORS_FROM_WARNINGS = "true")
# install from github
remotes::install_github("asheshrambachan/HonestDiD")
```

After installation, load in the package using library('HonestDiD').

Background: choices of Δ

Following Rambachan and Roth [2021], the parameter of interest is $\theta = l'\tau_{post}$, where τ_{post} is the vector of dynamic causal effects of interest in the post-periods and l is a vector specified by the user. For instance, if the user is interested in the effect in the first period after treatment, then l should be set to the basis vector with a 1 in the 1st position and zeros elsewhere.

To construct confidence sets for θ that are robust to violations of the parallel trends assumption, the user must specify the set Δ , which describes the set of possible violations of the parallel trends assumption that the user is willing to consider.

The HonestDiD package currently allows for several choices of Δ . We discuss these possible choices of Δ below. We refer the reader to Section 2.3 for extensive details on these choices.

Smoothness Restrictions

A reasonable baseline in many cases is $\Delta = \Delta^{SD}(M)$, which requires that the underlying trend not deviate "too much" from linearity. It imposes that the change in the slope of the underlying trend (i.e. the second difference in δ) be no more than M between consecutive periods, where M is a parameter that is specified by the researcher. Formally, this set is defined as

$$\Delta^{SD}(M) = \{ \delta : |(\delta_t - \delta_{t-1}) - (\delta_{t-1} - \delta_{t-2})| \le M \}.$$

For the choice M=0, this choice of Δ limits the violation of parallel trends to be linear, while M>0 relaxes the assumption of exact linearity. See Section 2.3 of Rambachan and Roth [2021] for further discussion.

The user may additionally restrict the sign of the bias in the post-period. This may be reasonable, for instance, in cases where there is a simulataneous policy change which we think affects the outcome of interest in a particular direction. We refer to restrictions that combine Δ^{SD} with a restriction on the post-period bias by $\Delta = \Delta^{SDB}(M)$. For example, $\Delta^{SDPB}(M)$ additionally imposes that the violation of parallel trends must be positive in the post-periods, $\delta_t \geq 0$ for $t \geq 0$. Likewise, $\Delta^{SDNB}(M)$ additionally imposes that the violation of parallel trends must be negative in the post-periods $\delta_t < 0$ for t > 0.

The researcher may specify additional shape restrictions that specify that the violation of parallel trends must be monotonically increasing or decreasing. Such restrictions may be reasonable in cases where the researcher is concerned about secular trends that would have continued absent treatment. We refer to restrictions that combine Δ^{SD} with monotonicity restrictions by $\Delta = \Delta^{SDM}(M)$. In the case where the violation of parallel trends must be increasing, denoted by $\Delta^{SDI}(M)$, this additionally restricts $\delta_t \geq \delta_{t-1}$ for all t. In the case where the violation of parallel trends must be decreasing, denoted by $\Delta^{SDD}(M)$, this additionally restricts $\delta_t \leq \delta_{t-1}$ for all t.

These "smoothness restriction" based choices of Δ are implemented in HonestDiD.

Bounding Relative Magnitudes

Alternatively, the researcher may specify Δ in a manner that bounds the worst-case violation of parallel trends in the post-treatment period based on the observed worst-case violation in the pre-treatment period. Rambachan and Roth [2021] consider two forms of such Δ .

First, $\Delta^{RM}(\bar{M})$ bounds the maximum post-treatment violation of parallel trends (between consecutive periods) by \bar{M} times the maximum pre-treatment violation of parallel trends. This is defined as

$$\Delta^{RM}(\bar{M}) = \{\delta : \forall t \geq 0, |\delta_{t+1} - \delta_t| \leq \bar{M} \cdot \max_{s < 0} |\delta_{s+1} - \delta_s| \}$$

Second $\Delta^{SDRM}(\bar{M})$ bounds the maximum deviation from a linear trend in the post-treatment period by \bar{M} times the observed maximum deviation from a linear trend in the pre-treatment period. This is defined as

$$\Delta^{SDRM}(\bar{M}) = \{\delta : \forall t \geq 0, |(\delta_{t+1} - \delta_t) - (\delta_t - \delta_{t-1})| \leq \bar{M} \cdot \max_{s < 0} |(\delta_{s+1} - \delta_s) - (\delta_s - \delta_{s-1})|\}$$

Notice that this choice of $\delta = \Delta^{SDRM}(\bar{M})$ is analogous to the earlier choice $\Delta^{SD}(M)$, but it allows the magnitude of the possible deviations from a linear trend to depend on the observed pre-treatment trends (rather than being imposed a priori by the researcher). Both of these choices $\Delta^{RM}(\bar{M})$ and $\Delta^{SDRM}(\bar{M})$ may also be combined with the sign and shape restrictions discussed above.

These "relative magnitude" based choices of Δ are implemented in HonestDiD.

Constructing a sensitivity plot

We next show to use the package HonestDiD to conduct a formal sensitivity analysis. We recommend that the user creates a sensitivity plot that shows how the robust confidence sets vary under different assumptions about Δ (e.g., letting M vary or adding sign/shape restrictions).

The function createSensitivityResults provides a wrapper function to conduct sensitivity analysis for the "smoothness restriction" based choices of Δ discussed in the previous section. This function takes as inputs the estimated event study coefficients, the estimated variance-covariance matrix of the estimates along with the user's choice of Δ and chosen method for constructing robust confidence intervals. It returns the upper and lower bounds of the robust confidence sets for a vector of choices of M as a dataframe. The researcher may specify that Δ equals $\Delta^{SD}(M)$, $\Delta^{SDB}(M)$ or $\Delta^{SDM}(M)$. In the latter two cases, the user additionally specifies the sign/direction of the bias/monotonicity.

If the user leaves the desired method as NULL in createSensitivityResults, the function automatically selects the robust confidence interval based upon the recommendations in Section 5.3 of Rambachan and Roth [2021]. If $\Delta = \Delta^{SD}(M)$, the FLCI is used. If $\Delta = \Delta^{SDB}(M)$ or $\Delta = \Delta^{SDM}(M)$, the conditional FLCI hybrid confidence set is used. As a default, the function sets the parameter of interest to be the first post-period causal effect, $\theta = \tau_1$. The user may directly specify the parameter of interest by setting the input 1_vec.

The function createSensitivityResults_relativeMagnitudes provides a wrapper function to conduct sensitivity analysis for the "relative magnitudes" based choices of Δ discussed in the previous section. This function also takes as inputs the estimated event study coefficients, the estimated variance-covariance matrix of the estimates along with the user's choice of Δ and chosen method for constructing robust confidence intervals. It returns the upper and lower bounds of the robust confidence sets for a vector of choices of \bar{M} as a dataframe. The user may choose $\Delta^{RM}(\bar{M})$ by setting bound = "deviation from parallel trends and $\Delta^{SDRM}(\bar{M})$ by setting bound = deviation from linear trend. The user may also specify additional sign/shape restrictions which requires further specifying the sign/direction of the bias/monotonicity.

If the user leaves the desired method as NULL in createSensitivityResults_relativeMagnitudes, the function automatically selects the robust confidence interval based upon the recommendations in Section 5.3 of Rambachan and Roth [2021]. For $\Delta^{RM}(\bar{M})$, $\Delta^{SDRM}(\bar{M})$ and their variants that incorporate sign/shape restrictions, the function uses the conditional least favorable hybrid confidence set by default. Again, as a default, the function sets the parameter of interest to be the first post-period causal effect, $\theta = \tau_1$. The user may directly specify the parameter of interest by setting the input 1_vec.

Sensitivity Analysis: Incidence of Value-Added Tax Cut

Preliminaries

The included data frame BCdata_EventStudy contains the estimated event study coefficients and estimated variance-covariance matrix for the baseline estimates for profits based on the event study specification of Benzarti and Carloni [2019]. As discussed in Section 6.1 of Rambachan and Roth [2021], the authors estimate the effect of a reduction in the value-added tax in France in July 2009 on restaurant profits. Comparing restaurants to a control group of other market services firms that were unaffected by the policy change, the authors estimate the event study specification

$$Y_{it} = \sum_{s \neq 2008} \beta_s \times 1[t = s] \times D_i + \phi_i + \lambda_t + \epsilon_{it},$$

where Y_{it} is the log of (before-tax) profits for firm i in in year t; D_i is an indicator for whether firm i is a restaurant; ϕ_i and λ_t are firm and year fixed effects; and standard errors are clustered at the regional level. BCdata_EventStudy contains the estimated event study coefficients $\hat{\beta}_s$, the associated variance-covariance matrix of these estimates and some additional information about the event study specification. The next code snippet loads the data.

```
data("BCdata_EventStudy", package = "HonestDiD")
# Number of pre-periods

BC_numPrePeriods = length(BCdata_EventStudy$prePeriodIndices)

BC_numPostPeriods = length(BCdata_EventStudy$postPeriodIndices)
```

Conducting Sensitivity Analyses

We now show how to use the package HonestDiD to conduct a formal sensitivity analysis using the estimated event study from Benzarti and Carloni [2019].

In the next code snippet, we conduct the sensitivity analysis plotted in the top right panel of Figure 4 in Rambachan and Roth [2021], which shows a sensitivity analysis using $\Delta = \Delta^{SDRM}(\bar{M})$ for the effect on profits in 2009, $\theta = \tau_{2009}$. To do so, we set bound = "deviation from linear trend" in createSensitivityResults_relativeMagnitudes.

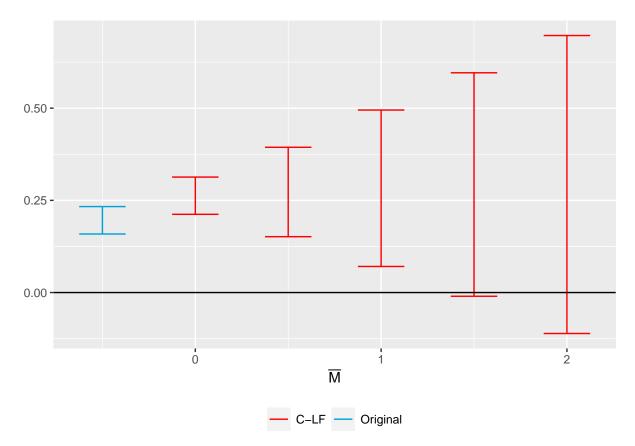
```
# Create l_vec to define the parameter of interest, the
# first post-treatment period.
BC_l_vec = basisVector(index = 1, size = BC_numPostPeriods)

# Construct robust confidence intervals for
# Delta^{SDRM}(Mbar) for first post-treatment period. We
# specify 100 gridPoints over [-1, 1] for the underlying
```

```
# test inversion to construct the robust confidence set.
# Users may wish to leave this at the default values.
BC_DeltaSDRM_RobustResults = createSensitivityResults_relativeMagnitudes( # betahat = BCdata_EventStudy$betahat,
    sigma = BCdata_EventStudy$sigma,
    bound = "deviation from linear trend",
    numPrePeriods = BC_numPrePeriods,
    numPostPeriods = BC_numPostPeriods,
    l_vec = BC_l_vec,
    Mbarvec = seq(from = 0, to = 2, by = 0.5),
    gridPoints = 100, grid.lb = -1, grid.ub = 1)
head(BC_DeltaSDRM_RobustResults)
```

```
#> # A tibble: 5 x 5
#>
         1b
              ub method Delta
                                   Mbar
      <dbl> <dbl> <chr> <chr>
#>
                                  <dbl>
#> 1 0.212 0.313 C-LF DeltaSDRM
                                    0
#> 2 0.152 0.394 C-LF DeltaSDRM
                                    0.5
#> 3 0.0707 0.495 C-LF
                        DeltaSDRM
#> 4 -0.0101 0.596 C-LF DeltaSDRM
                                   1.5
#> 5 -0.111 0.697 C-LF
                        DeltaSDRM
                                    2
```

The function createSensitivityPlot_relativeMagnitudes can then be used to construct a sensitivity plot presenting these results. createSensitivityPlot_relativeMagnitudes takes two key inputs. The first input is the dataframe that is produced by createSensitivityResults_relativeMagnitudes, which contains the robust confidence intervals. The second input is a dataframe that contains the OLS confidence set for the parameter of interest. This dataframe can be constructed using the function constructOriginalCS. In the next code snippet, we show how these functions can be used to replicate the top right panel of Figure 4 in Rambachan and Roth [2021].



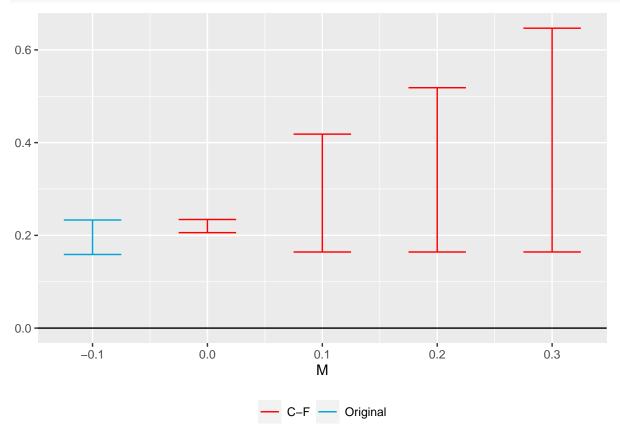
This sensitivity analysis finds that the "breakdown value" of \bar{M} is about 1.5, which means that the significant treatment effect found in 2009 is robust to allowing for a non-linearity in the differential trend between restaurants and other service firms in the post-treatment period that is about 1.5 times the maximum observed non-linearity in the pre-treatment period.

We also discuss how additional context-specific knowledge may inform the sensitivity analysis. As discussed in Section 6.1 of Rambachan and Roth [2021], Benzarti and Carloni [2019] indicate that their event-study estimates may be biased since other confounding policy changes occurred at the same time of the value-added tax change. This suggests that we may wish to incorporate an additional sign restriction in the sensitivity analysis, which imposes that the sign of the bias be negative. The next code snippet therefore conducts the sensitivity analysis plotted in the bottom right panel of Figure 4 in Rambachan and Roth [2021], which shows a sensitivity analysis using $\Delta = \Delta^{SDNB}(M) := \Delta^{SD}(M) \cap \{\delta: \delta_{post} \leq 0\}$. We construct the sensitivity analysis using createSensitivityResults and specify that biasDirection = "negative". We plot the results using createSensitivityPlot.

```
# Construct robust confidence intervals for Delta^{SDNB}(M)
# for first post-treatment period

BC_DeltaSDNB_RobustResults = createSensitivityResults( #
    betahat = BCdata_EventStudy$betahat,
    sigma = BCdata_EventStudy$sigma,
    numPrePeriods = BC_numPrePeriods,
    numPostPeriods = BC_numPostPeriods,
    l_vec = BC_l_vec,
    Mvec = seq(from = 0, to = 0.3, by = 0.1),
```

```
biasDirection = "negative")
BC_DeltaSDNB_SensitivityPlot = createSensitivityPlot( #
    robustResults = BC_DeltaSDNB_RobustResults,
    originalResults = BC_OriginalResults)
BC_DeltaSDNB_SensitivityPlot
```



Sensitivity Analysis: Effect of Public Sector Bargaining Laws

Preliminaries

The included dataframe LWdata_EventStudy contains the estimated event study coefficients and estimated variance-covariance matrix for the baseline estimates for female employment based on the event study specification of Lovenheim and Willen [2019]. As discussed in Section 6.2 of Rambachan and Roth [2021], the authors use the American Community Survey to study the impact of public-sector duty-to-bargain (DTB) laws, which strengthen teachers' unions, on adult labor market outcomes. Exploiting the differential timing of the passage of DTB laws across states, the authors estimate the event study specification

$$Y_{sct} = \sum_{r=-11}^{21} D_{scr} \beta_r + X_{sct}' \gamma + \lambda_{ct} + \phi_s + \epsilon_{sct},$$

where Y_{sct} is the average employment for a cohort of students born in state s in cohort c in ACS calendar year t and D_{scr} is an indicator for whether state s passed a DTB law r years before cohort c turned age 18. LWdata_EventStudy contains the estimated event study coefficients $\hat{\beta}_r$, the associated

variance-covariance matrix of these estimates and some additional information about the event study specification. The next code snippet loads the data.

```
data("LWdata_EventStudy", package = "HonestDiD")
# Number of pre-periods
LW_numPrePeriods = length(LWdata_EventStudy$prePeriodIndices)
LW_numPostPeriods = length(LWdata_EventStudy$postPeriodIndices)
```

We provide additional details on how the results in LWdata_EventStudy are constructed in the section titled "Details on replicating Lovenheim and Willen [2019]' below.

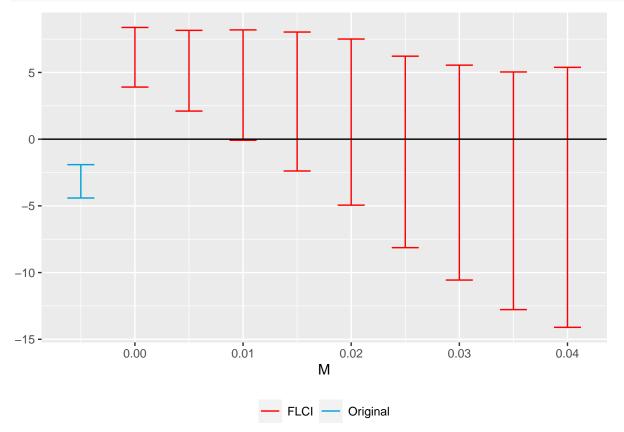
Conducting Sensitivity Analyses

We now show how to use the package HonestDiD to conduct a formal sensitivity analysis using the estimated event study from Lovenheim and Willen [2019].

In the next code snippet, we conduct the sensitivity analysis plotted in the right panel of Figure 6 in Rambachan and Roth [2021], which shows a sensitivity analysis using $\Delta = \Delta^{SD}(M)$ for the effect on female employment after 15 years of exposure to a duty-to-bargain law, $\theta = \tau_{15}$.

```
# Create l_vec corresponding with 15 years of exposure
# Reference is -2 years of exposure, so want effect 17 pds
# later
LW_l_vec = basisVector(15 - (-2), LW_numPostPeriods)
# Construct robust confidence intervals for Delta^{SD}(M)
# for 15 years of exposure
LW_DeltaSD_RobustResults = createSensitivityResults(betahat = LWdata_EventStudy$betahat,
   sigma = LWdata_EventStudy$sigma, numPrePeriods = LW_numPrePeriods,
   numPostPeriods = LW_numPostPeriods, l_vec = LW_l_vec, Mvec = seq(from = 0,
       to = 0.04, by = 0.005)
head(LW_DeltaSD_RobustResults)
#> # A tibble: 6 x 5
#>
         lb ub method Delta
                                     Μ
      <dbl> <dbl> <chr> <chr> <dbl>
#>
#> 1 3.91
           8.37 FLCI DeltaSD 0
#> 2 2.11
             8.16 FLCI DeltaSD 0.005
#> 3 -0.0829 8.19 FLCI DeltaSD 0.01
#> 4 -2.38 8.03 FLCI DeltaSD 0.015
#> 5 -4.95
             7.51 FLCI
                         DeltaSD 0.02
#> 6 -8.13
             6.22 FLCI
                         DeltaSD 0.025
```

The function createSensitivityPlot can then be used to construct a sensitivity plot presenting these results. createSensitivityPlot takes two key inputs. The first input is the dataframe that is produced by createSensitivityResults, which contains the robust confidence intervals. The second input is a dataframe that contains the OLS confidence set for the parameter of interest. This dataframe can be constructed using the function constructOriginalCS. In the next code snippet, we show how these functions can be used to replicate the right panel of Figure 6 in Rambachan and Roth [2021].

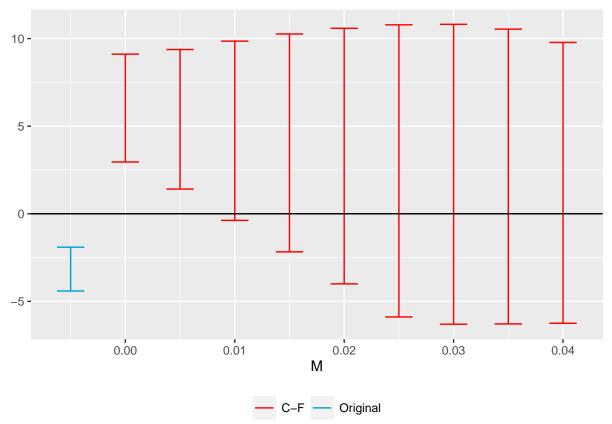


In the next code snippet, we conduct an additional sensitivity analysis. The exercise is similar to that shown above, except we now impose that any violations of parallel trends be (weakly) decreasing ($\Delta = \Delta^{SDD}(M)$). This incorporates the intuition from Lovenheim and Willen [2019] that the pre-trends for women are likely due to secular trends in female labor supply that would have continued absent treatment.

```
# Construct robust confidence intervals for Delta^{SDD}(M)
LW_DeltaSDD_RobustResults = createSensitivityResults( #
   betahat = LWdata_EventStudy$betahat,
   sigma = LWdata_EventStudy$sigma,
   monotonicityDirection = "decreasing",
```

```
numPrePeriods = LW_numPrePeriods,
numPostPeriods = LW_numPostPeriods,
l_vec = LW_l_vec,
Mvec = seq(from = 0, to = 0.04, by = 0.005))

# Construct sensitivity plot
LW_DeltaSDD_SensitivityPlot = createSensitivityPlot( #
robustResults = LW_DeltaSDD_RobustResults,
originalResults = LW_OriginalResults)
LW_DeltaSDD_SensitivityPlot
```



Benchmarking M

The sensitivity plots discussed above show how our conclusions change as we allow for larger degrees of possible non-linearity in the violations of parallel trends, parameterized by M. Rambachan and Roth [2021] discuss multiple ways for benchmarking M in applied settings.

One approach for benchmarking M is to use context-specific knowledge about the magnitudes of potential confounds. For instance, in the context of Lovenheim and Willen [2019], one concern is differential changes in education quality that would have occurred even absent the passage of DTB laws. Section 6.2 of Rambachan and Roth [2021] calibrates M using estimates of the effect of teacher quality on adult employment from Chetty et al. [2014]. In this calibration, a value of M=0.01 corresponds with a change in slope of the diffferential trend corresponding with a change in teacher quality of 0.025 standard deviations.

In some cases, it may also be useful to benchmark M – which bounds the change in slope of the differential trend between consecutive periods – using estimates of the largest change in slope in the pre-period. We provide the functions <code>DeltaSD_lowerBound_Mpre</code> and <code>DeltaSD_upperBound_Mpre</code>, which create one-sided confidence intervals for the largest change in slope in the pre-period. Values of M below the values computed by <code>DeltaSD_lowerBound_Mpre</code> are rejected by the data (at the given significance level), and thus should be viewed with caution. On the other hand, we stress that data from the pre-period cannot, on its own, place an upper bound on the possible degree of non-linearity under the counterfactual in the post-periods. However, in some cases it may be useful to benchmark the assumed maximal degree of non-linearity M in terms of the largest change in slope in the pre-period. These functions can also be used analogously to benchmark M using event-studies for placebo groups. See the R documentation for additional details.

Both functions require the user to specify the vector of estimated event study coefficients, the variance covariance matrix, the number of pre-periods and the desired size of the one-sided confidence intervals. They can be used as follows:

Details on replicating Lovenheim and Willen [2019]

We now provide additional details on the construction of the event-study results from Lovenheim and Willen [2019] used in the example above. This event study specification can be fully replicated using a dataframe provided in the package HonestDiD. Within the subdirectory inst/extdata, the package provides the stata dataset LWdata_RawData.dta. This contains the estimation sample for females that is used to estimate the above event study specification. This dataset is provided in the replication files for Lovenheim and Willen [2019] and can be found in the subdirectory of the replication files, Data files/Estimation samples/Estimation_FEMALE.dta. The following code snippet shows how to reproduce the event study above using the provided data

```
# Load in LWdata_RawData.dta
LWdata_RawData = haven::read_dta(system.file("extdata", "LWdata_RawData.dta",
                                             package = "HonestDiD"))
# Estimate event study using lfe package
EmpFemale.EventStudy = lfe::felm(emp ~ rtESV13 + rtESV14 + rtESV15 +
                                   rtESV16 + rtESV17 + rtESV18 +
                                   rtESV19 + rtESV110 + rtESV111 + # End Pre-periods
                                   rtESV113 + rtESV114 + rtESV115 +
                                   rtESV116 + rtESV117 + rtESV118 +
                                   rtESV119 + rtESV120 + rtESV121 +
                                   rtESV122 + rtESV123 + rtESV124 +
                                   rtESV125 + rtESV126 + rtESV127 +
                                   rtESV128 + rtESV129 + rtESV130 +
                                   rtESV131 + rtESV132 + rtESV133 +
                                   rtESV134 + rtESV135 + # End post-periods
                                   yearsfcor + yearsflr + aveitc + fscontrol +
```

```
asian + black + hispanic + other |
                                   factor(PUS_SURVEY_YEAR)*factor(BIRTHYEAR) +
                                   factor(PUS_SURVEY_YEAR) + factor(BIRTHSTATE) |
                                   0 | BIRTHSTATE,
                                 data = LWdata_RawData,
                                 weights = LWdata_RawData$nobs)
# Extract coefficients of regression associated with event study coefficients
coefIndex = which(grepl(x = dimnames(EmpFemale.EventStudy$coefficients)[[1]],
                        pattern = "rtESV"))
betahat = EmpFemale.EventStudy$beta[coefIndex, ]
# Extract estimated variance-covariance matrix of event study coefficients
sigma = EmpFemale.EventStudy$clustervcv[coefIndex, coefIndex]
#Rescale by 100 so that results will be in units of percentage points
betahat = 100 * betahat
sigma = 100^2 * sigma
# Construct vector of event times and the scalar reference period
timeVec = c(seq(from = -11, to = -3, by = 1), seq(from = -1, to = 21, by = 1))
referencePeriod = -2
postPeriodIndices = which(timeVec > -2)
prePeriodIndices = which(timeVec < -2)</pre>
# Construct standard errors associated with event study coefficients
stdErrors = summary(EmpFemale.EventStudy)$coefficients[coefIndex,2]
# Create list containing objects produced by the event study
LWdata_EventStudy = list(
 betahat = betahat,
 sigma = sigma,
 timeVec = timeVec,
 referencePeriod = referencePeriod.
 prePeriodIndices = prePeriodIndices,
 postPeriodIndices = postPeriodIndices,
 stdErrors = stdErrors
)
```

References

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