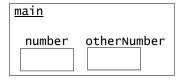
Unit 4, Part 3

# Recursion

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### Review: Method Frames

 When you make a method call, the Java runtime sets aside a block of memory known as the *frame* of that method call.

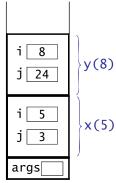


- The frame is used to store:
  - · the formal parameters of the method
  - any local variables variables declared within the method
- A given frame can only be accessed by statements that are part of the corresponding method call.

### Frames and the Stack

- The frames we've been speaking about are stored in a region of memory known as *the stack*.
- For each method call, a new frame is added to the top of the stack.

```
public class Foo {
  public static int y(int i) {
     int j = i * 3;
     return j;
  }
  public static int x(int i) {
     int j = i - 2;
     return y(i + j);
  }
  public static void
     main(String[] args) {
        System.out.println(x(5));
   }
}
```



When a method completes, its stack frame is removed.

#### Iteration

- Whenever we've encountered a problem that requires repetition, we've used *iteration* i.e., some type of loop.
- Sample problem: printing the series of integers from n1 to n2, where n1 <= n2.</li>
  - example: printSeries(5, 10) should print the following: 5, 6, 7, 8, 9, 10
- Here's an iterative solution to this problem:

```
public static void printSeries(int n1, int n2) {
    for (int i = n1; i < n2; i++) {
        System.out.print(i + ", ");
    }
    System.out.println(n2);
}</pre>
```

### Recursion

- An alternative approach to problems that require repetition is to solve them using a method that calls itself.
- Applying this approach to the print-series problem gives:

```
public static void printSeries(int n1, int n2) {
    if (n1 == n2) {
        System.out.println(n2);
    } else {
        System.out.print(n1 + ", ");
        printSeries(n1 + 1, n2);
    }
}
```

- · A method that calls itself is a recursive method.
- This approach to problem-solving is known as recursion.

### Tracing a Recursive Method

```
public static void printSeries(int n1, int n2) {
    if (n1 == n2) {
        System.out.println(n2);
    } else {
        System.out.print(n1 + ", ");
        printSeries(n1 + 1, n2);
    }
}
```

• What happens when we execute printSeries(5, 7)?

```
printSeries(5, 7):
    System.out.print(5 + ", ");
    printSeries(6, 7):
        System.out.print(6 + ", ");
        printSeries(7, 7):
            System.out.println(7);
            return
        return
    return
    return
```

### **Recursive Problem-Solving**

- When we use recursion, we solve a problem by reducing it to a simpler problem of the same kind.
- We keep doing this until we reach a problem that is simple enough to be solved directly.
- This simplest problem is known as the base case.

 The base case stops the recursion, because it doesn't make another call to the method.

# Recursive Problem-Solving (cont.)

• If the base case hasn't been reached, we execute the recursive case.

- The recursive case:
  - reduces the overall problem to one or more simpler problems of the same kind
  - makes recursive calls to solve the simpler problems

### Structure of a Recursive Method

```
recursiveMethod(parameters) {
    if (stopping condition) {
        // handle the base case
} else {
        // recursive case:
        // possibly do something here
        recursiveMethod(modified parameters);
        // possibly do something here
}
```

- There can be multiple base cases and recursive cases.
- When we make the recursive call, we typically use parameters that bring us closer to a base case.

# Tracing a Recursive Method: Second Example

What happens when we execute mystery(2)?

# Printing a File to the Console

Here's a method that prints a file using iteration:

```
public static void print(Scanner input) {
    while (input.hasNextLine()) {
        System.out.println(input.nextLine());
    }
}
```

· Here's a method that uses recursion to do the same thing:

```
public static void printRecursive(Scanner input) {
    // base case
    if (!input.hasNextLine()) {
        return;
    }

    // recursive case
    System.out.println(input.nextLine());
    printRecursive(input); // print the rest
}
```

# Printing a File in Reverse Order

- What if we want to print the lines of a file in reverse order?
- · It's not easy to do this using iteration. Why not?
- It's easy to do it using recursion!
- How could we modify our previous method to make it print the lines in reverse order?

### Printing a File in Reverse Order (cont.)

- An iterative approach to reversing the file would need to:
  - read all of the lines in the file and store them in a temporary data structure (e.g., an array)
  - retrieve the lines from the data structure and print them in reverse order
- The recursive method doesn't need a separate data structure.
  - the lines are stored in the stack frames for the recursive method calls!

### A Recursive Method That Returns a Value

• Simple example: summing the integers from 1 to n

```
public static int sum(int n) {
    if (n <= 0) {
        return 0;
    }
    int rest = sum(n - 1);
    return n + rest;
}</pre>
```

• Example of this approach to computing the sum:

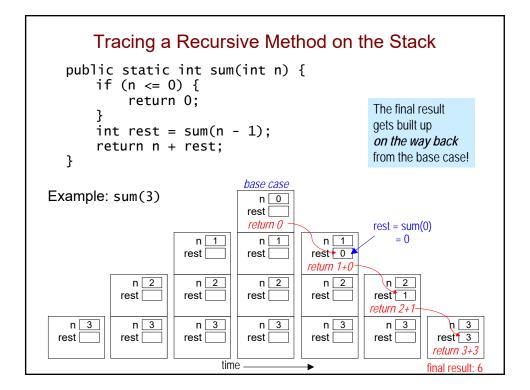
```
sum(6) = 6 + sum(5)
= 6 + 5 + sum(4)
```

. . .

# Tracing a Recursive Method

```
public static int sum(int n) {
    if (n <= 0) {
        return 0;
    }
    int rest = sum(n - 1);
    return n + rest;
}</pre>
```

 What happens when we execute int x = sum(3); from inside the main() method?



# Another Option for Tracing a Recursive Method

```
public static int sum(int n) {
    if (n <= 0) {
        return 0;
    }
    int rest = sum(n - 1);
    return n + rest;
}</pre>
```

### Infinite Recursion

- We have to ensure that a recursive method will eventually reach a base case, regardless of the initial input.
- Otherwise, we can get infinite recursion.
  - produces *stack overflow* there's no room for more frames on the stack!
- Example: here's a version of our sum() method that uses a different test for the base case:

```
public static int sum(int n) {
    if (n == 0) {
        return 0;
    }
    int rest = sum(n - 1);
    return n + rest;
}
```

what values of n would cause infinite recursion?

# Designing a Recursive Method

- 1. Start by programming the base case(s).
  - What instance(s) of this problem can I solve directly (without looking at anything smaller)?
- 2. Find the recursive substructure.
  - How could I use the solution to any smaller version of the problem to solve the overall problem?
- 3. Solve the smaller problem using a recursive call!
  - store its result in a variable
- 4. Do your one step.
  - build your solution from the result of the recursive call
  - use concrete cases to figure out what you need to do

# Processing a String Recursively

- A string is a recursive data structure. It is either:
  - empty ("")
  - · a single character, followed by a string
- Thus, we can easily use recursion to process a string.
  - · process one or two of the characters ourselves
  - · make a recursive call to process the rest of the string
- Example: print a string vertically, one character per line:

```
public static void printVertical(String str) {
    if (str == null || str.equals("")) {
        return;
    }

    System.out.println(str.charAt(0)); // first char
    printVertical(str.substring(1)); // rest of string
}
```

#### **Short-Circuited Evaluation**

- The second operand of both the && and || operators
  will <u>not</u> be evaluated if the result can be determined on the
  basis of the first operand alone.
- expr1 || expr2 if expr1 evaluates to true, expr2 is not evaluated, because we already know that expr1 || expr2 is true
  - example from the last slide:

```
if (str == null || str.equals("")) {
    return;
}
// if str is null, we won't check for empty string.
// This prevents a null pointer exception!
```

expr1 && expr2

if expr1 evaluates to \_\_\_\_\_\_, expr2 is not evaluated, because we already know that expr1 && expr2 is \_\_\_\_\_\_.

# Counting Occurrences of a Character in a String

- numOccur(c, s) should return the number of times that the character c appears in the string s
  - numOccur('n', "banana") should return 2
  - numOccur('a', "banana") should return 3
- · Take the approach outlined earlier:
  - base case: empty string (or null)
  - delegate s.substring(1) to the recursive call
  - we're responsible for handling s.charAt(0)

# Applying the String-Processing Template

### **Determining Our One Step**

```
public static int numOccur(char c, String s) {
   if (s == null || s.equals("")) {
      return 0;
   } else {
      int rest = numOccur(c, s.substring(1));
      // do our one step!
```

- In our one step, we take care of s.charAt(0).
  - we build the solution to the larger problem on the solution to the smaller problem (in this case, rest)
  - does what we do depend on the value of s.charAt(0)?
- Use concrete cases to figure out the logic!

### Consider this concrete case...

```
public static int numOccur(char c, String s) {
   if (s == null || s.equals("")) {
      return 0;
   } else {
      int rest = numOccur(c, s.substring(1));
      // do our one step!
      ...
numOccur('r', "recurse")
```

```
numOccur('r', "recurse")
c = 'r', s = "recurse"
```

### **Consider Concrete Cases**

numOccur('r', "recurse") # first char is a match

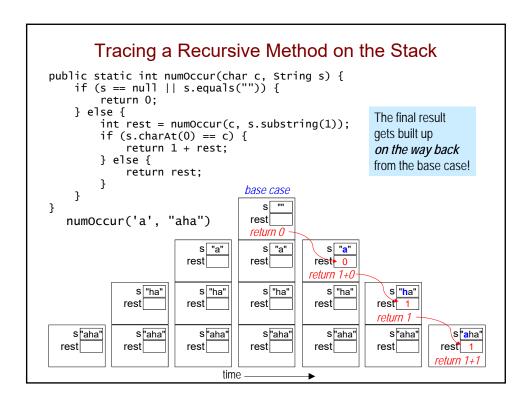
- · what is its solution?
- · what is the next smaller subproblem?
- · what is the solution to that subproblem?
- how can we use the solution to the subproblem?
   What is our one step?

numOccur('a', "banana") # first char is not a match

- · what is its solution?
- · what is the next smaller subproblem?
- · what is the solution to that subproblem?
- how can we use the solution to the subproblem?
   What is our one step?

### Now complete the method!

```
public static int numOccur(char c, String s) {
    if (s == null || s.equals("")) {
        return 0;
    } else {
        int rest = numOccur(c, s.substring(1));
        if (s.charAt(0) == c) {
            return _____;
        } else {
            return _____;
        }
}
```



### Common Mistake

• This version of the method does *not* work:

```
public static int numOccur(char c, String s) {
    if (s == null || s.equals("")) {
        return 0;
    }

    int count = 0;
    if (s.charAt(0) == c) {
        count++;
    }

    numOccur(c, s.substring(1));
    return count;
}
```

### **Another Faulty Approach**

• Some people make count "global" to fix the prior version:

```
public static int count = 0;
public static int numOccur(char c, String s) {
    if (s == null || s.equals("")) {
        return 0;
    }
    if (s.charAt(0) == c) {
        count++;
    }
    numOccur(c, s.substring(1));
    return count;
}
```

- · Not recommended, and not allowed on the problem sets!
- Problems with this approach?

#### Recursion vs. Iteration

- Some problems are much easier to solve using recursion.
- Other problems are just as easy to solve using iteration.
- Recursion is a bit more costly because of the overhead involved in invoking a method.
  - also: in some cases, there may not be room on the stack
- Rule of thumb:
  - if it's easier to formulate a solution recursively, use recursion, unless the cost of doing so is too high
  - otherwise, use iteration

### Extra Practice: A Recursive Palindrome Checker

- A *palindrome* is a string that reads the same forward and backward.
  - examples: "radar", "mom", "abcddcba"
- isPal(s) should return true if s is a palindrome, and false otherwise.
- · We need more than one base case. What are they?
- How should we reduce the problem in the recursive call?

### **Consider Concrete Cases!**

#### isPal("radar")

- · what is its solution?
- · what is the next smaller subproblem?
- · what is the solution to that subproblem?
- how can we use the solution to the subproblem...? What is our one step?

#### isPal("modem")

- · what is its solution?
- · what is the next smaller subproblem?
- · what is the solution to that subproblem?
- how can we use the solution to the subproblem...?
   What is our one step?

# A Recursive Palindrome Checker (cont.)

• Method definition (assuming no nulls):

```
public static boolean isPal(String s) {
    int len = s.length();
    if (len <= 1) {
        return _____;
    } else if (_______) {
        return _____;
    } else {
        boolean isPalRest = ______;
        // do our one step!
}</pre>
```