

Introduction to Recursion

"Recursion, n : see 'Recursion'"



What is recursion?

- Recursion is an approach to problem solving
 - It is typically used to solve problems that break down into smaller (simpler!) versions of themselves
 - Recursive methods are ones that call themselves



A bad example of recursion

- Sample code:

```
public class BadRecursion {
    public void doSomething() {
        System.out.println( "Hi there!" );
        doSomething();
    }
    static void main( String [] args ) {
        (new BadRecursion).doSomething();
    }
}
```
- What will this code do?

Steps for recursion

- There are 4 main steps in solving problems recursively:
 - 1) Define a test to decide if you should stop (or continue) recursing
 - 2) Define one or more end cases to terminate the recursion
 - 3) Define recursive call(s) that continue the function's recursion
 - 4) Identify any "error cases" that need to be handled.

A classic recursion example

- Consider the "factorial" function
 - $n! = n * (n-1) * (n-2) * \dots * 2 * 1$
 - $0! = 1$
- An example:
 - $5! = 5 * 4 * 3 * 2 * 1 = 120$

Designing factorial recursively

- Design decisions:
 - What is the base case for factorial?
 - Assume that "n" is not the base case, and fill in the blank with a recursive definition of n!
 $n! = \underline{\hspace{2cm}}$
 - What is the test going to be that decides when to stop recursing?
 - Are there any error cases to be handled?

Writing factorial recursively

- Fill in the code for the method:

```
public long factorial( int n )
{

}

}
```

Looking at factorial() running

- [Whiteboard outline of the execution process when we calculate "factorial(5)"]

Some possible problems

- What happens with a really big number?
- What happens if our test cases are wrong?

- Recursive problems can always be solved using an "iterative" approach (i.e., using loops)
- How would we write factorial() without recursion?
 - What problems does this solve?

- Fibonacci numbers
 - Basic formula:
 - $\text{Fib}(0) = 0$
 - $\text{Fib}(1) = 1$
 - $\text{Fib}(n) = \text{Fib}(n-1) + \text{Fib}(n-2)$
 - Example:
 - $$\begin{aligned} \text{Fib}(4) &= \text{Fib}(3) + \text{Fib}(2) \\ &= (\text{Fib}(2) + \text{Fib}(1)) + (\text{Fib}(1) + \text{Fib}(0)) \\ &= ((\text{Fib}(1) + \text{Fib}(0)) + \text{Fib}(1)) + (\text{Fib}(1) + \text{Fib}(0)) \\ &= ((1 + 0) + 1) + (1 + 0) \\ &= (1 + 1) + 1 \\ &= 2 + 1 \\ &= 3 \end{aligned}$$

- Write a recursive implementation of Fibonacci's algorithm.
- Write an iterative implementation.
- Which do you think is more efficient? (Why?)
 - Hint #1: Both implementations will be doing most of the same core *math* for the algorithm.
 - Hint #2: Think about what they do *differently*, and how "expensive" these operations may be....

- Binary searches can also be written recursively
- Finish the code on the next slide
 - The `binarySearch()` method is to be called by users
 - The `binarySearch2()` method does the work, and is recursive

```

public int binarySearch( int [] data, int value )
{
    return binarySearch2( data, 0, data.length, value );
}

private int binarySearch2(
    int [] data, int first,
    int numElements, int value )
{
    if ( numElements <= 0 )
        return NOT_FOUND;
    int middleIndex = (numElements / 2) + first;
    //
    // What happens next?
    //
}

```

- "Tail recursion" means that the last thing that a function does is call itself recursively.
 - Our implementation of factorial was not tail recursive, since it did a multiplication before returning
- Tail recursion usually allows the compiler to perform some optimizations on the code, improving its performance.
 - Tail-recursive functions are also the easiest to convert to iterative implementations



Tail recursive factorial

```
public long factorial( int n )
{
    return factorial( n, 1 );
}

private long factorial( int n, long total )
{
    if ( n < 0 )
        throw new IllegalArgumentException();
    if ( n == 0 || n == 1 )
        return total;
    else {
        total *= n;
        return factorial( n-1, total );
    }
}
```



Tail recursion details

- Tail recursion is often very easy to convert into an iterative (i.e., looping) solution
- It is usually very inefficient (compared to iterative solutions), and should be avoided whenever possible.



When to use recursion

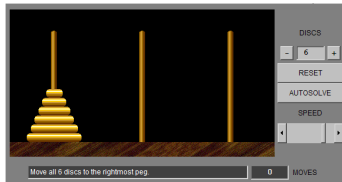
- You want to consider using recursion if:
 - A recursive approach is a natural and obvious solution to the problem, **and**
 - A recursive solution won't result in extra work, **and**
 - An iterative solution will be much more complicated than the recursive solution, **and**
 - The depth of the recursion won't be too great
- Given these criteria, was factorial() a good fit for a recursive approach?
 - Review the criteria, and defend your reasoning



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A good example of recursion

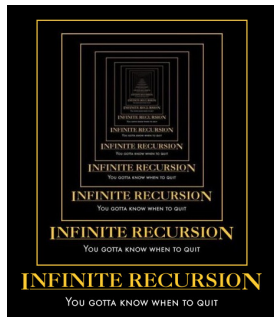
- The Towers of Hanoi
 - Example: <http://www.ypass.net/java/toh/>





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Another bad example of recursion





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Any Questions?
