

Definite Loops

Computer Science S-111
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Using a Variable for Counting

- Let's say that we're using a variable `i` to count the number of times that something has been done:

`int i = 0;` `i` 0

- To increase the count, we can do this:

`i = i + 1;`
0 + 1
↘ 1 `i` 1

- To increase the count again, we repeat the same assignment:

`i = i + 1;`
1 + 1
↘ 2 `i` 2

Increment and Decrement Operators

- Instead of writing
`i = i + 1;`
we can use a shortcut and just write
`i++;`
- `++` is known as the *increment operator*.
 - increment = increase by 1
- Java also provides a *decrement operator* (`--`).
 - decrement = decrease by 1
 - example:
`i--;`

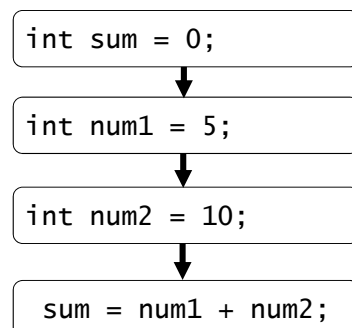
Review: Flow of Control

- Flow of control = the order in which instructions are executed
- By default, instructions are executed in sequential order.

instructions

```
int sum = 0;  
int num1 = 5;  
int num2 = 10;  
sum = num1 + num2;
```

flowchart



- When we make a method call, the flow of control "jumps" to the method, and it "jumps" back when the method completes.

Altering the Flow of Control: Repetition

- To solve many types of problems, we need to be able to modify the order in which instructions are executed.
- One reason for doing this is to allow for *repetition*.
- We saw this in Scratch:



Example of the Need for Repetition

- Here's a method for writing a large block letter L:

```
public static void writeL() {  
    System.out.println("|");  
    System.out.println("|");  
    System.out.println("|");  
    System.out.println("|");  
    System.out.println("|");  
    System.out.println("|");  
    System.out.println("|");  
    System.out.println("+-----");  
}
```

- Rather than duplicating the statement
 `System.out.println("|");`
seven times, we'd like to have this statement appear just once
and execute it seven times.

for Loops

- To repeat one or more statements multiple times, we can use a construct known as a *for loop*.
- Here's a revised version of our writeL method that uses one:

```
public static void writeL() {  
    for (int i = 0; i < 7; i++) {  
        System.out.println("|");  
    }  
    System.out.println("+-----");  
}
```

for Loops

- Syntax:

```
for (<initialization>; <continuation test>; <update>) {  
    <one or more statements>  
}
```

- In our example: *initialization* *continuation test*

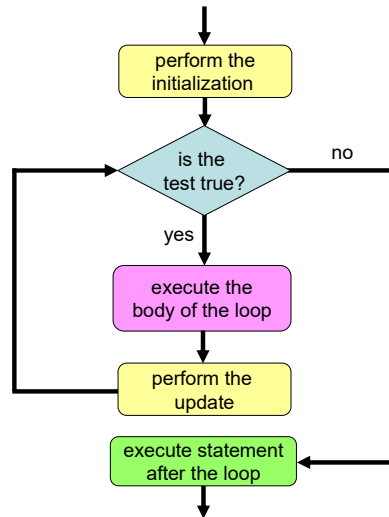
```
for (int i = 0; i < 7; i++) {  
    System.out.println("|");  
}
```

update

- The statements inside the loop are known as the *body* of the loop.
- In our example, we use the variable *i* to count the number of times that the body has been executed.

Executing a for Loop

```
for (<initialization>; <continuation test>; <update>) {  
    <body of the loop>  
}
```

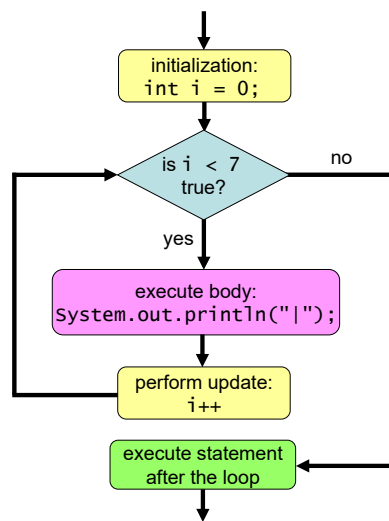


Notes:

- the initialization is only performed once
- the body is only executed if the test is true
- we repeatedly do:
 - test
 - body
 - updateuntil the test is false

Executing Our for Loop

```
for (int i = 0; i < 7; i++) {  
    System.out.println("|");  
}
```



i	i < 7	action
0	true	print 1 st " "
1	true	print 2 nd " "
2	true	print 3 rd " "
3	true	print 4 th " "
4	true	print 5 th " "
5	true	print 6 th " "
6	true	print 7 th " "
7	false	execute stmt. after the loop

Definite Loops

- For now, we'll limit ourselves to *definite loops* – which repeat actions a fixed number of times.
- To repeat the body of a loop **<N>** times, we typically take one of the following approaches:

```
for (int i = 0; i < <N>; i++) {  
    <body of the loop>  
}
```

OR

```
for (int i = 1; i <= <N>; i++) {  
    <body of the loop>  
}
```



- Each time that the body of a loop is executed is known as an *iteration* of the loop.
 - the loops shown above perform **<N>** iterations

Other Examples of Definite Loops

- What does this loop do?

```
for (int i = 0; i < 3; i++) {  
    System.out.println("Hip! Hip!");  
    System.out.println("Hooray!");  
}
```

- What does this loop do?

```
for (int i = 0; i < 10; i++) {  
    System.out.println(i);  
}
```

Using Different Initializations, Tests, and Updates

- The second loop from the previous page would be clearer if we expressed it like this:

```
for (int i = 0; i <= 9; i++) {  
    System.out.println(i);  
}
```

- Different problems may require different initializations, continuation tests, and updates.
- What does this code fragment do?

```
for (int i = 2; i <= 10; i = i + 2) {  
    System.out.println(i * 10);  
}
```

Tracing a for Loop

- Let's trace through the final code fragment from the last slide:

```
for (int i = 2; i <= 10; i = i + 2) {  
    System.out.println(i * 10);  
}
```

<u>i</u>	<u>i <= 10</u>	<u>value printed</u>
----------	-------------------	----------------------

Common Mistake

- You should not put a semi-colon after the for-loop header:

```
for (int i = 0; i < 7; i++); {  
    System.out.println("|");  
}
```

- The semi-colon ends the for statement.
 - thus, it doesn't repeat anything!
- The println is independent of the for statement, and only executes once.

Practice

- Fill in the blanks below to print the integers from 1 to 10:

```
for (_____; _____; _____) {  
    System.out.println(i);  
}
```

- Fill in the blanks below to print the integers from 10 to 20:

```
for (_____; _____; _____) {  
    System.out.println(i);  
}
```

- Fill in the blanks below to print the integers from 10 down to 1:

```
for (_____; _____; _____) {  
    System.out.println(i);  
}
```


Other Java Shortcuts

- Recall this code fragment:

```
for (int i = 2; i <= 10; i = i + 2) {  
    System.out.println(i * 10);  
}
```

- Instead of writing

```
i = i + 2;
```

we can use a shortcut and just write

```
i += 2;
```

- In general

```
<variable> += <expression>;
```

is equivalent to

```
<variable> = <variable> + (<expression>);
```

Java Shortcuts

- Java offers other shortcut operators as well.
- Here's a summary of all of them:

<u>shortcut</u>	<u>equivalent to</u>
<var> ++;	<var> = <var> + 1;
<var> --;	<var> = <var> - 1;
<var> += <expr>;	<var> = <var> + (<expr>);
<var> -= <expr>;	<var> = <var> - (<expr>);
<var> *= <expr>;	<var> = <var> * (<expr>);
<var> /= <expr>;	<var> = <var> / (<expr>);
<var> %= <expr>;	<var> = <var> % (<expr>);

- Important: the = must come *after* the mathematical operator.

+= is correct

=+ is not!

More Practice

- Fill in the blanks below to print the even integers in reverse order from 20 down to 6:

```
for (_____; _____; _____) {  
    System.out.println(i);  
}
```

Find the Error

- Let's say that we want to print the numbers from 1 to n.
- Where is the error in the following code?

```
for (int i = 1; i < n; i++) {  
    System.out.println(i);  
}
```
- This is an example of an *off-by-one error*. Beware of these when writing your loop conditions!

Example Problem: Printing a Pattern, version 1

- Ask the user for a positive integer (call it n), and print a pattern containing n asterisks.

- example:

```
Enter a positive integer: 3
***
```

- Let's use a `for` loop to do this:

```
// code to read n goes here...
for ( _____ ) {
    System.out.print("*");
}
System.out.println();
```

Example Problem: Printing a Pattern, version 2

- Print a pattern containing n lines of n asterisks.

- example:

```
Enter a positive integer: 3
***
***
***
```

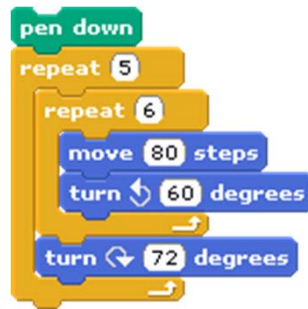
- One way to do this is to use a *nested loop* – one loop inside another:

```
// code to read in n goes here...
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        System.out.print("*");
    }
    System.out.println();
}
```

- This makes it easier to create a similar box of a different size.

Nested Loops

- When you have a nested loop, the inner loop is executed to completion for every iteration of the outer loop.
- Recall our Scratch drawing program:



- How many times is the *move* statement executed?

Nested Loops (cont.)

- How many times is the `println` statement executed below?

```
for (int i = 0; i < 5; i++) {  
    for (int j = 0; j < 7; j++) {  
        System.out.println(i + " " + j);  
    }  
}
```

- How many times is the `println` statement executed below?

```
for (int i = 0; i < 5; i++) {  
    for (int j = 0; j < i; j++) {  
        System.out.println(i + " " + j);  
    }  
}
```

Tracing a Nested for Loop

```
for (int i = 0; i < 5; i++) {  
    for (int j = 0; j < i; j++) {  
        System.out.println(i + " " + j);  
    }  
}
```

<u>i</u>	<u>i < 5</u>	<u>j</u>	<u>j < i</u>	<u>value printed</u>
----------	-----------------	----------	-----------------	----------------------

Recall: Variable Scope

- The *scope* of a variable is the portion of a program in which the variable can be used.
- By default, the scope of a variable in Java:
 - begins at the point at which it is declared
 - ends at the end of the innermost block that encloses the declaration

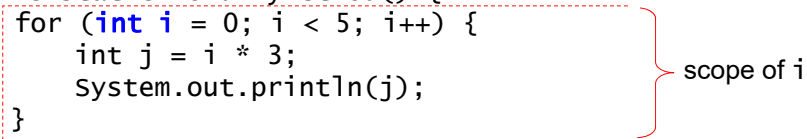
```
public class MyProgram2 {  
    public static void main(String[] args) {  
        System.out.println("welcome!");  
        System.out.println("Let's do some math!");  
        int j = 10;  
        System.out.println(j / 5);  
    }  
}
```

} scope of j

Special Case: for Loops and Variable Scope

- When a variable is declared in the initialization clause of a for loop, its scope is limited to the loop.
- Example:

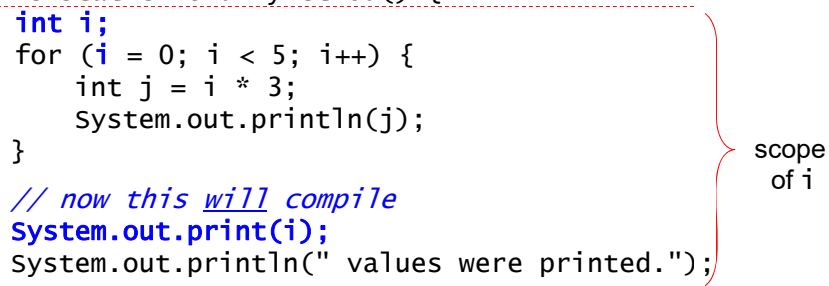
```
public static void myMethod() {  
    for (int i = 0; i < 5; i++) {  
        int j = i * 3;  
        System.out.println(j);  
    }  
    // the following line won't compile  
    System.out.print(i);  
    System.out.println(" values were printed.");  
}
```



Special Case: for Loops and Variable Scope (cont.)

- To allow *i* to be used outside the loop, we need to declare it outside the loop:
- Example:

```
public static void myMethod() {  
    int i;  
    for (i = 0; i < 5; i++) {  
        int j = i * 3;  
        System.out.println(j);  
    }  
    // now this will compile  
    System.out.print(i);  
    System.out.println(" values were printed.");  
}
```



Special Case: for Loops and Variable Scope (cont.)

- Limiting the scope of a loop variable allows us to use the standard loop templates multiple times in the same method.
- Example:

```
public static void myMethod() {  
    for (int i = 0; i < 5; i++) {  
        int j = i * 3;  
        System.out.println(j);  
    }  
    for (int i = 0; i < 7; i++) {  
        System.out.println("Go Crimson!");  
    }  
}
```

scope of first i

scope of second i

Review: Simple Repetition Loops

- Recall our two templates for performing **<N>** repetitions:

```
for (int i = 0; i < <N>; i++) {  
    // code to be repeated  
}
```

```
for (int i = 1; i <= <N>; i++) {  
    // code to be repeated  
}
```

- How many repetitions will each of the following perform?

```
for (int i = 1; i <= 15; i++) {  
    System.out.println("Hello");  
    System.out.println("How are you?");  
}  
  
for (int i = 0; i < 2*j; i++) {  
    ...  
}
```

More Practice: Tracing a Nested for Loop

```
for (int i = 1; i <= 3; i++) {
    for (int j = 0; j < 2*i + 1; j++) {
        System.out.print("*");
    }
    System.out.println();
}
```

i i <= 3 j j < 2*i + 1

output

Case Study: Drawing a Complex Figure

- Here's the figure:

[illegible]

- To begin with, we'll focus on creating this exact figure.
- Then we'll modify our code so that the size of the figure can easily be changed.
 - we'll use for loops to allow for this

Problem Decomposition

- We begin by breaking the problem into subproblems, looking for groups of lines that follow the same pattern:

```

      ( )
      ( ( ) )      ← flame
      ( ( ( ) ) )
      ( ( ( ( ) ) ) )

=====      ← rim of torch

| : : : : : |
| : : : : : |      ← top of torch

| : : |
| : : |
| : : |      ← handle of torch
| : : |

+ - - +      ← bottom of torch

```

Problem Decomposition (cont.)

- This gives us the following initial pseudocode:

```

      ( )      draw the flame
      ( ( ) )  draw the rim of the torch
      ( ( ( ) ) ) draw the top of the torch
      ( ( ( ( ) ) ) ) draw the handle of the torch
                  draw the bottom of the torch

```

```
=====
```

```
| : : : : : |
| : : : : : |
```

```
| : : |
| : : |
| : : |
| : : |
```

```
+ - - +
```

- This is a high-level description of what needs to be done.
- We'll gradually expand the pseudocode into more and more detailed instructions – until we're able to implement them in Java.

Drawing the Flame

- Let's begin by refining our specification for drawing the flame.

()
(())
((()))
(((())))
- Here's our initial pseudocode for this task:

```
for (each of 4 lines) {  
    print some spaces (possibly 0)  
    print some left parentheses  
    print some right parentheses  
    go to a new line  
}
```
- We need formulas for how many spaces and parens should be printed on a given line.

Finding the Formulas

- To begin with, we:

1 ()
2 (())
3 ((()))
4 (((())))

 - number the lines in the flame
 - form a table of the number of spaces and parentheses on each line:

<u>line</u>	<u>spaces</u>	<u>parens (each type)</u>
1	3	1
2	2	2
3	1	3
4	0	4

- Then we find the formulas.
 - assume the formulas are *linear functions* of the line number:
$$c1 * line + c2$$

where $c1$ and $c2$ are constants
 - parens = ?
 - spaces = ?

Refining the Pseudocode

- Given these formulas, we can refine our pseudocode:

```
for (each of 4 lines) {  
    print some spaces (possibly 0)  
    print some left parentheses  
    print some right parentheses  
    go to a new line  
}
```



```
for (line going from 1 to 4) {  
    print 4 - line spaces  
    print line left parentheses  
    print line right parentheses  
    go to a new line  
}
```

Implementing the Pseudocode in Java

- We use nested for loops:

```
for (line going from 1 to 4) {  
    print 4 - line spaces  
    print line left parentheses  
    print line right parentheses  
    go to a new line  
}
```



```
for (int line = 1; line <= 4; line++) {  
    for (int i = 0; i < 4 - line; i++) {  
        System.out.print(" ");  
    }  
    for (int i = 0; i < line; i++) {  
        System.out.print("(");  
    }  
    for (int i = 0; i < line; i++) {  
        System.out.print(")");  
    }  
    System.out.println();  
}
```

A Method for Drawing the Flame

- We put the code in its own static method, and add some explanatory comments:

```
public static void drawFlame() {
    for (int line = 1; line <= 4; line++) {
        // spaces to the left of the current line
        for (int i = 0; i < 4 - line; i++) {
            System.out.print(" ");
        }

        // left and right parens on the current line
        for (int i = 0; i < line; i++) {
            System.out.print("(");
        }
        for (int i = 0; i < line; i++) {
            System.out.print(")");
        }

        System.out.println();
    }
}
```

Drawing the Top of the Torch

- What's the initial pseudocode for this task?

```
for (each of 2 lines) {
```

```
1 | ::::: |
2 | ::::: |
```

```
}
```

- Here's a table for the number of spaces and number of colons:

<u>line</u>	<u>spaces</u>	<u>colons</u>
1	0	6
2	1	4

- spaces = ?
- colons decreases by 2 as line increases by 1
 $\rightarrow \text{colons} = -2 * \text{line} + c2$ for some number $c2$
- try different values, and eventually get: colons = ?

Refining the Pseudocode

- Once again, we use the formulas to refine our pseudocode:

```
for (each of 2 lines) {  
    print some spaces (possibly 0)  
    print a single vertical bar  
    print some colons  
    print a single vertical bar  
    go to a new line  
}
```



```
for (line going from 1 to 2) {  
    print line - 1 spaces  
    print a single vertical bar  
    print -2*line + 8 colons  
    print a single vertical bar  
    go to a new line  
}
```

A Method for Drawing the Top of the Torch

```
public static void drawTop() {  
    for (int line = 1; line <= 2; line++) {  
        // spaces to the left of the current line  
        for (int i = 0; i < line - 1; i++) {  
            System.out.print(" ");  
        }  
  
        // bars and colons on the current line  
        System.out.print("|");  
        for (int i = 0; i < -2*line + 8; i++) {  
            System.out.print(":");  
        }  
        System.out.print("|");  
        System.out.println();  
    }  
}
```

Drawing the Rim

- This always has only one line, so we *don't* need *nested* loops. =====
- However, we still need a single loop, because we want to be able to scale the size of the figure.
- What should the code look like?

```
for (          ;          ;          ) {  
  
    }  
}
```

- This code also goes in its own method, called `drawRim()`

Incremental Development

- We take similar steps to implement methods for the remaining subtasks.
- After completing a given method, we test and debug it.
- The main method just calls the methods for the subtasks:

```
public static void main(String[] args) {  
    drawFlame();  
    drawRim();  
    drawTop();  
    drawHandle();  
    drawBottom();  
}
```

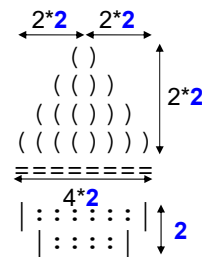
- See the example program `DrawTorch.java`

Using Class Constants

- To make the torch larger or smaller, we'd need to make many changes.
 - the size of the figure is hard-coded into most methods
- To make the program more flexible, we can store info. about the figure's dimensions in one or more *class constants*.
 - like variables, but their values are fixed
 - can be used throughout the program

Using Class Constants (cont.)

- We only need one constant for the torch.
 - for the default size, it equals 2
 - its connection to some of the dimensions is shown at right



- We declare it at the very start of the class:

```
public class DrawTorch2 {  
    public static final int SCALE_FACTOR = 2;  
    ...  
}
```

- General syntax:

```
public static final <type> <name> = <expression>;
```

- conventions:
 - capitalize all letters in the name
 - put an underscore ('_') between multiple words

Scaling the Figure

- Here are some other versions of the figure:

Diagram illustrating a structure with 10 levels of parentheses (roof) and 10 vertical lines (columns) below it, representing a 10-story building.

SCALE_FACTOR = 3

$$\begin{array}{ccccccc} & & (&) & & & \\ & (& (&) &) & & \\ = & = & = & = & & & \\ | & : & : & | & & & \\ & | & | & & & & \\ & + & + & & & & \end{array}$$

SCALE_FACTOR = 1

Revised Method for Drawing the Flame

- We replace the two 4s with 2*SCALE_FACTOR:

```
public static void drawFlame() {
    for (int line = 1; line <= 2*SCALE_FACTOR; line++) {
        // spaces to the left of the flame
        for (int i = 0; i < 2*SCALE_FACTOR - line; i++) {
            System.out.print(" ");
        }

        // the flame itself, both left and right halves
        for (int i = 0; i < line; i++) {
            System.out.print("(");
        }
        for (int i = 0; i < line; i++) {
            System.out.print(")");
        }

        System.out.println();
    }
}
```

2×2
 $()$
 $(())$
 $((()))$
 $(((())))$
 2×2

Diagram illustrating the recursive structure of the $2^n \times 2^n$ matrix A_n . The matrix is divided into four quadrants, each of size $2^{n-1} \times 2^{n-1}$. The top-left and top-right quadrants are labeled 2×2 . The bottom-left quadrant contains a recursive structure of parentheses, and the bottom-right quadrant is labeled 2×2 . A vertical double-headed arrow on the right indicates the height of the matrix is 2^n .

Making the Rim Scaleable

- How does the width of the rim depend on SCALE_FACTOR?

```

      ( )          ( )          ( )
     ( ( )        ( ( )        ( ( )
    ( ( ( )      ( ( ( )      =====
   ( ( ( ( )    ( ( ( ( )
  ( ( ( ( ( )  ( ( ( ( ( )
 ( ( ( ( ( ( ) ( ( ( ( ( ( )
( ( ( ( ( ( ( ) ( ( ( ( ( ( ( )
=====
  
```

- Use a table!

<u>SCALE_FACTOR</u>	<u>width of rim</u>
1	4
2	8
3	12

width of rim = ?

Revised Method for Drawing the Rim

- Original version (for the default size):

```

public static void drawRim() {
    for (int i = 0; i < 8; i++) {
        System.out.print("=");
    }
    System.out.println();
}
  
```

- Scaleable version:

```

public static void drawRim() {
    for (int i = 0; i < 4*SCALE_FACTOR; i++) {
        System.out.print("=");
    }
    System.out.println();
}
  
```

Making the Top of the Torch Scaleable

- For SCALE_FACTOR = 2, we got:

number of lines = 2
spaces = line - 1
colons = -2 * line + 8

```

1 | : : : : : |
2 | : : : : |

```

- What about SCALE_FACTOR = 3?

line	spaces	colons
1	0	10
2	1	8
3	2	6

```

1 | : : : : : : : |
2 | : : : : : : |
3 | : : : : : |

```

number of lines = 3
spaces = ?
colons = ?

- in general, number of lines = ?

Making the Top of the Torch Scaleable (cont.)

- Compare the two sets of formulas:

SCALE_FACTOR = 2
spaces = line - 1
colons = -2 * line + 8

SCALE_FACTOR = 3
spaces = line - 1
colons = -2 * line + 12

- There's no change in:
 - the formula for spaces
 - the first constant in the formula for colons

- Use a table for the second constant:

SCALE_FACTOR	constant
2	8
3	12

constant = ?

- Scaleable formulas: spaces = line - 1
colons = ?

Revised Method for Drawing the Top of the Torch

```
public static void drawTop() {
    for (int line = 1; line <= SCALE_FACTOR; line++) {
        // spaces to the left of the current line
        for (int i = 0; i < line - 1; i++) {
            System.out.print(" ");
        }

        // bars and colons on the current line
        System.out.print("|");
        for (int i = 0; i < -2*line + 4*SCALE_FACTOR; i++) {
            System.out.print(":");
        }
        System.out.print("|");
        System.out.println();
    }
}
```

Practice: The Torch Handle

- Pseudocode for default size:

```

      ( )
      ( ( ) )
      ( ( ( ) ) )
      ( ( ( ( ) ) ) )
      =====
      | : : : : : |
      | : : : : : |
1    | : : : : : |
2    | : : : : : |
3    | : : : : : |
4    | : : : : : |
      +==+
```

- Java code for default size:

```
public static void drawHandle() {
```

```
}
```

Practice: Making the Handle Scaleable

- We again compare two different sizes.

<u>SCALE_FACTOR</u>	<u># lines</u>	<u>spaces</u>	<u>colons</u>
2	4	2	2
3	6	3	4

```

| : : : : : |
| : : : : |
1
2
3
4
| : : : : |

```

- number of lines = ?
spaces = ?
colons = ?

```

| : : : : : : : |
| : : : : : : |
| : : : : : |
1
2
3
4
5
6
| : : : : |

```

Revised Method for Drawing the Handle

- What changes do we need to make?

```

public static void drawHandle() {
    for (int line = 1; line <= 4; line++) {
        for (int i = 0; i < 2; i++) {
            System.out.print(" ");
        }
        System.out.print("|");
        for (int i = 0; i < 2; i++) {
            System.out.print(":");
        }
        System.out.println("|");
    }
}

```

Extra Practice: Printing a Pattern, version 3

- Print a triangular pattern with lines containing n , $n - 1$, ..., 1 asterisks.

- example:

Enter a positive integer: 3

**

*

- How would we use a nested loop to do this?

```
for ( _____ ) {  
    for ( _____ ) {  
        System.out.print("*");  
    }  
    System.out.println();  
}
```