

Probability Methods in Engineering CSE-209

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Lecture 4





Counting Methods

- Counting methods for determination of probability
 - Experiments with finite sample spaces
 - Equiprobable outcomes
- > Probability of an event is the ratio of:
 - □ Number of outcomes in the event of interest
 - ☐ Total number of outcomes in the sample space





Counting Methods (Cont.)

- > Sampling with replacement
 - With ordering
 - Without ordering
- > Sampling without replacement
 - With ordering
 - Without ordering





Counting Methods (Cont.)

- > Sampling with replacement with ordering
 - \square k draws from n objects
 - Number of distinct ordered k-tuples = n^k
- > Sampling without replacement with ordering
 - \square k draws from n objects
 - Number of distinct ordered k-tuples = n(n-1) ... (n-k+1)





Sampling with replacement with ordering

An urn contains five balls numbered 1 to 5. Suppose we select two balls from the urn with replacement. How many distinct ordered pairs are possible? What is the probability that the two draws yield the same number?





Sampling without replacement with ordering

An urn contains five balls numbered 1 to 5. Suppose we select two balls in succession without replacement. How many distinct ordered pairs are possible? What is the probability that the first ball has a number larger than that of the second ball?





Sampling with replacement with ordering

An urn contains five balls numbered 1, 2, ..., 5. Suppose we draw three balls with replacement. What is the probability that all three balls are different?





Permutations

- > Arrangement of things
- Sampling without replacement with ordering
 - □ E.g. form a number of 3 digits from 1, 2, 3, 4
- > Number of all possible permutations

$$\stackrel{n}{P} = \frac{n!}{(n-k)!} = n(n-1)...(n-k+1)$$

- ightharpoonup If all objects are drawn, (n = k)
 - \square Number of all possible permutations is n factorial or n!





Combinations

- Selection of things
- Sampling without replacement and without ordering
 E. g. make a team of 5 players from a total of 9
- > Record the result without considering the order
- \triangleright k objects are drawn and termed as a combination
- \triangleright Number of combinations for n objects and k draws

Also called "n choose k"



- Find the number of permutations of three distinct objects {1, 2, 3} while
 - Drawing all objects
 - Drawing 2 objects
- Also find the number of combinations of three distinct objects {1, 2, 3} while
 - Drawing all objects
 - □ Drawing 2 objects





> Suppose that 4 balls are placed at random into 4 cells, where more than 1 ball is allowed to occupy a cell. What is the probability that all cells are occupied?

