

## Assignment 5, PME, 4<sup>th</sup> Semester, Spring

*Deadline:* Before the final exam paper of PME

*Assignment should be hand written.*

*Write your name, registration No. and section; else your assignment may not be marked.*

*Copying is not allowed.*

*Properly staple your pages (binding is not required).*

1. Let  $X$  be the number of heads obtained when a fair coin is flipped four times.
  - a. Plot the cdf of  $X$ .
  - b. Use properties of cdf to find  $P[2 < X \leq 3]$ ,  $P[0.7 \leq X \leq 1.3]$  and  $P[1 \leq X < 3]$ .
2. An urn contains nine Rs. 10 notes and one Rs. 50 note. Let the random variable  $X$  be the total amount that results when two notes are drawn from the urn without replacement.
  - a. Plot the cdf of  $X$ .
  - b. Use properties of cdf to find  $P[20 \leq X < 60]$ .
3. Let  $X$  be a random variable with pmf  $p_k = 0.6/k^2$  for  $k = 1, 2, 3, \dots$ . Plot the cdf of  $X$  for  $k = 0$  to 4. Use the properties of cdf to find
  - a.  $P[X > 4]$ .
  - b.  $P[6 \leq X \leq 8]$ .
4. The transmission time  $X$  of messages in a communication system has an exponential distribution. If  $\lambda = 1$ , find
  - a.  $P[X > 3]$ .
  - b.  $P[2 \leq X \leq 4]$ .
5. Let  $Y$  be the difference between the number of heads and the number of tails in the 3 tosses of a fair coin.
  - a. Plot the cdf of  $Y$ .
  - b. Determine the mean and variance of  $Y$ .
6.  $S_C = \{1, 2, 3, 4\}$  where  $C$  is a uniform random variable having four possible values of electric current. If  $W$  is a random variable and represents the corresponding power values such that  $W = 3C^2$ . Plot the cdf of  $C$  and  $W$ .