Data Structures and Algorithms

2.2 Outline

This topic will describe:

- The concrete data structures that can be used to store information.
- The basic forms of memory allocation
 - Contiguous
 - Linked
 - Indexed
- The prototypical examples of these: arrays and linked lists
- Other data structures:
 - Trees
 - Hybrids
 - Higher-dimensional arrays
- Finally, we will discuss the run-time of queries and operations on arrays and linked lists

2.2.1

Memory Allocation

Memory allocation can be classified as either

- Contiguous
- Linked
- Indexed

Prototypical examples:

Contiguous allocation: arrays

Linked allocation: linked lists

Memory Allocation

Contiguous, adj.

Touching or connected throughout in an unbroken sequence.

Meriam Webster

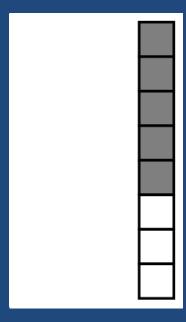
Touching, in actual contact, next in space; meeting at a common boundary, bordering, adjoining.

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2.2.1.1 Contiguous Allocation

An array stores n objects in a single contiguous space of memory Unfortunately, if more memory is required, a request for new memory usually requires copying all information into the new memory

 In general, you cannot request for the operating system to allocate to you the next n memory locations



Linked Allocation

Linked storage such as a linked list associates two pieces of data with each item being stored:

- The object itself, and
- A reference to the next item
 - In C++ that reference is the address of the next node



Linked Allocation

This is a class describing such a node

```
template <typename Type>
class Node {
    private:
        Type element;
        Node *next_node;
    public:
        // ...
};
```

Linked Allocation

The operations on this node must include:

- Constructing a new node
- Accessing (retrieving) the value
- Accessing the next pointer

```
Node( const Type& = Type(), Node* = nullptr );
Type retrieve() const;
Node *next() const;
```

Linked Allocation

For a linked list, however, we also require an object which links to the first object

The actual linked list class must store two pointers

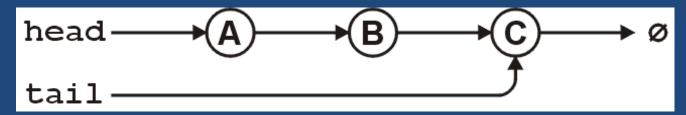
– A head and tail:

Node *head;
Node *tail;

Optionally, we can also keep a count

int count;

The next_node of the last node is assigned nullptr



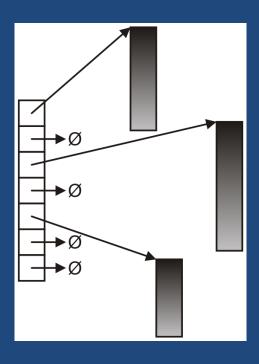
Linked Allocation

The class structure would be:

```
template <typename Type>
class List {
    private:
        Node<Type> *head;
        Node<Type> *tail;
        int count;
    public:
        // constructor(s)...
        // accessor(s)...
        // mutator(s)...
};
```

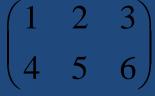
Indexed Allocation

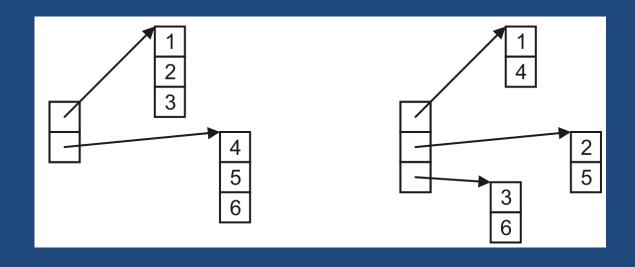
With indexed allocation, an array of pointers (possibly NULL) link to a sequence of allocated memory locations



Indexed Allocation

Matrices can be implemented using indexed allocation:

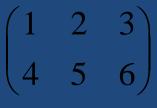


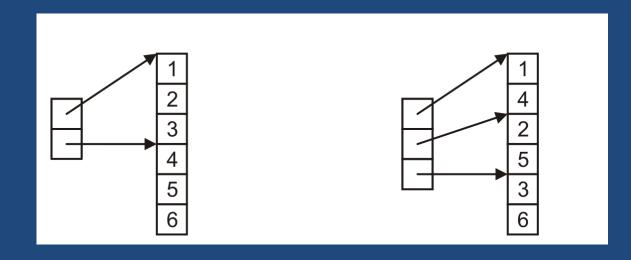


Indexed Allocation

Matrices can be implemented using indexed allocation

 Most implementations of matrices (or higher-dimensional arrays) use indices pointing into a single contiguous block of memory





2.2.2

Other Allocation Formats

We will look at some variations or hybrids of these memory allocations including:

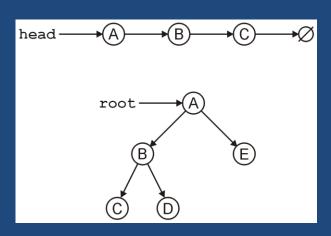
- Trees
- Graphs
- Deques (linked arrays)
- inodes

2.2.2.2 Trees

The linked list can be used to store linearly ordered data

– What if we have multiple next pointers?

A rooted tree is similar to a linked list but with multiple next pointers



Trees

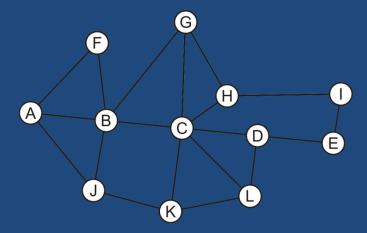
A tree is a variation on a linked list:

- Each node points to an arbitrary number of subsequent nodes
- Useful for storing hierarchical data
- We will see that it is also useful for storing sorted data
- Usually we will restrict ourselves to trees where each node points to at most two other nodes

Graphs

Suppose we allow arbitrary relations between any two objects in a container

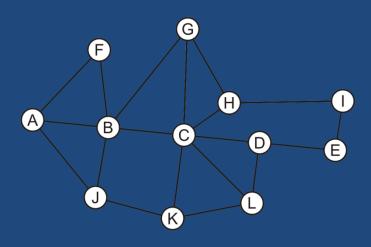
- Given n objects, there are $n^2 n$ possible relations
 - If we allow symmetry, this reduces to $\frac{n^2 n}{2}$
- For example, consider the network

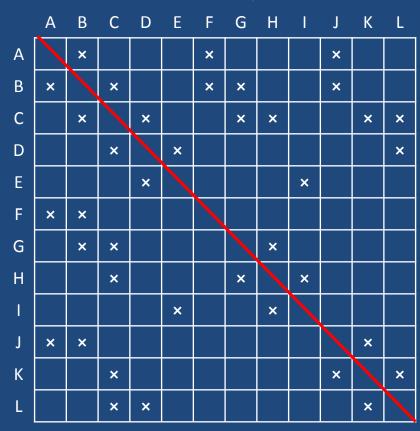


Arrays

Suppose we allow arbitrary relations between any two objects in a container

- We could represent this using a two-dimensional array
- In this case, the matrix is symmetric

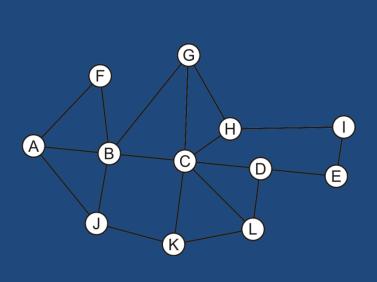


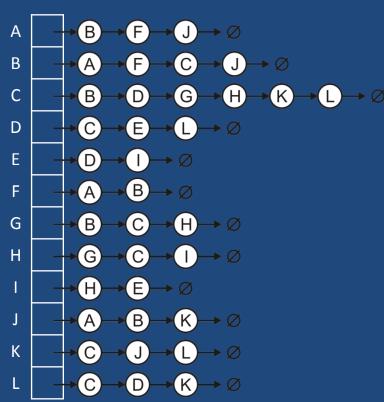


Array of Linked Lists

Suppose we allow arbitrary relations between any two objects in a container

Alternatively, we could use a hybrid: an array of linked lists



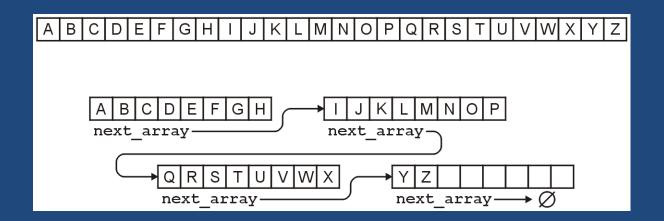


Linked Arrays

Other hybrids are linked lists of arrays

For example, the alphabet could be stored either as:

- An array of 26 entries, or
- A linked list of arrays of 8 entries



2.2.3

Algorithm run times

Once we have chosen a data structure to store both the objects and the relationships, we must implement the queries or operations as algorithms

- The Abstract Data Type will be implemented as a class
- The data structure will be defined by the member variables
- The member functions will implement the algorithms

The question is, how do we determine the efficiency of the algorithms?

2.2.3

Operations

We will us the following matrix to describe operations at the locations within the structure

	Front/1st	Arbitrary Location	Back/n th
Find	?	?	?
Insert	?	?	?
Erase	?	?	?

Operations on Sorted Lists

Given an sorted array, we have the following run times:

	Front/1st	Arbitrary Location	Back/n th
Find	Good	Okay	Good
Insert	Bad		Good* Bad
Erase	Bad		Good

^{*} only if the array is not full

Operations on Lists

If the array is not sorted, only one operations changes:

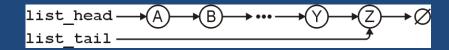
	Front/1st	Arbitrary Location	Back/n th
Find	Good	Bad	Good
Insert	Bad	Bad	Good* Bad
Erase	Bad		Good

^{*} only if the array is not full

Operations on Lists

However, for a singly linked list where we a head and tail pointer, we have:

	Front/1 st	Arbitrary Location	Back/n th
Find	Good		Good
Insert	Good		Good
Erase	Good		



Operations on Lists

If we have a pointer to the k^{th} entry, we can insert or erase at that location quite easily

	Front/1st	Arbitrary Location	Back/n th
Find	Good	Bad	Good
Insert	Good	Good	Good
Erase	Good	Good	Bad
	list_head → A → A	$\mathbb{B} \longrightarrow \cdots \longrightarrow \mathbb{Y} \longrightarrow \mathbb{Z} \longrightarrow \mathbb{Z}$	

Operations on Lists

For a doubly linked list, one operation becomes more efficient:

	Front/1st	Arbitrary Location	Back/n th
Find	Good		Good
Insert	Good	Good	Good
Erase	Good	Good	Good

