

1. Design a modulo-6 counter, which counts 0,1,2,3,4,5,0,1,..... The counter counts the clock pulses if its enable input, w, is equal to 1. Use D flip flops in your circuit. If the circuit ever finds itself in an unused state (6 or 7), it should transition to state 0 with the next clock trigger to avoid being stuck in an unused state. Use a formal design procedure.

Drawing the state table for the given modulo 6 counter.

Present state			Input	Next state		
Q2	Q1	Q0	W	Q2+	Q1+	Q0+
0	0	0	0	0	0	0
0	0	0	1	0	0	1
0	0	1	0	0	0	1
0	0	1	1	0	1	0
0	1	0	0	0	1	0
0	1	0	1	0	1	1
0	1	1	0	0	1	1
0	1	1	1	1	0	0
1	0	0	0	1	0	0
1	0	0	1	1	0	1
1	0	1	0	1	0	1
1	0	1	1	0	0	0
1	1	0	0	0	0	0
1	1	0	1	0	0	0
1	1	1	0	0	0	0
1	1	1	1	0	0	0

For D flip-flops, the input into the flip-flops is the same as the next state that are shown in the table. ($D_2=Q_{2+}$, $D_1 = Q_{1+}$, $D_0 = Q_{0+}$).

Now drawing 4-variable K maps for D flip flop inputs D_2 , D_1 and D_0 we get the following result (K-maps not shown):

$$D_2 = Q_2Q_1'Q_0' + Q_2Q_1'W' + Q_2'Q_1Q_0W$$

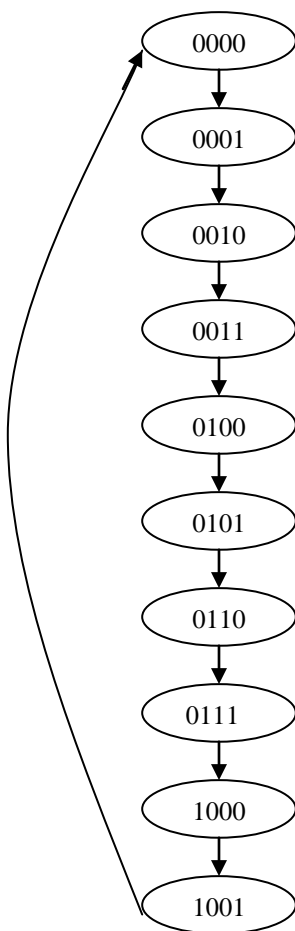
$$D_1 = Q_2'Q_1Q_0' + Q_2'Q_1W' + Q_2'Q_1'Q_0W$$

$$D_0 = Q_2'Q_0'W + Q_1'Q_0'W + Q_2'Q_0W' + Q_1'Q_0W'$$

The above equations completely define the required circuit.

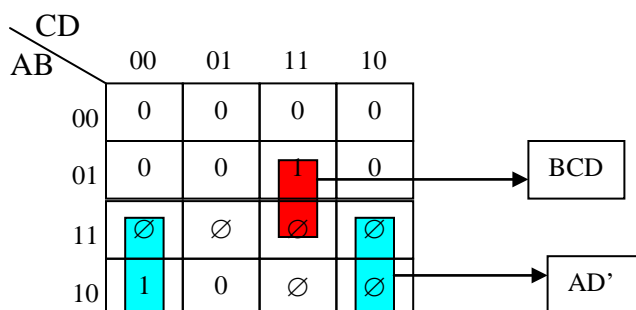
2. Consider the design of a 4-bit BCD counter that counts in the following way: 0000, 0001, 0010, 0011, ..., 1001 and back to 0000.

A) Draw the state diagram and next state table.

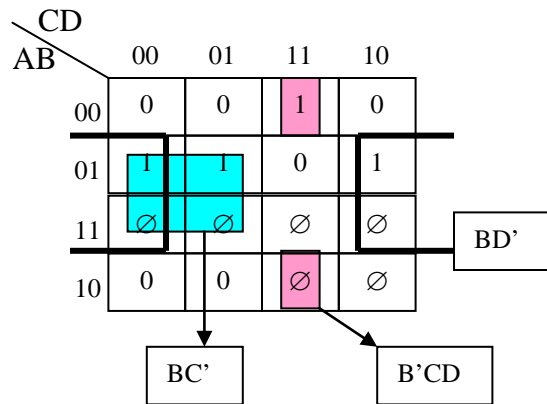


Present Stage				Next Stage				D Flip Flop Input			
A	B	C	D	A+	B+	C+	D+	Da	Db	Dc	Dd
0	0	0	0	0	0	0	1	0	0	0	1
0	0	0	1	0	0	1	0	0	0	1	0
0	0	1	0	0	0	1	1	0	0	1	1
0	0	1	1	0	1	0	0	0	1	0	0
0	1	0	0	0	1	0	1	0	1	0	1
0	1	0	1	0	1	1	0	0	1	1	0
0	1	1	0	0	1	1	1	0	1	1	1
0	1	1	1	1	0	0	0	1	0	0	0
1	0	0	0	1	0	0	1	1	0	0	1
1	0	0	1	0	0	0	0	0	0	0	0

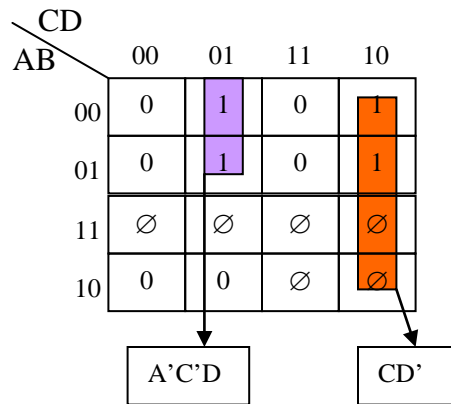
B) Implement the counter using D flip-flops.



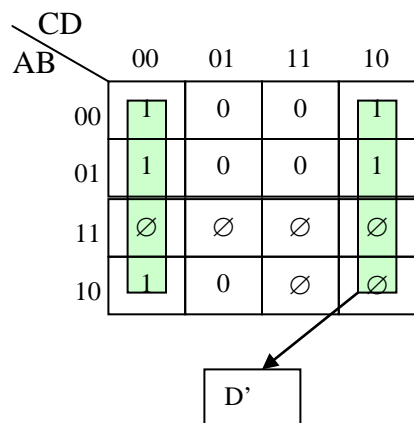
$$Da = AD' + BCD$$



$$D_b = BC' + B'CD + BD'$$



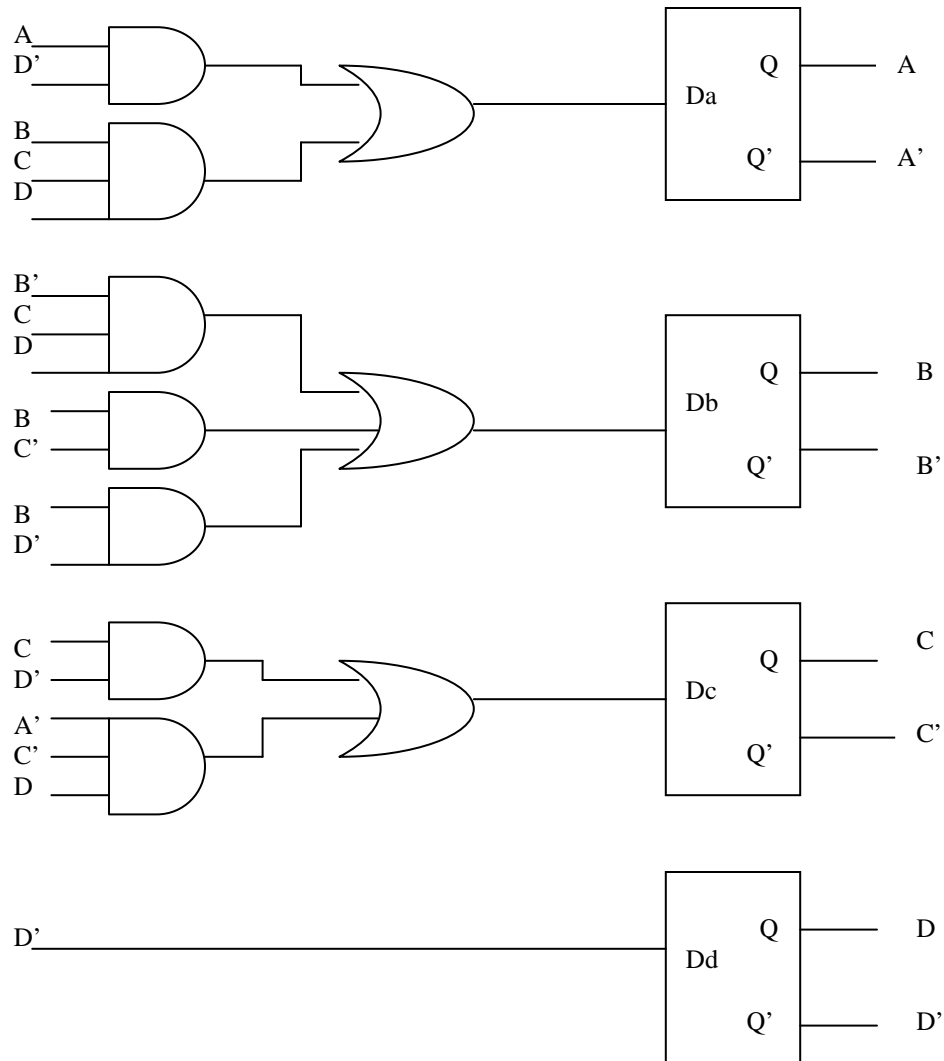
$$D_c = CD' + A'C'D$$



$$D_d = D'$$

Note that ∅s represent don't cares.

Logic circuit



3. The 4-bit Johnson counter advances thru the sequence: 0000, 1000, 1100, 1110, 1111, 0111, 0011, 0001 and repeat.

A) Implement this counter using D flip-flops.

Present Stage				Next Stage				D Flip Flop Input			
A	B	C	D	A+	B+	C+	D+	Da	Db	Dc	Dd
0	0	0	0	1	0	0	0	1	0	0	0
1	0	0	0	1	1	0	0	1	1	0	0
1	1	0	0	1	1	1	0	1	1	1	0
1	1	1	0	1	1	1	1	1	1	1	1
1	1	1	1	0	1	1	1	0	1	1	1
0	1	1	1	0	0	1	1	0	0	1	1
0	0	1	1	0	0	0	1	0	0	0	1
0	0	0	1	0	0	0	0	0	0	0	0

CD \ AB		00	01	11	10
AB \ CD	00	1	0	0	\emptyset
	01	\emptyset	\emptyset	0	\emptyset
	11	1	\emptyset	0	1
	10	1	\emptyset	\emptyset	\emptyset

$$D_a = D'$$

CD \ AB		00	01	11	10
AB \ CD	00	0	0	0	\emptyset
	01	\emptyset	\emptyset	0	\emptyset
	11	1	\emptyset	1	1
	10	1	\emptyset	\emptyset	\emptyset

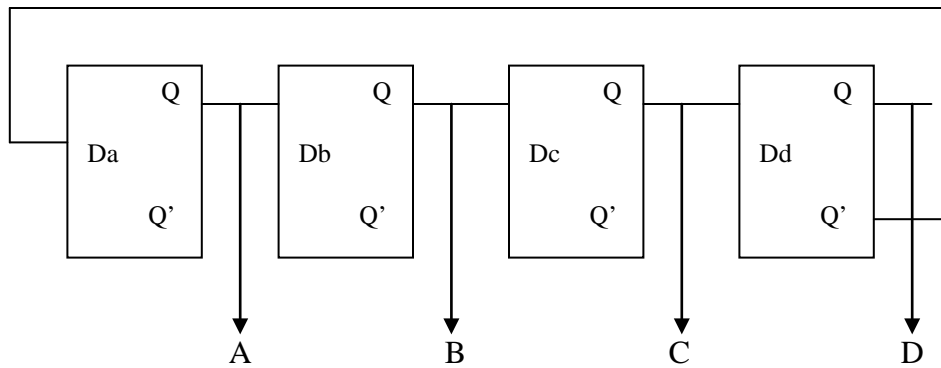
$$D_b = A$$

CD \ AB		00	01	11	10
AB \ CD	00	0	0	0	\emptyset
	01	\emptyset	\emptyset	1	\emptyset
	11	1	\emptyset	1	1
	10	0	\emptyset	\emptyset	\emptyset

$$D_c = B$$

CD \ AB		00	01	11	10
AB \ CD	00	0	0	1	\emptyset
	01	\emptyset	\emptyset	1	\emptyset
	11	0	\emptyset	1	1
	10	0	\emptyset	\emptyset	\emptyset

$$D_d = C$$



B) Implement this counter using T flip-flops.

Present Stage				Next Stage				T Flip Flop Input			
A	B	C	D	A+	B+	C+	D+	Ta	Tb	Tc	Td
0	0	0	0	1	0	0	0	1	0	0	0
1	0	0	0	1	1	0	0	0	1	0	0
1	1	0	0	1	1	1	0	0	0	1	0
1	1	1	0	1	1	1	1	0	0	0	1
1	1	1	1	0	1	1	1	1	0	0	0
0	1	1	1	0	0	1	1	0	1	0	0
0	0	1	1	0	0	0	1	0	0	1	0
0	0	0	1	0	0	0	0	0	0	0	1

CD \ AB	CD			
	00	01	11	10
00	1	0	0	∅
01	∅	∅	0	∅
11	0	∅	1	0
10	0	∅	∅	∅

$$T_a = A'D' + AD$$

CD \ AB	CD			
	00	01	11	10
00	0	0	0	∅
01	∅	∅	1	∅
11	0	∅	0	0
10	1	∅	∅	∅

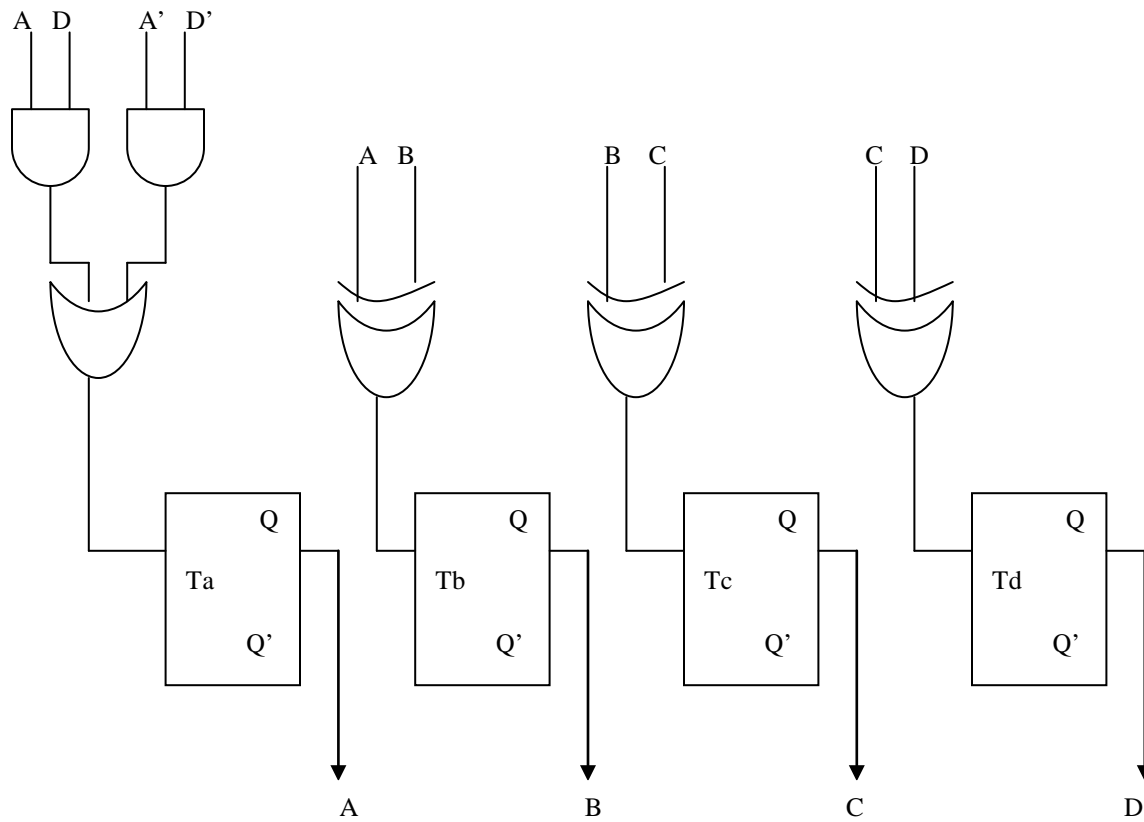
$$T_b = A'B + AB'$$

CD \ AB	CD			
	00	01	11	10
00	0	0	0	∅
01	∅	∅	1	∅
11	1	∅	1	1
10	0	∅	∅	∅

$$T_c = BC' + B'C$$

CD \ AB	CD			
	00	01	11	10
00	0	0	1	∅
01	∅	∅	1	∅
11	0	∅	1	1
10	0	∅	∅	∅

$$T_d = C'D + CD'$$

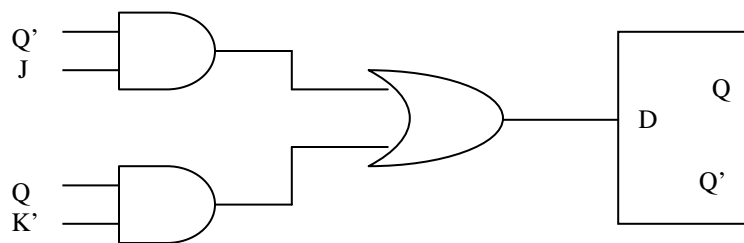


4. Show how to implement a JK flip-flop with a D flip-flop.

J	K	Q	Q+	D
0	0	0	0	0
0	0	1	1	1
0	1	0	0	0
0	1	1	0	0
1	0	0	1	1
1	0	1	1	1
1	1	0	1	1
1	1	1	0	0

		JK			
Q		00	01	11	10
	0	0	0	1	1
	1	1	0	0	1

$$D = Q'J + QK'$$

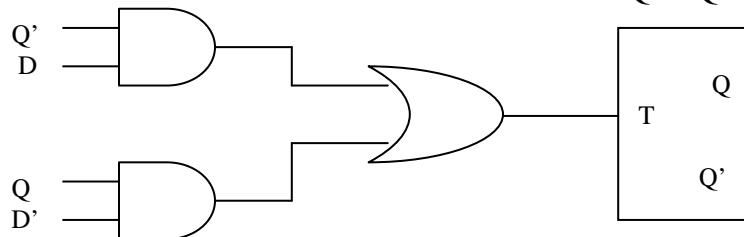


5. Show how to implement a D flip-flop with a T flip-flop.

D	Q	Q+	T
0	0	0	0
0	1	0	1
1	0	1	1
1	1	1	0

		D	
Q		0	1
	0	0	1
	1	1	0

$$T = DQ' + QD'$$



6. Show how to implement a JK flip-flop with a T flip-flop.

J	K	Q	Q+	D
0	0	0	0	0
0	0	1	1	1
0	1	0	0	0
0	1	1	0	0
1	0	0	1	1
1	0	1	1	1
1	1	0	1	1
1	1	1	0	0

		JK			
		00	01	11	10
Q	0	0	0	1	1
	1	0	1	1	0

$$T = Q'J + QK$$

