Topics of last week

Control Systems - 7th Semester - Week 4 Step Response of Systems

Dr. Salman Ahmed f

Two Domain

Model - Recalling concepts

A model is representation or abstraction of reality/system.

Who invent model? We, human beings, invent model based on our knowledge.

 $\frac{d^2}{dt} = 0x + 84$ 4 = (n + by)Sfordoræl

What is mathematical model?

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We find

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In last weeks, we studied about obtaining state-space ential equations

Then we studied about converting state-space model to tran using formula

We also studied on converting transfer function to state-space model using

Model - Recalling concepts

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Types of Model

Model - Recalling concepts

A model is representation or abstraction of reality/system.

Who invent model? We, human beings, invent model based on our knowledge.

This means the more knowledge a person has, the better he/she can write a model

What is mathematical model? A set of equations (linear or differential) that describes the relationship between input and output of a system.

There are three types of mathematical models

- Black Box
- Grey Box
- White Box

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Introduction to Transient Analysis

Sometimes we cannot write white box models for the systems

Either we do NOT know what is inside the system or either the system is too complex to verify the components

Perhaps sometimes the components are not easily identifiable and their configuration or layout is not readable

So another way to obtain model of a system is to apply a test input signal and obtain the output signal

Standard Input Signals

Though there are many possible combinations of input signals, the following are famous or popular input signals

- Impulse Signal
- Step Signal
- Ramp Signal
- · Parabolic Signal



Model - Recalling concepts

Transient Analysis

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Step Signal

The step signal is used to imitate the sudden change of a signal

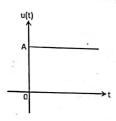


Figure: Step Signal

$$u(t) = \begin{cases} A & \text{if } t \ge 0 \\ 0 & \text{if } t < 0 \end{cases}$$

If A=1, the step signal is called unit step signal

Step Response

Impulse response is the best response because transfer function is defined as impulse response of a system

However, in practical life generating impulse signal is not easy

We use unit step signal as test input signal and then analyze the $\ensuremath{\mathsf{output}}$ of the system

Topic

Model - Recuting concepts

Transiert Analysis

Model - Recalling concepts

Tramient Analysis

First Order System

A first order system has a single pole (irrespective of number of zeros).

Many systems are of first order. Examples include

- velocity of a car on road
- control of angular velocity of rotating systems
- · an RLC circuit with only one capacitor and no inductor
- an RLC circuit with only one inductor and no capacitor
- · fluid flow in a pipeline
- · level control in a tank
- · pressure control in a gas cylinder

First Order System - Examples

Examples of first order system from computing system domain:

- speed control of dc motor in hard disk system
- time taken by queries in database management system, e.g. SELECT * from STUDENT where ATTENDANCE_PERCENTAGE > 75;
- time taken to read a temperature sensor interfaced with an embedded system
- energy consumed by an IoT device
- control of

in networks e.g. CSMA/CA

time taken by PS4 or Xbox one device to boot



Step Response of First Order System

general first order system without zeros can be written as follows:

$$G(s) = \frac{b}{s+a}$$

Let C(s) be the output of a system having transfer function G(s) (expressed above). If the input to G(s) is a unit step, then the output can be expressed as follows:

Output Signal = Input Signal × Transfer function

We can further write the following:

Honds - Recalling concepts

$$C(s) =$$
Unit step signal $\times G(s)$

$$C(s) = \frac{1}{s} \times \frac{b}{s+a} = \frac{b}{s(s+a)}$$

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Step Response of First Order System

The term a is an important term. The inverse of a is called time constant

$$\tau = \frac{1}{a}$$

where au is called time-constant of first order systems. For example compute au of the following system:

$$G(s) = \frac{3}{s+2}$$

Here $au=rac{1}{2}=0.5$ and gain K is computed as $rac{3}{2}=1.5$

The value of gain K indicates the final steady-state value of the step response



Step Response of First Order System

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Step Response of First Order System

Rise Time: T_r , time taken to reach 90% or 0.9 of final value from 10% or 0.1. Mathematically:

$$T_r = \frac{2.2}{a}$$

Settling Time: T_s , time taken to stay within 2% of its final value (or reach 98% of final value). Mathematically:

$$T_s = \frac{4}{a}$$

function from the previous plot.

Step Response of First Order System

Time constant: Time to reach 63% of final value. Compute the transfer

Step Response of First Order System

Can you compute the transfer function?

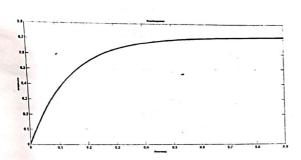


Figure: Step Response of a transfer function

Model - Recalling concepts

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Transient Analysis

Step Response of First Order System

Time constant: Time to reach 63% of final value. Compute the transfer function from the previous plot.

Final value = steady-state value = gain K=0.72 63% of final value is $0.63\times0.72=0.4464$ Time taken to reach 0.45 value is 0.15 seconds The final transfer function is

$$G(s) = \frac{\frac{0.72}{0.15}}{s + \frac{1}{0.15}}$$

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Pole is inverse of time constant which comes out to be $\frac{1}{0.15}=6.67$

Another way of writing the transfer function is

$$G(s) = \frac{4.802}{s + 6.67}$$

Topics .

Step Response of First Order System

The previous step-response was obtained for the following actual transfer function:

$$G(s) = \frac{5}{s+7}$$

MATLAB code for obtaining step response

step(num,den)



Step Response of First Order System

Effects of increasing gains (remember its K not the term b)

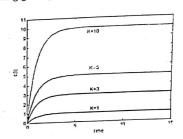


Figure: Effects of increasing gains of first order transfer function

Step Response of First Order System Effects of decreasing time constant

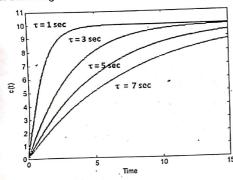


Figure: Effects of decreasing time constants of first order transfer function

Step Response of First Order System

Question: NADRA manages the registration database of Pakistani citizens. Previously, till 2001 people had 11 digit NIC numbers. Each citizen of Pakistan is issued a 13 digit CNIC number. The first 5 digits in a CNIC are based on a citizen locality, the next 7 numbers are random, and the final last digit is gender based (even for females, and odd for males). The current database entries in NADRA are estimated as 90 million. If a person details are required and his/her CNIC is entered in the NADRA database, its take 1 min to search 98% of the records in a NADRA database. Assuming the query search process to be a first-order system, find the time constant.

