



Module 3, Day 2

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Goal

- Perform **linear regression** in its most basic form through simplest example
 - Predict house price with just single feature, i.e., house size

Machine Learning Purpose

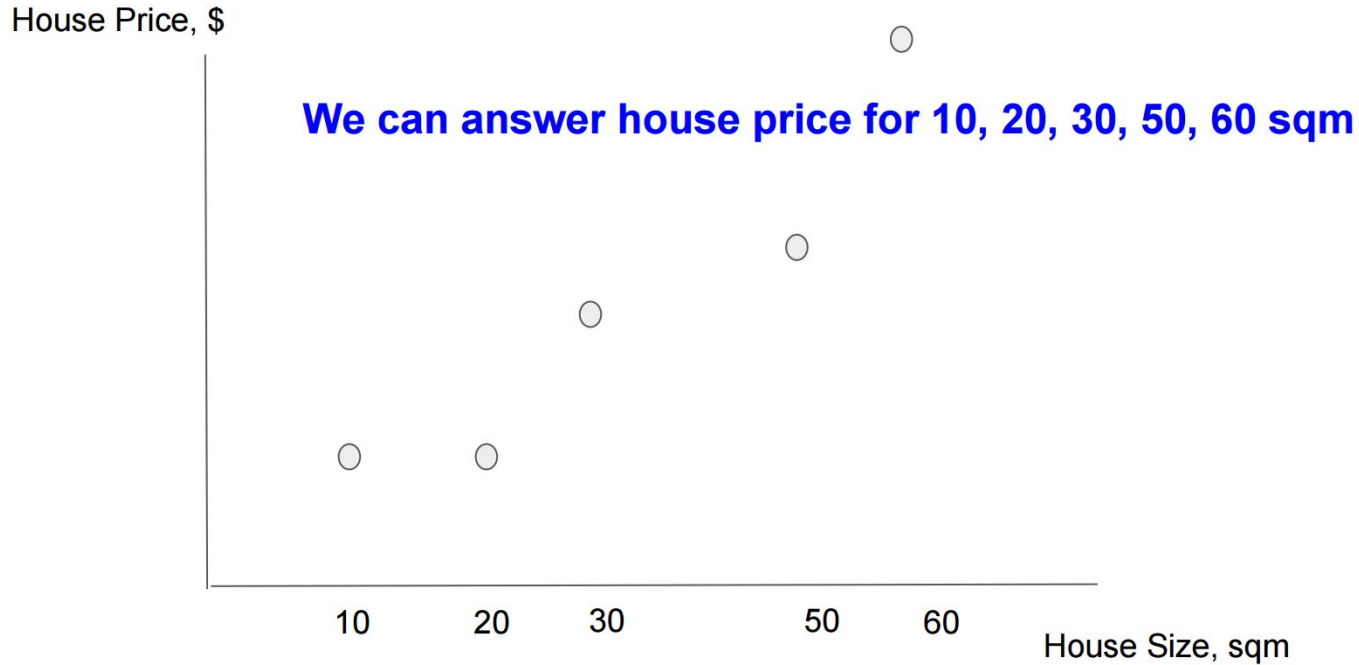
- **Predict** something given a set of **features** that influences prediction:
 - Predict house price given its size, location, configuration (features)

Machine Learning Training

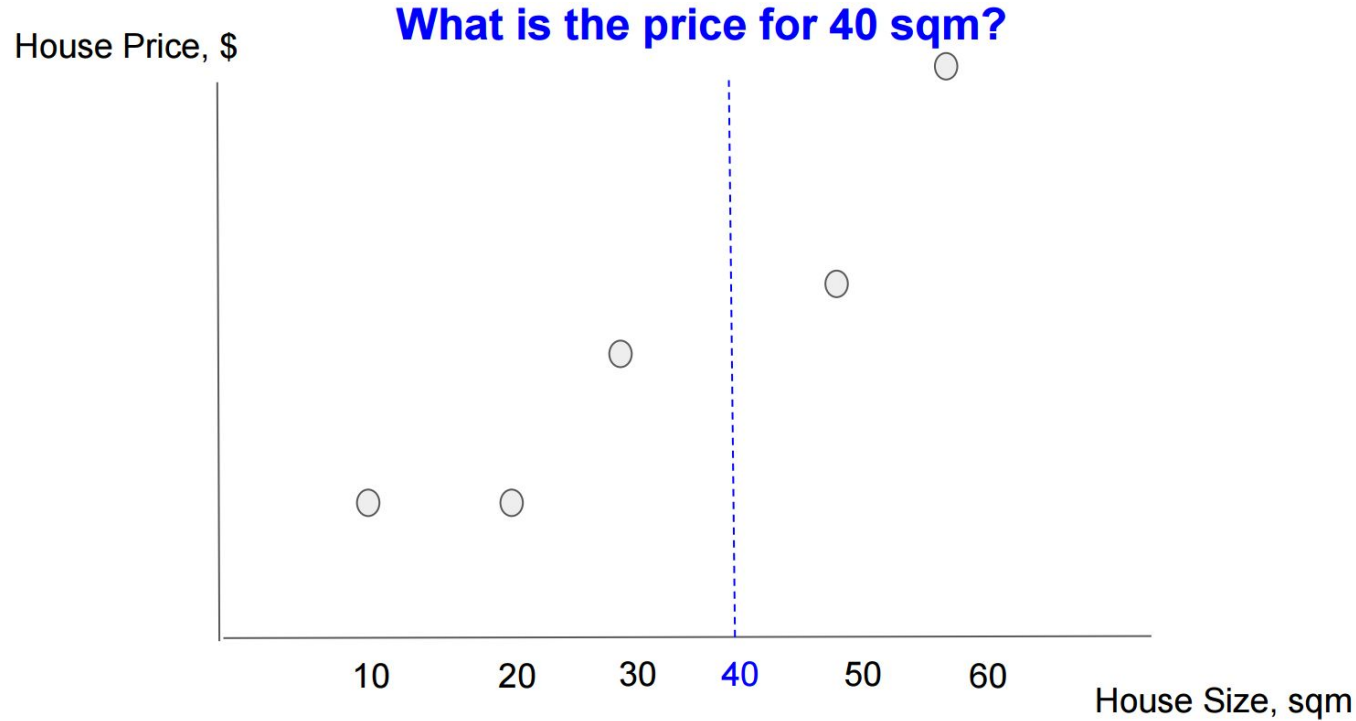
Before predicting, we have to:

- Choose/Create a **model**
- **Train** the model to learn prediction with **data**

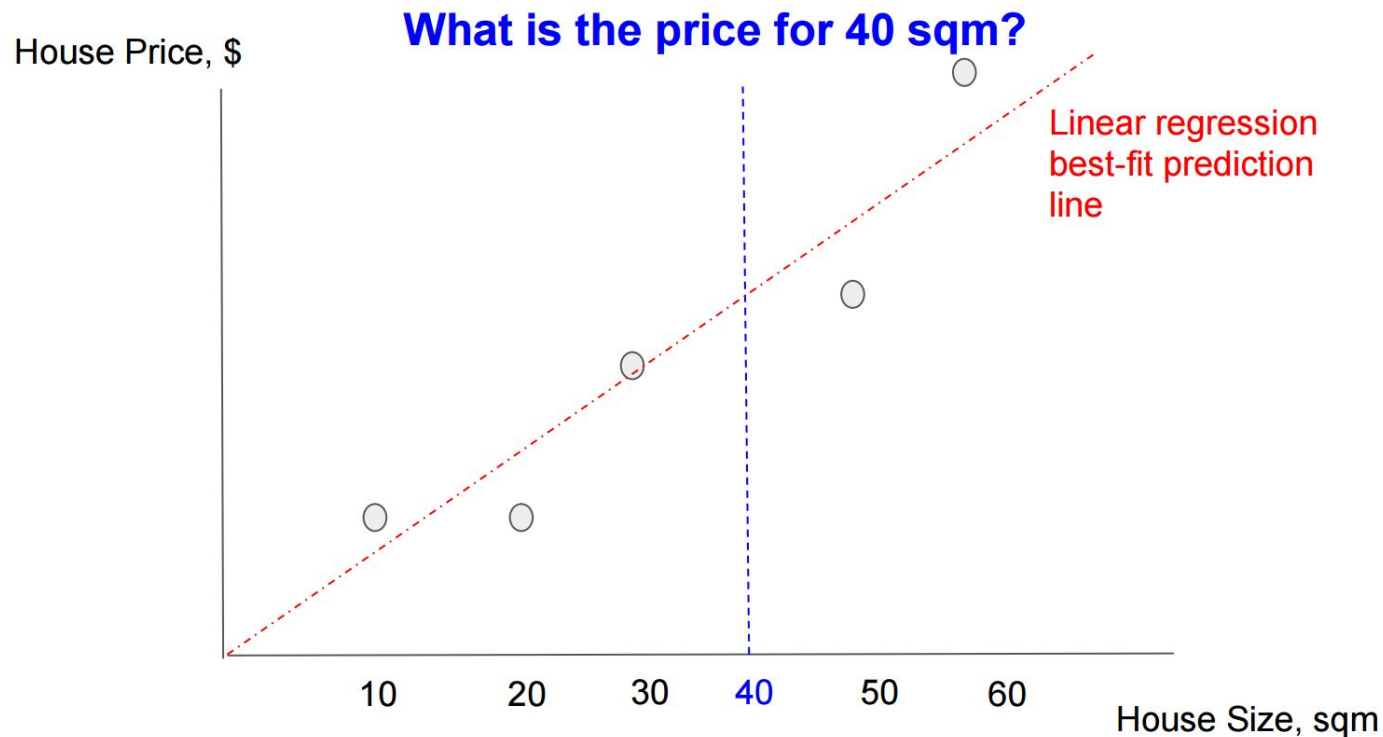
What is the House Price?



What is the House Price?



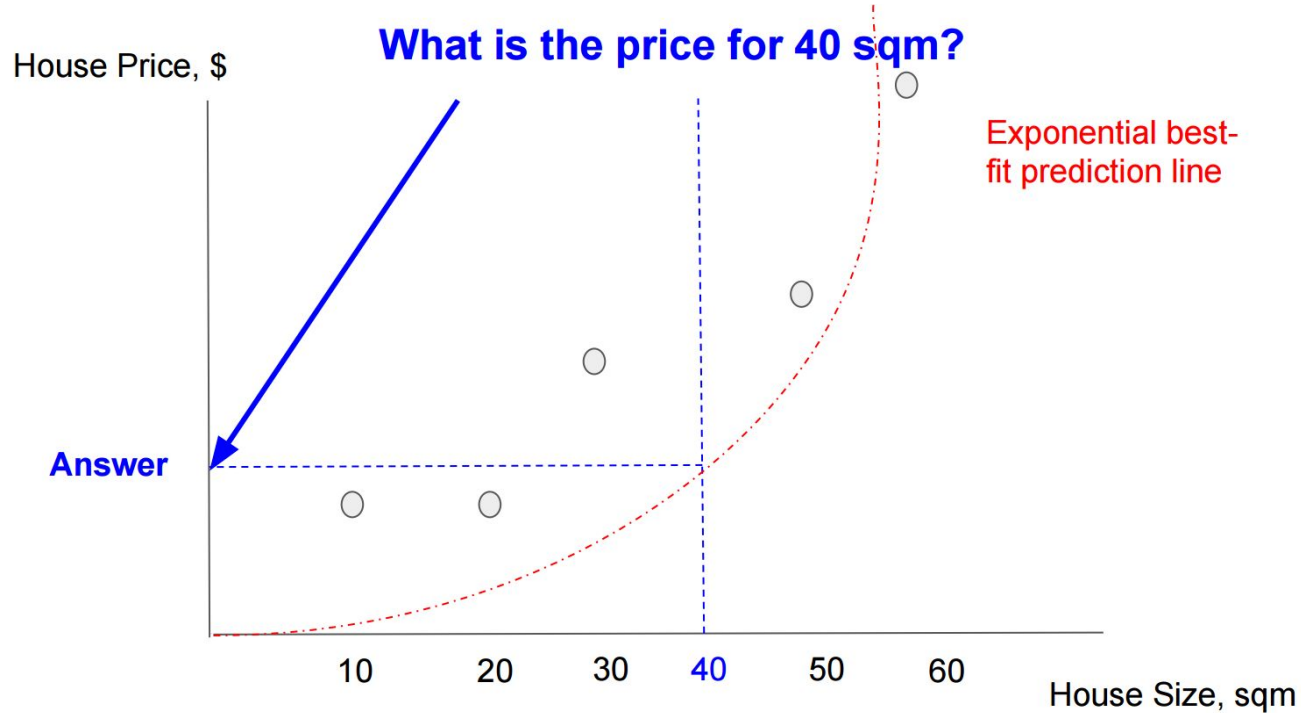
What is the House Price?



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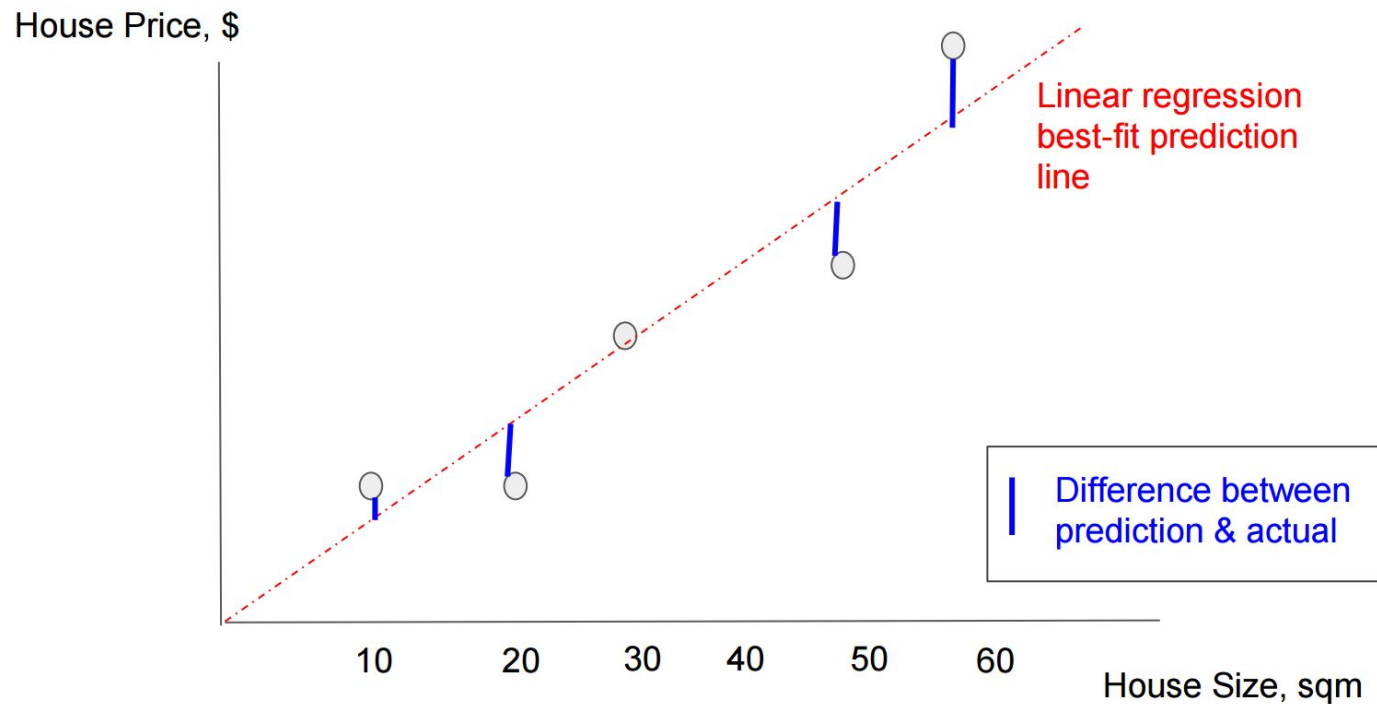
Cost Function: Best-fit Prediction

Minimize difference between predicted
& actual values

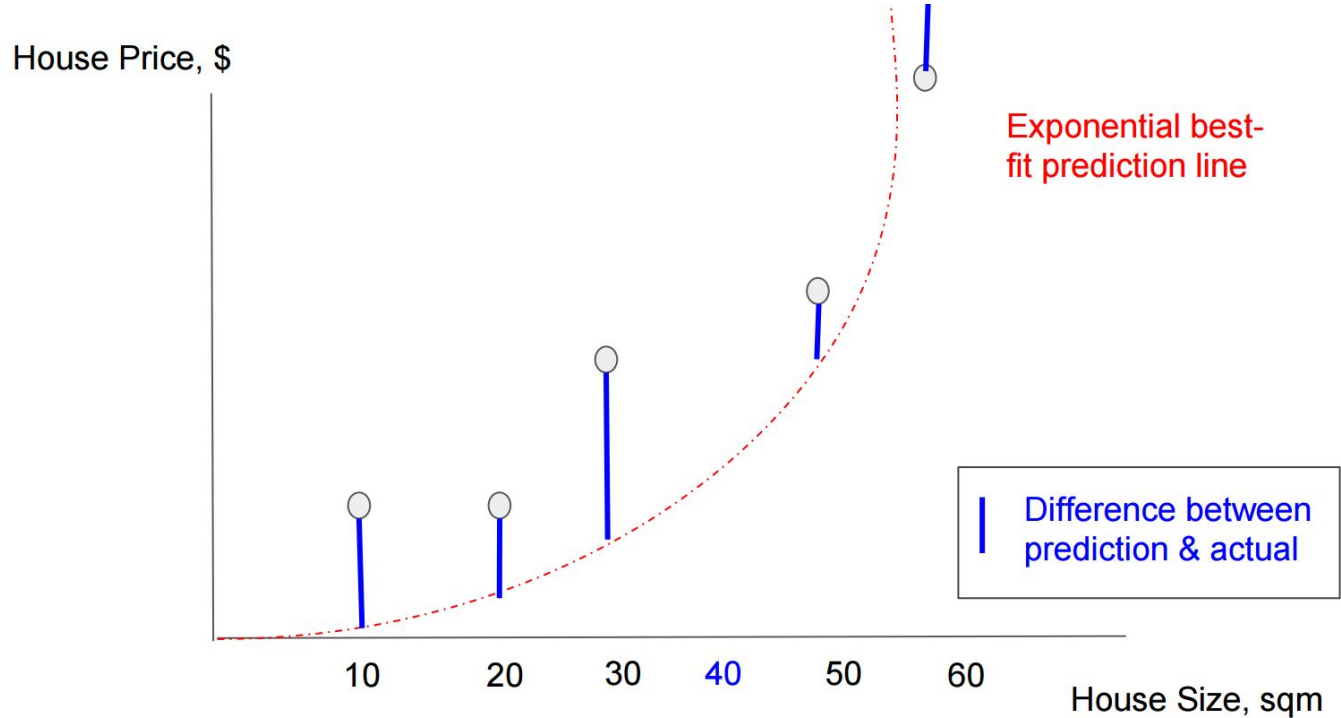


MLDS

What is the House Price?



What is the House Price?



Cost function: How different is your model from reality

$$\text{sum}((y_ - y)^{**2})$$

Where:

$y_$: Actual value

y : Predicted value

$**2$: Power of 2

Linear Regression

$$\mathbf{y} = \mathbf{W}.\mathbf{x} + \mathbf{b}$$

y: Predicted house price

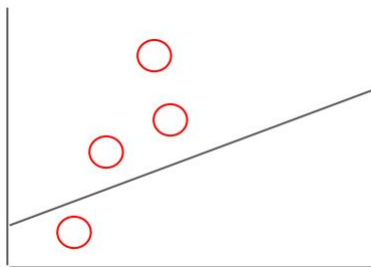
x: House size from dataset

Find a good W, b

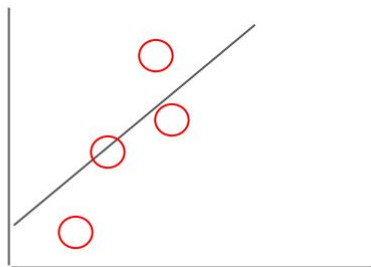
W: Gradient (Steepness)

$$W1 < W2 < W3$$

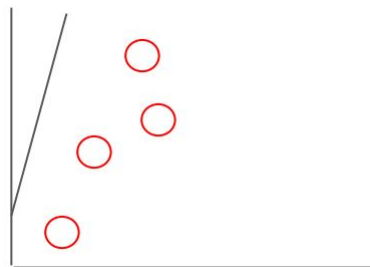
$$y = W1.x + b$$



$$y = W2.x + b$$



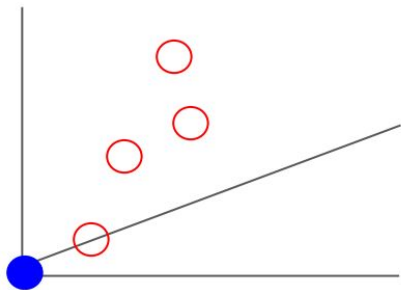
$$y = W3.x + b$$



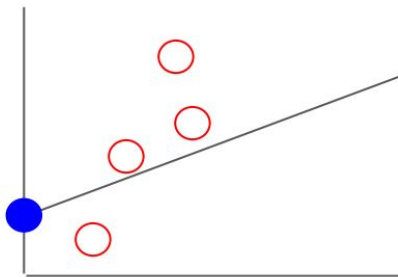
b: Intersect

$$b_1 < b_2 < b_3$$

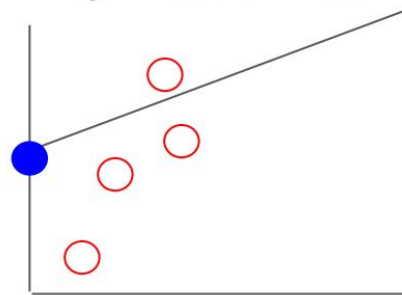
$$y = W.x + b_1$$



$$y = W.x + b_2$$



$$y = W.x + b_3$$



Train: Find W , b

$W_{\text{best}}, b_{\text{best}} = 0, 0$

Loop J times:

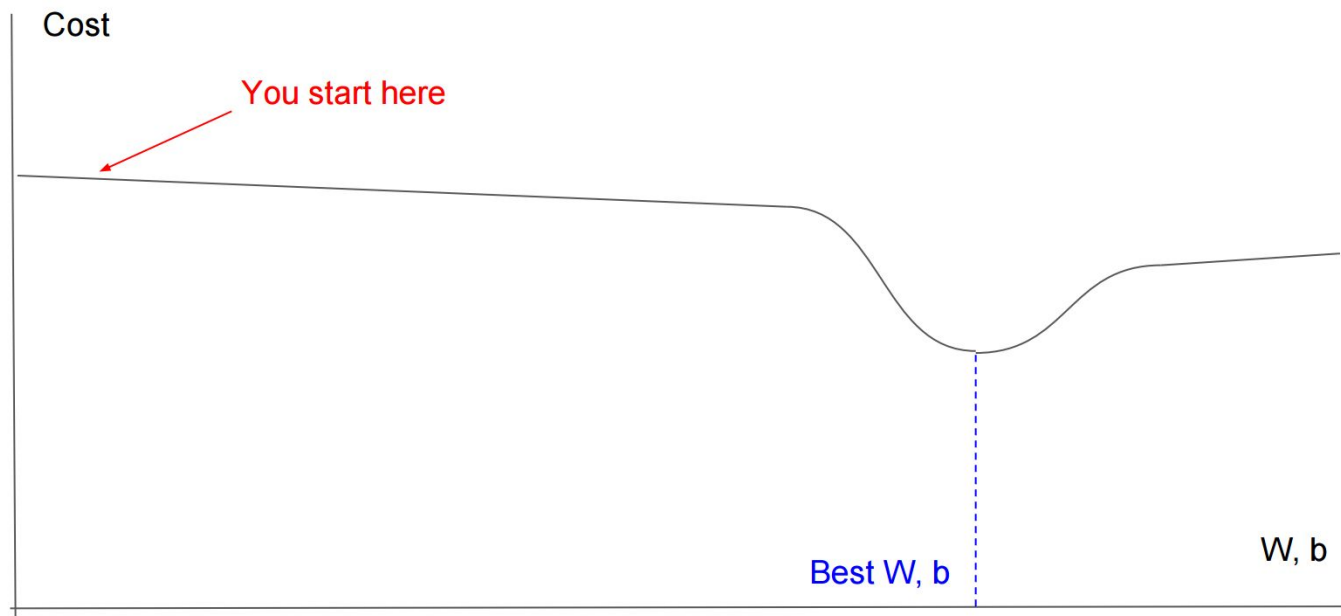
Choose $\text{current_}W, \text{current_}b$

If $\text{cost}(\text{current_}W, \text{current_}b) < \text{cost}(W_{\text{best}}, b_{\text{best}})$:

$W_{\text{best}}, b_{\text{best}} = \text{current_}W, \text{current_}b$

What is the best way to choose
 $\text{current_}W, \text{current_}b$?

Finding Minimum Cost Function



Choosing Training Method

- Random
 - Could take forever
- Gradient descent
 - From current viewpoint, move towards direction where steepness is greatest

Ready?

Recap:

- Model: Linear regression, $y = W.x + b$
- Cost: Least squared, $\text{cost} = \text{sum}((y_{\text{pred}} - y)^2)$
- Train: Gradient descent

Step 1: Model $y = W.x + b$

Tensorflow Model

Recap:

- Model: Linear regression, $y = W.x + b$
- Cost: Least squared, $\text{cost} = \text{sum}((y_ - y)^*2)$
- Train: Gradient descent

Tensorflow Model

tf.placeholder

- Hold data to be feed into the model
- `x = tf.placeholder(tf.float32, [None, 1])`

tf.Variable

- Hold variables to be trained
- `W = tf.Variable(tf.zeros([1, 1]))`
- `b = tf.Variable(tf.zeros([1]))`

One output, house price

One feature, house size

Tensorflow Model

`tf.matmul(x,W)`

- Multiply 2 matrices
- `product = tf.matmul(x,W)`

`‘+’`

- `y = product + b`
- Expands to:
 - `y = tf.matmul(x,W) + b = W.x + b`

Step 2: Cost Function

$\text{sum}((y_ - y)^{} 2)$**

Best-fit: Minimize Difference Prediction and Actual

Actual values:

One output, house price

- `y_ = tf.placeholder(tf.float32, [None, 1])`

Minimize difference between actual and prediction:

- `cost = tf.reduce_sum(tf.pow((y_-y), 2))`

Step 3: Data



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Faking Data

```
for i in range(100):
```

```
    // Create fake data for actual data
```

```
    xs = np.array([[i]])
```

```
    ys = np.array([[2*i]])
```

- $xs = 0, 1, 2, \dots, 99$
- $ys = 0, 2, 4, \dots, 198$
- ys is always twice of xs
- **$y = W.x + b$ where $W = 2, b = 0 \Rightarrow$ Best fit: $y = 2x$**

Step 4: Train



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Train using Gradient Descent

Train using Gradient Descent with steps in 0.000001

- `train_step = tf.train.GradientDescentOptimizer(0.00001).minimize(cost)`

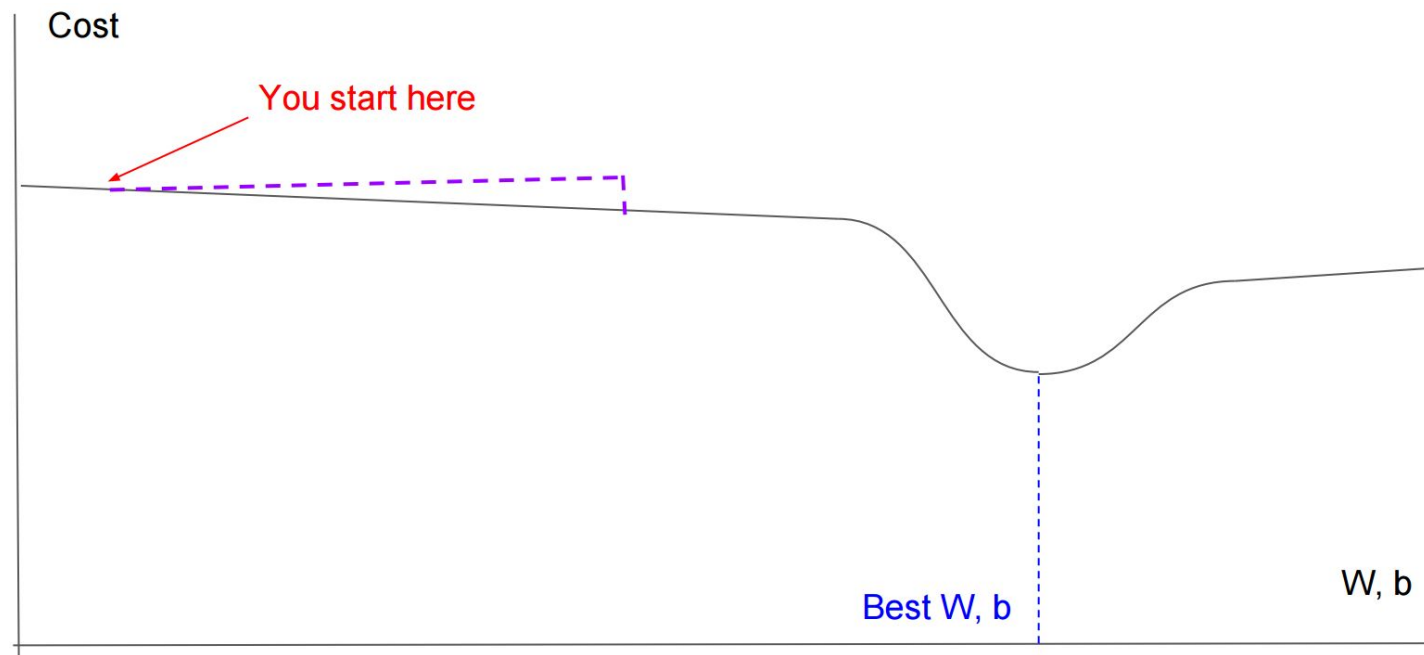
Train Model

- `sess = tf.Session()`
- `init = tf.initialize_all_variables()`
- `sess.run(init)`
- `steps = 100`

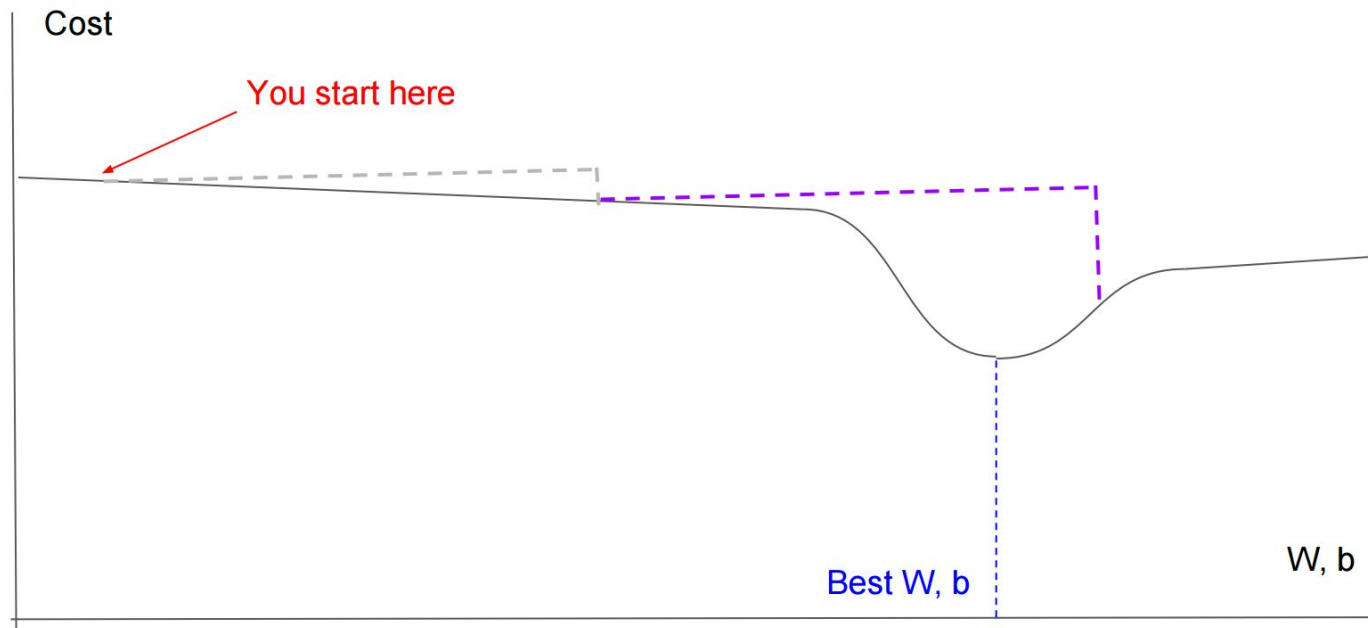
Tensorflow Non-interactive Mode

Nothing is actually executed until `sess.run(...)`

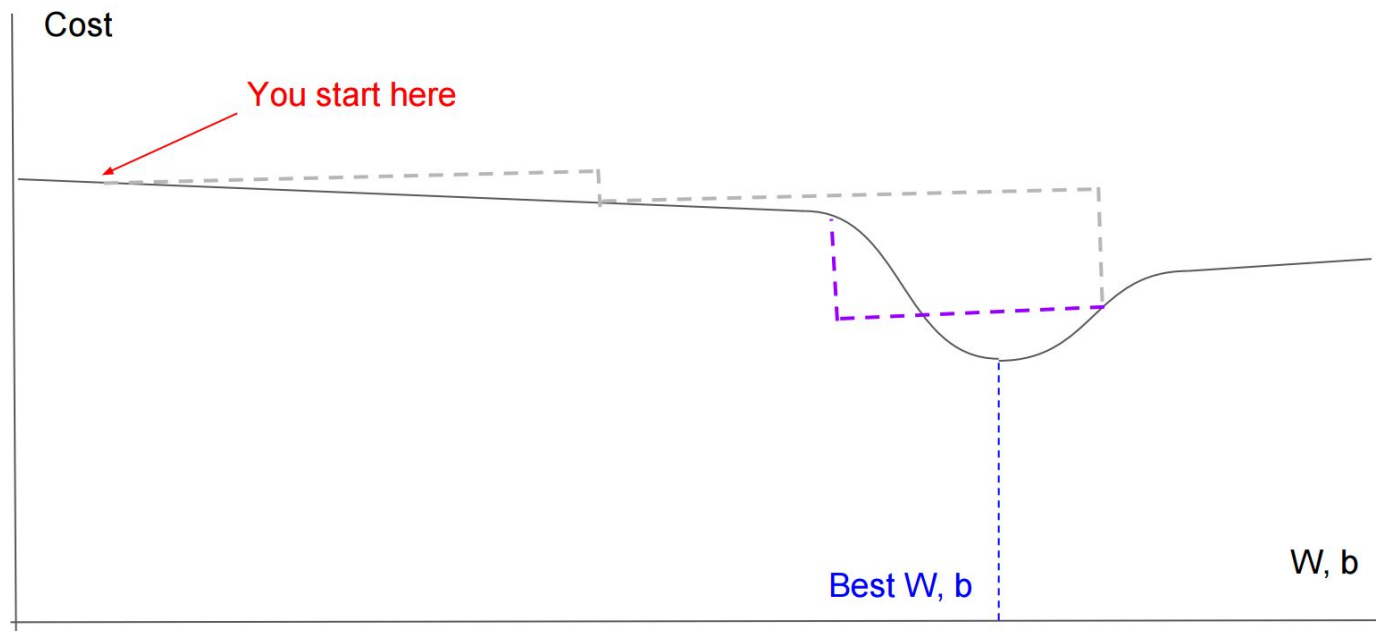
Finding Minimum Cost Function



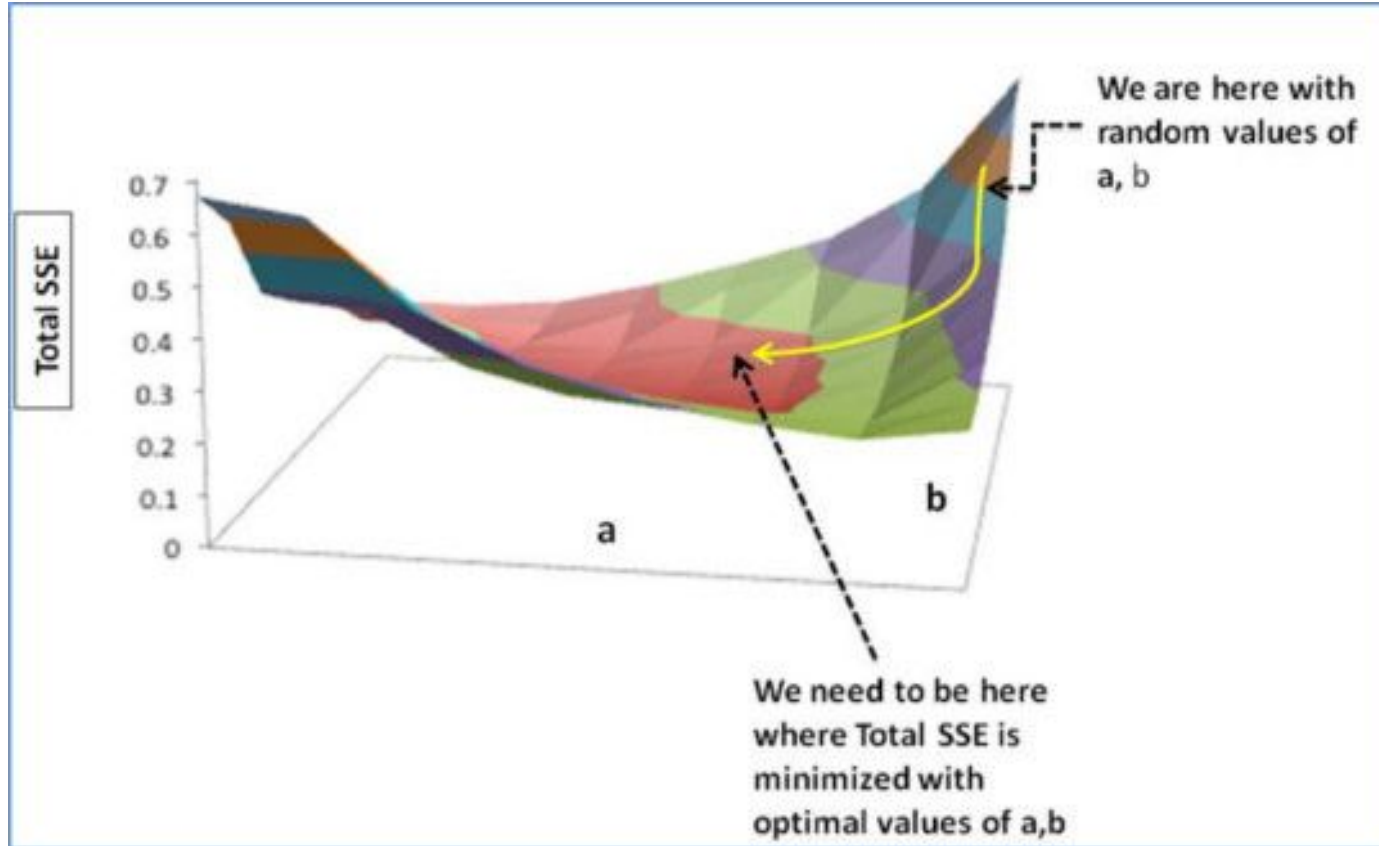
Finding Minimum Cost Function



Finding Minimum Cost Function



Finding Minimum Cost Function



Go!!!!

```
for i in range(steps):  
    # Create fake data for  $y = W.x + b$  where  $W = 2$ ,  $b = 0$   
    xs = np.array([[i]])  
    ys = np.array([[2*i]])  
  
    # Train  
    feed = { x: xs, y_: ys }  
    sess.run(train_step, feed_dict=feed)  
  
    print("After %d iteration:" % i)  
    print("W: %f" % sess.run(W))  
    print("b: %f" % sess.run(b))
```

Thanks!

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May 2017



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