STAT 701 Final Project - Laptop Pricing Analysis

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Executive Summary

Key Findings

We developed predictive models with the goal of predicting laptop price based on a bevvy of provided features. We applied clustering technique to learn more about different types of laptops within our data set. These clusters were later used as a feature along with various continuous and categorical variables to predict laptop price. We realized that the target variable (laptop price) was right-skewed so we applied a log transformation to the values

before starting our analysis and modeling. We also grouped multiple levels within some categorical variables that contained only a few records to aid in model development. Model performance was primarily assessed based on R^2 and RMSE in a validation data set which wasn't used during training across different predictive modelling approaches.

While we leveraged multiple predictive models, the Gradient Bossted Decision Tree (GBDT) model ultimately proved to be the most accurate in predicting laptop price. Our R^2'S were fairly high for all models. However, our RMSE on the actual prices was also fairly high whereas the RMSE on the log scale was fairly low. We believe we can further improve our models by applying various tuning techniques and introducing additional data for training.

Summary of Various R^2's and RMSE of the best models are given below:

Best Linear Model:

- The R² value of stepAIC is 0.720237665739132.
- The RMSE value of stepAIC is 298.724753420143.
- The R^2 value of stepAIC in log scale is 0.826822166731771.
- The RMSE value of stepAIC in log scale is 0.206641333801683.

Best Ensemble Model:

- The R² value for XGboost is 0.846570354015489.
- The RMSE value of XGboost is 218.695470595025.
- The R² value for XGboost in log scale is 0.886013879258513.
- The RMSE value of XGboost in log scale is 0.165913472726158.

Interpretations

Based on our validation metrics (R² and RMSE), we observed the following across different modeling techniques:

- 1. **Linear models**: StepAIC was a slightly better stepwise approach if we were to use a linear model to predict laptop prices. We also found that though regularization using lasso could give us a fairly good model (high R^2 and low RMSE), it wasn't better than our stepwise regression approach.
- 2. **Decision trees**: A basic tree and a pruned tree gave us worse predictive models than linear models.
- 3. Ensemble methods: GBDT model trained using XGboost gave us the best predictive model. Analysis of important variables across the ensemble approaches such as GBDT and random process revealed that our feature creation by clustering and our treatment of missing values in display size were useful. We also noticed that three of the top five variables in Random Forest and GBDT were different.
- 4. Lastly, our analysis using partial dependence suggested that higher performance laptops (i.e laptops with higher RAM, SSD, Graphic card) were priced higher. Intuitively, this makes sense.

Implications

Pricing products is a difficult problem for any e-commerce platform. The approach and findings here suggest that we can build a fairly accurate model to predict prices for a laptop based on common features. This type of model can be used by platforms such as Flipkart to recommend prices to their sellers to minimize friction on uploading their catalog to Flipkart. This is also a great prototype to prove that we can use similar techniques to price any other category of products which can further help smaller sellers when they try to list products on an e-commerce platform.

Introduction to the Data Set

Data source: https://www.kaggle.com/datasets/kuchhbhi/latest-laptop-price-list

Using data scraped from Indian e-commerce company Flipkart on 3/29/22, we developed models that predict laptop price based on various available attributes.

We know that that laptop price can often be driven by brand recognition (on top of actual performance attributes). For example, a basic macbook may command a higher price than a superior performing, custom-built computer due to Apple's brand recognition and amazing customer support. We also know that customers often care about features such has RAM, Graphic Card, Solid State Drive (ssd) etc. Additionally, online ratings and reviews can sometimes drive up a customer's willingness to pay for a laptop. Our data set has strong representative coverage across all these important features.

Our master data set, laptop.data has 896 observations and 23 variables. Below is a description of the columns:

```
##
    [1] "brand"
                           "model"
                                              "processor_brand" "processor_name"
    [5] "processor_gnrtn" "ram_gb"
                                              "ram type"
                                                                  "ssd"
                           "os"
                                              "os_bit"
    [9] "hdd"
                                                                  "graphic_card_gb"
  [13] "weight"
                           "display_size"
                                              "warranty"
                                                                  "Touchscreen"
                           "latest_price"
                                              "old_price"
  [17]
        "msoffice"
                                                                  "discount"
  [21] "star_rating"
                           "ratings"
                                              "reviews"
```

All the column names are self-explanatory. For example "touchscreen" column indicates if the laptop has a touch screen. Similarly "weight" tells us about the weight of the laptop.

Next, let us look at our data set a bit more closely to understand type of values each column has:

## ## ## ##	brand Length:896 Class:character Mode:character	model Length:896 Class :character Mode :character	processor_brand Length:896 Class :characte Mode :characte	Length:896 r Class:character
## ## ##				
##	processor_gnrtn	ram_gb	ram_type	ssd
##	Length:896	Length:896	Length:896	Length:896
##	Class :character	Class :character	Class :characte	r Class :character
##	Mode :character	Mode :character	Mode :characte	r Mode :character
##				
##				
##				
##	hdd	OS	os_bit	graphic_card_gb
##	Length:896	Length:896	Length:896	Min. :0.000
##	Class :character	Class : character		• • • • • • • • • • • • • • • • • • • •
##	Mode :character	Mode :character	Mode :characte	
##				Mean :1.199
## ##				3rd Qu.:2.000 Max. :8.000
##	weight	display_size	warranty	Touchscreen
##	Length:896	Length:896	Min. :0.000	Length:896
##	Class : character	Class : character	1st Qu.:0.000	Class :character
##	Mode :character	Mode :character	Median :1.000	Mode :character
##			Mean :0.692	
##			3rd Qu.:1.000	
##			Max. :3.000	
##	msoffice	latest_price	old_price	discount
##	Length:896	Min. : 13990	Min. : 0	Min. : 0.00
##	Class :character	1st Qu.: 45490	1st Qu.: 54940	1st Qu.:11.00
##	Mode :character	Median : 63494	Median : 78052	Median :19.00
##		Mean : 76310	Mean : 88134	Mean :18.53

```
##
                        3rd Qu.: 89090
                                           3rd Qu.:111020
                                                             3rd Qu.:26.00
##
                                :441990
                                                   :377798
                                                                     :57.00
                        Max.
                                           Max.
                                                             Max.
##
                       ratings
     star_rating
                                           reviews
##
                                                   0.00
    Min.
           :0.00
                    Min.
                           :
                                 0.0
                                       Min.
                                               :
##
    1st Qu.:0.00
                    1st Qu.:
                                 0.0
                                       1st Qu.:
                                                   0.00
   Median:4.10
##
                    Median:
                                19.0
                                       Median:
                                                   3.00
##
           :2.98
                               367.4
                                                  46.15
   Mean
                    Mean
                                       Mean
##
    3rd Qu.:4.40
                    3rd Qu.:
                               179.5
                                       3rd Qu.:
                                                  23.25
           :5.00
                                               :1947.00
   Max.
                    Max.
                            :15279.0
                                       Max.
```

Cleaning Up the Data and Creating New Features

Making the Data More Intuitive

While our data set is relatively clean, we chose to further refine it to make analysis easier and more intuitive. For example, we removed redundant units / characters from columns (e.g., "GB" for ssd, hdd and "bit" for os_bit). We also identified missing data and reclassified those entries as "NA." The variables with the most NAs were model (95), processor—gnrtn (239), and display—size (332).

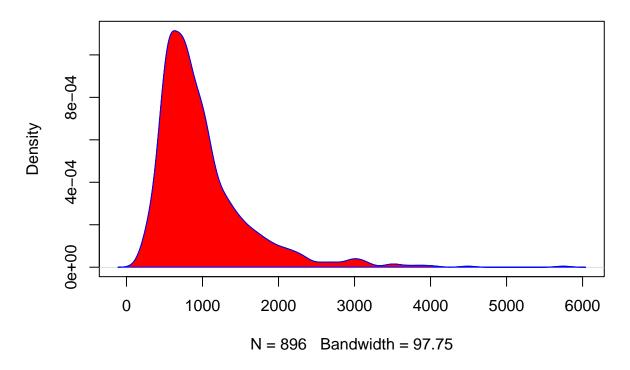
Converting Laptop Price to USD for Better Understanding

The information in this data set was pulled from Flipkart, so the prices are in Indian rupees. Although it was not necessary for modeling, we converted all prices from rupees to USD using a 1 to 0.013 ratio (current exchange rate as of 4/12/22) to make it easy for us to understand.

Applying Log Transform to the Target Variable

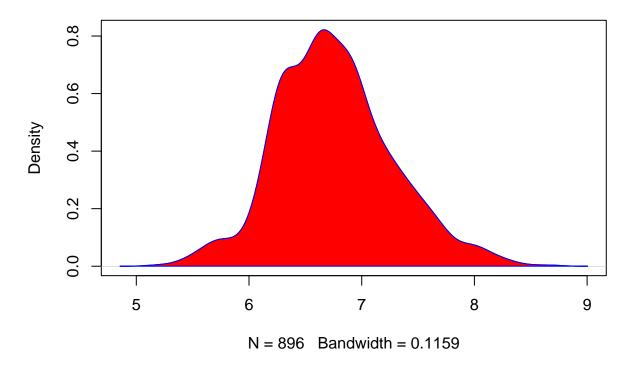
Next we studied our target variable a bit closer and observed the following distribution:

Kernel Density of Latest Price



As you can see, our target variable is right skewed which prompted us to we apply a log transformation and create a new column called log_latest_price.

Kernel Density of Log Latest Price



This transformation makes the data close to normal (shown above), so we will be using log_latest_price as our target y variable for the rest of our analysis.

Missing Value Treatment:

We saw that display sizes had many missing records and we know from our intuition that display sizes impact pricing of a laptop (i.e., Macbook 17inch more expensive than Macbook 13inch). So, we created a new column in the dataframe called "Display Size Given?" and populated it with "Yes" or "No" values. We then replaced any missing display size values with the average of display size from all available records. In addition to a Y/N column, we wanted to leverage the available records in the display size column, so we replaced the missing records with the column average. We also grouped a few levels in some categorical variables (such as processor name, brand, etc.) to make the levels more dense and make them easier to model.

We chose to drop some columns for which there were many NAs (i.e., missing) or variables that did not seem to be useful for our use case: (1) model, (2) processor_gnrtn, (3) discount, and (4) old_price. We felt comfortable removing the first 2 columns from the list above because a laptop's model is dependent on the laptop brand which we were already considering, while processor's generation is reflected in the processor name (3 in i3 represents generation). We did not want to use other pricing related variables in our predictive models and so we removed discount and old_price variables. We wanted to make sure that we can predict the price of a laptop given it's attributes and not be dependent on discount or old listed price from a single e-commerce platform.

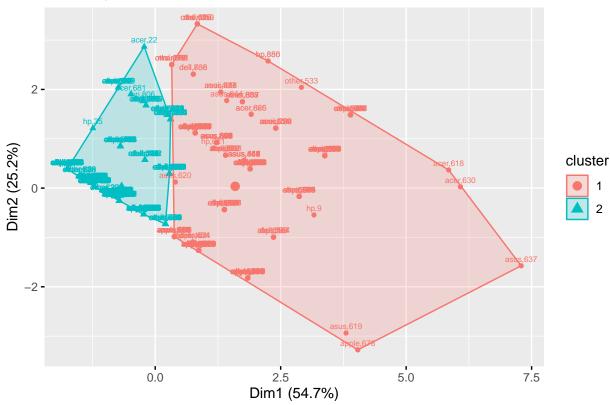
After applying all cleanup and variable selection, we created a new dataframe laptop.data.clean for the rest of this analysis.

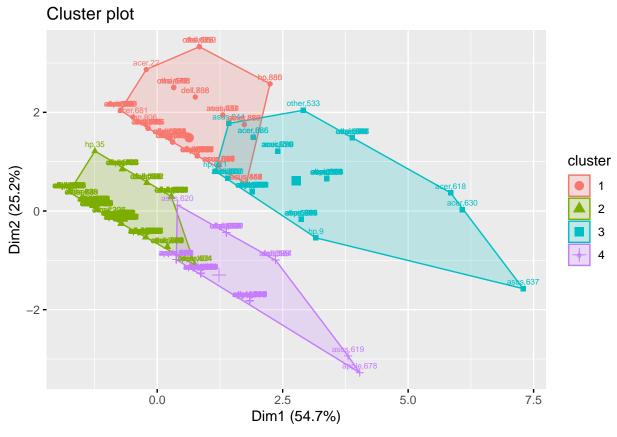
Clustering the Laptops Based on Performance Attributes

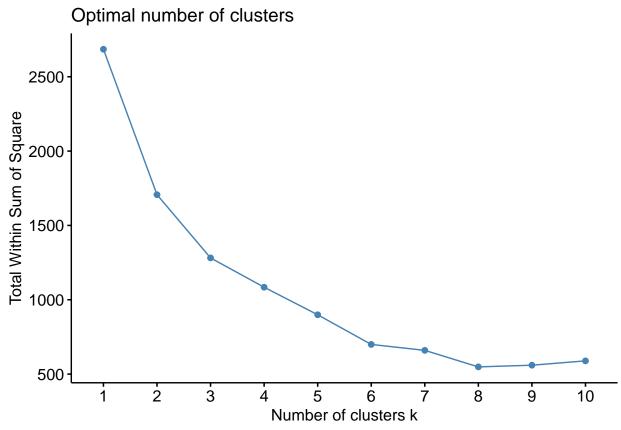
We believed it would be beneficial to perform cluster analysis on our data set. We know that RAM, ssd, and Graphic Card memory are common performance attributes that buyers consider when determining if a laptop

would be suitable for their use case. We extracted these three columns to conduct cluster analysis as shown in the plots below.



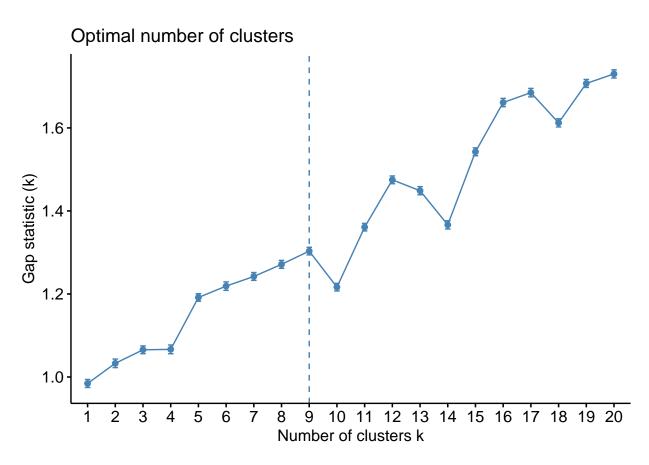






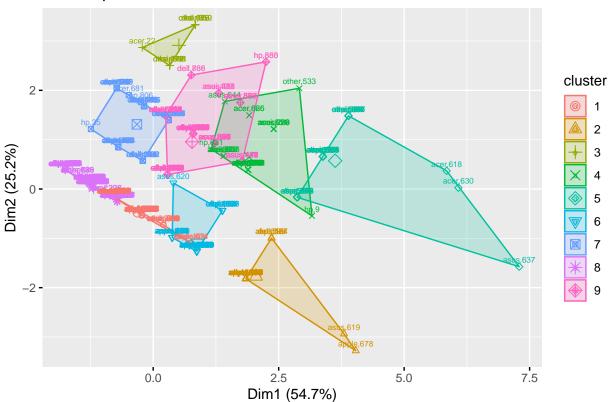
Warning: did not converge in 10 iterations

Warning: did not converge in 10 iterations
Warning: did not converge in 10 iterations
Warning: did not converge in 10 iterations
Warning: did not converge in 10 iterations
Warning: did not converge in 10 iterations
Warning: did not converge in 10 iterations
Warning: did not converge in 10 iterations
Warning: did not converge in 10 iterations



We can see from above plots that the chosen attributes are able to cluster our laptops into cleanly separable clusters. We started by building clusters with 2 and 4 centers and then applied the elbow method and gapstatistics to learn that the optimal number of clusters possible from our attributes would be 9. Therefore, we finally created clusters with 9 centers using the K-means method. Below is a visual:

Cluster plot



Upon visually inspecting the clusters, we realized that these groupings across RAM, ssd, and graphics card is possibly an indication of the use cases (such as gaming vs. office use vs. personal use) of the laptops in each groups. We expect a natural shakeout of high-end, high-price laptops all the way down to low-end, low-price laptops (along with multiple other "buckets" in between).

Building a Feature Based on the Clusters Created

We had previously converted ram, ssd and graphic card into denser multilevel categorical variables. We felt that the the clusters created based on their raw values would provide additional predictive power over the previously created variables. Hence, we turned these clusters into a feature with 9 levels for our predictive models. See below the number of records in each of the nine levels:

Predictive Analysis

Overview of the Approaches

To predict the price of a laptop, we explored the following techniques:

- 1. Stepwise AIC/Stepwise BIC
- 2. Regularized Regression
- 3. Decision Trees
- 4. Ensemble : Random Forest5. Ensemble : Tuned XGBoost

Splitting Data Into Train and Validation We split our clean dataframe (laptop.data.clean) into training and validation (holdout) subsets. We used 2/3rd of the records for training and 1/3rd for validation. The same validation dat aset was used for all models for calculating R^2 and RMSE's.

Stepwise Regression

Comparing AIC and BIC

From our validation metrics, we can see that StepAIC is a slightly better stepwise approach if we were to use a linear model to predict laptop prices. Below is a brief summary of the R^2 and RMSE. We wanted to look at the validation metrics at both log scale and original scale. Although our underlying model is optimizing at the log scale, we would care more about about actual prices and how far we would be from them with our predictions. Our R^2 for both stepAIC and stepBIC are fairly high (log scale) indicating that our predictions and actuals are somewhat correlated. Additionally our RMSE in the log scale is fairly small indicating that we have a fairly good model. The larger discrepancy in RMSE in regular scale is possibly due to outliers (i.e., very highly priced laptops).

StepAIC Model Fit Summary:

[1] "The R^2 value of stepAIC is 0.804889136995938" [1] "The RMSE value of stepAIC is 253.418380673218" [1] "The R^2 value of stepAIC in log scale is 0.857404190399198" [1] "The RMSE value of stepAIC in log scale is 0.190957188483678"

StepBIC Model Fit Summary:

[1] "The R^2 value of stepBIC is 0.799925677459252" [1] "The RMSE value of stepBIC is 256.653973304625" [1] "The R^2 value of stepBIC in log scale is 0.85636750739433" [1] "The RMSE value of stepBIC in log scale is 0.191323071789122"

Coefficients and their interpretations:

The annova analysis we conducted (shown below) identifies the list of significant variables and the coefficients show that certain levels in categorical variables are significant whereas others are not. It is good to see that the presence of clusters is significant for the model. This is a further validation that our feature engineering was an useful trick. Also, both display size given (Y/N) and display size turned out be significant. StepwiseBIC had 29 significant variables (counting only stat sig ones), whereas stepwiseAIC picked 30 which is expected as BIC punishes for complexity more than AIC. (Note: Multi-levels are counted as separate variables)

```
## Analysis of Variance Table
##
## Response: log_latest_price
##
                       Df Sum Sq Mean Sq F value
                       10 90.974
                                  9.0974 218.8416 < 2.2e-16 ***
## processor_name
## cluster
                        8 24.850
                                  3.1063 74.7220 < 2.2e-16 ***
## processor_brand
                        2
                           8.573
                                  4.2867 103.1179 < 2.2e-16 ***
                           3.630
                                           17.4631 4.364e-16 ***
## ram_type
                                   0.7260
## Touchscreen
                           2.379
                                   2.3792
                                           57.2318 1.599e-13 ***
                        1
                           2.004
## os
                        2
                                  1.0021
                                           24.1067 9.057e-11 ***
## star_rating
                        1
                           1.843
                                  1.8425
                                           44.3229 6.653e-11 ***
## display_size
                        1
                           1.035
                                  1.0353
                                           24.9039 8.056e-07 ***
                                           22.6635 2.460e-06 ***
## graphic_card_gb
                        1
                           0.942
                                  0.9421
## ssd cat
                           0.512
                                   0.5121
                                           12.3184 0.0004846 ***
                        1
## display_size_given
                        1
                           0.415
                                  0.4146
                                            9.9723 0.0016747 **
                                  0.1658
## weight
                        2
                           0.332
                                            3.9877 0.0190719 *
## ratings
                        1
                           0.159
                                   0.1589
                                            3.8236 0.0510331 .
## Residuals
                      560 23.280
                                  0.0416
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

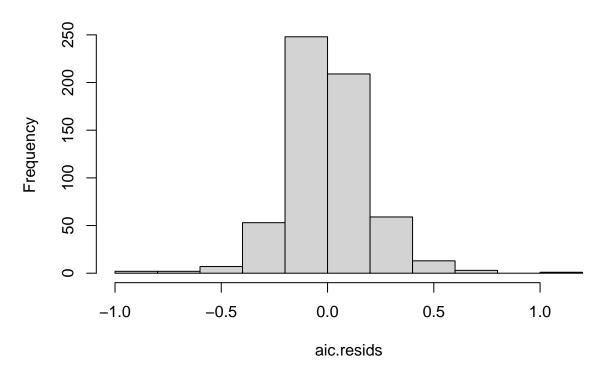
```
## [1] "The R^2 value of stepAIC is 0.804889136995938"
## [1] "The RMSE value of stepAIC is 253.418380673218"
## [1] "The R^2 value of stepAIC in log scale is 0.857404190399198"
## [1] "The RMSE value of stepAIC in log scale is 0.190957188483678"
##
## Call:
## lm(formula = log_latest_price ~ processor_name + cluster + processor_brand +
      Touchscreen + ram_type + os + star_rating + display_size +
##
       graphic_card_gb + ssd_cat + display_size_given, data = pred.laptop.train)
##
## Residuals:
##
       Min
                 1Q
                     Median
                                  3Q
                                          Max
## -0.90398 -0.11945 -0.00547 0.09710
                                     1.10748
##
## Coefficients:
##
                             Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                             4.462205
                                        0.254550 17.530 < 2e-16 ***
## processor_namecore i3
                             0.517700
                                        0.062088
                                                 8.338 5.82e-16 ***
                             0.869765
                                        0.063667 13.661 < 2e-16 ***
## processor_namecore i5
## processor_namecore i7
                             1.004909
                                        0.072684 13.826 < 2e-16 ***
## processor_namem1
                             2.008513
                                        0.197600 10.165 < 2e-16 ***
                                        0.087998 11.785 < 2e-16 ***
                             1.037052
## processor_nameother
## processor_namepentium quad 0.147120
                                        0.101696
                                                 1.447 0.148548
                                        0.112377 12.331 < 2e-16 ***
## processor_nameryzen 3
                             1.385709
## processor_nameryzen 5
                             1.694818
                                        0.108917 15.561 < 2e-16 ***
                                        0.112653 15.822 < 2e-16 ***
## processor_nameryzen 7
                             1.782434
## processor_nameryzen 9
                             2.070597
                                        0.133385 15.523 < 2e-16 ***
## cluster2
                             0.152507
                                        0.073593 2.072 0.038692 *
## cluster3
                             0.473053
                                        0.134193 3.525 0.000458 ***
                                        0.076765 0.382 0.702341
## cluster4
                             0.029352
                             0.149718
                                        0.105117 1.424 0.154914
## cluster5
## cluster6
                             0.169686
                                        0.037700 4.501 8.23e-06 ***
                                        0.061123 -2.230 0.026173 *
## cluster7
                            -0.136276
## cluster8
                            -0.088613
                                        0.025765 -3.439 0.000626 ***
                            -0.110375
                                        0.058277 -1.894 0.058740 .
## cluster9
                             0.933830
                                        0.081254 11.493 < 2e-16 ***
## processor_brandintel
                                        0.130632 -2.210 0.027499 *
                            -0.288711
## processor_brandother
## TouchscreenYes
                             0.268039
                                        0.030902 8.674 < 2e-16 ***
## ram_typeDDR4
                             0.108920
                                        0.075165 1.449 0.147875
                                        0.132030 3.664 0.000272 ***
## ram_typeDDR5
                             0.483772
                                        0.099006 5.434 8.22e-08 ***
## ram_typeLPDDR3
                             0.537994
                                        ## ram_typeLPDDR4
                             0.068075
## ram_typeLPDDR4X
                             0.170916
                                        0.080627 2.120 0.034457 *
## osMac
                             0.703859
                                        0.148427 4.742 2.68e-06 ***
                                        0.070968 -3.134 0.001814 **
## osWindows
                            -0.222420
## star_rating
                                        0.004632 -6.507 1.69e-10 ***
                            -0.030141
## display_size
                             0.058268
                                        0.012344 4.720 2.97e-06 ***
                             0.058192
                                        0.013598
                                                  4.280 2.20e-05 ***
## graphic_card_gb
## ssd_catless_than_1gb
                            -0.190275
                                        0.055027 -3.458 0.000586 ***
## display_size_givenYes
                            -0.059956
                                        0.019134 -3.134 0.001817 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

```
## Residual standard error: 0.2055 on 563 degrees of freedom
## Multiple R-squared: 0.8523, Adjusted R-squared: 0.8436
## F-statistic: 98.44 on 33 and 563 DF, p-value: < 2.2e-16
## Analysis of Variance Table
##
## Response: log_latest_price
##
                      Df Sum Sq Mean Sq F value
## processor_name
                      10 90.974 9.0974 215.4741 < 2.2e-16 ***
## cluster
                      8 24.850 3.1063 73.5722 < 2.2e-16 ***
                       2 8.573 4.2867 101.5311 < 2.2e-16 ***
## processor_brand
## Touchscreen
                       1 2.713 2.7129 64.2555 6.343e-15 ***
                       5 3.296 0.6592 15.6135 2.104e-14 ***
## ram_type
                       2 2.004 1.0021
                                        23.7357 1.269e-10 ***
## os
## star_rating
                      1 1.843 1.8425 43.6409 9.151e-11 ***
## display_size
                      1 1.035 1.0353
                                        24.5207 9.732e-07 ***
## graphic_card_gb
                       1 0.942 0.9421 22.3147 2.926e-06 ***
                       1 0.512 0.5121 12.1289 0.000535 ***
## ssd cat
## display_size_given 1 0.415
                                0.4146
                                         9.8188 0.001817 **
## Residuals
                     563 23.770 0.0422
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## [1] "The R^2 value of stepBIC is 0.799925677459252"
## [1] "The RMSE value of stepBIC is 256.653973304625"
## [1] "The R^2 value of stepBIC in log scale is 0.85636750739433"
## [1] "The RMSE value of stepBIC in log scale is 0.191323071789122"
```

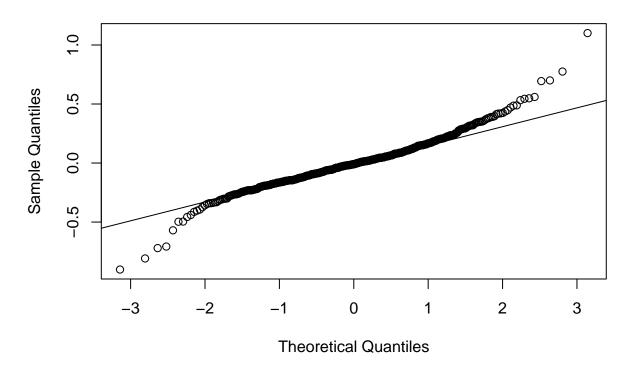
Residuals

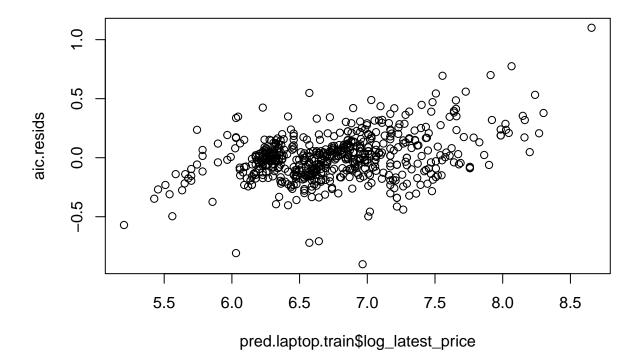
The residuals seems to be aligned with assumptions of linear regression (normally distributed, centered around 0, and equal variance). The qq plot showcases presence of heavy tails but it does not seem to be a big concern from the plot.

Histogram of aic.resids



Normal Q-Q Plot





Regularized Regression

Analysis - Validation Metrics

We applied a lasso regression to see if we could build a model with fewer features. We chose the penalty multiple (lambda) and number of features based on 1 standard error criteria. We found that while lasso could provide a fairly good model (high r square and low RMSE), it wasn't better than our Stepwise regression approach.

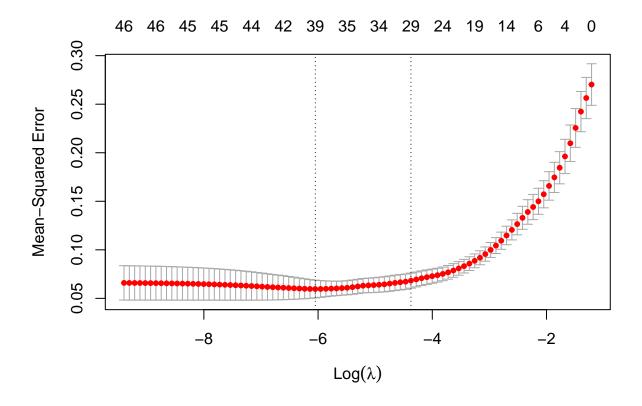
Regularized Regression Model Fit Summary:

[1] "The R^2 value of regularized regression is 0.739109086771972" [1] "The RMSE value of regularized regression is 296.652788037578" [1] "The R^2 value of regularized regression in log scale is 0.787245668133689" [1] "The RMSE value of regularized regression in log scale is 0.232685415075645"

Coefficients and Their Interpretations:

It is interesting to observe that lasso gave us 29 significant variables which is similar to our best stepwise regression (stepAIC). Cluster seems to be as important for the regularized regression as it was for stepwise regression. However, regularized regressions shrunk display size given (Y/N) unlike stepwise regression.

[1] 597 49



[1] 50 1

[1] "The lasso regression chose 29 variables and 1 intercept"

```
## 50 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                                6.7416819323
## (Intercept)
## brandapple
                                0.5558859411
## brandasus
                               -0.0020370338
## branddell
                                0.0048670322
## brandhp
## brandmsi
## brandother
## processor_brandintel
## processor_brandother
## processor_namecore i3
                              -0.0097100993
## processor_namecore i5
                                0.1985940376
## processor_namecore i7
                                0.2869211681
## processor_namem1
                                0.1365601575
## processor_nameother
## processor_namepentium quad -0.2503282289
## processor_nameryzen 3
                              -0.0362703686
## processor_nameryzen 5
                                0.0907451217
## processor_nameryzen 7
                                0.1362783961
## processor_nameryzen 9
                                0.3215072423
## ram_typeDDR4
                                0.3005891972
## ram_typeDDR5
```

```
## ram typeLPDDR3
                              0.3802361275
## ram_typeLPDDR4
## ram_typeLPDDR4X
                              0.0012034446
## osMac
## osWindows
                             -0.2671547136
## os_bit64
## graphic_card_gb
                            0.0448758096
## weightGaming
## weightThinNlight
                            0.0083628155
## display_size
                            0.0332215507
## warranty
                            0.0263151957
                            0.2750043592
## TouchscreenYes
## msofficeYes
## star_rating
                           -0.0281194638
## ratings
                             -0.0000391211
## reviews
## display_size_givenYes
## ram_gb_catless_than_8
                             -0.1557618406
## ssd_catless_than_1gb
                             -0.2561305868
## hdd_catlow_hdd
## cluster2
## cluster3
                             0.5303553466
## cluster4
## cluster5
                             0.1315500117
## cluster6
                              0.0068286880
## cluster7
## cluster8
                             -0.2059538924
## cluster9
## [1] "The R<sup>2</sup> value of regularized regression is 0.739109086771972"
## [1] "The RMSE value of regularized regression is 296.652788037578"
## [1] "The R^2 value of regularized regression in log scale is 0.787245668133689"
## [1] "The RMSE value of regularized regression in log scale is 0.232685415075645"
```

Decision Trees

Analysis - Validation Metrics Across Simple and Pruned Trees

We started by building a simple tree with default parameters and then pruned it based on complexity parameter (cp). Pruning did not change anything as we got the exact same tree after pruning. Additionally the R^2 and RMSE for a single tree seemed to be worse compared to linear models.

```
## Call:
## rpart(formula = log_latest_price ~ ., data = pred.laptop.train,
## parms = list(split = "information"), control = rpart.control(minsplit = 20))
## n= 597
##
## CP nsplit rel error xerror xstd
## 1 0.36654808     0 1.0000000 1.0060243 0.06412652
## 2 0.17344585     1 0.6334519 0.7029555 0.06058484
## 3 0.09453099     2 0.4600061 0.5687281 0.05477197
```

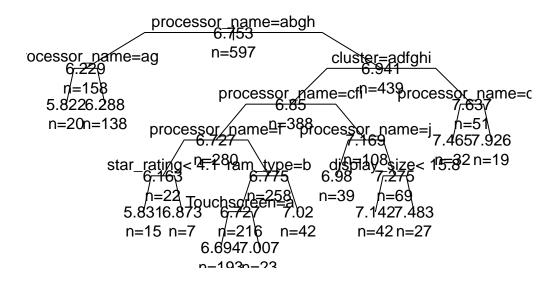
```
## 4 0.04720661
                      3 0.3654751 0.4107763 0.03427384
## 5 0.03220955
                      4 0.3182685 0.3551096 0.03287640
## 6 0.02356044
                      5 0.2860589 0.3482968 0.03289189
## 7
                      6 0.2624985 0.3234842 0.03071704
     0.01869464
## 8 0.01578159
                      7 0.2438038 0.3211953 0.03089951
## 9 0.01353413
                      8 0.2280223 0.3109761 0.03093254
## 10 0.01249174
                      9 0.2144881 0.2934783 0.03088260
## 11 0.01186462
                     10 0.2019964 0.2877812 0.03056464
## 12 0.01000000
                     11 0.1901318 0.2773660 0.03007320
##
## Variable importance
   processor name
                           cluster
                                            ssd cat graphic card gb
##
                                                                        display size
##
                43
                                26
                                                  5
                                                                   5
                                                                                   3
## processor_brand
                             brand
                                        star_rating
                                                                          ram_gb_cat
                                                           ram_type
##
                 3
                                 3
                                                  2
                                                                   2
                                                                                   2
##
                os
                           reviews
                                            ratings
                                                        Touchscreen
##
                                 2
                                                  1
                                                                   1
##
## Node number 1: 597 observations,
                                       complexity param=0.3665481
     mean=6.752586, MSE=0.2695605
##
     left son=2 (158 obs) right son=3 (439 obs)
##
##
     Primary splits:
         processor_name splits as LLRRRRLLRRR, improve=0.3665481, (0 missing)
##
##
                        splits as LRRRRRLLR,
                                                 improve=0.3478018, (0 missing)
         cluster
##
         ram_gb_cat
                        splits as RL,
                                                 improve=0.2637135, (0 missing)
                                                 improve=0.2517967, (0 missing)
##
         ssd_cat
                        splits as RL,
##
         display_size
                        < 15.8
                                to the left,
                                                 improve=0.1923546, (0 missing)
##
     Surrogate splits:
##
         cluster splits as RRRRRRLR, agree=0.821, adj=0.323, (0 split)
                          to the right, agree=0.742, adj=0.025, (0 split)
##
         reviews < 794
##
                        to the right, agree=0.740, adj=0.019, (0 split)
         ratings < 4914
##
## Node number 2: 158 observations,
                                        complexity param=0.02356044
     mean=6.228627, MSE=0.04839155
##
     left son=4 (20 obs) right son=5 (138 obs)
##
##
     Primary splits:
         processor_name splits as LR----LR---, improve=0.49589220, (0 missing)
##
##
                                                 improve=0.32979860, (0 missing)
         ram_type
                        splits as LR--LL,
##
                        splits as L-LRRRL,
                                                 improve=0.12698630, (0 missing)
         brand
##
         warranty
                        < 0.5
                                 to the left,
                                                 improve=0.09250302, (0 missing)
##
                        splits as R----L-,
                                                 improve=0.08363798, (0 missing)
         cluster
##
     Surrogate splits:
##
         ram_type splits as LR--LR, agree=0.911, adj=0.3, (0 split)
##
                                       complexity param=0.1734458
## Node number 3: 439 observations,
##
     mean=6.941164, MSE=0.2147928
     left son=6 (388 obs) right son=7 (51 obs)
##
##
     Primary splits:
                                                  improve=0.2960126, (0 missing)
##
         cluster
                         splits as
                                    LRRLRLLLL,
                                     --LRRL--LLR, improve=0.2477640, (0 missing)
##
         processor_name
                         splits as
##
         ssd cat
                                                  improve=0.2446011, (0 missing)
                         splits as
                                    RL,
##
         ram_gb_cat
                         splits as
                                   RL,
                                                  improve=0.2060381, (0 missing)
##
         graphic_card_gb < 5</pre>
                                   to the left,
                                                  improve=0.1837011, (0 missing)
##
     Surrogate splits:
##
                                                 agree=0.925, adj=0.353, (0 split)
         ssd_cat
                         splits as RL,
##
         graphic_card_gb < 5</pre>
                                  to the left,
                                                 agree=0.913, adj=0.255, (0 split)
```

```
##
         display size
                         < 13.15 to the right, agree=0.886, adj=0.020, (0 split)
##
## Node number 4: 20 observations
    mean=5.821713, MSE=0.0929088
##
##
## Node number 5: 138 observations
    mean=6.2876, MSE=0.01446495
##
##
## Node number 6: 388 observations,
                                       complexity param=0.09453099
##
    mean=6.849745, MSE=0.1527882
##
    left son=12 (280 obs) right son=13 (108 obs)
##
    Primary splits:
##
         processor_name splits as --LRRL--LRR, improve=0.2566158, (0 missing)
##
                       < 15.8
                                 to the left,
                                                improve=0.1844874, (0 missing)
         display size
                                                improve=0.1435471, (0 missing)
##
         cluster
                        splits as R--R-RRLR,
                                 to the right, improve=0.1039789, (0 missing)
##
         ratings
                        < 4.5
                                 to the right, improve=0.1030018, (0 missing)
##
                        < 95.5
        reviews
##
    Surrogate splits:
                                             agree=0.784, adj=0.222, (0 split)
##
        ram_gb_cat
                      splits as RL,
##
         cluster
                      splits as L--R-RLLL,
                                             agree=0.784, adj=0.222, (0 split)
##
         display_size < 15.8
                               to the left,
                                             agree=0.763, adj=0.148, (0 split)
##
         brand
                      splits as LRLLLLL,
                                             agree=0.755, adj=0.120, (0 split)
##
                                             agree=0.755, adj=0.120, (0 split)
         os
                      splits as LRL,
##
## Node number 7: 51 observations,
                                      complexity param=0.01578159
    mean=7.636661, MSE=0.1392158
##
##
    left son=14 (32 obs) right son=15 (19 obs)
##
    Primary splits:
##
        processor name
                            splits as
                                       --RLRR---LL, improve=0.3577031, (0 missing)
                                                    improve=0.2341135, (0 missing)
##
         display_size_given splits as RL,
##
         msoffice
                            splits as RL,
                                                    improve=0.2025396, (0 missing)
##
         star_rating
                            < 4.75
                                     to the left,
                                                    improve=0.1384419, (0 missing)
                            splits as LRRLLRR,
                                                    improve=0.1362138, (0 missing)
##
         brand
##
    Surrogate splits:
                                        agree=0.863, adj=0.632, (0 split)
##
        os
                    splits as RRL,
                    splits as LRLLLRL, agree=0.765, adj=0.368, (0 split)
##
        brand
##
         ram_type
                    splits as
                              -LLLRL, agree=0.765, adj=0.368, (0 split)
##
                                        agree=0.765, adj=0.368, (0 split)
         ram_gb_cat splits as LR,
##
         ssd_cat
                    splits as LR,
                                        agree=0.765, adj=0.368, (0 split)
##
## Node number 12: 280 observations,
                                        complexity param=0.04720661
##
    mean=6.726769, MSE=0.1167087
##
    left son=24 (22 obs) right son=25 (258 obs)
##
    Primary splits:
##
        processor_name splits as --R--L--R--, improve=0.2324729, (0 missing)
##
         processor brand splits as LRL,
                                                 improve=0.1943622, (0 missing)
                         < 218.5 to the right, improve=0.1519869, (0 missing)
##
        ratings
##
         cluster
                         splits as R--R-RRLR,
                                                 improve=0.1429508, (0 missing)
                         < 102
                                  to the right, improve=0.1403495, (0 missing)
##
        reviews
##
    Surrogate splits:
##
        reviews
                                  to the right, agree=0.939, adj=0.227, (0 split)
                         < 249
                                                agree=0.936, adj=0.182, (0 split)
##
         processor brand splits as RRL,
##
                         < 1887.5 to the right, agree=0.936, adj=0.182, (0 split)
##
## Node number 13: 108 observations,
                                        complexity param=0.01353413
    mean=7.168571, MSE=0.1054698
```

```
##
     left son=26 (39 obs) right son=27 (69 obs)
##
     Primary splits:
##
         processor_name splits as ---RR----LR, improve=0.19120930, (0 missing)
                                                 improve=0.15777240, (0 missing)
##
         display_size
                        < 15.8
                                  to the left,
##
         cluster
                        splits as L--L-RLLL,
                                                 improve=0.12301120, (0 missing)
##
         brand
                        splits as
                                   LRLLRLL,
                                                 improve=0.09585890, (0 missing)
##
                                                 improve=0.08480929, (0 missing)
         റട
                        splits as
                                   RRL,
##
     Surrogate splits:
##
         processor_brand splits as
                                    LRR,
                                                agree=0.898, adj=0.718, (0 split)
##
         cluster
                         splits as
                                    L--R-RRRL, agree=0.704, adj=0.179, (0 split)
##
                                                agree=0.657, adj=0.051, (0 split)
         brand
                         splits as
                                    LRLRRRR,
##
                         splits as
                                     -RLR-R,
                                                agree=0.657, adj=0.051, (0 split)
         ram type
##
                         splits as
         os_bit
                                    LR,
                                                agree=0.657, adj=0.051, (0 split)
##
## Node number 14: 32 observations
##
     mean=7.464709, MSE=0.07727019
##
## Node number 15: 19 observations
    mean=7.926265, MSE=0.1098771
##
##
## Node number 24: 22 observations,
                                        complexity param=0.03220955
##
     mean=6.162695, MSE=0.3764164
     left son=48 (15 obs) right son=49 (7 obs)
##
##
     Primary splits:
##
         star_rating
                         < 4.1
                                   to the left,
                                                 improve=0.6259276, (0 missing)
##
         processor_brand splits as LRL,
                                                 improve=0.5654994, (0 missing)
##
                         splits as R-RRLRL,
                                                 improve=0.2535976, (0 missing)
         brand
##
                         < 52
                                   to the right, improve=0.1595410, (0 missing)
         ratings
##
         reviews
                         < 9.5
                                   to the right, improve=0.1595410, (0 missing)
##
     Surrogate splits:
##
                         splits as ---L--RL-,
                                                 agree=0.909, adj=0.714, (0 split)
         cluster
##
         graphic_card_gb < 2</pre>
                                   to the left,
                                                 agree=0.864, adj=0.571, (0 split)
                                                 agree=0.818, adj=0.429, (0 split)
##
         brand
                         splits as R-LRLRL,
                                                 agree=0.818, adj=0.429, (0 split)
##
         processor brand splits as LRL,
##
         display_size
                         < 15.36 to the left, agree=0.773, adj=0.286, (0 split)
##
## Node number 25: 258 observations,
                                         complexity param=0.01869464
##
     mean=6.774869, MSE=0.0651179
##
     left son=50 (216 obs) right son=51 (42 obs)
##
     Primary splits:
                                              improve=0.17907190, (0 missing)
##
         ram_type
                      splits as RL-RRR,
##
         Touchscreen
                      splits as LR,
                                              improve=0.15686400, (0 missing)
##
                      < 2.5
                               to the right, improve=0.10946810, (0 missing)
         ratings
##
         star_rating < 0.8
                               to the right, improve=0.09652365, (0 missing)
##
                               to the left, improve=0.09615770, (0 missing)
         display_size < 15.8
##
     Surrogate splits:
##
         OS
                     splits as RRL,
                                             agree=0.872, adj=0.214, (0 split)
##
                     splits as LRLLLLL,
                                             agree=0.841, adj=0.024, (0 split)
                              to the left, agree=0.841, adj=0.024, (0 split)
##
         star_rating < 4.85
##
## Node number 26: 39 observations
     mean=6.97968, MSE=0.04893071
##
##
## Node number 27: 69 observations,
                                        complexity param=0.01186462
##
     mean=7.275335, MSE=0.1058613
##
     left son=54 (42 obs) right son=55 (27 obs)
```

```
##
     Primary splits:
##
                                                  improve=0.2613956, (0 missing)
         display_size
                         < 15.8
                                  to the left,
##
         cluster
                         splits as L--L-RLLR,
                                                  improve=0.1052999, (0 missing)
                                                  improve=0.1037542, (0 missing)
##
         processor_brand splits as RLR,
                         splits as ---LR----R, improve=0.1037542, (0 missing)
##
         processor_name
##
                                  to the right, improve=0.0797980, (0 missing)
         ratings
                         < 3.5
##
     Surrogate splits:
##
         processor_brand splits as
                                    RLL,
                                                  agree=0.725, adj=0.296, (0 split)
##
                                    ---LL----R, agree=0.725, adj=0.296, (0 split)
         processor_name
                         splits as
##
         ssd_cat
                         splits as
                                    RL,
                                                  agree=0.710, adj=0.259, (0 split)
##
         brand
                                    LLRLRLL,
                                                  agree=0.696, adj=0.222, (0 split)
                         splits as
##
         Touchscreen
                         splits as
                                    LR,
                                                  agree=0.696, adj=0.222, (0 split)
##
## Node number 48: 15 observations
     mean=5.831106, MSE=0.05287271
##
##
## Node number 49: 7 observations
    mean=6.873242, MSE=0.3292376
##
## Node number 50: 216 observations,
                                        complexity param=0.01249174
     mean=6.727252, MSE=0.04898566
##
##
     left son=100 (193 obs) right son=101 (23 obs)
     Primary splits:
##
##
         Touchscreen
                         splits as LR,
                                                 improve=0.18999010, (0 missing)
##
         cluster
                         splits as L--R-RLLR,
                                                 improve=0.11033980, (0 missing)
##
                         < 25
                                  to the right, improve=0.10179550, (0 missing)
        ratings
##
         display_size
                         < 15.8
                                  to the left,
                                                improve=0.09614241, (0 missing)
##
         graphic_card_gb < 1</pre>
                                  to the left, improve=0.09077926, (0 missing)
##
     Surrogate splits:
##
         warranty < 2.5
                           to the left, agree=0.903, adj=0.087, (0 split)
##
## Node number 51: 42 observations
    mean=7.019756, MSE=0.07645314
##
##
## Node number 54: 42 observations
     mean=7.14196, MSE=0.07555488
##
##
## Node number 55: 27 observations
    mean=7.482808, MSE=0.08228808
##
##
## Node number 100: 193 observations
##
    mean=6.693949, MSE=0.03826758
##
## Node number 101: 23 observations
    mean=7.006708, MSE=0.05152147
```

Basic Laptop Price Regression Tree



Basic Tree and Pruned Tree Model Fit Summary (values identical):

[1] "The R^2 value of pruned tree is 0.648006191517393" [1] "The RMSE value of pruned tree is 342.789650527593" [1] "The R^2 value of pruned tree in log scale is 0.737397757156823" [1] "The RMSE value of pruned tree in log scale is 0.261736301177269"

```
## [1] "Basic Decision Tree Model Summary:"
## [1] "The R^2 value of basic tree is 0.648006191517393"
## [1] "The RMSE value of basic tree is 342.789650527593"
## [1] "The R^2 value of basic tree in log scale is 0.737397757156823"
## [1] "The RMSE value of basic tree in log scale is 0.261736301177269"
##
## Regression tree:
## rpart(formula = log_latest_price ~ ., data = pred.laptop.train,
##
      parms = list(split = "information"), control = rpart.control(minsplit = 20))
##
## Variables actually used in tree construction:
  [1] cluster
                      display_size
                                   processor_name ram_type
                                                                    star_rating
  [6] Touchscreen
##
## Root node error: 160.93/597 = 0.26956
##
## n= 597
```

```
##
##
            CP nsplit rel error xerror
                                              xstd
## 1
     0.366548
                         1.00000 1.00602 0.064127
  2
      0.173446
                     1
                         0.63345 0.70296 0.060585
##
  3
                    2
##
      0.094531
                         0.46001 0.56873 0.054772
                         0.36548 0.41078 0.034274
##
  4
      0.047207
##
  5
      0.032210
                         0.31827 0.35511 0.032876
##
  6
      0.023560
                         0.28606 0.34830 0.032892
## 7
      0.018695
                    6
                         0.26250 0.32348 0.030717
## 8
     0.015782
                         0.24380 0.32120 0.030900
## 9 0.013534
                    8
                         0.22802 0.31098 0.030933
## 10 0.012492
                    9
                         0.21449 0.29348 0.030883
## 11 0.011865
                   10
                         0.20200 0.28778 0.030565
## 12 0.010000
                         0.19013 0.27737 0.030073
## [1] 0.01
##
    processor_name
                            cluster
                                            ssd_cat graphic_card_gb
                                                                         display_size
##
        90.8721761
                         54.4265141
                                         11.2820669
                                                          10.0768284
                                                                            6.1913430
   processor_brand
                              brand
                                        star_rating
                                                            ram_type
                                                                           ram_gb_cat
##
         5.7321403
                          5.5959114
                                          5.2550370
                                                           5.1933107
                                                                            4.3162652
```

Pruned Laptop Price Regression Tree

ratings

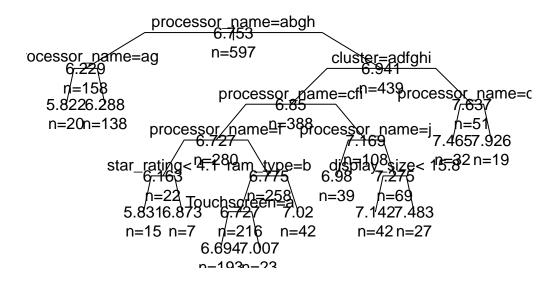
2.5012649

Touchscreen

2.4345657

warranty

0.1748058



##

##

##

##

os

4.0798443

os_bit 0.1116931 reviews

3.2199162

- ## [1] "The RMSE value of pruned tree is 342.789650527593"
- ## [1] "The R^2 value of pruned tree in log scale is 0.737397757156823"
- ## [1] "The RMSE value of pruned tree in log scale is 0.261736301177269"

Below is a table of variable importance from the pruned decision tree model:

##	<pre>processor_name</pre>	cluster	ssd_cat	<pre>graphic_card_gb</pre>	display_size
##	90.8721761	54.4265141	11.2820669	10.0768284	6.1913430
##	processor_brand	brand	star_rating	ram_type	ram_gb_cat
##	5.7321403	5.5959114	5.2550370	5.1933107	4.3162652
##	os	reviews	ratings	Touchscreen	warranty
##	4.0798443	3.2199162	2.5012649	2.4345657	0.1748058
##	os_bit				
##	0.1116931				

Ensemble Random Forest with Default Parameters

Analysis of Validation Metrics Compared to Linear Models

Our first attempt at an ensemble method gave us better results than a single tree. It was also superior to our initial StepAIC model.

Random Forest Model Fit Summary:

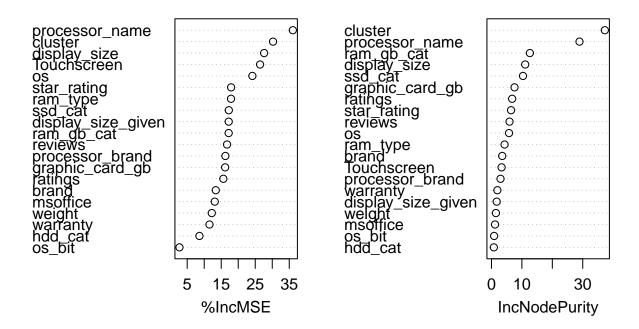
[1] "The R^2 value of Random Forest is 0.783106449815662" [1] "The RMSE value of Random Forest is 275.955222895206" [1] "The R^2 value of Random Forest in log scale is 0.856022265086323" [1] "The RMSE value of Random Forest in log scale is 0.191797362743207"

Important variables and their interpretations:

Processor name followed by cluster and ssd_cat had the most predictive power (most impact on %IncMSE). Our feature creation is further validated here.

##		%IncMSE	${\tt IncNodePurity}$
##	brand	0.0059684506	3.5434391
##	processor_brand	0.0153051988	2.9744342
##	processor_name	0.0923899754	28.9346092
##	ram_type	0.0087423660	4.3039938
##	os	0.0216309357	5.7705393
##	os_bit	0.0006633697	0.8664901
##	<pre>graphic_card_gb</pre>	0.0204087236	7.5760371
##	weight	0.0042694026	1.4592317
##	display_size	0.0275332441	11.0879834
##	warranty	0.0036213301	1.9348522
##	Touchscreen	0.0095114446	3.3301613
##	msoffice	0.0028293931	1.1686366
##	star_rating	0.0149630137	6.4254561
##	ratings	0.0206146725	6.7990646
##	reviews	0.0157708219	5.9301584
##	display_size_given	0.0064951843	1.7197173
##	ram_gb_cat	0.0225982440	12.6229860
##	ssd_cat	0.0214271808	10.3615372
##	hdd_cat	0.0017975182	0.7782949
##	cluster	0.0872089169	37.2697937

laptop.train.rf

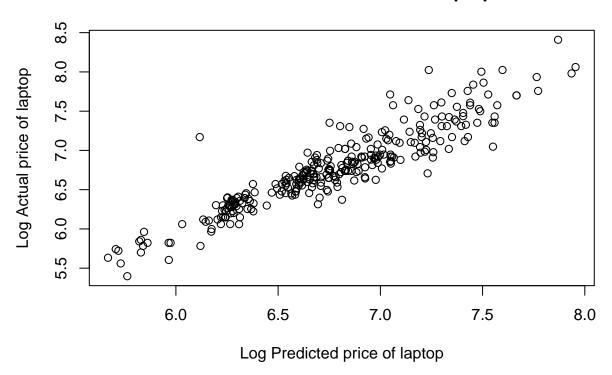


[1] "The most predictive variable with regard to price is:"

##

processor_name

Plot of Predictions vs. Actual for Laptop Price



- ## [1] "The R^2 value of Random Forest is 0.783106449815662"
- ## [1] "The RMSE value of Random Forest is 275.955222895206"
- ## [1] "The R^2 value of Random Forest in log scale is 0.856022265086323"
- ## [1] "The RMSE value of Random Forest in log scale is 0.191797362743207"

Ensemble Method - Use Caret to Set Up a Computer Experiment and Tune XGBoost

Analysis of Validation Metrics and Tuning Strategy Used

Next, we decided to expand our analysis to using XGBoost (known to have exceptional predictive power). We used the caret package to set up a grid and ran an experiment across a few parameters to find one of the best tuned XGBoost. XGBoost ended up delivering on its promise and gave us the best model (lowest RMSE and highest R^2) of all the ones we had tried out:

XGboost Model Fit Summary:

[1] "The R^2 value for XGboost is 0.848757272940201" [1] "The RMSE value of XGboost is 227.363013941365" [1] "The R^2 value for XGboost in log scale is 0.875737860057181" [1] "The RMSE value of XGboost in log scale is 0.177554536560491"

Below are the tuning steps we followed:

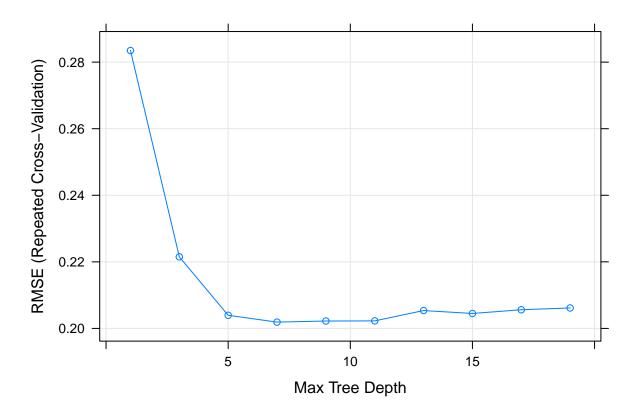
- 1. We defined our tuning parameters to be chosen via 5 fold cross-validation repeated 5 times.
- 2. We ran 100 iterations of boosting while running our grid search across various hyper parameters.
- 3. We chose a learning rate of 0.1 and searched for the max depth of trees by reviewing our reduction in RMSE. This gave us a max-depth of 9.

Important variables and their interpretations:

Analysis of important variables showed that laptop cluster 8 was providing the best predictive power followed by ram being below 1gb. Other variables such as ram, display size, and ram < 1 gb were also important. All of the important variables were suggesting that our clustering exercise and various treatments on multilevel variables and missing data treatment were useful.

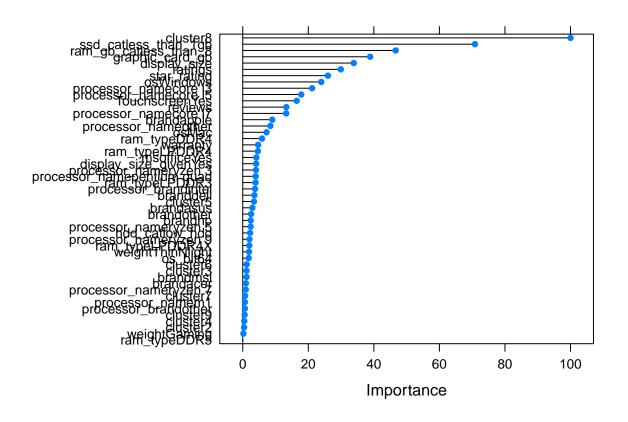
We also applied a partial dependence calculation to understand the direction/sign of associations across the top variables. Our partial dependence plot showcased the following:

- 1. We saw that higher performance factors such as RAM being higher than 8 gb and ssd greater than 1 gb were associated with highly priced laptops. Additionally, laptops with higher graphic card specs had higher average prices.
- 2. It is interesting to observe that as display sizes increased beyond 15.5 inches average prediction of prices went up a lot and then it came down when the display size was around 17.5 inches. This is perhaps an indication that customers are willing to pay higher for an optimal display size of laptops.
- 3. Lastly laptops not belonging to cluster8 had higher average price predictions. We investigated the reasons behind this a bit further and observed that the centers across the 3 variables used for clustering (ram, sdd and graphic card) were usually lower for cluster8. Hence, we can conclude that low performance laptops are priced lower.

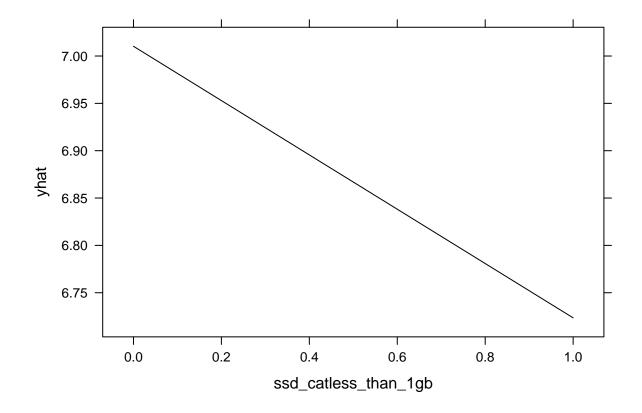


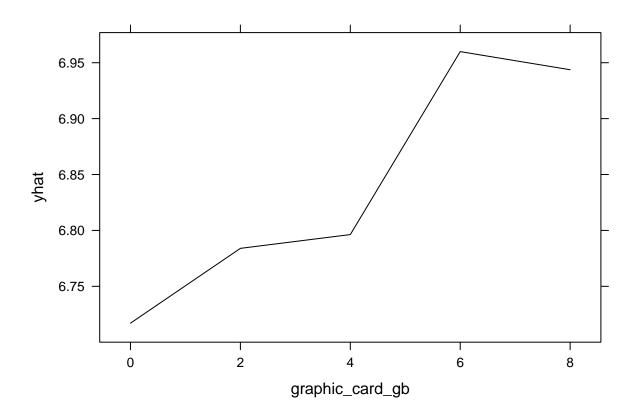
```
## xgbTree variable importance
##
## only 20 most important variables shown (out of 49)
##
## Overall
## cluster8 100.000
## ssd_catless_than_1gb 70.847
```

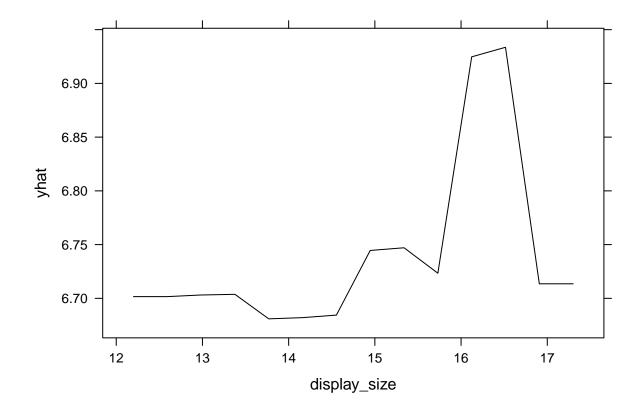
```
## ram_gb_catless_than_8 46.651
## graphic_card_gb
                          38.878
## display_size
                          33.874
## ratings
                          29.922
## star_rating
                          25.994
## osWindows
                          23.958
## processor_namecore i3 21.165
## processor_namecore i5 17.858
## TouchscreenYes
                          16.475
## reviews
                          13.303
## processor_namecore i7 13.261
## brandapple
                           9.018
## processor_nameother
                           8.435
## osMac
                           7.264
## ram_typeDDR4
                           5.880
## warranty
                           4.700
## ram_typeLPDDR4
                           4.615
## msofficeYes
                           4.138
```

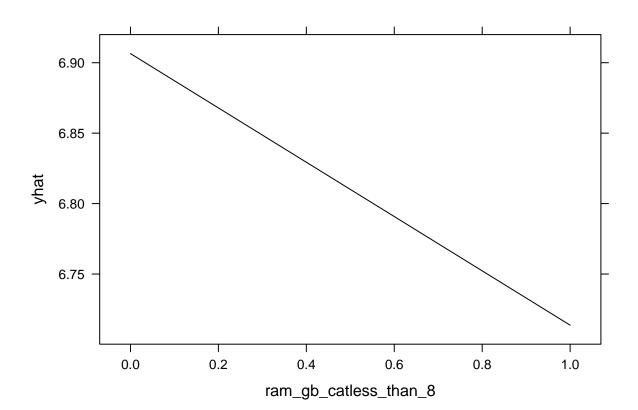


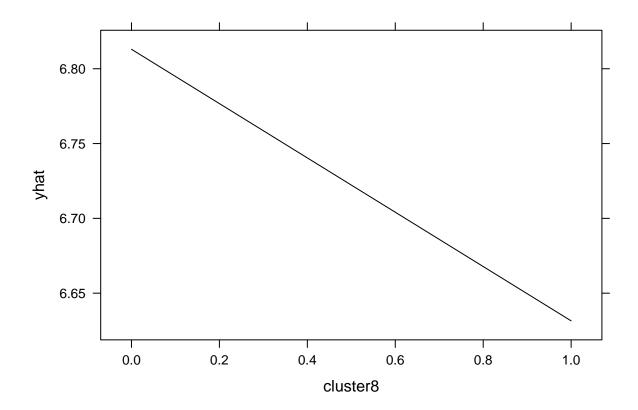
- ## [1] "The R^2 value for XGboost is 0.848757272940201"
- ## [1] "The RMSE value of XGboost is 227.363013941365"
- ## [1] "The R^2 value for XGboost in log scale is 0.875737860057181"
- ## [1] "The RMSE value of XGboost in log scale is 0.177554536560491"











```
##
         ram_gb
                        ssd graphic_card_gb
## 1 -0.3749096
                 0.36593430
                                 -0.5825943
     1.8175269
                 1.96985951
                                 -0.4353101
    -0.2044961 -1.36759329
                                   2.7754842
      1.8055490 -0.01880008
                                   1.5980072
  5
     1.8055490
                 2.13434446
                                  2.3861764
     1.7067312 0.13484168
                                  -0.4291087
## 7 -0.3364735 -1.04207616
                                  0.9612901
## 8 -0.5800469 -0.88112711
                                  -0.5825943
## 9 -0.3907221 0.62804222
                                   1.1966508
```

In conclusion, it is wise to review multiple predictive model methodologies when trying to model a particular y variable as results can vary. While our best performing model (XGboost) is still not as accurate as we would like, it is clear that it is a powerful tool for predictive analysis. We are confident the models we presented could be improved with the addition of other explanatory variables and more data points.