Show all of your work on this assignment and answer each question fully in the given context. You have 20 minutes. Each problem is designed to take 10 minutes. All answers in a topic must be correct for any credit for that topic. You may attempt multiple topics. You may use a calculator on this competency quiz.

## 1. Competency Topic: Discrete Random Variables

Let X be a random variable following a binomial distribution with probability function

$$f(x) = \frac{4!}{x!(4-x)!}(0.6)^x(0.4)^{4-x}$$

.

a. Complete the probability table for X.

$\boldsymbol{x}$	P(X=x)
0	
1	
2	
3	
4	

b. Find the value of E(X).

c. Sketch the cumulative probability function, F(x).

## 2. Competency Topic: Continuous Random Variables

Let X be a random variable with the following probability density function:

$$f(x) = \begin{cases} k \cdot x^3 & 0 \le x \le 2\\ 0 & o.w. \end{cases}$$

for some constant k.

a. Find the value of k that makes f(x) a valid pdf.

b. Sketch the probability density function and illustrate the region corresponding to the value of  $P(1 \le X \le 2)$ .

c. Find the value of E(X).