

Show **all** of your work on this assignment and answer each question fully in the given context.

*Please staple your assignment!!*

1. Chapter 5, Problem 37 (page 331 - ask if the “hint” in part d is confusing)
2. Chapter 5, Problem 33 (page 330 - this is a good example of CQ style problems)
3. Chapter 5, Problem 35 (page 330 notice that if  $y \leq x$ , then  $f(x, y) = 0$ )
4. Suppose that  $Z_1, Z_2, \dots, Z_n$  are  $n$  independent standard normal random variables. It may be helpful to recall that  $E(aZ_i + b) = aE(Z_i) + b$  and that  $Var(aZ_i + b) = a^2Var(Z_i)$  for any constants  $a, b$  in addition to knowing that  $\sum_{i=1}^n i = \frac{n(n+1)}{2}$  and  $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$ .
  - a. Find the expected value and variance of  $X$  where  $X = 3Z_1 + 5$
  - b. Find the expected value and variance of  $Y$  where  $Y = Z_1 - Z_2$
  - c. Find the expected value and variance of  $U$  where  $U = Z_1 - Z_1$
  - d. Find the expected value and variance of  $W$  where  $W = \sum_{i=1}^n \frac{i}{n} (Z_i + \frac{i}{n})$ .