STAT 105 Exam I Reference Sheet

Numeric Summaries

$$\sigma^2 = \frac{1}{n} \sum_{n}$$

$$\sigma^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$

 $\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$

population standard deviation
$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^{n} \left(x_i - \bar{x}\right)^2}$$

$$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2}$$

sample standard deviation

$$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})^2}$$

Linear Relationships

$$y \approx \beta_0 + \beta_1 x$$

$$\hat{y} = b_0 + b_1 x$$

Least squares estimates
$$b_1 = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^n (x_i - \bar{x})^2}$$

$$b_1 = \frac{\sum_{i=1}^n x_i y_i - n\bar{x}\bar{y}}{\sum_{i=1}^n x_i^2 - n\bar{x}^2}$$

$$b_0 = \bar{y} - b_1 \bar{x}$$

$$b_0 = \bar{y} - b_1$$

$$e_i = y_i - \hat{y}_i$$

Residuals

sample correlation coefficient
$$r = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 \sum_{i=1}^n (x_i - \bar{x})^2}}$$

$$r = \frac{\sum_{i=1}^{n} x_{i} y_{i} - n \bar{x} \bar{y}}{\sqrt{\left(\sum_{i=1}^{n} x_{i}^{2} - n \bar{x}^{2}\right)\left(\sum_{i=1}^{n} y_{i}^{2} - n \bar{y}^{2}\right)}}$$

 $R^2 = (r)^2$

$$\frac{\sum_{i=1}^{n}(y_{i}-\bar{y})^{2}-\sum_{i=1}^{n}(y_{i}-\hat{y}_{i})^{2}}{\sum_{i=1}^{n}(y_{i}-\bar{y})^{2}}$$

Multivariate Relationships

$$y \approx \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \ldots + \beta_k x_k$$

Fitted relationship
$$\hat{y} \approx b_0 + b_1 x_1 + b_2 x_2 + \ldots + b_k x_k$$

$$e_i = y_i - \hat{y}_i$$

Residuals

$$SSTO = \sum_{i=1}^{n} (y_i - \bar{y})^2$$

Sums of Squares

$$SSE = \sum_{i=1}^{n} (y_i - \hat{y}_i)^2$$

$$SSR = SSTO - SSE = \sum_{i=1}^{n} (\hat{y}_i - \bar{y})^2$$

 $R^2 = \frac{\sum_{i=1}^{n} (y_i - \bar{y})^2 - \sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{\sum_{i=1}^{n} (y_i - \bar{y})^2}$

coeffecient of determination

$$R^2 = \frac{\text{SSTO} - \text{SSE}}{\text{SSTO}}$$

$$R^2 = \frac{\text{SSR}}{\text{SSTO}}$$

$$\frac{\sum_{i=1}^{n}(y_{i}-\bar{y})^{2}-\sum_{i=1}^{n}(y_{i}-\hat{y}_{i})^{2}}{\sum_{i=1}^{n}(y_{i}-\bar{y})^{2}}$$

Functions

 $x_1 \le x_2 \le \ldots \le x_n$ and value p where $0 \le p \le 1$, let $i = \lfloor n \cdot p + 0.5 \rfloor$. Then the quantile function at p is: Quantile Function Q(p) For a dataset consisting of n values that are ordered so that

$$Q(p) = \begin{cases} x_i & [n \cdot p + 0.5] = n \cdot p + 0.5 \\ x_i + (n \cdot p - i + 0.5)(x_{i+1} - x_i) & [n \cdot p + 0.5] \neq n \cdot p + 0.5 \end{cases}$$