STAT 305 Quiz II Reference Sheet

Numeric Summaries

mean
$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

population variance
$$\sigma^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$

population standard deviation
$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{x})^2}$$

sample variance
$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

sample standard deviation
$$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})^2}$$

Linear Relationships

Form
$$y \approx \beta_0 + \beta_1 x$$

Fitted linear relationship
$$\hat{y} = b_0 + b_1 x$$

Least squares estimates
$$b_1 = \frac{\sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^{n} (x_i - \bar{x})^2}$$

$$b_1 = \frac{\sum_{i=1}^{n} x_i y_i - n\bar{x}\bar{y}}{\sum_{i=1}^{n} x_i^2 - n\bar{x}^2}$$

$$b_0 = \bar{y} - b_1 \bar{x}$$

Residuals
$$e_i = y_i - \hat{y}_i$$

sample correlation coeffecient
$$r = \frac{\sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^{n} (x_i - \bar{x})^2 \sum_{i=1}^{n} (x_i - \bar{x})^2}}$$

$$r = \frac{\sum_{i=1}^{n} x_i y_i - n\bar{x}\bar{y}}{\sqrt{\left(\sum_{i=1}^{n} x_i^2 - n\bar{x}^2\right)\left(\sum_{i=1}^{n} y_i^2 - n\bar{y}^2\right)}}$$

coeffecient of determination
$$R^2 = (r)^2$$

$$\frac{\sum_{i=1}^{n} (y_i - \bar{y})^2 - \sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{\sum_{i=1}^{n} (y_i - \bar{y})^2}$$

Multivariate Relationships

Form $y \approx \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \ldots + \beta_k x_k$

Fitted relationship $\hat{y} \approx b_0 + b_1 x_1 + b_2 x_2 + \ldots + b_k x_k$

Residuals $e_i = y_i - \hat{y}_i$

Sums of Squares $SSTO = \sum_{i=1}^{n} (y_i - \bar{y})^2$

$$SSE = \sum_{i=1}^{n} (y_i - \hat{y}_i)^2$$

$$SSR = SSTO - SSE = \sum_{i=1}^{n} (\hat{y}_i - \bar{y})^2$$

 $\text{coeffecient of determination} \quad R^2 = \frac{\sum_{i=1}^n (y_i - \bar{y})^2 - \sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2}$

$$R^2 = \frac{\text{SSTO} - \text{SSE}}{\text{SSTO}}$$

$$R^2 = \frac{\text{SSR}}{\text{SSTO}}$$

$$\frac{\sum_{i=1}^{n} (y_i - \bar{y})^2 - \sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{\sum_{i=1}^{n} (y_i - \bar{y})^2}$$

Functions

Quantile Function Q(p) For a univariate sample consisting of n values that are ordered so that $x_1 \leq x_2 \leq \ldots \leq x_n$ and value p where $0 \leq p \leq 1$, let $i = \lfloor n \cdot p + 0.5 \rfloor$. Then the quantile function at p is:

$$Q(p) = x_i + (n \cdot p + 0.5 - i)(x_{i+1} - x_i)$$