Example: [Concrete beams]

10 concrete beams were each measured for flexural strength (MPa). The data is as follows.

Null ~-13 -- [1] 8.2 8.7 7.8 9.7 7.4 7.8 7.7 11.6 11.3 11.8

The sample mean was 9.2 MPa and the sample variance Alternative

P-value

was 3.0933 MPa. Conduct a hypothesis test to find out if the flexural strength is different from 9.0 MPa. at a = 0.0

2.0=0.0

1. Ho: $\mu = 9$ US. Ha: $\mu \neq 9$

Level

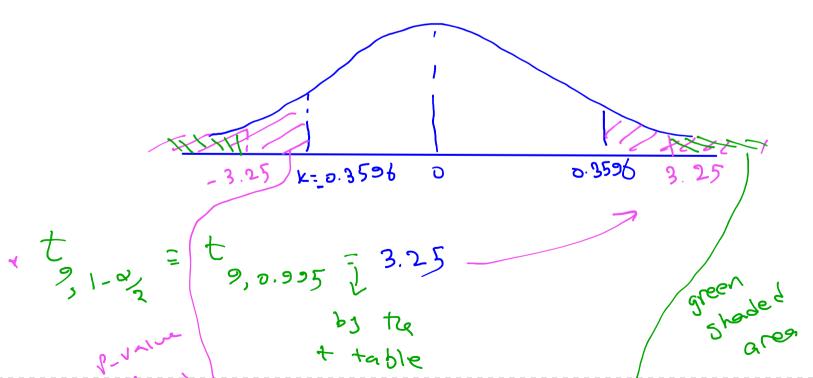
3. n=10 (225) + & is Unknown. 50

 $k = \frac{x - \mu_0}{s}$ (we know that $k \sim t$)

t-STUZENT

assumption Rigalso: X,, -, X, i'd N(M, er2)

4.
$$K = \frac{\bar{X} - r^{\circ}}{S_{1n}} = \frac{9.2 - 9}{\sqrt{\frac{9.0933}{10}}} = 0.3596$$



by t-table = f(|T| > 0.3596) > P(|T|>t 9,0.995)

P-value

Q=0.91

5. Since P-value is 2 d = 0.01, we Fail to loget to null Hypothesis (Ho)

6. There is NoT enough evidence to conclude that the tree near flexural strength of the beams is different from 9 Mpa.

Hypothesis Testing Heing Confidence Interval

Hypothesis testing using the CI

Null

We can also use the $1-\alpha$ confidence interval to perform hypothesis tests (instead of p-values). The confidence interval will contain μ_0 when there is little to no evidence against H_0 and will not contain μ_0 when there is strong evidence against H_0 .

Alternative

P-value

Hypothesis testing using the Cl

Null

Steps to perform a hypothesis test using a confidence interval:

Alternative Harmonian P-value 1. State H_0 and H_1 2. State α , significance level 1. State α and α 2. State α are significance level 1. State α 3. State the form of α 4. State the form of α 6. State α 4. State the form of α 6. State α 6. State α 8. State the form of α 6. State α 8. State the form of α 9. CI along α 1. State α 8. State the form of α 9. CI along α 1. State α 1. State α 2. State α 3. State the form of α 9. CI along α 1. State α 2. State α 3. State the form of α 1. State α 3. State the form of α 1. State α 2. State α 3. State α 3. State the form of α 1. State α 2. State α 3. State α 3. State α 3. State α 4. State α 3. State α 4. State α 5. State α 6. State α 7. State α 7. State α 8.

1. State H_0 and H_1

with all assumptions necessary. (use onesided CI for one-sided tests and two-sided CI for two sided tests)

4. Calculate the CI

- 5. Based on 100 (1-lpha) % CI, either reject H_0 (if μ_0 is not in the interval) or fail to reject (if μ_0 is in the interval)
- 6. Interpret the conclusion in the content of the problem

CI method

Null

P-value CLT

Example:[Breaking strength of wire, cont'd]

Suppose you are a manufacturer of construction equipment. You make 0.0125 inch wire rope and need to determine how much weight it can hold before breaking so that you can label it clearly. You have breaking Alternative strengths, in kg, for 41 sample wires with sample standard deviation breaking strength 91.85 kg and sample standard deviation 17.6 kg. Using the appropriate 95% confidence interval, conduct a hypothesis test to find out if the true mean breaking strength is above 85 kg.

Hypothesis Testing base 4

Example:[Breaking strength of wire, cont'd]

Null

> 3- One-sided test and we care about the lower bound. So, we use $(\overline{X}-z_{1-\alpha}\frac{s}{\sqrt{n}},+\infty)$.

Alternative

4- From the example in previous set of slides, the CI is $(87.3422, +\infty)$.

P-value

5- Since $\mu_0=85$ is not in the CI, we **reject** H_0 .

CI method

6- There is significant evidence to conclude that the true mean breaking strength of wire is greater than the 85kg. Hence the requirement is met.

Ha: M> 85

Example: [Concrete beams, cont'd]

10 concrete beams were each measured for flexural strength (MPa). The data is as follows.

[1] 8.2 8.7 7.8 9.7 7.4 7.8 7.7 11.6 11.3 11.8
$$\rightarrow \overline{x} = \frac{1}{10} \sum_{i=1}^{\infty} x_i - \frac{1}{2} \frac{1}{10} x_i$$

The sample mean was 9.2 MPa and the sample variance Alternative $\frac{3}{5}$ = was $\frac{3.0933}{4}$ (MPa)². At $\alpha = 0.01$, test the hypothesis that the true mean <u>flex</u>ural strength is 10 MPa using a confidence interval. Steps:

P-value

P-value
$$\begin{array}{c} \text{Considence interval, steps.} \\ \hline \begin{array}{c} 1\text{-}\ H_0:\ \mu=10 \ vs. \end{array} & H_1:\ \mu\not\equiv 10 \\ \hline \end{array}$$

$$2 - \alpha = 0.01$$



3- This is two-sided test with n=10 and 100 (1-lpha) % CI is

$$(\overline{X})t_{(n-1,1-\alpha/2)}\frac{s}{\sqrt{n}},\overline{X})t_{(n-1,1-\alpha/2)}\frac{s}{\sqrt{n}})$$

) two_sided test = two_sided c]

one-sided test = one-sided c7

Example:[Breaking strength of wire, cont'd]

4- Check that the CI is (7.393, 11.007)

5- Since $\mu_0=10$ is within the CI, we **fail** to reject H_0 .

Null

Alternative

P-value

CI method

6- There is **not enough evidence** to conclude that the true mean flexural strength is different from 10 Mpa.

Example:[Paint thickness, cont'd]

Consider the following sample of observations on coating thickness for low-viscosity paint.

Null

[1] 0.83 0.88 0.88 1.04 1.09 1.12 1.29 1.31 1.48 1.49 1.59 1.62 1.65 1.71 [13] 1.76 1.83

Alternative

Using $\alpha=0.1$ test the hypothesis that the true mean paint thickness is 1.00 mm. Note, the 90\% confidence interval for the true mean paint thickness was calculated from before as (1.201, 1.499).

P-value

CI method

3- This is two-sided test with
$$n=16$$
, σ unknown, so $100~(1-\alpha)$ % CI is

1- $H_0: \;\; \mu=1$ $vs. \quad H_1: \;\; \mu
eq 1$

 $2 - \alpha = 0.1$

Null

Alternative

P-value

CI method

Example:[Breaking strength of wire, cont'd]

4- The CI is (1.201, 1.499).

5- Since $\mu_0=1$ is not in the CI, we **reject** H_0 .

6- There is enough evidence to conclude that the true mean paint thickness is not 1mm.

