

# Quiz IV

## STAT 305, Section 7 SPRING 2020

### Instructions

- The quiz is scheduled for 80 minutes, from 09:30 to 10:50 AM. At 10:50 AM the exam will end.
- Total points for the exam is 60. Points for individual questions are given at the beginning of each problem. Show all your calculations clearly to get full credit. Put final answers in the box at the right (except for the diagrams!).
- A formula sheet is attached to the end of the exam. Feel free to tear it off.
- Normal quantile table is attached to the end of the exam. Feel free to tear it off.
- You may use a calculator during this exam.
- Answer the questions in the space provided. If you run out of room, continue on the back of the page.
- If you have any questions about, or need clarification on the meaning of an item on this exam, please ask your instructor. No other form of external help is permitted attempting to receive help or provide help to others will be considered cheating.
- **Do not cheat on this exam.** Academic integrity demands an honest and fair testing environment. Cheating will not be tolerated and will result in an immediate score of 0 on the exam and an incident report will be submitted to the dean's office.

Name: \_\_\_\_\_

Student ID: \_\_\_\_\_

1. A small military subcontractor has secured a contract to develop drones capable of providing light air support for smaller naval vessels. Successfully fulfilling the contract requires that the drone be able to takeoff with a minimum runway of 10 meters. However, late changes in the prototype's weight distribution have led to concerns that they are no longer satisfying this requirement. Using 100 takeoffs, they found the average distance before takeoff was 9.92 meters with a standard deviation of 0.4 meters.

(a) (4 points) Provide a two-sided 95% confidence interval for the true average distance before takeoff.

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- (b) (4 points) Provide a 90% lower bound confidence interval for the true average distance before take-off.
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- (c) (10 points) Conduct a hypothesis test at the  $\alpha = 0.01$  significance level for  $\mu$ , the true average distance before takeoff with the null hypothesis  $\mu \geq 10$  against the alternative hypothesis of  $\mu < 10$ . Include the hypothesis statement, the test statistic, the p-value, and the conclusion.  
Note: Write down all six steps for full credit.

2. An inspector examining the dependability of a certain gas pump fills 50 containers until the pump reads 1.00 gallons. If the pump is completely accurate, then each container should have 1.00 gallons of gasoline. However, since nothing is completely consistent, there will be differences from one container to the next. Suppose that it is known that the true standard deviation of the amount of gasoline the pump recognizes as 1.00 gallons is  $\sigma = 0.2$  gallons.

The average of the 50 gallon samples is  $\bar{x} = 0.992$  gallons

The following table may be useful:

Table 1: z's for use in **Two-sided** Large- $n$  intervals for the mean

Desired Confidence	$z$
80%	1.28
90%	1.645
95%	1.96
98%	2.33
99%	2.58

- (a) (4 points) Provide a two-sided 90% confidence interval for the mean volume of gasoline recognized by the pump to be 1.00 gallons.

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- (b) (4 points) Provide a one-sided upper bound 95% confidence interval for the mean volume of gasoline recognized by the pump to be 1.00 gallons.

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- (c) (10 points) Conduct a hypothesis test at the  $\alpha = 0.05$  significance level for  $\mu$ , the true mean volume of gasoline recognized by the pump with the null hypothesis  $\mu = 1$  against the alternative hypothesis of  $\mu \neq 1$ . Include the hypothesis statement, the test statistic, the p-value, and the conclusion.  
Note: Write down all six steps for full credit.



