Quiz IV

STAT 305, Section 7 SPRING 2020

Instructions

- The quiz is scheduled for 100 minutes on April 23, 2020. You can start anytime between 01:00 04:00 PM, but your MUST SUBMIT YOUR ANSWER WITHIN 100 MINUTES.
- Total points for the exam is 64. Points for individual questions are given at the beginning of each problem. Show all your calculations clearly to get full credit. Put final answers in the box at the right (except for the diagrams!).
- A formula sheet is attached to the end of the exam. Feel free to tear it off.
- Normal quantile table is attached to the end of the exam. Feel free to tear it off.
- You may use a calculator during this exam.
- Answer the questions in the space provided. If you run out of room, continue on the back of the page.
- If you have any questions about, or need clarification on the meaning of an item on this exam, please ask your instructor. No other form of external help is permitted attempting to receive help or provide help to others will be considered cheating.
- Do not cheat on this exam. Academic integrity demands an honest and fair testing environment. Cheating will not be tolerated and will result in an immediate score of 0 on the exam and an incident report will be submitted to the dean's office.

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(c) (10 points) Conduct a hypothesis test at the $\alpha=0.01$ significance level for μ , the true average distance before takeoff with the null hypothesis $\mu\geq 10$ against the alternative hypothesis of $\mu<10$. Include the hypothesis statement, the test statistic, the p-value, and the conclusion. Note: Write down all six steps for full credit.

2. An inspector examining the dependability of a certain gas pump fills 50 containers until the pump reads 1.00 gallons. If the pump is completely accurate, then each container should have 1.00 gallons of gasoline. However, since nothing is completely consistent, there will be differences from one container to the next.

Suppose that it is known that the true standard deviation of the amount of gasoline the pump recognizes as 1.00 gallons is $\sigma = 0.2$ gallons.

The average of the 50 gallon samples is $\bar{x} = 0.992$ gallons

The following table may be useful:

Table 1: z's for use in **Two-sided** Large-n intervals for the mean

Desired Confidence	z
80%	1.28
90%	1.645
95%	1.96
98%	2.33
99%	2.58

(a) (4 points) Provide a two-sided 90% co	onfidence interval for the mean	volume of gasolin	e recognized
by the pump to be 1.00 gallons.	(,)

(b) (4 points) Provide a one-sided upper bound 95% confidence of the confidence o	idence interval f	or the mean vol	ume of gasoline
recognized by the pump to be 1.00 gallons.	(,)

(c) (10 points) Conduct a hypothesis test at the $\alpha=0.05$ significance level for μ , the true mean volume of gasoline recognized by the pump with the null hypothesis $\mu=1$ against the alternative hypothesis of $\mu\neq 1$. Include the hypothesis statement, the test statistic, the p-value, and the conclusion. Note: Write down all six steps for full credit.

3. O-rings are elastomer loops designed to create a seal between the interface of two parts of a mechanical device. Because the elasticity of the material used to make them can be impacted by temperature (which can lead to the seal being broken) it is important to make sure that the O-ring is functional at the temperatures the part they are used in will be exposed to. Two composites (Composite X and Composite Y) are being tested in an O-ring that will be used in a part of a satellite that will be exposed to very low temperatures. A sample of 50 O-rings from each composite are placed in a chamber, where the temperature is gradually reduced until the seal is broken. Suppose that each composite has some mean failure temperature, μ_X for Composite X and μ_Y for Composite Y, and some variance in failure temperature, σ_X^2 for Composite X and σ_Y^2 for Composite Y. Before any observations are recorded, we can consider the sampled values from Composite X to be random variables X_1, X_2, \ldots, X_{50} with $\mathbb{E}(X_i) = \mu_X$ and $Var(X_i) = \sigma_X^2$. We can also consider the sampled values from Composite Y to be random variables Y_1, Y_2, \ldots, Y_{50} with $\mathbb{E}(Y_i) = \mu_Y$ and $Var(Y_i) = \sigma_Y^2$.

Let $\bar{X} = \frac{1}{50}X_1 + \frac{1}{50}X_2 + \ldots + \frac{1}{50}X_{50}$ and let $\bar{Y} = \frac{1}{50}Y_1 + \frac{1}{50}Y_2 + \ldots + \frac{1}{50}Y_{50}$.

After running the O-ring experiment, the researchers found $\bar{x}=50$ K and $\bar{y}=53$ K. Suppose that $\sigma_X=10$ and $\sigma_Y=20$.

(a) (4 points) Provide a two-sided 90% confidence interval for μ_X .

Hint: Consider the **Large** sample size and **known** variances σ_y and σ_X

(b) (4 points) Provide a one-sided lower bound 99% confidence interval for μ_X .

(c) (4 points) Provide a two-sided 95% confidence interval for μ_Y .

(d) (6 points) Provide a two-sided 95% confidence interval for $\mu_X - \mu_Y$. Does this provide any evidence that one O-ring is better than the other?

Hint: Consider the Large sample size and known variances σ_y and σ_X

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(e) (10 points) Conduct a hypothesis test at the $\alpha=0.05$ significance level for the claim that the difference between the true means of the two O-rings $(\mu_X-\mu_Y)$ are significantly different from zero.

Note: Write down all six steps for full credit.

Hint: Consider the **Large** sample size and **known** variances σ_y and σ_X