EXPLANATIONS •

TYPE-I

- 1. (3) Using Rule 1, Required number
 - $= \frac{LCM \times HCF}{First number}$
 - $=\frac{864\times144}{288}=432$
- **2.** (3) Using Rule 1, $LCM \times HCF = 1st Number \times 2nd$ Number
 - \Rightarrow 225 × 5 = 25 × x

$$\therefore x = \frac{225 \times 5}{25} = 45$$

- **3.** (3) Using Rule 1, Given that
 - L.C.M. of two numbers = 1820H.C.F. of those numbers = 26One of the number is 130
 - : Another number

$$=\frac{1820\times26}{130}=364$$

- **4.** (2) Using Rule 1,
 - We have.

First number × second number = LCM \times HCF

- : Second number

$$=\frac{1920\times16}{128}=240$$

5. (1) Using Rule 1,

Product of two numbers

- = HCF \times LCM
- $\Rightarrow 12906 \times 14818$
- $= LCM \times 478$

$$\Rightarrow LCM = \frac{12906 \times 14818}{478}$$

- = 400086
- **6.** (4) Using Rule 1,

H.C.F. of the two 2-digit numbers

Hence, the numbers can be expressed as 16x and 16y, where *x* and *y* are prime to each other.

First number × second number = $H.C.F. \times L.C.M.$

 $\Rightarrow 16x \times 16y = 16 \times 480$

$$\Rightarrow xy = \frac{16 \times 480}{16 \times 16} = 30$$

The possible pairs of x and y, satisfying the condition xy = 30 are: (3, 10), (5, 6), (1, 30), (2, 15)

Since the numbers are of 2-digits each.

Hence, admissible pair is (5, 6)

- \therefore Numbers are : 16 × 5 = 80 and $16 \times 6 = 96$
- 7. (2) Using Rule 1,

We know that,

First number \times Second number

- = LCM \times HCF
- ⇒ Second number

$$=\frac{16 \times 160}{32} = 80$$

8. (2) Using Rule 1,

$$LCM = \frac{Product of two numbers}{HCF}$$

$$=\frac{4107}{37}=111$$

Obviously, numbers are 111 and 37 which satisfy the given condition.

Hence, the greater number = 111

9. (2) Using Rule 1,

First number × Second number $= HCF \times LCM$

.. Second number

$$= \frac{15 \times 300}{60} = 75$$

- **10.** (3) Let the numbers be 12x and 12y where x and y are prime to each other.
 - \therefore LCM = 12xy
 - $\therefore 12xy = 924$
- $\Rightarrow xy = 77$
- \therefore Possible pairs = (1,77) and (7,11)
- **11.** (3) Using Rule 1,

First number × second number = LCM \times HCF

Let the second number be x.

 $10x = 30 \times 5$

$$\Rightarrow x = \frac{30 \times 5}{10} = 15$$

12. (1) Using Rule 1,

 $HCF \times LCM = Product of two$ numbers

 \Rightarrow 8 × LCM = 1280

$$\Rightarrow$$
 LCM = $\frac{1280}{8}$ = 160

13. (4) Using Rule 1,

First number × second number = HCF \times LCM

 \Rightarrow 24 × second number = 8 × 48

 $\therefore \text{ Second number} = \frac{8 \times 48}{24} = 16$

14. (2) Using Rule 1,

First number \times second number

- = HCF \times LCM
- ⇒ 84 × second number
- $= 12 \times 336$
- .. Second number

$$= \frac{12 \times 336}{84} = 48$$

- **15.** (4) Let the numbers be 6x and 6y where x and y are prime to each other.
 - $\therefore 6x \times 6y = 216$

$$\Rightarrow xy = \frac{216}{6 \times 6} = 6$$

- :. LCM = $6xy = 6 \times 6 = 36$
- **16.** (1) Using Rule 1, Second number

$$= \frac{HCF \times LCM}{First number}$$

- $=\frac{18\times378}{54}=126$
- 17. (3) Let the number be 15x and 15y, where x and y are co-prime.
 - $\therefore 15x \times 15y = 6300$

$$\Rightarrow xy = \frac{6300}{15 \times 15} = 28$$

- So, two pairs are
- (7, 4) and (14, 2)
- 18. (4) Using Rule 1,

First number × Second number = HCF \times LCM

- \Rightarrow 75 × Second number $= 15 \times 225$
- : Second number

$$= \frac{15 \times 225}{75} = 45$$

19. (1) Using Rule 1,

First number × second number = HCF \times LCM

- \Rightarrow 52 × second number
 - $= 4 \times 520$
- ⇒ Second number

$$= \frac{4 \times 520}{52} = 40$$

20. (4) Using Rule 1,

First number × Second number = HCF \times LCM

- ⇒ 864 × Second number
- = $96 \times 1296 \Rightarrow$ Second number

$$= \frac{96 \times 1296}{864} = 144$$

21. (2) Using Rule 1,

Let LCM be L and HCF be H, then

$$L = 4H$$

$$\Rightarrow H = \frac{125}{5} = 25$$

$$\therefore L = 4 \times 25 = 100$$

: Second number

$$= \frac{L \times H}{\text{First number}}$$

$$= \frac{100 \times 25}{100} = 25$$

- **22.** (1) HCF of two-prime numbers = 1
 - \therefore Product of numbers = their LCM = 117
 - $117 = 13 \times 9$ where 13 & 9 are co-prime. L.C.M (13,9) = 117.
- **23.** (2) HCF = 12

Numbers = 12x and 12y

where x and y are prime to each other.

 $\therefore 12x \times 12y = 2160$

$$\Rightarrow xy = \frac{2160}{12 \times 12}$$

 $= 15 = 3 \times 5, 1 \times 15$

Possible pairs = (36, 60) and (12, 180)

24. (1) Using Rule 1,

Second number

$$= \frac{\text{H.C.F.} \times \text{L.C.M.}}{\text{First Number}}$$

$$=\frac{27\times2079}{189}=297$$

25. (2) Here, HCF = 13

Let the numbers be 13x and 13y where x and y are Prime to each other.

Now, $13x \times 13y = 2028$

$$\Rightarrow xy = \frac{2028}{13 \times 13} = 12$$

The possible pairs are: (1, 12), (3, 4), (2, 6)

But the 2 and 6 are not co-prime.

 \therefore The required no. of pairs = 2

26. (2) HCF = 13

Let the numbers be 13x and 13y. Where x and y are co-prime.

$$\therefore xy = \frac{455}{13} = 35 = 5 \times 7$$

 \therefore Numbers are $13 \times 5 = 65$ and $13 \times 7 = 91$

27. (4) HCF of two numbers is 8.

This means 8 is a factor common to both the numbers. LCM is common multiple for the two numbers, it is divisible by the two numbers. So, the required answer = 60

- **28.** (4) Let the numbers be 23x and 23y where x and y are co-prime.
 - ∴ LCM = 23 xy

As given,

$$23xy = 23 \times 13 \times 14$$

- x = 13, y = 14
- \therefore The larger number = 23y
- $= 23 \times 14 = 322$
- **29.** (4) LCM = 2 × 2 × 2 × 3 × 5 Hence, HCF = 4, 8, 12 or 24 According to question 35 cannot be H.C.F. of 120.
- **30.** (3) Using Rule 1,

First number = $2 \times 44 = 88$

- \therefore First number \times Second number
- = $H.C.F. \times L.C.M.$
- \Rightarrow 88 × Second numebr
- $= 44 \times 264$
- \Rightarrow Second number

$$= \frac{44 \times 264}{88} = 132$$

TYPE-II

- **1.** (3) Using Rule 4, L.C.M. of 4, 6, 8, 12 and 16 = 48
 - :. Required number
 - =48 + 2 = 50
- **2.** (4) Using Rule 4, LCM of 15, 12, 20, 54 = 540

Then number = 540 + 4 = 544 [4 being remainder]

3. (4) Using Rule 4,

The greatest number of five digits is 99999.

LCM of 3, 5, 8 and 12

 $\therefore LCM = 2 \times 2 \times 3 \times 5 \times 2 = 120$ After dividing 99999 by 120, we

get 39 as remainder 99999 – 39 = 99960

99999 - 39 = 9996

 $= (833 \times 120)$

99960 is the greatest five digit number divisible by the given divisors.

In order to get 2 as remainder in each case we will simply add 2 to 99960.

- :. Greatest number
- = 99960 + 2 = 99962

4. (3) Using Rule 4,

LCM of 4, 5, 6, 7 and 8

 $= 2 \times 2 \times 2 \times 3 \times 5 \times 7 = 840.$

let required number be 840 K + 2 which is multiple of 13.

Least value of K for which (840 K + 2) is divisible by 13 is K = 3

- \therefore Required number
- $= 840 \times 3 + 2$
- = 2520 + 2 = 2522
- **5.** (4) Required time = LCM of 252, 308 and 198 seconds

	1,	1,	1
11	1,	11,	11
9	9,	11,	99
7	63,	77,	99
2	126,	154,	99
2	252,	308	198

- \therefore LCM = $2 \times 2 \times 7 \times 9 \times 11$
- = 2772 seconds
- = 46 minutes 12 seconds

6. (2)
$$15 = 3 \times 5$$

$$18 = 3^2 \times 2$$

$$21 = 3 \times 7$$

$$24 = 2^3 \times 3$$

LCM = $8 \times 9 \times 5 \times 7 = 2520$ The largest number of four digit

The largest number of four digits = 9999

2520)9999(3

$$\frac{7560}{2439}$$

Required number

$$= 9999 - 2439 - 4 = 7556$$

(Because

$$15 - 11 = 4$$

$$18 - 14 = 4$$

 $21 - 17 = 4$

$$24 - 20 = 4$$

- **7.** (3) LCM of 21, 36 and 66
 - $\therefore LCM = 3 \times 2 \times 7 \times 6 \times 11$
 - = $3 \times 3 \times 2 \times 2 \times 7 \times 11$ \therefore Required number
 - $= 3^2 \times 2^2 \times 7^2 \times 11^2$
 - = 213444
- **8.** (1) Using Rule 5,

Here
$$4 - 1 = 3$$
, $5 - 2$

- = 3, 6 3 = 3
- \therefore The required number
- = LCM of (4, 5, 6) 3
- = 60 3 = 57

- **9.** (2) LCM of 4, 6, 10, 15 = 60 Least number of 6 digits
 - = 100000

The least number of 6 digits which is exactly divisible by 60 = 100000 + (60 - 40)

- = 100020
- : Required number (N)
 - = 100020 + 2 = 100022

Hence, the sum of digits = 1 + 0+0+0+2+2=5

10. (3) The LCM of 12, 18, 21, 30

- \therefore LCM = 2 × 3 × 2 × 3 × 7 × 5
- = 1260
- :. The required number

$$=\frac{1260}{2}=630$$

11. (4) We find LCM of = 10, 16, 24

2	10,	16,	24
2	5,	8,	12
2	5,	4,	6
2	5,	2,	3,
3	5,	1,	3
5	5,	1,	1
	1,	1,	1

- \therefore LCM = $2^2 \times 2^2 \times 3 \times 5$
- .. Required number
- $= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 5$ = 3600
- 12. (2) Required number of students = LCM of 6, 8, 10 = 120
- **13.** (2) LCM of 4, 6, 8, 9

2	4,6,8,9
$\overline{2}$	2,3,4,9
3	1,3,2,9
	1,1,2,3

- $\therefore LCM = 2 \times 2 \times 3 \times 2 \times 3 = 72$
- ∴ Required number = 72, because it is exactly divisible by 4, 6, 8 and 9 and it leaves remainder 7 when divided by 13.
- **14.** (2) Using Rule 5,

Here, 12 - 5 = 7,

$$16 - 9 = 7$$

- :. Required number
- = (L.C.M. of 12 and 16) 7
- = 48 7 = 41

15. (3) Using Rule 5,

Here, Divisor - remainder = 1e.g., 10 - 9 = 1, 9 - 8 = 1, 8 - 7 = 1

- .. Required number
- = (L.C.M. of 10, 9, 8) -1= 360 - 1 = 359
- **16.** (4) We find LCM of 5, 6 and 8 5 = 5
 - $6 = 3 \times 2$
 - $8 = 2^3$
 - $= 2^3 \times 3 \times 5 = 8 \times 15 = 120$

Required number = 120K + 3

 \therefore when K = 2, 120 × 2 + 3 = 243 required no.

It is completely divisible by 9

- **17.** (4) LCM of 16, 18, 20 and 25 = 3600
 - :. Required number = 3600K + 4 which is exactly divisible by 7 for certain value of K.

When K = 5.

number = $3600 \times 5 + 4$

= 18004 which is exactly divisible by 7.

- **18.** (2) LCM of 3, 5, 6, 8, 10 and 12 = 120
 - ∴ Required number
 - = 120x + 2, which is exactly divisible by 13.

 $120x + 2 = 13 \times 9x + 3x + 2$ Clearly 3x + 2 should be divisible by 13.

For x=8,3x+2 is divisible by 13.

- ∴ Required number
- $= 120x + 2 = 120 \times 8 + 2$
- = 960 + 2 = 962
- 19. (4) LCM of 6, 9, 15 and 18

- \therefore LCM = 2 × 3 × 3 × 5 = 90
- \therefore Required number = 90k + 4, which must be a multiple of 7 for some value of k.

For k = 4,

Number = $90 \times 4 + 4 = 364$, which is exactly divisible by 7.

20. (2) Using Rule 9,

We will find the LCM of 16, 24, 30 and 36.

2	16,	24,	30,	36
2	8,	12,	15,	18
2	4,	6,	15,	9
3	2,	3,	15,	9
	2	1	5	3

 \therefore LCM = 2 × 2 × 2 × 3 × 2 × 5 $\times 3 = 720$

The largest number of five digits = 99999

On dividing 99999 by 720, the remainder = 639

- : The largest five-digit number divisible by 720
- = 99999 639 = 99360
- \therefore Required number = 99360 + 10 = 99370
- **21.** (2) LCM of 5, 10, 12, 15

- \therefore LCM = 2 × 3 × 5 × 2 = 60
- \therefore Number = 60k + 2

Now, the required number should be divisible by 7.

Now, $60k + 2 = 7 \times 8k + 4k + 2$ If we put k = 3, (4k + 2) is equal to 14 which is exactly divisible

- \therefore Required number = $60 \times 3 + 2$ = 182
- **22.** (3) LCM of 9, 10 and 15 = 90
 - ⇒ The multiple of 90 are also divisible by 9, 10 or 15.
 - $\therefore 21 \times 90 = 1890$ will be divisible by them.
 - ∴ Now, 1897 will be the number that will give remainder 7.

1936 - 1897

Required number

= 1936 - 1897 = 39

- **23.** (1) The difference between the divisor and the corresponding remainder is same in each case ie. 18 - 5 = 13, 27 - 14 = 13, 36 - 23 = 13
 - ∴ Required number
 - = (LCM of 18, 27, and 36) 13 = 108 - 13 = 95
- **24.** (2) The LCM of 5, 6, 7 and 8 = 840
 - \therefore Required number = 840 k + 3 which is exactly divisible by 9 for some value of k.

Now, 840 k + 3 = 93×9 k + (3k)

When k = 2, 3k + 3 = 9, which is divisible by 9.

- : Required number
- $= 840 \times 2 + 3 = 1683$

25. (1) Using Rule 5,

Here,
$$12 - 2 = 10$$
; $16 - 6 = 10$; $24 - 14 = 10$

Now, LCM of 12, 16 and 24 = 48

- \therefore The greatest 4-digit number exactly divisible by 48 = 9984
- :. Required number
- = 9984 10 = 9974
- 26. (1) Using Rule 5,

LCM of 15, 20 and 35 = 420

- :. Required least number
- = 420 + 8 = 428
- **27.** (3) Using Rule 5,

The smallest number divisible by 12 or 10 or 8

- = LCM of 12, 10 and 8 = 120
- \Rightarrow Required number = 120 + 6
- **28.** (2) LCM of 24, 36 and 54 seconds
 - = 216 seconds
 - = 3 minutes 36 seconds
 - :. Required time = 10 : 15 : 00 +
 - 3 minutes 36 seconds
 - = 10 : 18 : 36 a.m.
- 29. (3) A makes one complete round

of the circular track in
$$\frac{5}{\frac{5}{2}}$$

= 2 hours

B in
$$\frac{5}{3}$$
 hours and C in $\frac{5}{2}$ hours.

That is after 2 hours A is at the

starting point, B after $\frac{5}{3}$ hours

and C after $\frac{5}{2}$ hours.

Hence the required time

= LCM of 2,
$$\frac{5}{3}$$
 and $\frac{5}{2}$ hours

$$= \frac{LCM \text{ of } 2, 5, 5}{HCF \text{ of } 3, 2}$$

$$=\frac{10}{1}$$
 = 10 hours.

- **30.** (1) Required time = LCM of 200, 300, 360 and 450 seconds
 - = 1800 seconds
- **31.** (1) LCM of 4, 6, 8, 14
 - = 168 seconds
 - = 2 minutes 48 seconds

They ring again at 12 + 2 min. 48 sec.

= 12 hrs. 2 min. 48 sec.

- **32.** (4) $1\frac{1}{2}$ hours = 90 minutes
 - 1 hour and 45 minutes
 - = 105 minutes
 - 1 hour = 60 minutes
 - .. LCM of 30 minutes, 60 minutes, 90 minutes and 105 minutes

<u>3</u>	30,	60,	90,	105
5	10,	20,	30,	35
$\overline{2}$	2,	4,	6,	7
	1.	2.	3.	$\overline{7}$

 $\therefore LCM = 3 \times 5 \times 2 \times 2 \times 3 \times 7$ = 1260 minutes

$$1260 \text{ minutes} = \frac{1260}{60} = 21 \text{ hours}$$

- \therefore The bell will again ring simultaneously after 21 hours.
- ∴ Time will be
- = 12 noon + 21 hours = 9 a.m.
- **33.** (1) The LCM of 5, 6, 8 and 9 = 360 seconds = 6 minutes
- **34.** (2) LCM of 20, 30 and 40 minutes = 120 minutes

Hence, the bells will toll together again after 2 hours i.e. at 1 p.m.

35. (1) The difference between divisor and the corresponding remainder is equal.

LCM of 3, 5, 7 and 9 = 315 Largest 4-digit number = 9999

315)9999(31

945

549

 $\frac{315}{234}$

- ∴ Number divisible by 315
- = 9999 234 = 9765

Required number

= 9765 - 2 = 9763

- **36.** (3) Required time = LCM of 6, 7, 8, 9 and 12 seconds
 - = 504 seconds
- **37.** (2) Using Rule 2,

LCM =
$$\frac{\text{LCM of 2, 4, 5}}{\text{HCF of 3, 9, 6}}$$

$$=\frac{20}{3}$$

38. (2) LCM of 3, 4, 5, 6, 7, 8 = 840

840)10000(11

840

1600

840

760

- Since, the remainder 760 is more than half of the divisor 840.
- \therefore The nearest number
- = 10000 + (840 760) = 10080
- **39.** (2) Using Rule 8,

The largest number of 4-digits is 9999. L.C.M. of divisors

 $LCM = 2 \times 2 \times 3 \times 3 \times 3 \times 5$

= 540

Divide 9999 by 540, now we get 279 as remainder.

9999 - 279 = 9720

Hence, 9720 is the largest 4-digit number exactly divisible by each of 12, 15, 18 and 27.

- **40.** (2) The smallest number divisible by 16, 20 and 24
 - = LCM of 16, 20 and 24

2	16,	20,	24
$\overline{2}$	8,	10,	12
$\overline{2}$	4,	5,	6
	2,	5,	3

- $\therefore LCM = 2 \times 2 \times 2 \times 2 \times 5 \times 3$
 - $= 2^2 \times 2^2 \times 5 \times 3$

∴ Required complete square number = $2^2 \times 2^2 \times 5^2 \times 3^2 = 3600$

41. (2) LCM of 25, 50 and 75 = 150

On dividing 43582 by 150, remainder = 82

150) 43582 (290

300

1358

1350

82

∴ Required number

=43582 + (150 - 82) = 43650

42. (2) Required number = (LCM of 24, 32, 36 and 54) – 5 Now,

2	24,	32,	36,	54
2	12,	16,	18,	27
2	6,	8,	9,	27
3	3,	4,	9,	27
3	1,	4,	3,	9
	1.	4.	1.	3

 $LCM = 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 4$ = 864

∴ Required number = 864 – 5 = 859

- **43.** (2) 2 | 20, 28, 32. 35 2 10, 14, 16. 35 5 5, 8, 35 $\overline{7}$ 7 7, 1, 8, 1, 1, 8, 1
 - \therefore LCM = $2 \times 2 \times 5 \times 7 \times 8$
 - = 1120
 - : Required number
 - = 5834 1120 = 4714
- 44. (4) The LCM of 6, 12 and 18 $= 36 = 6^2$
- **45.** (2) Using Rule 8, LCM of 10, 15 and 20 = 60Largest 4-digit number = 9999
 - :. 60)9999(166 60 399 360 399 360 39
 - ... Required number = 9999 - 39 = 9960
- **46.** (4) Using Rule 4,

Required number = (LCM of 15,20, 36 and 48) + 3

2	15,	20,	36,	48
$\overline{2}$	15,	10,	18,	24
3	15,	5,	9,	12
5	5,	5,	3,	4
	1,	1,	3,	4

- \therefore LCM = $2 \times 2 \times 3 \times 5 \times 3 \times 4$
- = 720
- :. Required number
- = 720 + 3 = 723
- **47.** (3) Required distance = LCM of 63, 70 and 77 cm.
 - = 6930 cm.

- \therefore LCM = $7 \times 9 \times 10 \times 11$ = 6930
- 48. (2) Required answer = LCM of 36, 40 and 48 seconds = 720 seconds
 - minutes = 12 minutes

Illustration: 2 | 36, 40, 48 2 18, 20, 24 2 9, 10, 12 3 9, 5, 6 3, 5, 2

 \therefore LCM = $2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5$ = 720

- **49.** (2) 2 | 60 2 30 3 15 5
 - $\therefore 60 = 2 \times 2 \times 3 \times 5$
 - i.e., Numbers = 2, 3, 4 and 5
 - ∴ Required sum = 2 + 3 + 4 + 5 = 14
- **50.** (1) LCM of x and y = 161
 - $\therefore xy = 23 \times 7$
 - x = 23; y = 7
 - $3y x = 3 \times 7 23$
 - = 21 23 = -2
- **51.** (1) Required time = LCM of 48, 72 and 108 seconds
 - 48, 72, 108 $\overline{2}$ 24, 36, 54 $\overline{2}$ 12, 18, 54 3 6, 9, 27 3 2, 3, 9 2, 1, 3
 - \therefore LCM = $2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3$ = 432 seconds

 - = 7 minutes 12 second
 - :. Required time
 - = 10:07:12 hours

TYPE-III

- 1. (1) Maximum number of students = The greatest common divisor = HCF of 1001 and 910 = 91
- **2.** (3) Using Rule 7, Required number = HCF of (989 - 5) and (1327 - 7) = HCF of 984 and 1320 = 24 ∴ HCF = 24
- 3. (2) Using Rule 3,

HCF of
$$\frac{2}{3}$$
, $\frac{4}{5}$ and $\frac{6}{7}$

- HCF of 2, 4 and 6 LCM of 3, 5 and 7

4. (1) Using Rule 7,

The greatest number N = HCF of (1305 - x), (4665 - x) and (6905)-x), where x is the remainder = HCF of (4665 - 1305), (6905-

- 4665) and
- (6905 1305)

= HCF of 3360, 2240 and 5600

Again,

$$1120)5600(5) \\ \underline{5600}_{\times}$$

- ∴ N = 1120
- Sum of digits
- = 1 + 1 + 2 + 0 = 4

5. (1) Using Rule 7, The number will be HCF of 307 -3 = 304 and

$$330 - 7 = 323.$$

- ∴ Required number = 19
- **6.** (3) Using Rule 7,

3026 - 11 = 3015 and

5053 - 13 = 5040

Required number = HCF of 3015 and 5040

$$3015) 5040 (1) \\ 3015 \\ 2025) 3015 (1) \\ 990) 2025 (2) \\ 1980 \\ \hline 45) 990 (22) \\ 90 \\ \hline 90 \\ \times$$

- :. Required number = 45
- **7.** (1) Using Rule 7,

We have to find HCF of (1657 - 6 = 1651) and

(2037 - 5 = 2032)

 $1651 = 13 \times 127$

 $2032 = 16 \times 127$

∴ HCF = 127

So, required number will be 127.

- 8. (1) Using Rule 7,
 - Let x be the remainder.

Then, (25 - x), (73 - x), and (97 - x) Will be exactly divisible by the required number.

- :. Required number
- = HCF of (73 x) (25 x),

(97-x)-(73-x)

and (97 - x) - (25 - x)

= HCF of (73 -25), (97 -73),

and

(97 - 25) = HCF of 48, 24 and

72 = 24

9. (2) Using Rule 7,

Required number

- = HCF of (110 2) and (128 2)
- = HCF of 108 and 126 = 18
- **10.** (3) Required maximum capacity of container

= HCF of 75 l and 45 l

Now, $75 = 5 \times 5 \times 3$

 $45 = 5 \times 3 \times 3$

∴ HCF = 15 litres

11. (4) Length of the floor

= 15 m 17 cm = 1517 cm

Breadth of the floor

= 9m 2 cm = 902 cm.

Area of the floor

 $= 1517 \times 902~\mathrm{cm}^2$

The number of square tiles will be least, when the size of each tile is maximum.

- ∴ Size of each tile = HCF of 1517 and 902 = 41
- .. Required number of tiles

$$= \frac{1517 \times 902}{41 \times 41} = 814$$

12. (1) Number of books in each stack = HCF of 336, 240, 96 = 48

96) 240 (2

192

48) 96(2

96

48) 96 (2

∴Total number of stacks

$$= \frac{336}{48} + \frac{240}{48} + \frac{96}{48}$$

=7 + 5 + 2 = 14

13. (3) First of all we find the HCF of 945 and 2475. HCF = 45 Illustration:

945)2475(2 1890

585)945(1 585

360)585(1 360

225)360(1 225 135)225(1

5)225(1 135 90)135(1

0)135(1 90 45)90(2 90 ×

∴ Maximum number of animals in each flock = 45

Required total number of flocks

$$=\frac{945}{45}+\frac{2475}{45}=21+55=76$$

14. (2) Maximum quantity in each can = HCF of 21, 42 and 63 litres = 21 litres

Required least number of cans

$$= \frac{21}{21} + \frac{42}{21} + \frac{63}{21}$$

$$= 1 + 2 + 3 = 6$$

15. (3) Using Rule 7,

Required number = HCF of 411

-3 = 408; 684 - 4 = 680 and

821 - 5 = 816

HCF of 408 and 816 = 408

HCF of 408 and 680

 $\frac{408}{272}$)408(1

 $\frac{(72)408(1)}{272}$

 $\overline{136}$) 272(2 $\underline{272}$

- ∴ Required number = 136
- **16.** (4) Required number = HCF of 200 and 320 = 40

Illustration:

80 × **17.** (3) As the height of each stack is same, the required number of books in each stack

= HCF of 84, 90 and 120

$$84 = 2 \times 2 \times 3 \times 7$$

$$90 = 2 \times 3 \times 3 \times 5$$

$$120 = 2 \times 2 \times 2 \times 3 \times 5$$

$$\therefore$$
 HCF = 2 × 3 = 6

18. (2) Using Rule 7,

Required number

- = HCF of (729 9)
- = 720 and (901 5)
- = 896

$$720$$
) 896 (1)

 $\frac{720}{176}$ 720 (4

$$H.C.F = 16$$

- **19.** (1) Greatest capacity of measuring vessel
 - = HCF of 403 litres, 434 litres and 465 litres
 - = 31 litres

Illustration:

HCF of 403 and 434

$$\begin{array}{r}
403)434 \left(1 \\
\underline{403} \\
31\right)403 \left(13 \\
\underline{31} \\
93 \\
\underline{93} \\
\underline{\times}
\end{array}$$

HCF of 31 and 465

- \Rightarrow 31 litres
- **20.** (3) Minimum number of rows = Maximum number of fruits in each row
 - ∴ HCF of 24, 36 and 60 = 12
 - : Minimum number of rows

$$= \frac{24}{12} + \frac{36}{12} + \frac{60}{12}$$

= 2 + 3 + 5 = 10

- **21.** (4) Using Rule 7, Required number = HCF of 2300 – 32 = 2268 and 3500 – 56 = 3444
 - $\begin{array}{c} 2268)3444(1\\ \underline{2268}\\ 1176)2268(1\\ \underline{1176}\\ 1092)1176(1\\ \underline{1092}\\ 84)1092(13\\ \underline{84}\\ 252\\ 252\\ \end{array}$
- ∴ HCF = 84
- **22.** (3) HCF of numbers = 12 Let the numbers be 12x and 12y where x and y are co-prime. According to the question, $12x \times 12y = 2160$

$$\Rightarrow xy = \frac{2160}{12 \times 12} = 15$$
$$= 3 \times 5 \text{ or } 1 \times 15$$

- :. Required numbers
- = 12 × 3 = 36 and 12 × 5 = 60 **23.** (2) Required number = HCF of 390, 495 and 300 = 15

Illustration:

HCF of 15 and 300 = 15 **24.** (4) First of all we find HCF of 391 and 323.

∴ Number of classes = 17 **25.** (3) Maximum length of each piece = HCF of 1.5 metre and 1.2 metre = 0.3 metre

Illustration:

∴ HCF of 1.5 and 1.2 metre = 0.3 metre

TYPE-IV

1. (1) L.C.M. of 28 and 42

$$\begin{array}{c|cccc}
2 & 28, & 42 \\
\hline
2 & 14, & 21 \\
\hline
7 & 7, & 21 \\
\hline
1, & 3
\end{array}$$

 $= 2 \times 2 \times 7 \times 3 = 84$ H.C. F. of 28 and 42

28)42(1 <u>28</u> 14)28(2 <u>28</u> 00

∴ H.C. F = 14

Required ratio = $\frac{84}{14}$ = 6:1

2. (3) Let the two numbers are 2x and 3x respectively.

According to question,

LCM = 54

$$x(3\times 2)=54$$

$$\Rightarrow$$
 x = 9

Numbers = $2x = 2 \times 9 = 18$ and, $3x = 3 \times 9 = 27$

 $Sum \ of \ the \ two \ numbers$

$$= 18 + 27 = 45$$

3. (3) Suppose the numbers are 4x and 5x respectively

According to question

$$x \times 4 \times 5 = 120$$

$$\Rightarrow$$
 x = 6

: Required numbers

$$= 4 \times 6 = 24$$

and =
$$5 \times 6 = 30$$

- **4.** (1) Let the numbers be 2x, 3x and 4x respectively.
 - \therefore HCF = x = 12
 - ∴ Numbers are : 2 ×12 = 24

$$3 \times 12 = 36, 4 \times 12 = 48$$

LCM of 24, 36, 48

$$= 2 \times 2 \times 2 \times 3 \times 3 \times 2 = 144$$

5. (3) Let the number be 3x and 4x. Their LCM = 12x

According to the question,

$$12x = 240$$

$$\Rightarrow x = \frac{240}{12} = 20$$

 $\therefore \text{ Smaller number} = 3x = 3 \times 20$ = 60

- **6.** (3) Let the numbers be 3x and 4x.
 - \therefore Their LCM = 12x
 - 12x = 84

$$\Rightarrow x = \frac{84}{12} = 7$$

: Larger number

$$=4x=4\times7=28$$

7. (1) Numbers = 3x and 4xHCF = x = 4

$$\therefore$$
 LCM = $12x = 12 \times 4 = 48$

8. (3) Let the numbers be 4x and 4y where x and y are prime to each other.

$$LCM = 4xy$$

$$\therefore \frac{\left(4x+4y\right)}{4xy} = \frac{7}{12}$$

$$\Rightarrow$$
 12 (x + y) = 7 xy

$$\Rightarrow x = 3, y = 4$$

∴ Smaller number

$$= 4 \times 3 = 12$$

9. (4) Using Rule 1,

Let the numbers be 3x and 4x respectively

First number \times second number

$$=$$
 HCF \times LCM

 $\Rightarrow 3x \times 4x = 2028$

$$\Rightarrow x^2 = \frac{2028}{3 \times 4} = 169$$

$$x = \sqrt{169} = 13$$

∴ Sum of the numbers

$$=3x + 4x = 7x = 7 \times 13 = 91$$

10. (3) If the numbers be 2x and 3x, then LCM = 6x

$$\therefore 6x = 48 \Rightarrow x = 8$$

- $\therefore \text{ Required sum} = 2x + 3x = 5x$ $= 5 \times 8 = 40$
- **11.** (4) Let the numbers be 4x and 5x.

$$\therefore$$
 H.C.F. = $x = 8$

 \therefore Numbers = 32 and 40

12. (2) If the numbers be 3x and 4x, then

$$HCF = x = 5$$

- ∴ Numbers = 15 and 20
- ∴ LCM = 60
- **13.** (1) Numbers = x, 2 x and 3 x (let) Their H.C.F. = x = 12
 - ∴ Numbers = 12, 24 and 36

14. (4) Using Rule 1,

Product of two numbers

- = HCF \times LCM
- \Rightarrow Numbers = zx and zy
- $\therefore zx \times zy = z \times LCM$
- \Rightarrow LCM = xyz
- **15.** (4) HCF of numbers = 21
 - \therefore Numbers = 21x and 21y Where x and y are prime to each other.

Ratio of numbers = 1:4

 \therefore Larger number = $21 \times 4 = 84$

TYPE-V

1. (4) Using Rule 1,

Let the numbers be x and (x + 2).

- ∴ Product of numbers
- $= HCF \times LCM$
- \Rightarrow x(x+2) = 24

$$\Rightarrow \qquad x^2 + 2x - 24 = 0$$

- $\Rightarrow x^2 + 6x 4x 24 = 0$
- $\Rightarrow x(x+6) 4(x+6) = 0$
- \Rightarrow (x-4)(x+6)=0
- \Rightarrow x = 4, as $x \neq -6 = 0$
- ... Numbers are 4 and 6.
- **2.** (1) Using Rule 1,

Suppose 1st number is x then,

2nd number

- = 100 x
- \therefore LCM \times HCF = 1st number \times 2nd number
- \Rightarrow 495 × 5 = x × (100 x)
- $\Rightarrow 495 \times 5 = 100x x^2$
- $\Rightarrow x^2 55x 45x 2475 = 0$
- \Rightarrow (x 45) (x 55) = 0
- $\Rightarrow x = 45 \text{ or } x = 55$

Then, difference = 55 - 45 = 10

3. (2) Let the number be 29x and 29y respectively

where x and y are prime to each other.

∴ LCM of 29x and 29y = 29xy Now, 29xy = 4147

$$\therefore xy = \frac{4147}{29} = 143$$

Thus $xy = 11 \times 13$

- ∴ Numbers are 29 × 11
- = 319 and $29 \times 13 = 377$
- ∴ Required sum
- = 377 + 319 = 696
- **4.** (4) Let HCF be h and LCM be l.

- Then, l = 84h and l + h
- = 680
- \Rightarrow 84h + h = 680

$$\Rightarrow h = \frac{680}{85} = 8$$

- l = 680 8 = 672
- ∴ Other number

$$= \frac{672 \times 8}{56} = 96$$

5. (2) HCF = 12

 \therefore Numbers = 12x and 12y where x and y are prime to each other.

- $\therefore 12x + 12y = 84$
- \Rightarrow 12 (x + y) = 84

$$\Rightarrow x + y = \frac{84}{12} = 7$$

- ∴ Possible pairs of numbers satisfying this condition
- = (1,6), (2,5) and (3,4). Hence three pairs are of required numbers.
- **6.** (3) Let the numbers be 21x and 21y where x and y are prime to each other.
 - $\therefore 21x + 21y = 336$
 - \Rightarrow 21 (x + y) = 336

$$\Rightarrow x + y = \frac{336}{21} = 16$$

- :. Possible pairs
- =(1, 15), (5, 11), (7, 9), (3, 13)
- **7.** (3) Let the number be *x* and *y*. According to the question,

$$x + y = 45$$
 (i)

Again,
$$x - y = \frac{1}{9}(x + y)$$

or
$$x - y = \frac{1}{9} \times 45$$

or x - y = 5 (ii)

By (i) + (ii) we have,

- x + y = 45
- x y = 5

$$2x = 50$$

- or, x = 25
- $\therefore y = 45 25 = 20.$

Now, LCM of 25 and 20 = 100.

8. (3) Let the numbers be 17x and 17y where x and y are co-prime. LCM of 17x and 17y = 17xy According to the question, 17xy = 714

$$\Rightarrow xy = \frac{714}{17} = 42 = 6 \times 7$$

- $\Rightarrow x = 6 \text{ and } y = 7$
- or, x = 7 and y = 6.
- \therefore First number = 17x
 - $= 17 \times 6 = 102$
 - Second number = 17y

$$=17 \times 7 = 119$$

- \therefore Sum of the numbers
 - = 102 + 119 = 221
- 9. (3) Using Rule 1,

Let the larger number be x.

- \therefore Smaller number = x 2
- ∴ First number × Second number = HCF × LCM
 - $\Rightarrow x(x-2) = 24$
 - $\Rightarrow x^2 2x 24 = 0$
 - $\Rightarrow x^2 6x + 4x 24 = 0$
 - $\Rightarrow x(x-6) + 4(x-6) = 0$
- \Rightarrow (x-6)(x+4)=0
- \Rightarrow x = 6 because $x \neq -4$
- **10.** (2) HCF of two numbers = 27
 - ∴ Let the numbers be 27*x* and 27*y* where *x* and *y* are prime to each other.

According to the question,

- 27x + 27y = 216
- \Rightarrow 27 (x + y) = 216

$$\Rightarrow x + y = \frac{216}{27} = 8$$

- \therefore Possible pairs of x and y = (1, 7) and (3, 5)
- \therefore Numbers = (27, 189) and (81, 135)
- **11.** (1) Using Rule 1,

Let the HCF of numbers = H

- ∴ Their LCM = 12H
- According to the question,

12H + H = 403

⇒13H = 403

$$\Rightarrow$$
 H = $\frac{403}{13}$ = 31

 \Rightarrow LCM = 12 × 31

Now,

First number × second number

- = HCF \times LCM
- $= 93 \times Second Number$
- $= 31 \times 31 \times 12$

Second number =
$$\frac{31 \times 31 \times 12}{93}$$
$$= 124$$

12. (3) Let the numbers be 48x and 48y where x and y are co-primes.

$$\therefore 48x + 48y = 384$$

$$\Rightarrow$$
 48 ($x + y$) = 384

$$\Rightarrow x + y = \frac{384}{48} = 8$$
(i)

Possible and acceptable pairs of x and y satisfying this condition are : (1, 7) and (3, 5).

- \therefore Numbers are : $48 \times 1 = 48$ and $48 \times 7 = 336$
- and $48 \times 3 = 144$ and $48 \times 5 = 240$
- \therefore Required difference
- = 336 48 = 288
- **13.** (3) Let the numbers be 3x and 3y.

$$\therefore 3x + 3y = 36$$

$$\Rightarrow x + y = 12$$

and
$$3xy = 105$$
 ... (ii)

Dividing equation (i) by (ii), we have

$$\frac{x}{3xy} + \frac{y}{3xy} = \frac{12}{105}$$

$$\Rightarrow \frac{1}{3y} + \frac{1}{3x} = \frac{4}{35}$$

- **14.** (4) Let the numbers be 10*x* and 10*y* where *x* and *y* are prime to each other.
 - ∴ LCM = 10 xu
 - $\Rightarrow 10xy = 120$
 - $\Rightarrow xy = 12$

Possible pairs = (3, 4) or (1, 12)

- \therefore Sum of the numbers = 30 + 40 = 70
- 30 + 40 70
- **15.** (3) Let the numbers be x, y and z which are prime to one another. Now, xy = 551

$$yz = 1073$$

- \therefore y = HCF of 551 and 1073
- $\therefore y = 29$

$$\therefore x = \frac{551}{29} = 19$$

and
$$z = \frac{1073}{29} = 37$$

- \therefore Sum = 19 + 29 + 37 = 85
- **16.** (3) HCF of two numbers = 4.

Hence, the numbers can be given by 4x and 4y where x and y are co-prime. Then,

$$4x + 4y = 36 \Rightarrow 4(x + y) = 36$$

$$\Rightarrow x + y = 9$$

Possible pairs satisfying this condition are: (1, 8), (4, 5), (2, 7)

- **17.** (2) Let the numbers be 2x and 2y where x and y are prime to each other.
 - \therefore LCM = 2xy
 - $\Rightarrow 2xy = 84$
 - $\Rightarrow xy = 42 = 6 \times 7$
 - ∴ Numbers are 12 and 14.

Hence Sum = 12 + 14 = 26

- **18.** (3) Let the numbers be *x* H and *y*H where H is the HCF and *y*H > *x* H.
 - \therefore LCM = xy H

$$\therefore xyH = 2yH \Rightarrow x = 2$$

Again, xH - H = 4

- \Rightarrow 2H H = 4 \Rightarrow H = 4
- \therefore Smaller number = xH = 8
- **19.** (4) Using Rule 1,

Let the H.C.F. be H.

∴ L.C.M. = 20H

Then, H + 20H = 2520

⇒ 21 H = 2520

$$\Rightarrow H = \frac{2520}{21} = 120$$

 \therefore L.C.M. = 20H = 20×120= 2400 As,

First number \times Second number = L.C.M. \times H.C.F.

- \Rightarrow 480 × Second number = 2400 × 120
- ⇒ Second number

$$= \frac{2400 \times 120}{480} = 600$$

20. (1) Using Rule 1,

If the HCF = H, then

LCM = 44 H

 \Rightarrow 45 H = 1125

$$\therefore H = \frac{1125}{45} = 25$$

$$\therefore$$
 LCM = 44 × 25 = 1100

Now

First number \times Second number

- = $LCM \times HCF$
- \Rightarrow 25 × Second number
- $=1100\times25$
- .. Second number

$$= \frac{1100 \times 25}{25} = 1100$$

21. (4) Let no. are *x* and *y* and HCF = A, LCM = B

Using Rule, we have

$$xy = AB$$

$$\Rightarrow x + y = A + B$$
 (given) ...(i)

$$(x-y)^2 = (x+y)^2 - 4xy$$

or,
$$(x-y)^2 = (A + B)^2 - 4 AB$$

or,
$$(x-y)^2 = (A - B)^2$$

or,
$$(x-y) = A - B$$
 ...(ii)

Using (i) and (ii), we get

$$x = A$$
 and $y = B$

$$A^3 + B^3 = x^3 + y^3$$

22. (3) Let the numbers be 7x and 7y where x and y are co-prime. Now, LCM of 7x and 7y = 7xy

$$\therefore 7xy = 140$$

$$\Rightarrow xy = \frac{140}{7} = 20$$

Now, required values of x and y whose product is 50 and are coprime, will be 4 and 5.

- \therefore Numbers are 28 and 35 which lie between 20 and 45.
- \therefore Required sum = 28 + 35 = 63.
- **23.** (4) Firstly, we find the LCM of 30, 36 and 80.

- $\therefore LCM = 2 \times 2 \times 3 \times 5 \times 3 \times 4$ = 720
- \therefore Required number = Multiple of $720 = 720 \times 5 = 3600$;

because 3000 < 3600 < 4000

24. (3) LCM of 5, 6, 7 and 8 = 840

- $\therefore LCM = 2 \times 5 \times 3 \times 7 \times 4 = 840$
- \therefore Required number = 840x + 3 which is divisible by 9 for a certain least value of x.

Now.

 $840x + 3 = 93x \times 9 + 3x + 3$

3x + 3, is divisible by 9 for x = 2

- \therefore Required number = 840 × 2
- = 1680 + 3 = 1683
- \therefore Sum of digits = 1 + 6 + 8 + 3 = 18
- **25.** (1) Using Rule 1,

∴ LCM = $2 \times 2 \times 3 \times 3 \times 7 = 252$ The largest 4-digit number = 9999

- : Required number
- = 9999 171 = 9828
- **26.** (4) LCM of 8, 12 and 16 = 48
 - ∴ Required number
 - = 48a + 3 which is divisible by 7.
 - $\therefore x = 48a + 3$
 - = $(7 \times 6a) + (6a + 3)$ which is divisible by 7.

i.e. 6a + 3 is divisible by 7. When a = 3, 6a + 3 = 18 + 3= 21 which is divisible by 7.

- $\therefore x = 48 \times 3 + 3 = 144 + 3 = 147$
- **27.** (1) 2 | 12, 16, 18, 21 2 | 6, 8, 9, 21 3 | 3, 4, 9, 21 1, 4, 3, 7
 - $\therefore LCM = 2 \times 2 \times 3 \times 4 \times 3 \times 7$ = 1008

Multiple of 1008 = 2016

- : Required number
- = 2016 2000 = 16 = x
- \therefore Sum of digits of x = 1 + 6 = 7
- **28.** (3) 2 | 12, 18, 21 3 | 6, 9, 21 2. 3. 7

.: LCM of 12, 18 and 21 = $2 \times 3 \times 2 \times 3 \times 7 = 252$ Of the options, $10080 \div 252 = 40$

29. (1)We find LCM of 30, 36 and 80.

- $\therefore LCM = 2 \times 2 \times 3 \times 3 \times 4 \times 5$ = 720
- :. Required number
- $= 2 \times 720 + 11$
- = 1440 + 11 = 1451

- **30.** (2) 2 | 12, 18, 21. 2 6, 9, 21, 16 3 3, 8 9, 21, 1, 3, 7. 8
 - $\therefore LCM = 2 \times 2 \times 3 \times 3 \times 7 \times 8$ = 2016
 - :. Required number
 - $= 2016 \times 2 = 4032$
- 31. (4) 2 | 210 3 | 105 5 | 35 7
 - $\therefore 210 = 2 \times 3 \times 5 \times 7 = 5 \times 6 \times 7$
 - \therefore Required answer = 5 + 6 = 11

TYPE-VI

- **1.** (3) Let the numbers be 12x and 12y.
 - \therefore Their LCM = 12xy when x and y are prime to each other.

$$y = \frac{1056}{132} = 8 [\because 12x = 132]$$

- \therefore Other number = 12y
- $= 12 \times 8 = 96$
- **2.** (2) When 36798 is divided by 78, remainder = 60
 - \therefore The least number to be subtracted = 60
- 3. (1) LCM of 18, 21 and 24

LCM = $2 \times 3 \times 3 \times 7 \times 4 = 504$ Now compare the divisors with their respective remainders. We observe that in all the cases the remainder is just 11 less than their respective divisor. So the number can be given by 504 K – 11. Where K is a positive integer Since $23 \times 21 = 483$

We can write 504 K - 11

- = (483 + 21) K 11
- = 483 K + (21 K 11)

 $483\,\mathrm{K}$ is multiple of 23, since 483 is divisible by 23.

So, for (504K-11) to be multiple of 23, the remainder (21K-11) must be divisible by 23.

Put the value of $K = 1, 2, 3, 4, 5, 6, \dots$ and so on successively. We find that the minimum value of K for which (21K - 11) is divisible by 23. is $6, (21 \times 6 - 11)$ = 115 which is divisible by 23.

Therefore, the required least number

- $= 504 \times 6 11 = 3013$
- **4.** (4) Using Rule 7, Clearly, 122 - 2 = 120 and 243 - 3 = 240 are exactly divisible by
 - the required number.
 ∴ Required number
 - = HCF of 120 and 240 = 120
- **5.** (2) $P = 2^3 \times 3^{10} \times 5$ $Q = 2^5 \times 3 \times 7$ $HCF = 2^3 \times 3$
- **6.** (4) Let the original fraction be $\frac{x}{y}$.

$$\therefore \frac{x-4}{y+1} = \frac{1}{6}$$

$$\Rightarrow 6x - 24 = y+1$$

$$\Rightarrow 6x - y = 25 \qquad \dots \dots (i)$$
Again,

$$\frac{x+2}{y+1} = \frac{1}{3}$$

- $\Rightarrow 3x + 6 = y + 1$
- $\Rightarrow 3x y = -5 \qquad(ii)$ By equation (i) (ii),
- 6x y 3x + y = 25 + 5 $\Rightarrow 3x = 30 \Rightarrow x = 10$
 - From equation (i),
 - $60 y = 25 \Rightarrow y = 35$ LCM of 10 and 35 = 70
- **7.** (4) HCF of *a* and b = 12
- \therefore Numbers = 12x and 12y where x and y are prime to each other.
 - $\therefore a > b > 12$
 - a = 36; b = 24
- **8.** (4) Let the numbers be 9x and 9y where x and y are prime to each other.

According to the question,

$$9x + 9y = 99$$

$$\Rightarrow$$
 9(x + y) = 99

$$\Rightarrow x + y = 11$$

Possible pairs = (1, 10) (2, 9), (3, 8), (4, 7), (5, 6)