

Lab 5

This lab demonstrates 16 QAM modulation and demodulation with AWGN with SNR varying between -10 and 10 with steps of 1.

Random input bits is generated using ~~rand~~ in "randin" and mapped to a constellation points for gray labelling and without gray labelling.

Without gray code:

0011	0111	1011	1111
0010	0110	1010	1110
0001	0101	1001	1101
0000	0100	1000	1100

3	7	11	15
2	6	10	14
1	5	9	13
0	4	8	12

With gray code:

0010	0110	1110	1010
0011	0111	1111	1011
0001	0101	1101	1001
0000	0100	1100	1000

2	6	14	10
3	7	15	11
1	5	13	9
0	4	12	8

To calculate BER for each
gray and without gray labelling:

- (a) generate random signal
- (b) generate AWGN
- (c) received signal $(y) = S + n$
- (d) Check whether the received value
lies near or far away from the
constellation point.
- (e) If there is an error increment
the error count.

From the plot it can be seen that
BER is more for gray label and
without gray label for low SNR values.
and decreases with increasing SNR value.

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clc;
clear all;
close all;

M = 16; %Number of points in constellation is 16
%%x1 is an array of symbols to which mapping is to be done%%
%As we have b symbols 2 to the left of 0 and 2 to the right of zero.
x1 = [-3,-1,1,3];
const = x1 + 1i*x1.';
k=double(1.0)/double(sqrt(10)); %normalizing factor
const=k*const; %Normalising the constellation to make its power unity.

%This array is used to map between non-gray and gray constellation points.
maparr=[0 1 3 2 4 5 7 6 12 13 15 14 8 9 11 10];

inputs = 10000; %number of bits
input=zeros(1,inputs);
%generating 4bit random input between 0 and 15
for k=1:inputs
    input(k)= randi([0, (M-1)]);
end
input_withoutgray=const(input(:)+1); %constellation symbols for non gray
input_gray=maparr(input(:)+1);%corresponding gray input for the same constellation
input.

snr = -10:10; %SNR from -10 to 10 dB in steps of 1.
decisions_bin = zeros(1,inputs);
number_snrs = length(snr);
%To estimate BER error for each SNR value and add it to estimate for both
%gray and non gray labelling
berr_estimate_withoutgray = zeros(number_snrs,1);
berr_estimate_gray = zeros(number_snrs,1);

%looping through each SNR value
for k=1:number_snrs
    snr_now = snr(k);
    ebno=10^(snr_now/10);
    sigma=sqrt(1/(ebno));
    % add 2d Gaussian noise to our symbols.
    received_withoutgray = input_withoutgray+ (sigma*randn(inputs,1)+1j*sigma*randn(
inputs,1))/sqrt(10);% add complex AWGN noise to our input signal
    decisions=zeros(inputs,1);
    %calculating absolute distance of every signal point from each point of
constellation.
    %The minimum distance constellation point is the signal.
    for n=1:inputs
        distancesbin = abs(received_withoutgray(n)-const);
        [min_dist_bin,decisions_bin(n)] = min(distancesbin(:));
    end
    %map the decoded signal back to gray code input to compare error for gray
    %decisions_bin are index values while they correspond to some
    %decisions_gray value.
    decisions_gray=maparr(decisions_bin);

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decisions_bin=decisions_bin-1;

%To calculate bit error for both gray and non gray labelling
num=zeros(1,inputs);

%%calculating BER for 16QAM without gray labelling%%
for s=1:length(input)
    d_bin=de2bi(decisions_bin(s),4); %4bit binary string for ease of comparing
    i_bin=de2bi(input(s),4);
    biterror=0;
    for t=1:4
        if d_bin(t)~=i_bin(t)
            biterror=biterror+1; %%adding the error
        end
        num(s)=biterror; %%storing the total error
    end
end
error=num;

%%calculating BER for 16QAM with gray labelling
for s=1:length(input_gray)
    d_bin=de2bi(decisions_gray(s),4); %4bit binary string for ease of comparing
    i_bin=de2bi(input_gray(s),4);
    biterror=0;
    for t=1:4
        if d_bin(t)~=i_bin(t)
            biterror=biterror+1; %%adding the error
        end
        num(s)=biterror; %%storing the total error
    end
end
error_gray=num;
berr_estimate_withoutgray(k) =berr_estimate_withoutgray(k)+ sum(error)/inputs;
berr_estimate_gray(k) =berr_estimate_gray(k)+ sum(error_gray)/inputs;

end

%Plotting the Bit Error Rate
figure;
semilogy(snr,berr_estimate_withoutgray,'o'); %plotting the BER without gray label.
hold on;
semilogy(snr,berr_estimate_gray,'*'); %plotting the BER with gray label.
hold on;
semilogy(snr,3*qfunc(sqrt((10.^(snr/10))))); % plotting BER theoretical using Q-
function .
legend("Experimental BER without gray code","Experimental BER with gray code","
Theoretical using Q function");
xlabel("SNR (dB)");
ylabel("BER (Bit Error Rate .)");
title("BER plot for 16 QAM with and without gray-labelling");

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