

Project

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I added two new columns:

1. total_gdp, the dataset already has gdp per capita
2. medal_pct, which is total medals divided by total athletes

```
# make the chr to factor
olympics <- olympics %>%
  mutate(country = factor(country),
         country_code = factor(country_code),
         region = factor(region))

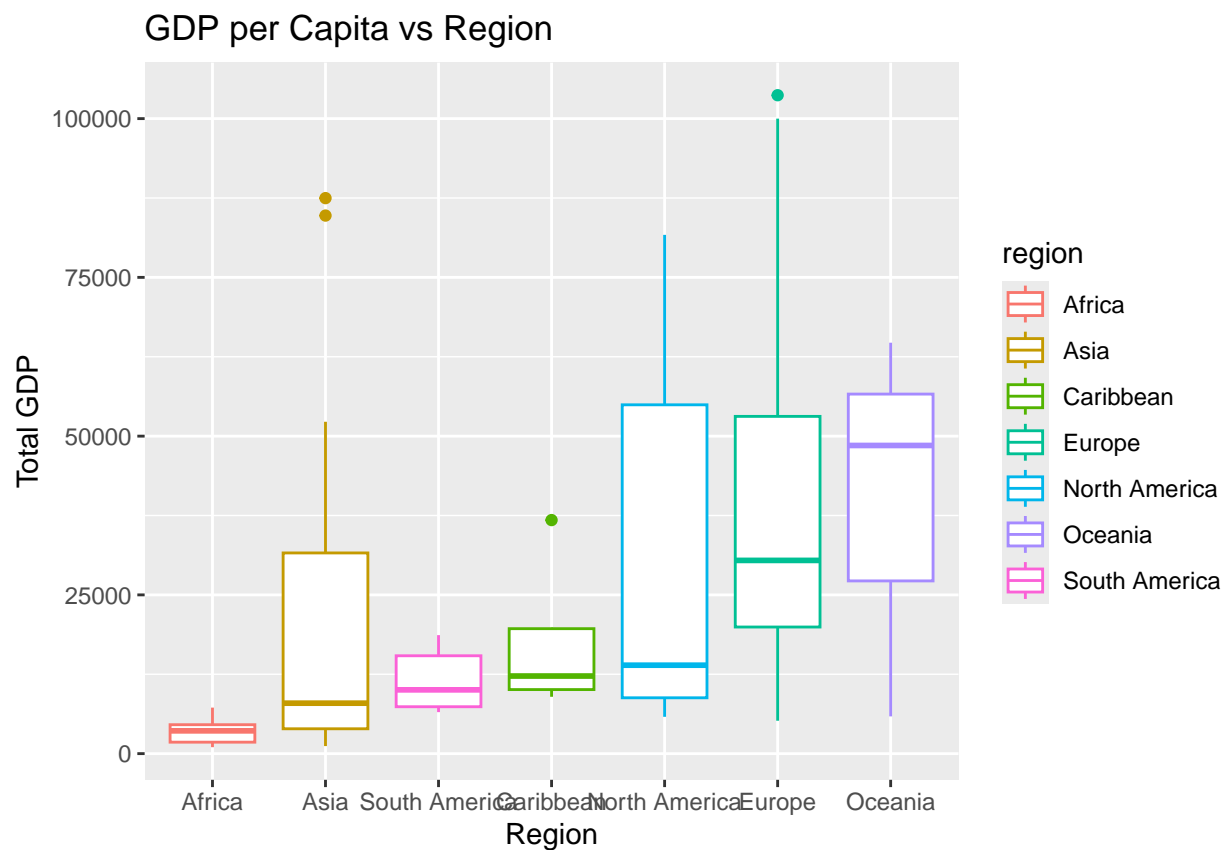
olympics <- olympics %>%
  mutate(total_gdp = gdp * population,
         medal_pct = total / athletes)

summary(olympics)
```

```
##      country  country_code      region      gold
## Albania   : 1  ALB       : 1  Africa      :12  Min.     : 0.000
## Algeria   : 1  ARG       : 1  Asia        :26  1st Qu.: 0.000
## Argentina: 1  ARM       : 1  Caribbean  : 4  Median : 1.000
## Armenia   : 1  AUS       : 1  Europe     :31  Mean    : 3.644
## Australia: 1  AUT       : 1  North America: 7  3rd Qu.: 3.000
## Austria   : 1  AZE       : 1  Oceania    : 3  Max.    :40.000
## (Other)   :84  (Other):84  South America: 7
##      silver      bronze      total      gdp
## Min.     : 0.000  Min.     : 0.000  Min.     : 1.00  Min.     : 1014
## 1st Qu.: 0.000  1st Qu.: 1.000  1st Qu.: 2.00  1st Qu.: 5815
## Median : 1.000  Median : 2.000  Median : 5.00  Median : 13061
## Mean    : 3.633  Mean    : 4.256  Mean    : 11.53  Mean    : 24478
## 3rd Qu.: 3.000  3rd Qu.: 5.000  3rd Qu.: 9.00  3rd Qu.: 34485
## Max.    :44.000  Max.    :42.000  Max.    :126.00  Max.    :103685
##
##      gdp_year  population  athletes  total_gdp
## Min.     :2022  Min.     : 0.100  Min.     : 4.0  Min.     : 895
## 1st Qu.:2023  1st Qu.: 5.325  1st Qu.: 26.0  1st Qu.: 68724
## Median :2023  Median : 12.150  Median : 60.5  Median : 256882
## Mean    :2023  Mean    : 69.028  Mean    :111.6  Mean    :1085174
## 3rd Qu.:2023  3rd Qu.: 48.550  3rd Qu.:135.5  3rd Qu.: 621058
## Max.    :2023  Max.    :1428.600  Max.    :619.0  Max.    :27359719
```

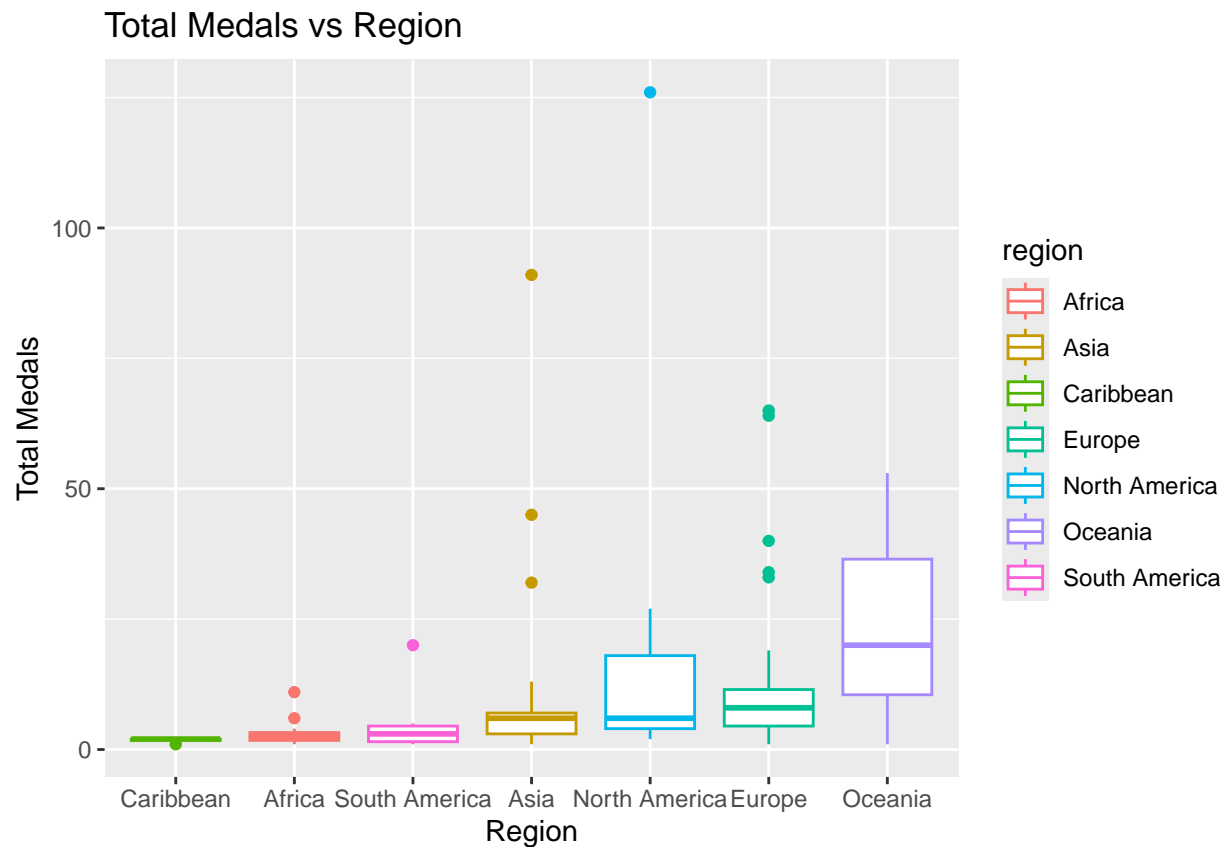
```
##
## medal_pct
## Min. :0.01911
## 1st Qu.:0.05430
## Median :0.09046
## Mean :0.11846
## 3rd Qu.:0.14509
## Max. :0.50000
##
```

```
olympics %>%
  ggplot(aes(x=reorder(region, gdp, FUN = median), y=gdp, col=region)) +
  geom_boxplot() +
  labs(title = "GDP per Capita vs Region",
       x = "Region",
       y = "Total GDP")
```



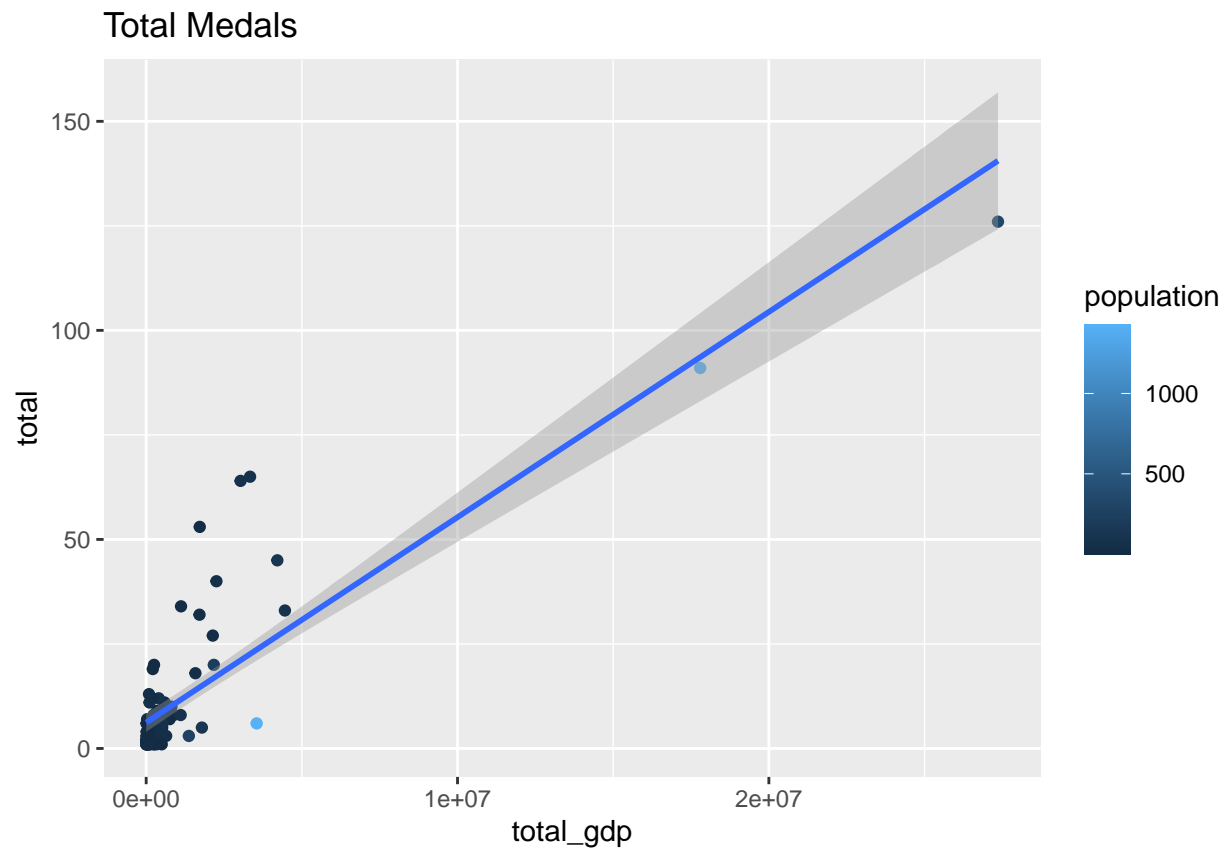
```
ggsave("chart1.png", plot = last_plot(), width = 8, height = 6, dpi = 300)
```

```
olympics %>%
  ggplot(aes(x=reorder(region, total, FUN = median), y=total, col=region)) +
  geom_boxplot() +
  labs(title = "Total Medals vs Region",
       x = "Region",
       y = "Total Medals")
```

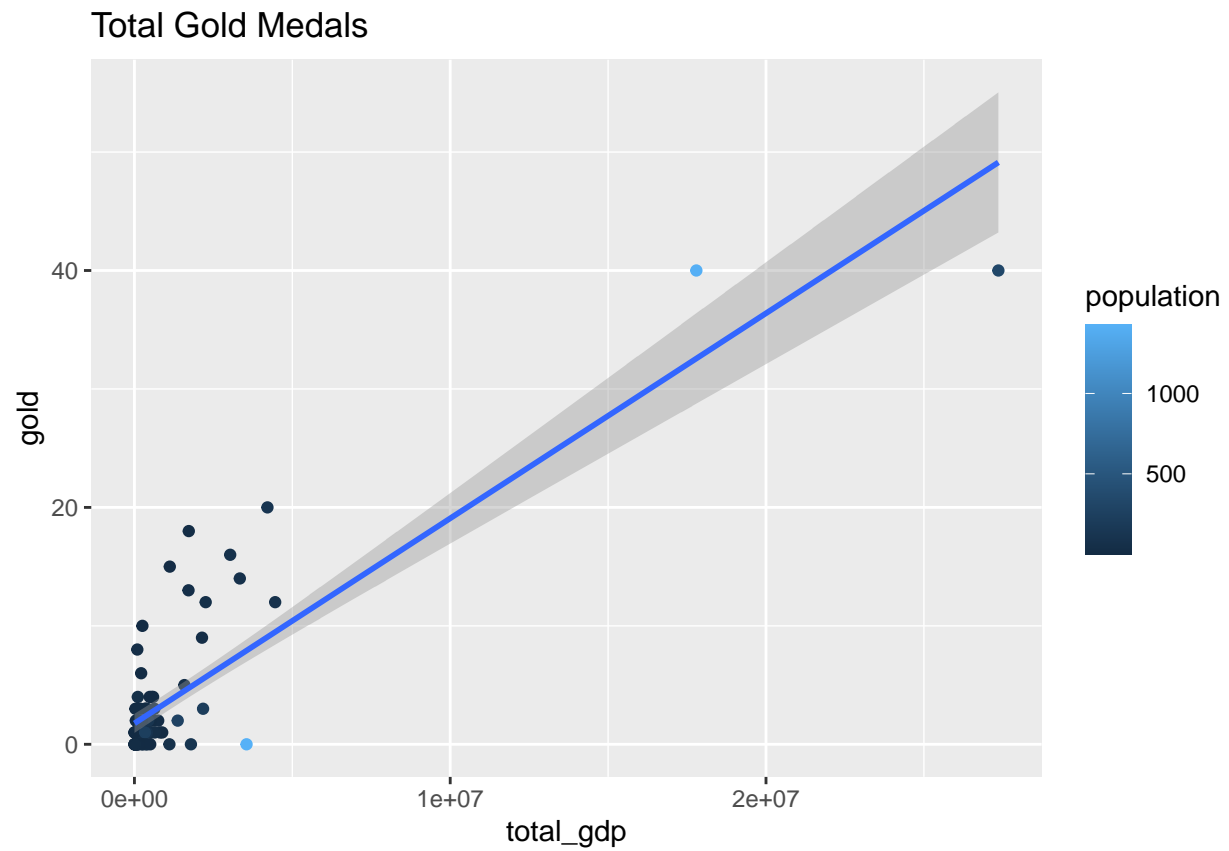


```
ggsave("chart1.png", plot = last_plot(), width = 8, height = 6, dpi = 300)
```

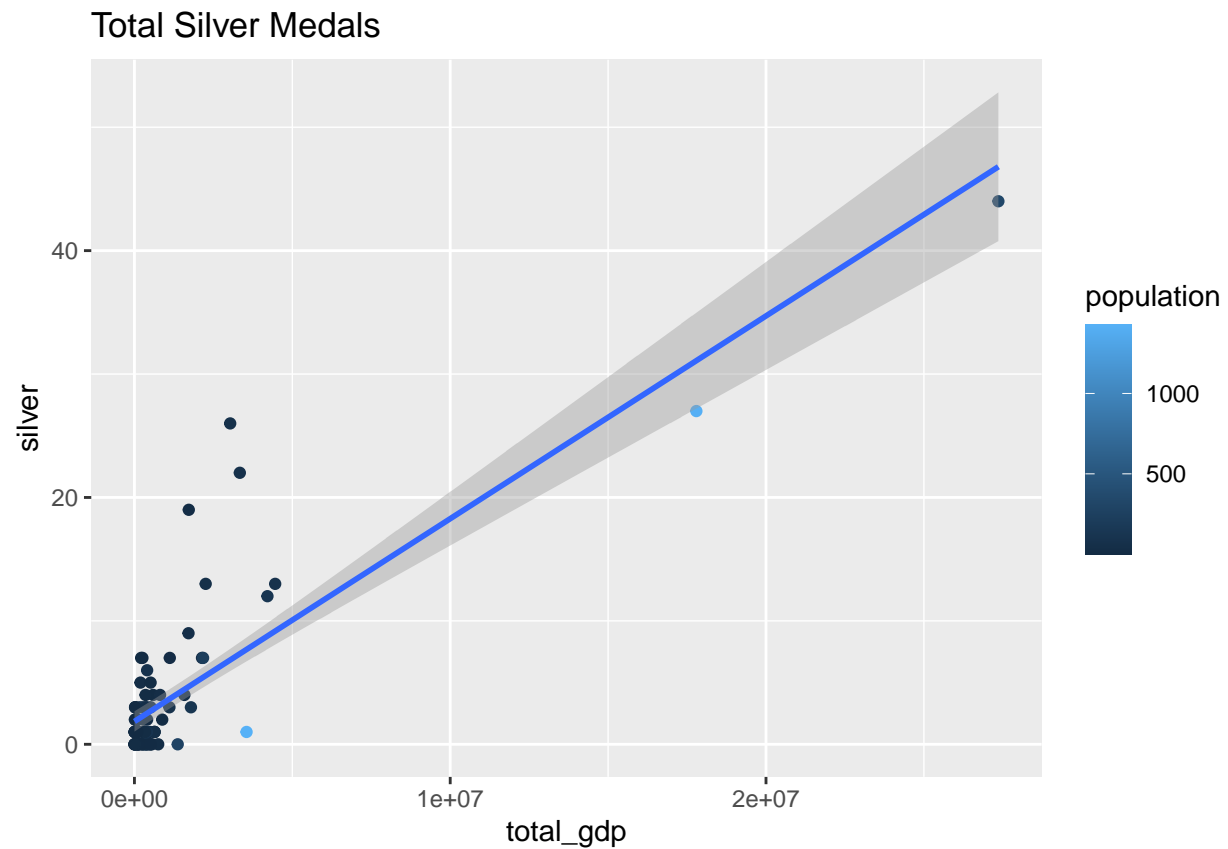
```
olympics %>%
  ggplot(aes(x=total_gdp, y=total, col=population)) +
  geom_point() +
  geom_smooth(method='lm') +
  labs(
    title = "Total Medals"
  )
)
```



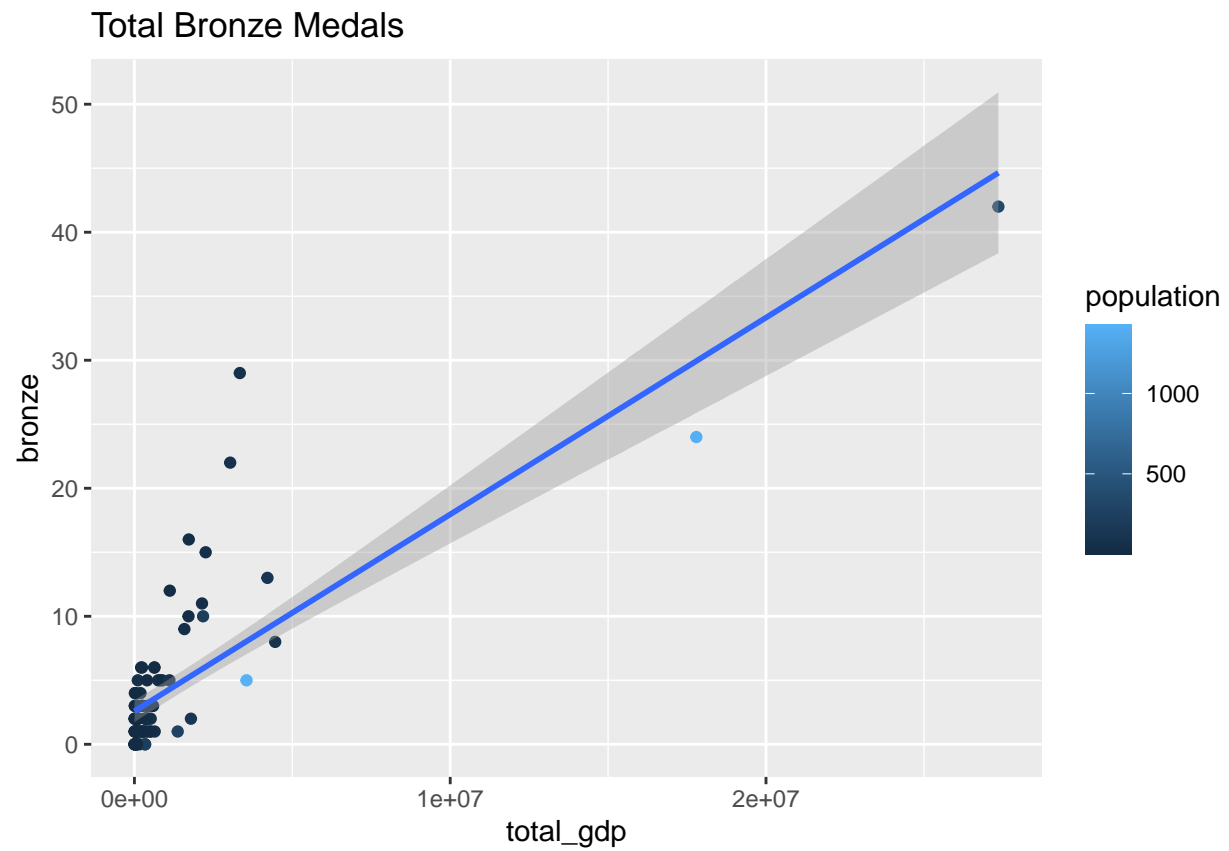
```
ggsave("chart1.png", plot = last_plot(), width = 8, height = 6, dpi = 300)
olympics %>%
  ggplot(aes(x=total_gdp, y=gold, col=population)) +
  geom_point() +
  geom_smooth(method='lm') +
  labs(
    title = "Total Gold Medals"
  )
)
```



```
ggsave("chart2.png", plot = last_plot(), width = 8, height = 6, dpi = 300)
olympics %>%
  ggplot(aes(x=total_gdp, y=silver, col=population)) +
  geom_point() +
  geom_smooth(method='lm') +
  labs(
    title = "Total Silver Medals"
  )
)
```



```
ggsave("chart3.png", plot = last_plot(), width = 8, height = 6, dpi = 300)
olympics %>%
  ggplot(aes(x=total_gdp, y=bronze, col=population)) +
  geom_point() +
  geom_smooth(method='lm') +
  labs(
    title = "Total Bronze Medals"
  )
)
```

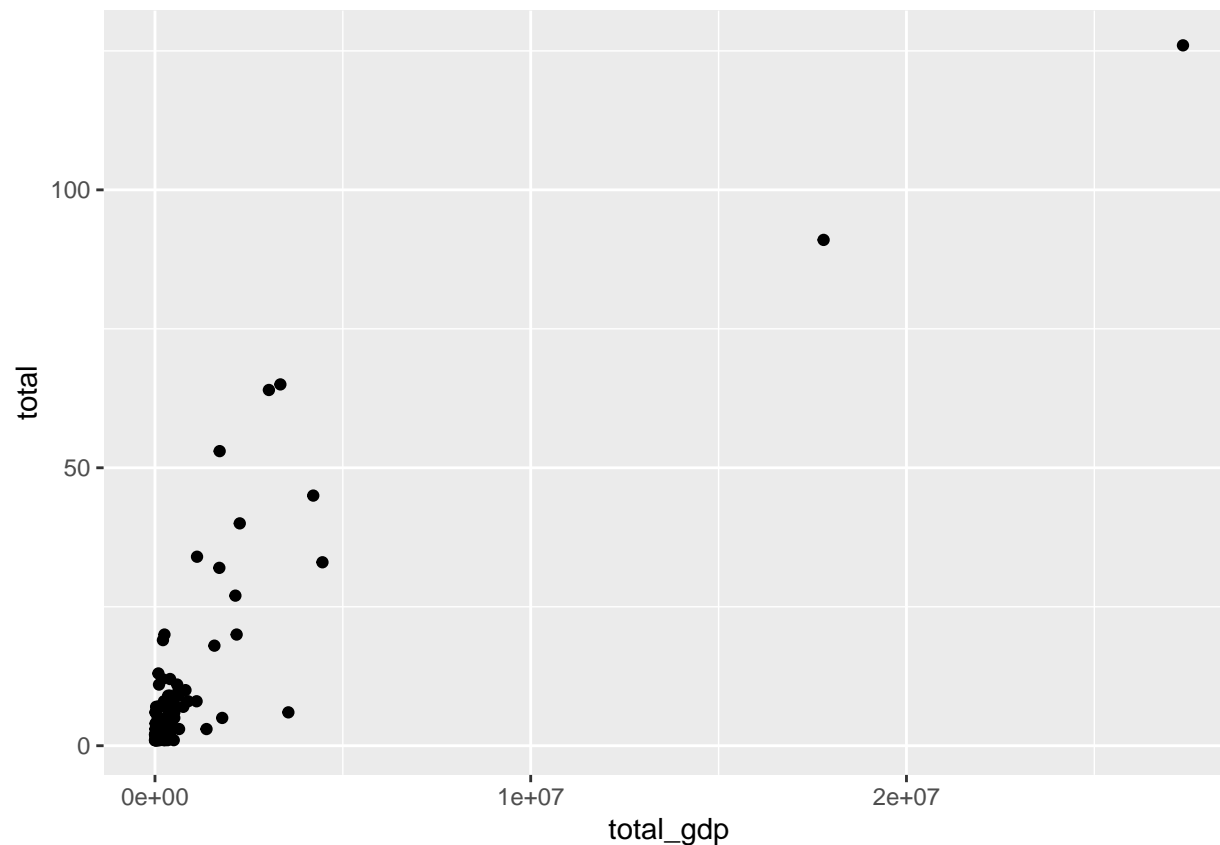


```
ggsave("chart4.png", plot = last_plot(), width = 8, height = 6, dpi = 300)
```

Check Conditions:

Linearity

```
ggplot(olympics, aes(x=total_gdp, y=total)) +  
  geom_point()
```



```
ggsave("chart1.png", plot = last_plot(), width = 8, height = 6, dpi = 300)
```

Independence:

Normality of the residuals

```
# Run SLR model
```

```
mod <- lm(total ~ total_gdp, data = olympics)
```

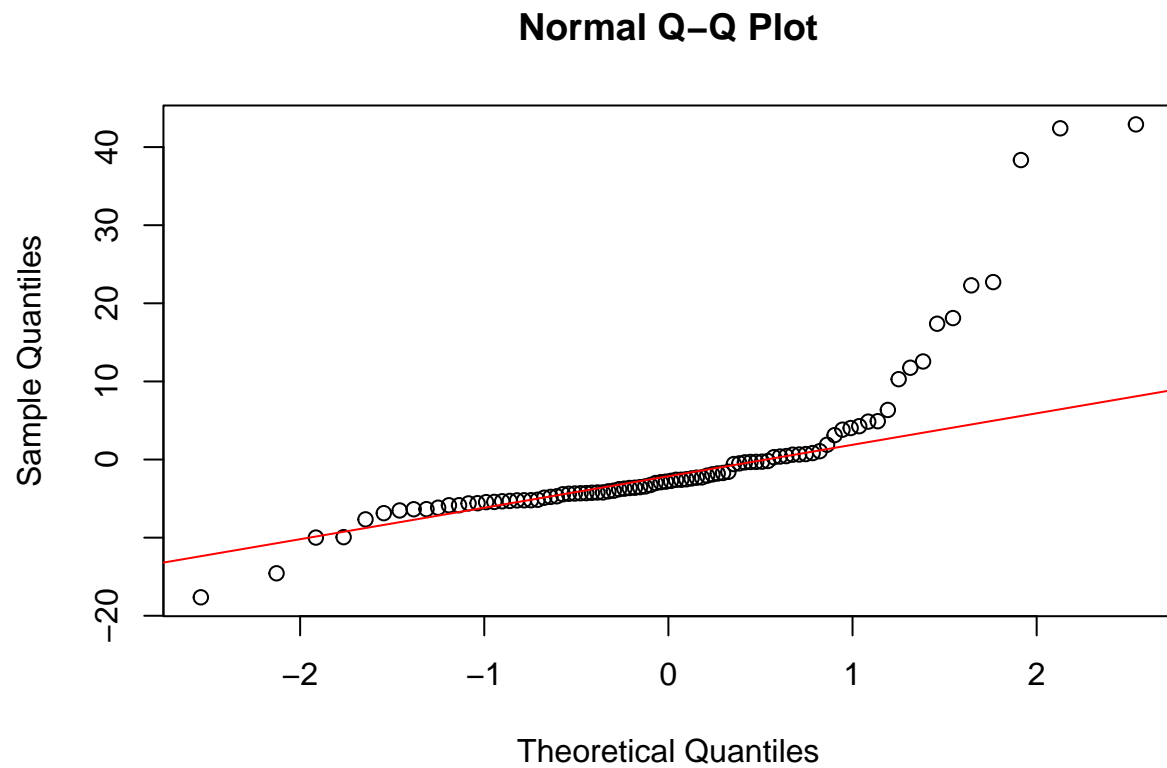
```
summary(mod)
```

```
##
## Call:
## lm(formula = total ~ total_gdp, data = olympics)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -17.637  -4.860  -2.783   0.576  42.905
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  6.204e+00  1.123e+00   5.527 3.28e-07 ***
## total_gdp    4.911e-06  3.108e-07  15.798 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```



```
## Residual standard error: 10.16 on 88 degrees of freedom
## Multiple R-squared:  0.7393, Adjusted R-squared:  0.7364
## F-statistic: 249.6 on 1 and 88 DF,  p-value: < 2.2e-16
```

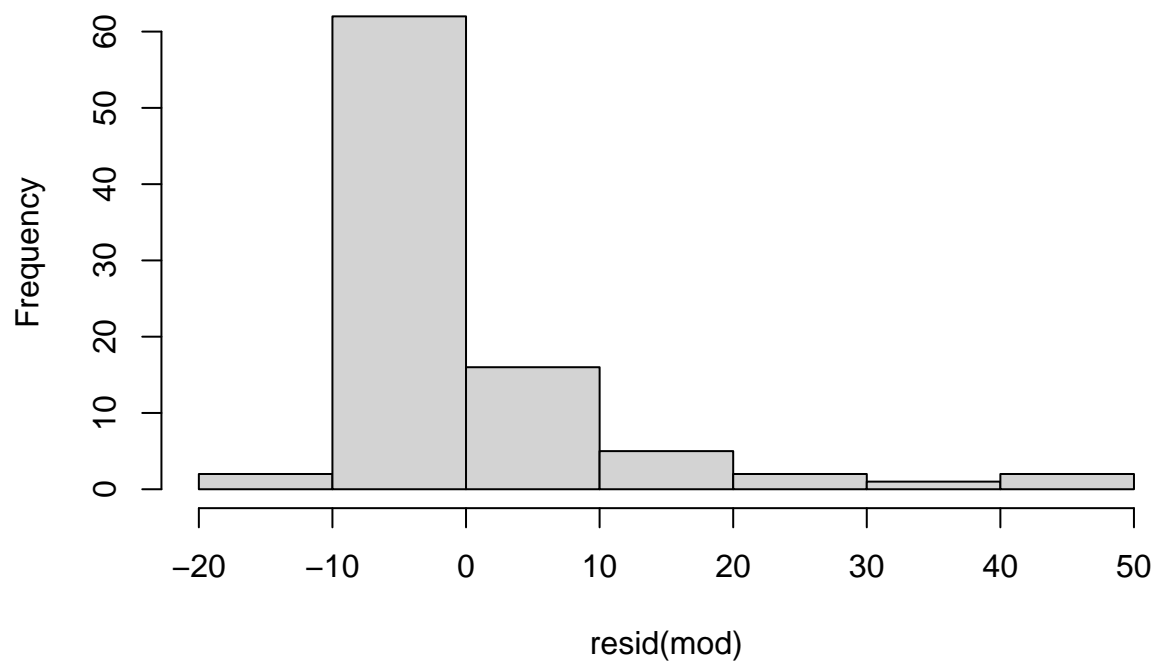
```
# Check Normality Assumption
qqnorm(resid(mod))
qqline(resid(mod), col = "red")
```



```
ggsave("chart1.png", plot = last_plot(), width = 8, height = 6, dpi = 300)

hist(resid(mod))
```

Histogram of resid(mod)

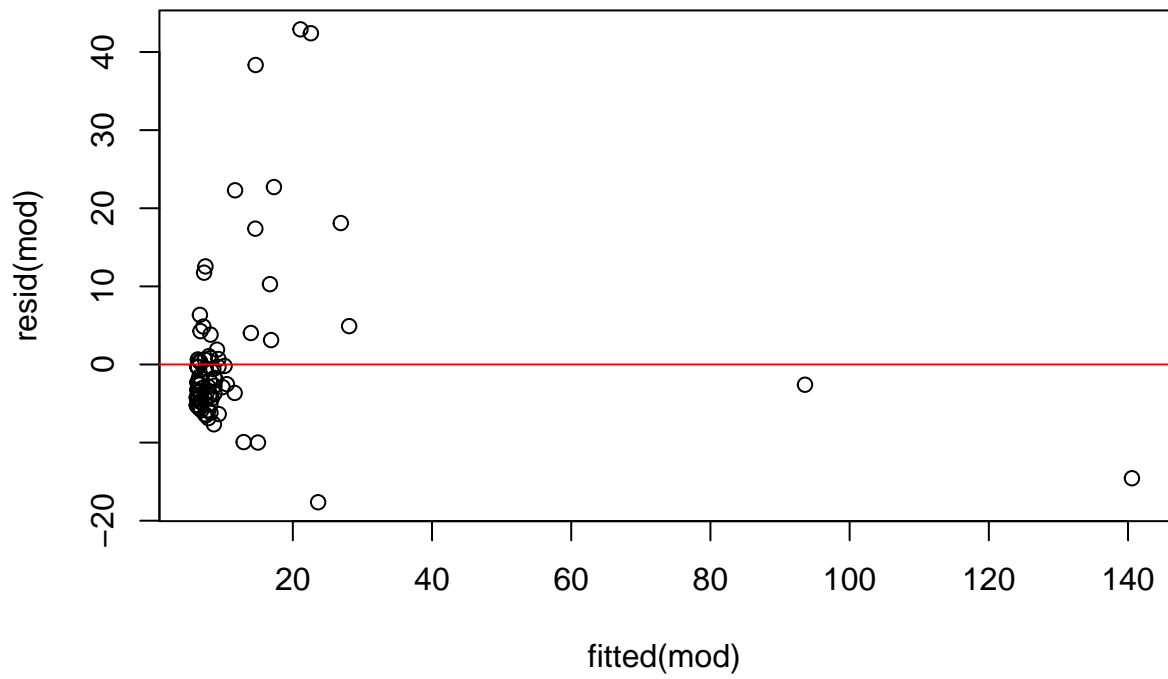


```
ggsave("chart2.png", plot = last_plot(), width = 8, height = 6, dpi = 300)
```

Equal (constant) Variance of the residuals

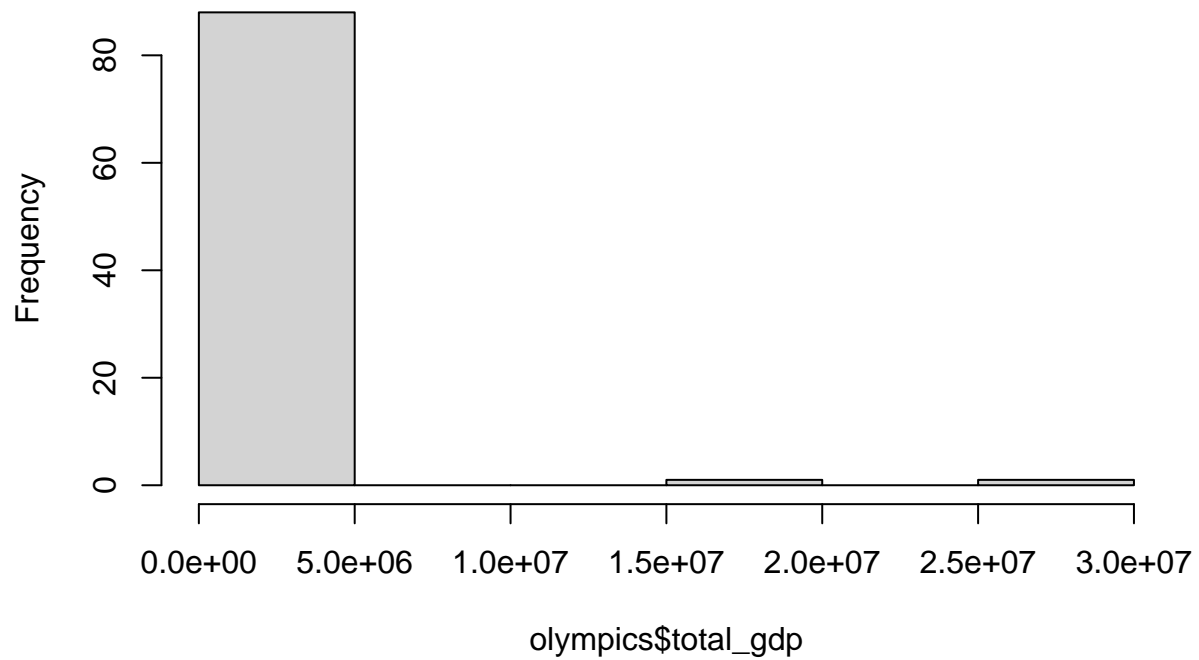
```
plot(resid(mod) ~ fitted(mod), main = "Residuals vs. Fitted")  
abline(h = 0, col = "red")
```

Residuals vs. Fitted



```
hist(olympics$total_gdp)
```

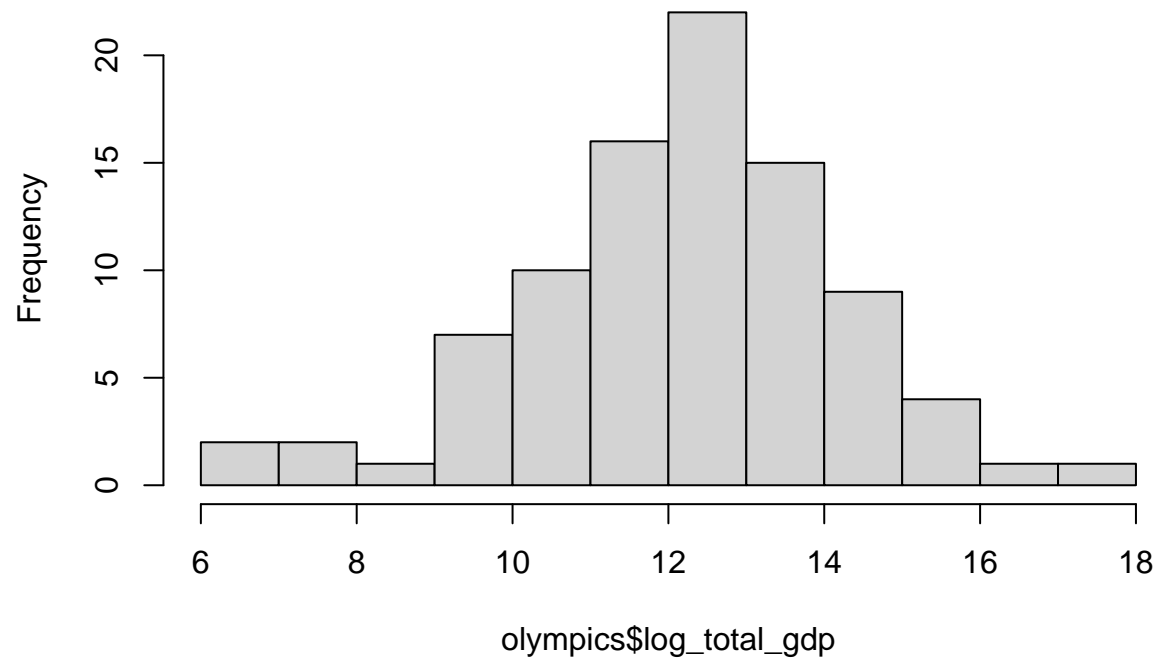
Histogram of olympics\$total_gdp



I checked the assumptions for total gdp, and most of them were not meet, therefore, we transformed the gdp by “log function” and retest all the assumptions.

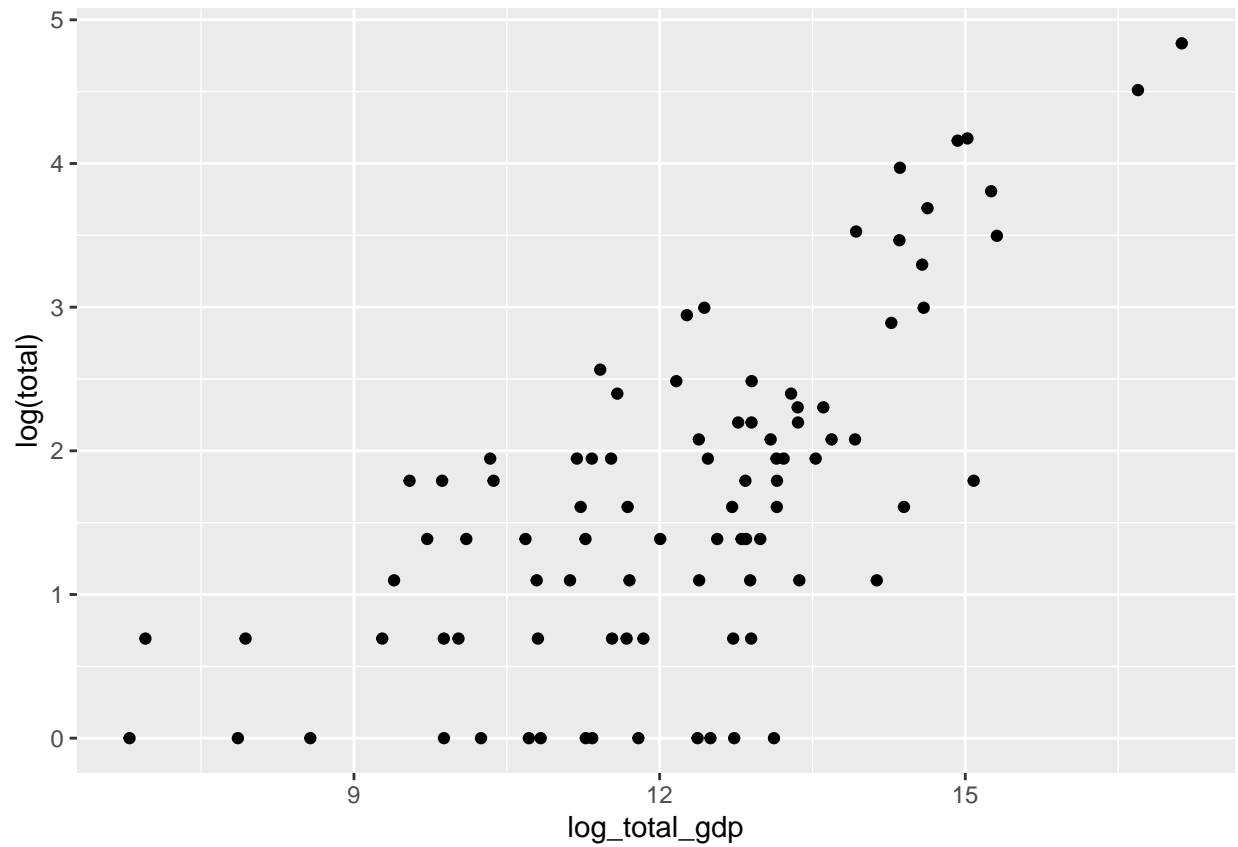
```
olympics <- olympics %>%  
  mutate(log_total_gdp = log(total_gdp))  
  
hist(olympics$log_total_gdp)
```

Histogram of olympics\$log_total_gdp



Check Assumptions

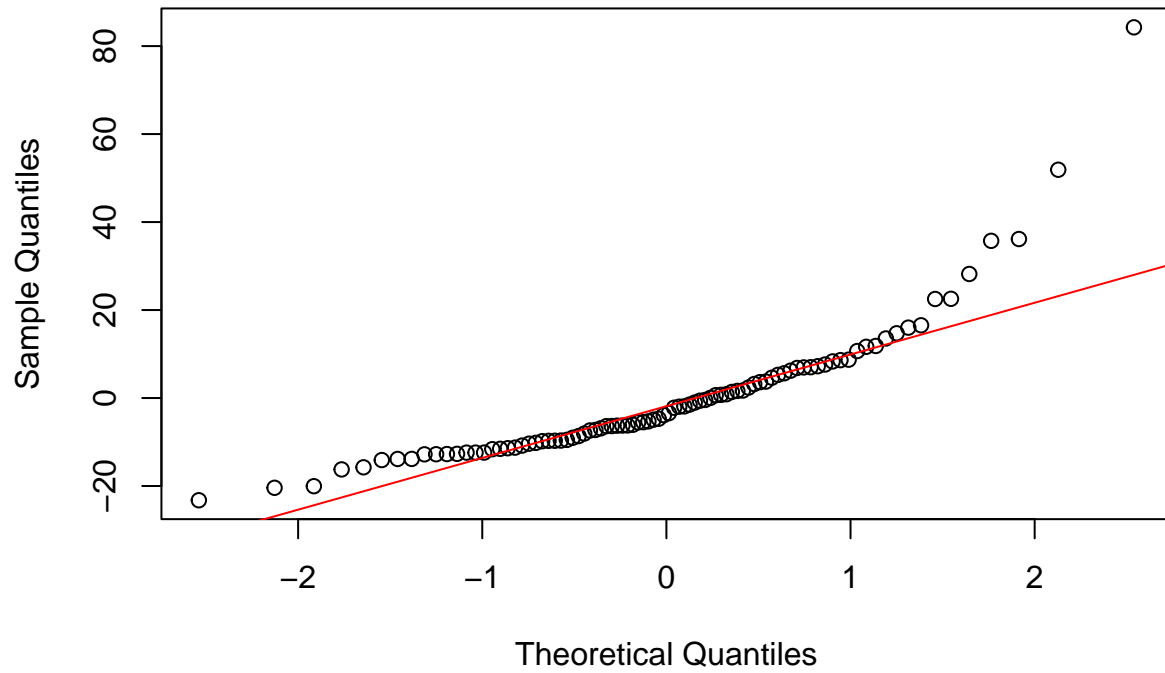
```
ggplot(olympics, aes(x = log_total_gdp, y = log(total))) +  
  geom_point()
```



```
# Run model with transformed x
mod_new <- lm(total ~ log_total_gdp, data = olympics)

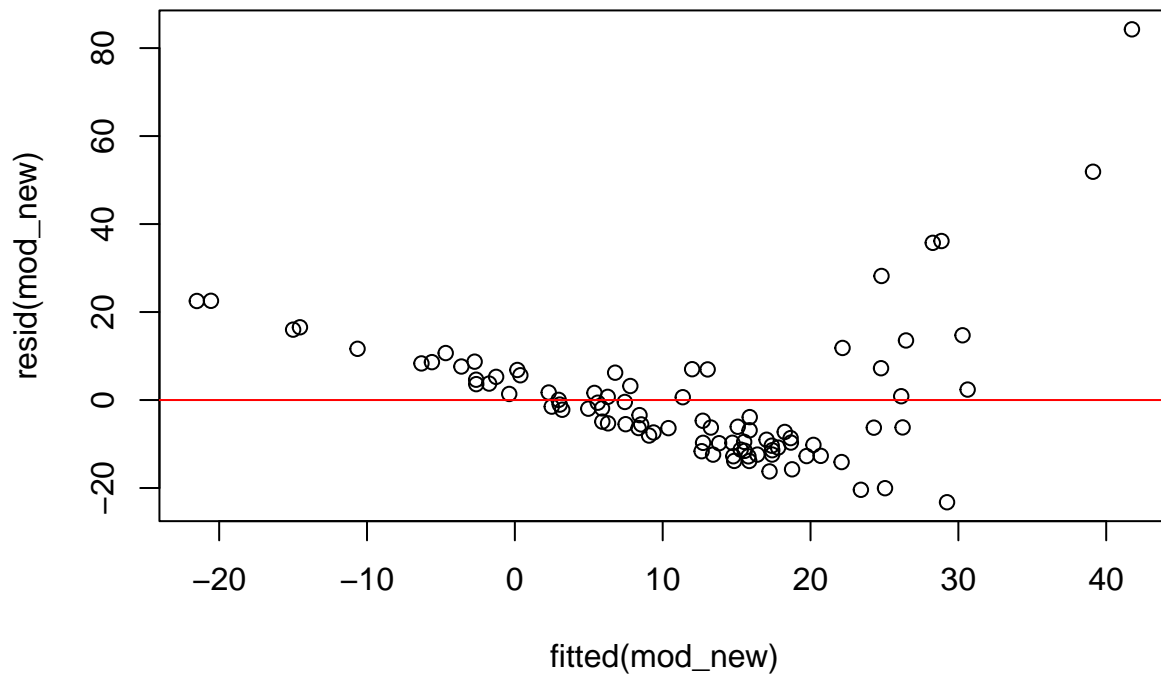
# Check Normality Assumption
qqnorm(resid(mod_new))
qqline(resid(mod_new), col = "red")
```

Normal Q-Q Plot



```
# Check Equal (Constant) Variance Assumption  
plot(resid(mod_new) ~ fitted(mod_new), main = "Residuals vs. Fitted")  
abline(h = 0, col = "red")
```

Residuals vs. Fitted



```
summary(mod_new)
```

```
##
## Call:
## lm(formula = total ~ log_total_gdp, data = olympics)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -23.233  -9.794  -3.659   6.069  84.259
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -63.142     10.448  -6.044 3.55e-08 ***
## log_total_gdp    6.125      0.846   7.239 1.61e-10 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.75 on 88 degrees of freedom
## Multiple R-squared:  0.3733, Adjusted R-squared:  0.3661
## F-statistic: 52.41 on 1 and 88 DF,  p-value: 1.608e-10
```

References:

chrome-extension://efaidnbmnmnibpcajpcgglefindmkaj/https://repository.gatech.edu/server/api/core/bitstreams/1aa2b537-c3de-4177-8295-3fcd3a03a965/content

chrome-extension://efaidnbmnnnibpcajpcgclefindmkaj/https://faculty.tuck.dartmouth.edu/images/
uploads/faculty/andrew-bernard/olymp60restat_finaljournalversion.pdf