

# KRR: Language Quick Reference.

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## Introduction

The grammar, operator precedence and associativity rules are specified for four languages. The grammar uses EBNF where *non-terminals symbols are shown in italics*, **terminals symbols are in bold font**.

→	defines a rule	?	zero or one
	alternation	*	zero or more
ε	empty string	+	one or more
⟨...⟩	a group	'meta char'	<b>terminal</b>
▷	line comment	"	' (single quote)

## 1 First Order Logic

### 1.1 Grammar

1:	<i>program</i> →	⟨ <i>sentence</i> ⟩*	
2:	<i>sentence</i> →	<i>formula</i> .	
3:	<i>formula</i> →	<b>true</b>   <b>false</b>	
4:		<i>term</i> <i>copr</i> <i>term</i>	▷ comparison
5:		<b>name</b> ( <i>termList</i> )	▷ predicate
6:		<b>forall</b> <i>varList</i> <i>formula</i>	
7:		<b>exists</b> <i>varList</i> <i>formula</i>	
8:		{ <i>formula</i> }   ( <i>formula</i> )	
9:		⟨ ~   <b>not</b> ⟩ <i>formula</i>	
10:		<i>formula</i> <i>bopr</i> <i>formula</i>	
11:	<i>varList</i> →	<b>variable</b> ⟨ , <b>variable</b> ⟩*	
12:	<i>termList</i> →	<i>term</i> ⟨ , <i>term</i> ⟩*	
13:	<i>term</i> →	<i>expr</i>   <i>list</i>	▷ term
14:	<i>expr</i> →	<b>integer</b>   <b>float</b>	▷ numeric term
15:		<b>string</b>	▷ constant term
16:		<b>constant</b>	▷ constant term
17:		<b>name</b> ( <i>termList</i> ? )	▷ function term
18:		<b>variable</b>	▷ variable term
19:		( <i>expr</i> )	▷ term
20:		- <i>expr</i>	▷ negative term
21:		<i>expr</i> <i>aopr</i> <i>expr</i>	▷ arithmetic term
22:	<i>list</i> →	[ ]	▷ Nil list
23:		[ <i>expr</i> ]	▷ list term
24:		[ <i>expr</i> ' ' ⟨ <i>expr</i>   <i>list</i> ⟩ ]	▷ list term
25:	<i>copr</i> →	<b>lt</b>   <b>eq</b>   <b>ge</b>   <b>gt</b>   <b>ne</b>	▷ comparison
26:		<   =   >   !=	
27:		<b>le</b>	
28:	<i>bopr</i> →	<b>iff</b>   <=>	▷ boolean connectives
29:		<b>implies</b>   =>   <b>impliedby</b>   <=	
30:		<b>and</b>   &&   &   <b>or</b>        ' '   ' '   ' '	
31:	<i>aopr</i> →	'*'   '/'   '%'   '+'   '-'	

### 1.2 Symbols

Keywords: **forall**, **exists**, **iff**, **implied**, **impliedby**, **lt**, **le**, **eq**, **ge**, **gt**, **ne**, **true**, **false**, **not**.

User defined symbols:

Symbol	Syntax	Example
<b>name</b>	[a-z] [A-Za-z0-9_]*	man, mortal
<b>constant</b>	[a-z] [A-Za-z0-9_]*	john, mary
<b>string</b>	'...'	'Woody Allen'
<b>variable</b>	[A-Z] [A-Za-z0-9_]*	X, Y, Z

### 1.3 Operators

Operator precedence levels: highest first and operators with same precedence listed together.

Arity	Operators	Associativity
unary	-	Right-Left
binary	*, /, %	Left-Right
binary	+, -	Left-Right
binary	<, =, >=, >, !=, <>, <b>lt</b> , <b>le</b> , <b>eq</b> , <b>ge</b> , <b>gt</b> , <b>ne</b>	N/A
unary	<b>not</b> , ~, <b>forall</b> , <b>exists</b>	Right-Left
binary	<b>and</b> , &&, &	Left-Right
binary	<b>or</b> ,   ,	Left-Right
binary	<b>implies</b> , =>, <b>impliedby</b> , <=	Right-Left
binary	<b>iff</b> , <=>	Right-Left

### 1.4 Program Example

```
/* This is a block comment */
// This is a line comment

forall X ( man(X) implies mortal(X) ).
forall X ( man(X) => mortal(X) ).

forall X ( mortal(X) impliedby man(X) ).
forall X ( mortal(X) <= man(X) ).

exists X ( p(X) and q(x) && r(X) & t(X) ) .
exists X ( p(X) or q(x) || r(X) | t(X) ) .

forall X,Y,Z ( p(X,Y) & p(Y,Z) => p(X,Z) ).
forall X,Y ( p(X,Y) & p(Y,X) => X = Y ).

forall X,Y ( p(a,Y) => p(X,b) ).

forall A,B,C { append(A,B,C) & C=B <= A=[] }.
forall X,A,B,C {
    append([X|A],B,[X|C]) <= append(A,B,C)
}.

// End of program
```

## 2 Horn Clauses

### 2.1 Grammar

- 1:  $program \rightarrow \langle hornClause \rangle^*$
- 2:  $hornClause \rightarrow predicate :- body .$  ▷ rule
- 3:  $\quad \quad \quad | predicate .$  ▷ fact
- 4:  $\quad \quad \quad | predicate '?'$  ▷ query
- 5:  $predicate \rightarrow name ( termList )$
- 6:  $body \rightarrow subgoal \langle , subgoal \rangle^*$
- 7:  $subgoal \rightarrow !$  ▷ cut operator
- 8:  $\quad \quad \quad | literal$
- 9:  $\quad \quad \quad | \langle \sim | \backslash + | not \rangle literal$
- 10:  $literal \rightarrow true | false$
- 11:  $\quad \quad \quad | term copr term$  ▷ comparison
- 12:  $\quad \quad \quad | predicate$
- 13:  $\quad \quad \quad | ( literal )$
- 14:  $termList \rightarrow term \langle , term \rangle^*$
- 15:  $term \rightarrow expr | list$
- 16:  $expr \rightarrow integer | float$  ▷ numeric term
- 17:  $\quad \quad \quad | string$  ▷ constant term
- 18:  $\quad \quad \quad | constant$  ▷ constant term
- 19:  $\quad \quad \quad | name ( termList? )$  ▷ function term
- 20:  $\quad \quad \quad | variable$  ▷ variable term
- 21:  $\quad \quad \quad | ( expr )$  ▷ term
- 22:  $\quad \quad \quad | - expr$  ▷ negative term
- 23:  $\quad \quad \quad | expr aopr expr$  ▷ arithmetic term
- 24:  $list \rightarrow [ ]$  ▷ Nil list
- 25:  $\quad \quad \quad | [ expr ]$  ▷ list term
- 26:  $\quad \quad \quad | [ expr ' ' \langle expr | list \rangle ]$  ▷ list term
- 27:  $copr \rightarrow lt | le | eq | ge | gt | ne$
- 28:  $\quad \quad \quad | < | <= | = | >= | > | !=$
- 29:  $aopr \rightarrow '*' | '/' | \% | '+' | -$

### 2.2 Symbols

Keywords: **lt**, **le**, **eq**, **ge**, **gt**, **ne**, **true**, **false**, **not**.

User defined symbols:

Symbol	Syntax	Example
<b>name</b>	[a-z] [A-Za-z0-9_]*	person, father
<b>constant</b>	[a-z] [A-Za-z0-9_]*	john, mary
<b>string</b>	'...'	'Woody Allen'
<b>variable</b>	[A-Z] [A-Za-z0-9_]*	A, B, P, X

### 2.3 Operators

Operator precedence levels: highest first and operators with same precedence listed together.

Arity	Operators	Associativity
unary	<b>-</b>	Right-Left
binary	<b>*, /, %</b>	Left-Right
binary	<b>+, -</b>	Left-Right
binary	<b>&lt;, &lt;=, =, &gt;=, &gt;, !=, &lt;&gt;</b> , <b>lt, le, eq, ge, gt, ne</b>	N/A
unary	<b>not, ~, \+</b>	Right-Left

### 2.4 Program Example

```

/* This is a block comment */
// This is a line comment

// append(A,B,C) means C = A + B.

append([ ], B, B).
append([X|A], B, [X|C]) :- append(A, B, C).

append([1|2], [3|4], C)?

parent(P,X)          :- mother(P,X).
parent(P,X)          :- father(P,X).
grandparent(G,X)     :- parent(G,P), parent(P,X).

cousin(X,Y)          :- X != Y,
                        not sibling(X,Y),
                        grandparent(Z,X),
                        grandparent(Z,Y).

americanCousin(X,Y) :- cousin(X,Y), !,
                        american(X).

composite(N) :- N > 1, ~ prime(N).
composite(N) :- N > 1, \+ prime(N).
composite(N) :- N > 1, not (prime(N)).

// End of program

```

## 3 Production Systems

### 3.1 Grammar

- 1:  $program \rightarrow \langle sentence \rangle^*$
- 2:  $sentence \rightarrow rule | wme$
- 3:  $rule \rightarrow \text{if } condition + \text{ then } action +$
- 4:  $condition \rightarrow wme$
- 5:  $\quad \quad \quad | -wme$
- 6:  $action \rightarrow \text{add } wme$
- 7:  $\quad \quad \quad | \text{ remove integer}$
- 8:  $\quad \quad \quad | \text{ modify integer ( attribute spec )}$
- 9:  $wme \rightarrow ( \text{ type } attrSpec^* )$
- 10:  $attrSpec \rightarrow \text{attribute} : spec$
- 11:  $spec \rightarrow atom$
- 12:  $\quad \quad \quad | \{ testExpr \}$
- 13:  $\quad \quad \quad | [ evalExpr ]$
- 14:  $testExpr \rightarrow \text{true} | \text{false}$
- 15:  $\quad \quad \quad | atom \text{ copr} \quad \quad \quad \triangleright \text{comparison}$
- 16:  $\quad \quad \quad | \text{ copr } atom \quad \quad \quad \triangleright \text{comparison}$
- 17:  $\quad \quad \quad | [ evalExpr ] \text{ copr} \quad \quad \quad \triangleright \text{comparison}$
- 18:  $\quad \quad \quad | \text{ copr } [ evalExpr ] \quad \quad \quad \triangleright \text{comparison}$
- 19:  $\quad \quad \quad | ( testExpr )$
- 20:  $\quad \quad \quad | \langle \sim | \text{not} \rangle testExpr$
- 21:  $\quad \quad \quad | testExpr \text{ bopr } testExpr$
- 22:  $evalExpr \rightarrow atom$
- 23:  $\quad \quad \quad | ( evalExpr )$
- 24:  $\quad \quad \quad | - evalExpr$
- 25:  $\quad \quad \quad | evalExpr \text{ aopr } evalExpr$
- 26:  $atom \rightarrow \text{true} | \text{false}$
- 27:  $\quad \quad \quad | \text{integer} | \text{float}$
- 28:  $\quad \quad \quad | \text{string} \quad \quad \quad \triangleright \text{constant: 'John'}$
- 29:  $\quad \quad \quad | \text{constant} \quad \quad \quad \triangleright \text{constant: john}$
- 30:  $\quad \quad \quad | \text{variable} \quad \quad \quad \triangleright \text{variable: X, Y}$
- 31:  $copr \rightarrow < | <= | = | >= | > | != | <>$
- 32:  $bopr \rightarrow \text{or} | '||' | '|' | \text{and} | \&\& | \&$
- 33:  $aopr \rightarrow '*' | '/' | \% | '+' | -$

### 3.2 Symbols

Keywords: **if**, **then**, **add**, **remove**, **modify**, **true**, **false**, **not**, **or**, **and**.

User defined symbols:

Symbol	Syntax	Example
<b>type</b>	[a-z] [A-Za-z0-9_]*	brick, counter
<b>attribute</b>	[a-z] [A-Za-z0-9_]*	name, size
<b>constant</b>	[a-z] [A-Za-z0-9_]*	heap, hand
<b>string</b>	'...'	'A', 'B', 'C'
<b>variable</b>	[A-Z] [A-Za-z0-9_]*	S, N, I

### 3.3 Operators

Operator precedence levels: highest first and operators with same precedence listed together.

Arity	Operators	Associativity
unary	-	Right-Left
binary	*, /, %	Left-Right
binary	+, -	Left-Right
binary	<, <=, =, >=, >, !=, <>	N/A
unary	not, ~	Right-Left
binary	and, &&, &	Left-Right
binary	or,   ,	Left-Right

### 3.4 Program Example

```

/* This is a block comment */
// This is a line comment

(counter value: 1)
(brick name: 'A' size: 10 position: heap)
(brick name: 'B' size: 30 position: heap)
(brick name: 'C' size: 20 position: heap)

IF (brick position: heap name: N size: S)
  -(brick position: heap size: {> S})
  -(brick position: hand)
THEN
  MODIFY 1 (position hand)

IF (brick position: hand)
  (counter value: I)
THEN
  MODIFY 1 (position I)
  MODIFY 2 (value [I + 1])

// End of program

```

## 4 Description Logic

### 4.1 Grammar

- 1:  $program \rightarrow \langle sentence \rangle^*$
- 2:  $sentence \rightarrow ( concept\ bopr\ concept )$
- 3:           |  $( constantList \rightarrow concept )$
- 4:  $concept \rightarrow \text{name} \quad \triangleright \text{atomic concept}$
- 5:           |  $[ \text{fills}\ role\ constant ]$
- 6:           |  $[ \text{all}\ role\ concept ]$
- 7:           |  $[ \text{exists}\ integer\ role ]$
- 8:           |  $[ \text{and}\ concept\ concept^+ ]$
- 9:  $role \rightarrow : \text{name}$
- 10:  $constantList \rightarrow constant \langle , constant \rangle^*$
- 11:  $constant \rightarrow \text{integer} \mid \text{float}$
- 12:           |  $\text{string}$
- 13:           |  $\text{constant}$
- 14:           |  $( constant )$
- 15:           |  $- constant$
- 16:           |  $constant\ aopr\ constant$
- 17:  $bopr \rightarrow \text{isa} \mid << \quad \triangleright A \sqsubseteq B$
- 18:           |  $\text{subsumes} \mid >> \quad \triangleright A \sqsupseteq B$
- 19:           |  $\text{equivalentto} \mid == \quad \triangleright A \doteq B$
- 20:  $aopr \rightarrow '*' \mid / \mid \% \mid '+' \mid -$

### 4.2 Symbols

Keywords: **fills**, **all**, **exists**, **and**, **is**, **isa**, **subsumes**, **equivalentto**.

User defined symbols:

Symbol	Syntax	Example
<b>name</b>	<code>[A-Z] [A-Za-z0-9_]*</code>	Person, Man
<b>constant</b>	<code>[a-z] [A-Za-z0-9_]*</code>	john, mary
<b>string</b>	<code>'...'</code>	'Woody Allen'

### 4.3 Operators

Operator precedence levels: highest first and operators with same precedence listed together.

Arity	Operators	Associativity
unary	<code>-</code>	Right-Left
binary	<code>*, /, %</code>	Left-Right
binary	<code>+, -</code>	Left-Right
binary	<code>is, isa, &lt;&lt;, subsumes, &gt;&gt;, equivalentto, ==</code>	Left-Right

### 4.4 Program Example

```

/* This is a block comment */
// This is a line comment

( BlendedRedWine
  ==
  [AND Wine
    [FILLS :Color red]
    [EXISTS 2 :GrapeType]
  ]
)

( ProgressiveCompany
  ==
  [AND Company
    [EXISTS 7 :Director]
    [ALL :Manager
      [AND Woman [FILLS :Degree phD] ]
    ]
    [FILLS :MinSalary 24.00/hour]
  ]
)

// End of program

```