

**Total No. of pages. 03**  
**SEVENTH SEMESTER**

Roll No. MC/05  
B.TECH (MC)

NOVEMBER 2018

# MC 405 GRAPH THEORY

**Time: 3 Hours**

**Max.Marks: 40**

**Note:** Answer **ALL** by selecting any two parts from each. All questions carry equal marks.

✓ Q1(a) For a simple graph with  $n$  vertices, what is the minimum number of edges required to ensure that the graph is connected.

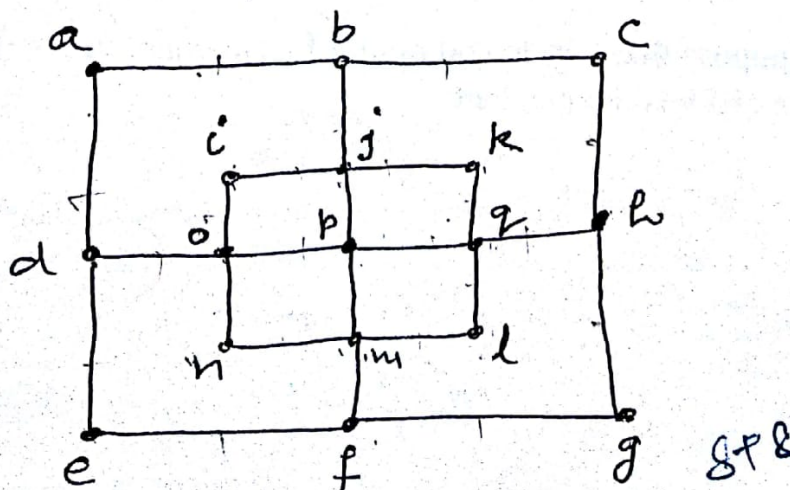
(b) Let  $G$  be a graph and  $\bar{G}$  its complement. Prove or disprove the following statements:

- i. If  $G$  is connected then  $\bar{G}$  is connected.
- ii. If  $G$  is connected then  $\bar{G}$  is disconnected.
- iii. If  $G$  is disconnected then  $\bar{G}$  is connected.
- iv. If  $G$  is disconnected then  $\bar{G}$  is disconnected.

(c) A simple graph has  $n$  vertices and exactly  $(n-1)$  edges. Prove that either there is an isolated vertex or at least one vertex of degree 1.

Q2(a). How many nonisomorphic simple graphs are there with 5 vertices and 3 edges? Draw each of these graphs.

(b) Does the graph below have a Hamiltonian path? If so, find such a path. If it does not, give an argument to justify your answer.

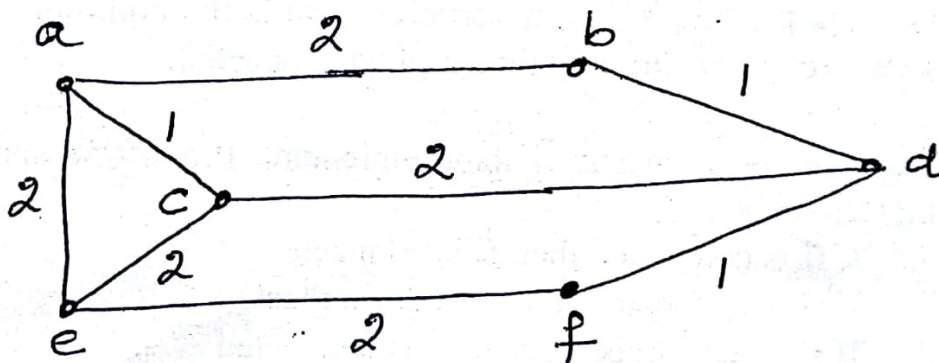


(c) Prove that a connected graph  $G$  is an Euler graph iff it can be decomposed into circuits.

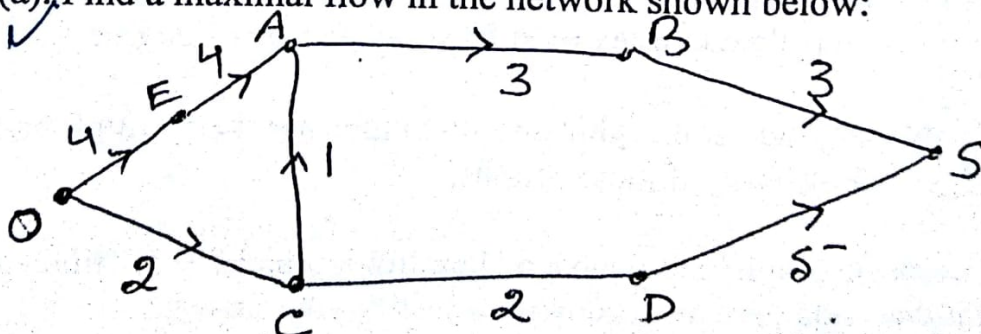
Q3(a) Prove that a tree with more than one vertex has at least two leaves.

(b) Suppose that a tree has two vertices of degree 2, four vertices of degree 3 and three vertices of degree 4. Find the number of pendant vertices in the tree.

(c) Find two distinct minimal spanning tree for the weighted graph given below:



Q4(a) Find a maximal flow in the network shown below:



(b) Suppose that  $v$  is an end point of a cut edge. Prove that  $v$  is a cut vertex iff  $v$  is not pendant.



✓(c) Prove that each cut set of a given connected graph  $G$  has at least one branch of each spanning tree of  $G$ .

✓Q5(a) Let  $G$  be a connected graph, every vertex is of degree 2. If  $G$  has even number of vertices, prove that it has perfect matching.

(b) Consider the examination schedule problem as given in the table. By using the concept of colouring, how many examination slots are required?

| Student | Subject |
|---------|---------|
| $x_1$   | $s_1$   |
| $x_1$   | $s_2$   |
| $x_2$   | $s_2$   |
| $x_2$   | $s_3$   |
| $x_2$   | $s_4$   |

✓(c) Define Matching in a graph. Let  $a(n)$  denotes the number of perfect matching in a complete graph with even number of vertices. Find a recurrence relation for  $a(n)$  and hence solve.

END

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SEVENTH SEMESTER

END SEMESTER EXAMINATION

MC-409 MATHEMATICAL MODELING AND SIMULATIONS

Time: 3: 00 hours

Roll No. me05

B.TECH. [MCE]

NOVEMBER-2018

Max. Marks: 40

Note: 1. Attempt any five questions.

2. Assume missing data, if any.

3. All questions carry equal marks.

✓ 1. Discuss the following:

[a] Quantitative approach of modeling.

[b] Conceptual model.

[c] Distributed model.

[d] Lumped model.

2. [a] Develop and explain a model for diffusion of glucose or medicine in the blood stream.

[b] Discuss the model for logistic growth of bacteria population.

3. [a] A battle is modelled by

$$x' = -4y, x(0) = 150$$

$$y' = -x, y(0) = 90$$

i) Write the solution in parametric form.

ii) Who wins and when? State the losses at each side.

[b] Show that the model represented by

$$\frac{dx}{dt} = x(4 - x - y), \frac{dy}{dt} = y(15 - 5x - 3y), x, y \geq 0$$

has a position of equilibrium, this position is stable and two species can coexist.

✓ 4. [a] Develop and explain the susceptible – infected – recovered model for disease transmission.

[b] Find all equilibrium solutions of the system of differential equations

P.T.O



$$\frac{dx}{dt} = 1 - xy, \frac{dy}{dt} = x - y^3$$

and determine (if possible) whether they are stable or unstable.

5. [a] Obtain the cubic spline approximation for the function defined by the data

|        |   |   |    |     |
|--------|---|---|----|-----|
| $x$    | 0 | 1 | 2  | 3   |
| $f(x)$ | 1 | 2 | 33 | 244 |

with  $f''(0) = 0, f''(3) = 0$ . Hence find an estimate of  $f(2.5)$ .

- [b] Estimate the value of  $\pi$  using Monte Carlo method.

- ✓ 6. Discuss the long term behavior of linear and nonlinear prey – predator model.

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7<sup>th</sup> Semester  
End Sem Examination

Roll No. mclos  
B.Tech. (MC)  
(November 2018)

### MC407: Cryptography and Network Security

Duration: 3 Hours

Maximum Marks: 50

#### Instructions:

- First question is compulsory. Attempt any four from rest of the questions.
- Calculator is allowed.
- Assume missing data suitably (if any).

- (a) How many one-to-one affine Caesar ciphers are there? [2]

(b) What is a product cipher? [2]

(c) Briefly define a field. [2]

(d) What is a dual signature and what is its purpose? [2]

(e) What problem was Kerberos designed to address? [2]
- (a) Which parameters and design choices determine the actual algorithm of a Feistel cipher? [5]

(b) Following ciphertext has been obtained using a Shift cipher.  
"XLILSYWIMWRSASJSVWEPIJSVJSYVQMPPMSRHSPPPEVWMXMW  
ASVXLQSVILYVVCFIJSVIXLIWIPPIVVIGIMZIWQSVISJJIW".  
Decrypt it using a statistical attack. [5]
- (a) What is RSA algorithm. Describe encryption and decryption using RSA algorithm with an example. [5]

(b) Describe Pretty Good Privacy in detail. [5]
- (a) Explain authentication functions in detail. [5]

(b) List and define the parameters that define an SSL session connect. [5]
- (a) What is kerberos? How it provides authentication service? [5]

(b) Consider the elliptic curve  $y^2 = x^3 + x + 1$  over  $\mathbb{Z}_{23}$ . Let  $P = (3, 10)$  and  $Q = (9, 7)$ . Find  $P + Q$  and  $2P$ . [5]
- (a) Why does ESP include a padding field? [5]



**(b)** Explain digital signature algorithm.

**[5]**

~All the best~

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SEVEN SEMESTER

Roll No. ....  
B.Tech.

END SEMESTER EXAMINATION

NOV/DEC-2018

SE417 Data Warehousing and Data Mining

Time: 3:00 Hours

Max. Marks: 40

Note: Answer FIVE questions. Question No. 1 is compulsory. Assume suitable missing data, if any.

1. Attempt any 4: (3\*4=12)
- ✓ [a] What is Fact Table?
  - [b] What are Junk Dimensions?
  - ✓ [c] How is prediction different from classification?
  - ✓ [d] State the Support and Confidence measures with formulas.
  - ✓ [e] What do you mean by Slicing and Dicing? Give examples.
2. [a] ✓ What are the major features of snow flake schema? What is fact constellation?
- [b] Explain several components of Data warehouse architecture with neat diagram. (3+4)
3. [a] What is multidimensional data model? Explain.
- [b] Explain various Data pre-processing techniques. How does data reduction helps in data pre-processing. (3+4)
4. [a] Compute the entropy and purity for the confusion matrix in the following table:

P.T.O.



| Cluster | Entertainm<br>ent | Financi<br>al | Foreign | Metro | Nationa<br>l | Sports | Total |
|---------|-------------------|---------------|---------|-------|--------------|--------|-------|
| C#1     | 1                 | 1             | 0       | 11    | 4            | 676    | 693   |
| C#2     | 27                | 89            | 333     | 827   | 253          | 33     | 1562  |
| C#3     | 326               | 465           | 8       | 105   | 16           | 29     | 949   |
| Total   | 354               | 555           | 341     | 943   | 273          | 738    | 3204  |

[b] Describe Fully Addictive, Semi-Addictive and Non-Addictive Measures with example. (3+4)

5. [a] Compare and contrast K-means and DBSCAN.

[b] State K-means algorithm. Apply k-means algorithm with two iterations to form two clusters by taking the initial cluster centers as subjects 1 and 4. (3+4)

*Value*

| Subject | A   | B   |
|---------|-----|-----|
| 1       | 1.0 | 1.0 |
| 2       | 1.5 | 2.0 |
| 3       | 3.0 | 4.0 |
| 4       | 5.0 | 7.0 |
| 5       | 3.5 | 5.0 |
| 6       | 4.5 | 5.0 |
| 7       | 3.5 | 4.5 |

6. What are the principles of APRIORI algorithms? Illustrate working of A-priori algorithm for the following dataset.

P.T.O.

| Transaction ID | Items                     |
|----------------|---------------------------|
| T001           | milk, dal, sugar, bread   |
| T002           | Dal, sugar, wheat, jam    |
| T003           | Milk, bread, curd, paneer |
| T004           | Wheat, paneer, dal, sugar |
| T005           | Milk, paneer, bread       |
| T006           | Wheat, dal, paneer, bread |

Can we design a method that mines the complete set of frequent item sets without candidate generation? If yes, explain with example table mentioned above. (7)

7. Considering the following data, it presents Fictional data set that describes the weather conditions for playing some unspecified game. Classification problem is to predict whether the game will be played or not. Using ID3 algorithms, draw Decision tree classifier.

| Day | Outlook  | Temperature | Humidity. | Wind   | Play Golf |
|-----|----------|-------------|-----------|--------|-----------|
| D1  | Sunny    | Hot         | High      | Weak   | No        |
| D2  | Sunny    | Hot         | High      | Strong | No        |
| D3  | Overcast | Hot         | High      | Weak   | Yes       |
| D4  | Rain     | Mild        | High      | Weak   | Yes       |
| D5  | Rain     | Cool        | Normal    | Weak   | Yes       |
| D6  | Rain     | Cool        | Normal    | Strong | No        |
| D7  | Overcast | Cool        | Normal    | Strong | Yes       |
| D8  | Sunny    | Mild        | High      | Weak   | No        |
| D9  | Sunny    | Cool        | Normal    | Weak   | Yes       |
| D10 | Rain     | Mild        | Normal    | Weak   | Yes       |
| D11 | Sunny    | Mild        | Normal    | Strong | Yes       |
| D12 | Overcast | Mild        | High      | Strong | Yes       |
| D13 | Overcast | Hot         | Normal    | Weak   | Yes       |
| D14 | Rain     | Mild        | High      | Strong | No        |

(7)