

## Chapter XI

# INTERNATIONAL PORTFOLIO INVESTMENT

## PROBLEMS

### Problem 1

An Indian investor purchased securities on the New York Stock Exchange when the exchange rate was Rs. 35/\$. One year later, his investments had fetched dollar returns of 50%. At that time, the spot rate was Rs. 36/\$. Calculate the investor's returns if he brings his funds back to India at the end of one year.

### Solution

Assume the investor wants to invest \$100,000

Rupee investment =  $(35) (100,000) = \text{Rs. } 3,500,000$

Value of investment after one year =  $\$ (100,000) (1+0.5)$   
= \$150,000  
= Rs.  $(36) (150,000)$   
= Rs. 5,400,000

Hence rupee returns

$$\begin{aligned} &= (5,400,000 - 3,500,000) / (3,500,000) \times 100 \\ &= 54.29\% \end{aligned}$$

The rupee returns are more than the dollar returns owing to appreciation of the dollar.

### Problem 2

An American investor purchased stocks on the Bombay Stock Exchange when the exchange rate was Rs. 35/\$. One year later, he finds that his portfolio has moved in line with the Bombay Sensex and appreciated by 25%. The spot rate prevailing at the end of one year was Rs. 36/\$. If the investor decides to withdraw from India, what would be his dollar returns?

### Solution

Suppose, the investor wants to buy stocks worth Rs.1,000,000.

$$\text{Dollar funds invested} = (1,000,000) / (35) = \$28,571.$$

$$\begin{aligned}\text{Value of portfolio after one year} &= \text{Rs. } (1,000,000) (1.25) \\ &= \text{Rs. } 1,250,000 \\ &= \$ (1,250,000)/36 \\ &= \$34,722\end{aligned}$$

$$\text{Return on investment} = \frac{(34,722 - 28,571)}{(28,571)} \times 100 = 21.53\%$$

The dollar returns are lesser than the rupee returns owing to depreciation of the rupee.

### **Problem 3**

An Indian investor obtains dollar returns of 15% in New York. At the time of investment, the exchange rate was Rs. 35/\$. The rates of inflation during the following year were 8% in India and 3% in USA. Estimate the investor's rupee returns if he decides to cash his investment at the end of the year.

#### **Solution**

$$\text{Spot rate} = \text{Rs. } 35/\$$$

$$\begin{aligned}\text{If we assume Purchasing Power Parity to hold good, the exchange rate after one year will} \\ \text{be } (35) (1.08/1.03) &= \text{Rs. } 36.70/\$\end{aligned}$$

Assume the investor decides to buy stocks worth \$100,000.

$$\text{Rupee funds needed} = (100,000) (35) = \text{Rs. } 3,500,000$$

$$\begin{aligned}\text{Value of investment after one year} &= \$ (100,000) (1.15) \\ &= \$115,000 \\ &= \text{Rs. } (36.70) (115,000) \\ &= \text{Rs. } 4,220,500\end{aligned}$$

$$\text{Rupee returns} = [(4,220,500 - 3,500,000) / (3,500,000)] \times 100 = 20.59\%$$

The rupee returns have exceeded the dollar returns owing to depreciation of the rupee.

### **Problem 4**

You are given that the risk free rate of return in India is 10%. An American investor decides to buy Indian securities with Beta = 1.50 and variance of returns = 20%. The

Indian rupee has been depreciating at 5% against the dollar with a variance of 15%. If the market portfolio fetches a return of 20% in India and the correlation between the return on security and the exchange rate is 0.20, estimate the expected return and risk for the US investor.

### Solution

$$\begin{aligned}\text{Expected returns in India} &= R_F + B (R_M - R_F) \\ &= 0.10 + 1.50 (0.20 - 0.10) \\ &= 0.25\end{aligned}$$

Suppose an investor buys Rs. 100,000 worth of securities.

$$\begin{aligned}\text{Then value of investment after one year} \\ &= \text{Rs. } (100,000) (1.25) \\ &= 125,000\end{aligned}$$

If spot rate was \$ S/Re at the beginning of the year, it is \$0.95S/Re at the end of the year.

$$\begin{aligned}\text{So, dollar return on investment} \\ &= \frac{(125,000) (0.95S) - (100,000) S}{(100,000) (S)} \\ &= 0.1875\end{aligned}$$

$$\text{Thus expected rate of return} = 18.75\%$$

$$\begin{aligned}\text{Variance} &= 20 + 15 + (2) (0.20) \vee (20) (15) \\ &= 41.93\%\end{aligned}$$

$$\text{So, total risk} = 41.93\%.$$

### Problem 5

The risk free rate of return in India is 8% and the market portfolio's rate of return is 25%. The security's beta is 1.15 and the variance of returns is 20%. The Indian Rupee has been depreciating relative to US \$ at the rate of 5% per annum with a variance of 15%.

Compute the return and total risk an US investor can expect from this security, assuming that the correlation between returns on the security and the exchange rate is 0.25

### Solution

$$R = 0.08 + 1.15 (0.25 - 0.08) = 0.2755$$

Thus, the expected rupee rate of return is 27.55%.

Suppose \$ 100 is invested.

If spot rate = Rs S/\$, investment in India = Rs 100 S

Rupee returns at the end of the year

$$= (100) (S) (1.2755) = 127.55S$$

$$= \$ [ ( 127.55 ) S ] / [ ( S/0.95 ) ]$$

$$= \$ 121.17$$

So, dollar returns = [ (121.17-100) / (100)] x (100) = 21.17%

Total Risk = 20% + 15% + (2) (0.25) [sq root of (20) (15)]

### Problem 6

Exchange rates at the beginning of 1981 and 1982 were Rs. 18.53 and Rs. 25.53 per US \$.

If the percentage return on American Securities is a) - 50% b) -25% c) 50% d) 25%, compute the net return to the Indian investor.

### Solution

To invest \$ 100, the Indian investor needs Rs. 1853.

The net return can now be worked out for each case separately.

$$\begin{array}{lcl} \text{Net Return} & (50) (25.53) - 1853 & \\ = & \frac{\text{-----}}{1853} & = - 31.11\% \end{array}$$

$$\begin{array}{lcl} \text{Net Return} & (75) (25.53) - 1853 & \\ = & \frac{\text{-----}}{1853} & = 3.33\% \end{array}$$

$$\begin{array}{lcl} \text{Net Return} & (150) (25.53) - 1853 & \\ = & \frac{\text{-----}}{1853} & = 106.66\% \end{array}$$

$$\begin{array}{lcl} \text{Net Return} & (125) (25.53) - 1853 & \\ = & \frac{\text{-----}}{1853} & = 72.22\% \end{array}$$

### Problem 7

The spot exchange rate in 1983 was Rs. 25/\$. The interest rate was 9% in India and 4% in USA. What would be expected percentage return to an American Investor, if the percentage return on Indian Securities is a) 10% b) 30% c) 50%

### Solution

We first calculate the expected spot rate after one year using the interest parity principle.

$$S_n = (25) ((1.09) / (1.04)) = 26.20$$

Suppose the American investor has surplus funds of \$100.

$$\text{\$ } 100 = \text{Rs } 2500$$

The investor can hence buy securities worth Rs 2500 in India.

We can now calculate the returns for each scenario as follows.

$$\frac{((2500) (1.1) / (26.20)) - 100}{100} * 100 = 4.96\%$$

$$\frac{((2500) (1.3) / (26.20)) - 100}{100} * 100 = 24.05\%$$

$$\frac{((2500) (1.5) / (26.20)) - 100}{100} * 100 = 43.13\%$$

### Problem 8

The spot exchange rate at the beginning of 1982 was Rs. 25 per US \$. The annual inflation rates are 11% in India and 3% in USA. Compute the expected percentage return to an Indian investor for that year, if the percentage return on American Securities is a) -5% b) 15% c) 50%

### Solution

We first determine the exchange rate after one year using the Purchasing Power Parity principle .

$$S_1 = (25) (1.11) / (1.03) = 26.94$$

Suppose the Indian investor has surplus funds of Rs 2500. Rs 25000 = \$ 100. So, the investor can buy American Securities worth \$ 100.

We can now work out the returns for each scenario.

$$\begin{array}{rclclcl}
 100 & (0.95) & (26.94) & - & 2500 & & \\
 \hline
 & & 2500 & & & * & 100 & = & 2.37\% \\
 100 & (1.15) & (26.94) & - & 2500 & & \\
 \hline
 & & 2500 & & & * & 100 & = & 23.92\% \\
 100 & (1.50) & (26.94) & - & 2500 & & \\
 \hline
 & & 2500 & & & * & 100 & = & 61.64\%
 \end{array}$$

### Problem 9

A company has surplus funds of £1,000,000. The following rates are being quoted.

Spot : DM 1.50/\$ 1.50/£  
 3 month interest rates : £ - 8% DM - 4% \$ - 5%  
 3 month forward : DM 1.45/\$ 1.40/£

In which currency should it invest ?

### Solution

#### Alternative 1

Invest in £.

$$\begin{array}{rclcl}
 \text{Returns after 3 months} & = & £ (1,000,000) (1+0.08/4) \\
 & = & £1,020,000 \\
 \text{Profits} & = & 1,020,000 - 1,000,000 \\
 & = & £20,000.
 \end{array}$$

#### Alternative 2

Invest in \$ after converting £1,000,000 at the rate of \$1.50/£

It can sell the \$ returns forward at \$1.40/£

$$\begin{array}{rclcl}
 \text{Returns after 3 months} & = & \$ (1,000,000) (1.5) (1+0.05/4) \\
 & = & \$1,518,750 \\
 & = & £ (1,518,750)/1.40 \\
 & = & £1,084,821.
 \end{array}$$

$$\begin{aligned}
 \text{So, profits} &= 1,084,821 - 1,000,000 \\
 &= \text{£}84,821.
 \end{aligned}$$

### Alternative 3

Invest in DM after converting £1,000,000 into DM at the rate of DM (1.5) (1.50) / £ = DM 2.25/£

The DM returns can be sold forward at DM (1.40)(1.45)/£

$$= \text{DM } 2.03/\text{£}$$

$$\begin{aligned}
 \text{Returns after 3 months} &= (2.25) (1,000,000) (1+0.04/4) \\
 &= \text{DM } 2,272,500 \\
 &= \text{£ } (2,272,500) / (2.03) \\
 &= \text{£}1,119,458.1
 \end{aligned}$$

$$\begin{aligned}
 \text{So, profits} &= 1,119,458.1 - 1,000,000 \\
 &= \text{£}119,458.1
 \end{aligned}$$

Investing in DM hence yields the best returns.